

Distributed Algorithms

Prof R. Guerraoui

<http://lpd.epfl.ch/education/da>

Exam: Written (60%) + Project (40%)

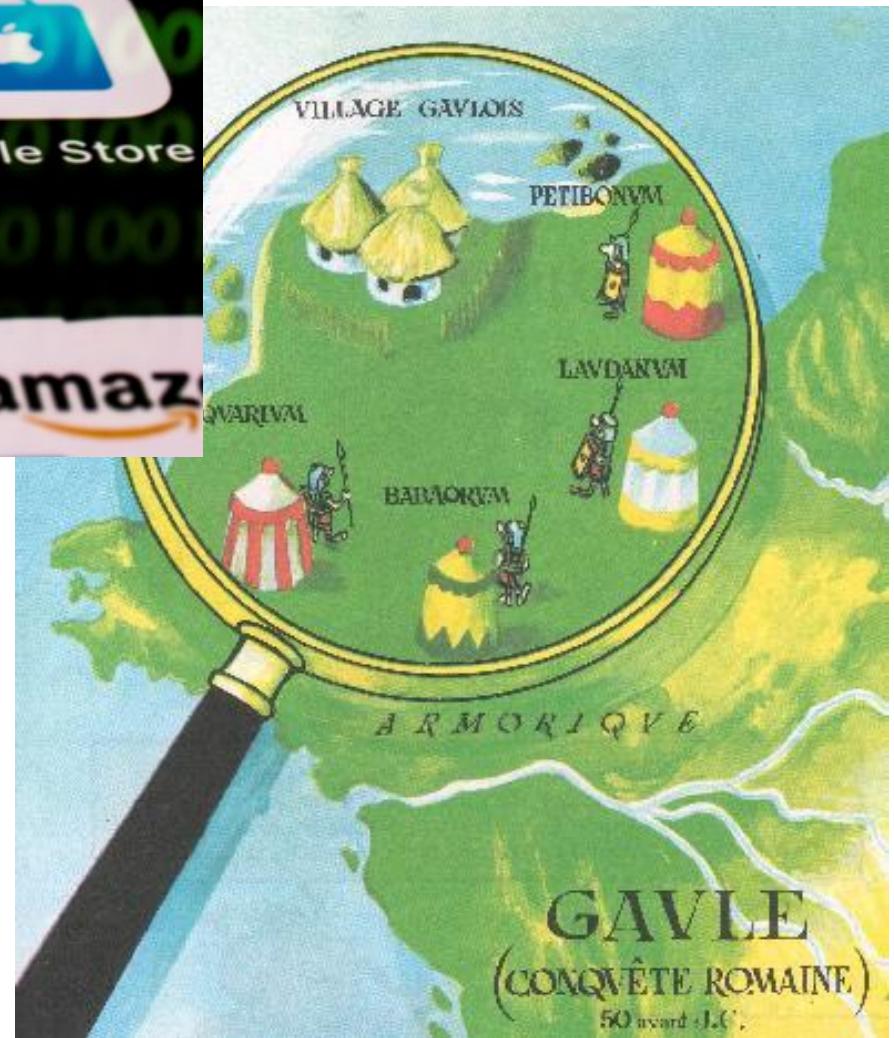
Reference: Book - Springer Verlag

Introduction to Reliable (and Secure) Distributed Programming

