

PAGINA 2 - Ejercicio 3.

	x	y	x <sup>2</sup>	y <sup>2</sup>	x·y
2	8	7	64	49	56
2	7	5	49	25	35
3	10	8	100	64	80
4	3	5	9	25	15
5	6	9	36	81	54
6	13	9	169	81	117
7	4	3	16	9	12
Σ	51	46	443	334	369

$$\bar{x} = 51/7 = 7,2857$$

$$\bar{y} = 46/7 = 6,5714$$

$$V(x) = \frac{443}{7} - (7,2857)^2 = 10,2042$$

$$V(y) = \frac{334}{7} - (6,5714)^2 = 4,5309$$

$$C_{xy} = \frac{369}{7} - (7,2857 \times 6,5714) = 4,8370$$

$$r = \frac{4,8370}{\sqrt{10,2042 \times 4,5309}} = 0,7113$$

6,2995

relación directa

$$r^2 = 0,7113^2 = 0,5059$$

$$b = \frac{48370}{102042} = 0,4740$$

$$a = 6,5714 - (0,4740 \times 7,2857)$$

$$a = 3,1179$$

$$y = 3,1179 + 0,4740 \cdot x$$



# Página 7 - Ejercicio 4

Datos	Media	Desvío
TARJETA	572	102
Efectiva	332	51

$$P(\text{Efectivo}) = 0,44$$

$$P(\text{Tarjeta}) = 0,56$$

a)  $P(X < 411) = P(Z < -1,5384) = 0,05821$   
(con Tarjeta)

$$Z = \frac{411 - 572}{102} = -1,5384$$

b)  $P(X < 411) = P(Z < 1,5490) = 0,9382$   
en efectivo

$$Z = \frac{411 - 332}{51} = 1,5490$$

c)  $P(X < 411) = P(\text{Efectivo}) \times P(X < 411) + P(\text{Tarjeta}) \times P(X < 411)$   

$$= (0,44 \times 0,9382) + (0,56 \times 0,05821)$$
  

$$= 0,4454$$

d)  $P(\text{Efectivo} | X < 411) = \frac{P(\text{Efectivo} \cap X < 411)}{P(X < 411)} = \frac{0,44 \times 0,9382}{0,4454} = 0,928$



# Página 7 - Ejercicio 6

$X$  = número de bolas verdes

$Y = \begin{cases} 0 & \text{si las azules son par o } \emptyset \\ 1 & \text{si el número de bolas azules es impar} \end{cases}$

Información:

8 verdes

4 azules

12 TOTAL

EXTRAER 3

$X \backslash Y$	0	1	2	3	$P(X)$
0	0	0	0	$\frac{1}{55}$	$\frac{1}{55}$
1	0	0	$\frac{12}{55}$	0	$\frac{12}{55}$
2	0	$\frac{28}{55}$	0	0	$\frac{28}{55}$
3	$\frac{14}{55}$	0	0	0	$\frac{14}{55}$
$P(Y)$	$\frac{14}{55}$	$\frac{28}{55}$	$\frac{12}{55}$	$\frac{1}{55}$	

$$P(X=0, Y=3) = \frac{\binom{8}{0} \binom{4}{3}}{\binom{12}{3}} = \frac{1}{55}$$

$$P(X=1, Y=2) = \frac{\binom{8}{1} \binom{4}{2}}{\binom{12}{3}} = \frac{12}{55}$$

$$P(X=2, Y=1) = \frac{\binom{8}{2} \binom{4}{1}}{\binom{12}{3}} = \frac{28}{55}$$

$$P(X=3, Y=0) = \frac{\binom{8}{3} \binom{4}{0}}{\binom{12}{3}} = \frac{14}{55}$$

$$N=12 \quad n=3$$

$$N_g=8 \quad N_a=4$$

$$E(X) = 1 \cdot \frac{12}{55} + 2 \cdot \frac{28}{55} + 3 \cdot \frac{14}{55} = 2$$

$$E(Y) = 1 \cdot \frac{28}{55} + 2 \cdot \frac{12}{55} + 3 \cdot \frac{1}{55} = 1$$

$$E(X^2) = 1^2 \cdot \frac{12}{55} + 2^2 \cdot \frac{28}{55} + 3^2 \cdot \frac{14}{55} = \frac{50}{11}$$

$$E(Y^2) = 1^2 \cdot \frac{28}{55} + 2^2 \cdot \frac{12}{55} + 3^2 \cdot \frac{1}{55} = \frac{17}{11}$$



$$V(x) = 50/11 - 2^2 = 6/11 = 0,5454$$

$$V(y) = 17/11 - 1^2 = 6/11 = 0,5454$$

$$E(xy) = 0 \cdot 3 \cdot \frac{1}{55} + 1 \cdot 2 \cdot \frac{16}{55} + 2 \cdot 1 \cdot \frac{28}{55} + 3 \cdot 0 \cdot \frac{14}{55} = \frac{122}{55} = \frac{10}{11}$$

$$\text{cov}(xy) = \frac{10}{11} - 2 \cdot 1 = -6/11$$

$$r = \frac{-6/11}{\sqrt{6/11 \times 6/11}} = -1 \quad r^2 = -1^2 = 1$$

0. SON  $x$  E  $y$  INDEPENDIENTES? PREGUNTAR

$$c. P(x \leq 1, y > 0) = P(x=1, y=2) + P(x=2, y=1) = \frac{16}{55} = 0,218$$

$$P(x < 1) = P(x=0, y=3) = \frac{1}{55} = 0,0181$$