# Exercise 11 - TFY4345 Classical Mechanics

#### 2020

#### 1 Binding energy of the deuteron

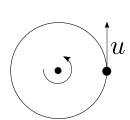
[This is a short one]

Deuteron can be split by gamma rays in a nuclear experiment in the reaction  $\gamma + {}^{2}{\rm H} \rightarrow p + n$ . Calculate the energy required for the gamma rays for this process to occur, in electron volts. The quantities needed are

- Mass of a proton ( ${}^{1}H = p$ ): 1.007825u
- Mass of a neutron (n): 1.008665u
- Mass of deuteron (<sup>2</sup>H): 2.014102
- 1  $u = 931.5 \text{ MeVc}^{-2}$

### 2 Frequency shift on a rotating disk

A radioactive  $^{57}$ Co element is situated on the periphery of a rotating disk. The peripheral velocity is u. The radiation from the cobalt is received by an observer located in the center of the disk. Let  $f_0$  be the eigenfrequency of the radiation in the the inertial system where the element is momentarily at rest. Find the frequency f of the radiation observed by the observer in the center.



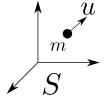
## 3 Fast moving particle in two inertial frames

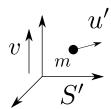
[Exam Dec. 2019]

We shall consider a particle with rest mass m seen from two different inertial reference systems. In the reference system S, the particle has velocity

$$\mathbf{u} = (u_x, u_y, u_z).$$

The reference system S' is moving along the z axis with a velocity v relative to the system S. In this frame, the particle has the velocity





$$\mathbf{u}' = (u_z', u_y', u_z').$$

Find the explicit relationship between  $\mathbf{u}$  and  $\mathbf{u}'$ , i.e. derive the transformation that give  $\mathbf{u}'$  from the components of  $\mathbf{u}$ . [Hint] Start with the relationship between the two frames, the Lorentz transformation. What is the definition of the components  $u_i, u_i'$ ?

#### 4 Lorentz transformation of energy and momentum

We continue the analysis of the particle in the last exercise. The relations derived there are Einstein's velocity addition formulas,

$$u'_x = \frac{u_x}{\gamma(1 - vu_z/c^2)}$$

$$u'_y = \frac{u_y}{\gamma(1 - vu_z/c^2)}$$

$$u'_z = \frac{u_z - v}{1 - vu_z/c^2}$$

(The difference between these, and the ones derived in the exercise 10, is that they do not assume the third reference system e.g. the particle moves along the z-axis).

a) Use these to show that

$$\frac{1}{\sqrt{1 - u'^2/c^2}} = \gamma \frac{1 - vu_z/c^2}{\sqrt{1 - u^2/c^2}}.$$

Here,  $\gamma = 1/\sqrt{1-(v/c)^2}, \, u^2 = |\mathbf{u}| = u_x^2 + u_y^2 + u_z^2$  and  $u'^2 = |\mathbf{u}'| = u_x'^2 + u_y'^2 + u_z'^2$ .

b) The energy E and 3-momentum  $\mathbf{p}$  of the particle in the reference system S are

$$E = \frac{mc^2}{\sqrt{1 - (u/c)^2}}, \quad \mathbf{p} = \frac{m\mathbf{u}}{\sqrt{1 - (u/c)^2}},$$

while in the S' system they are

$$E' = \frac{mc^2}{\sqrt{1 - (u'/c)^2}}, \quad \mathbf{p}' = \frac{m\mathbf{u}'}{\sqrt{1 - (u'/c)^2}}.$$

Use the equation derived in a) to to find the transformation rule of energy of momentum, i.e. express E' and  $\mathbf{p}'$  in terms of E and  $\mathbf{p}$ .