Complementary to the course Concurrent Algorithms



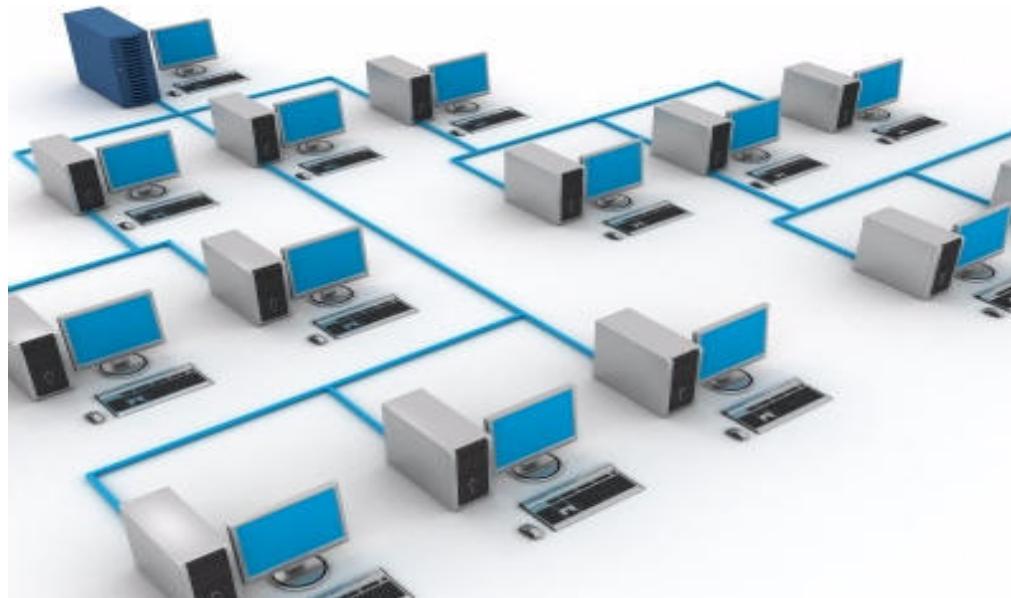
Algorithms



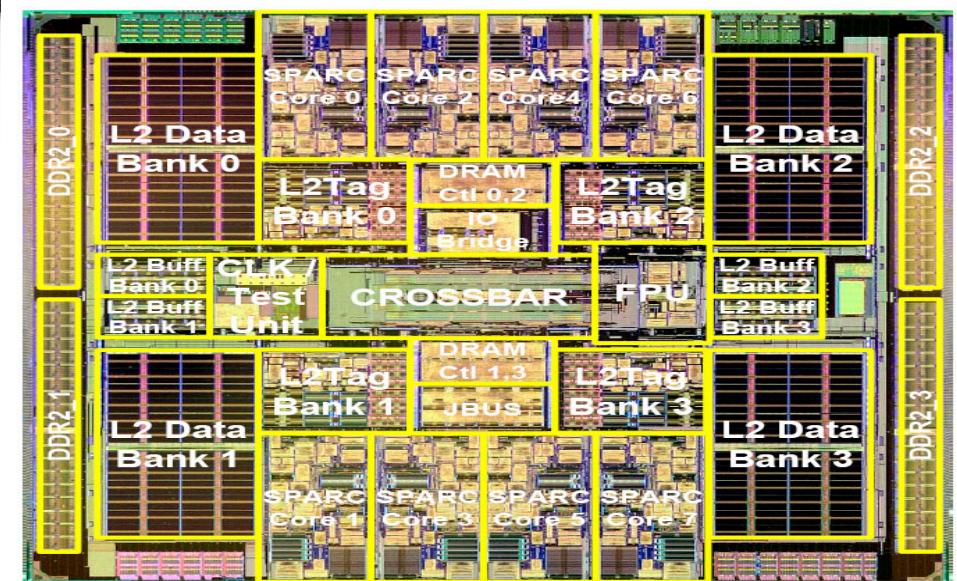
LA VOITURE SANS CONDUCTEUR

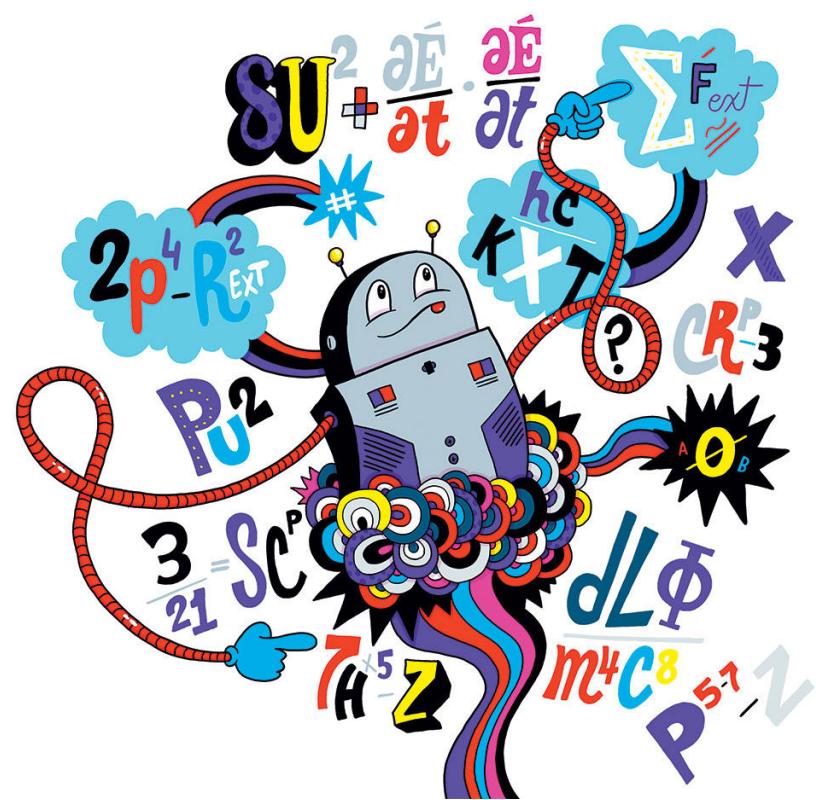
