Exercise 1 - TFY4345 Classical Mechanics

2020

1 Halley's comet

Halley's comet follows an elliptical orbit around the Sun, with a period of about 76 years. The sun is a focal point in the ellipse. The closest distance between the comet an the sun is 0.6AU., and the farthes ditance is 35AU. 1AU (astronomical unit) is the mean distance between the Sun and the earth. Use the Sun as the origin in your coordinate system

a) Explain why the net torque on Halley's comet is zero. This implies that the angular momentum is conserved
b) When the comet is closest to the Sun, it's velocity is 54kms^{-1}. Use conservation of angular momentum to calculate the velocity of the comet when it is farthes from the Sun.

2 Simple pendulum

(FIGUR)

Consider a simple pendulum, subeject to a uniform gravitational field $\vec{g} = -g\hat{e}_x$ Chose the pivot point as the origin of your coordinate system There are no friction forces.

a) Show that the position vector of the mass m is $\vec{R} = \ell\sin(\beta)\hat{e}_x - \ell\cos(\beta)\hat{e}_y$.
b) Find the potetial energy of the mass, as a function of the angle β.
c) Find the kinetic energy of the mass, as a function of β and $\dot{\beta} = \frac{\mathrm{d}\beta}{\mathrm{d}t}$.
d) The Lagrangian of the pendulum is $L = T - V$. Use Lagrange's equations to obtain the equation of motion of the pendulum.