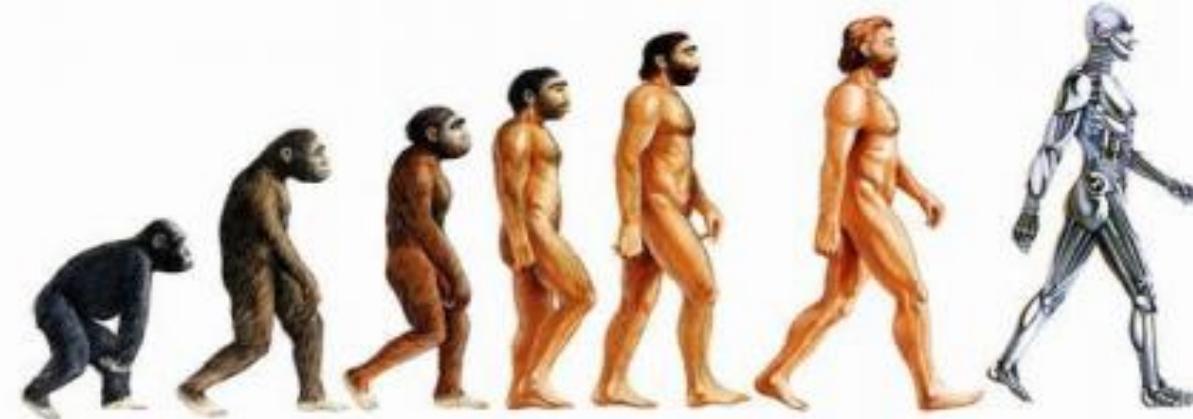


Ultra-Robust



Ultra-Fast





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Alan Turing

1912-1936-1954



Universal Machine

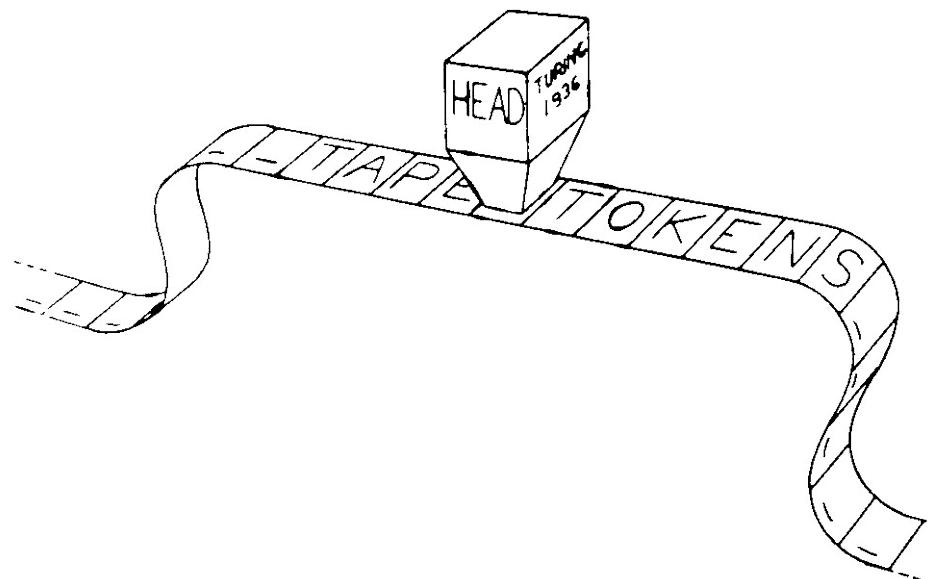
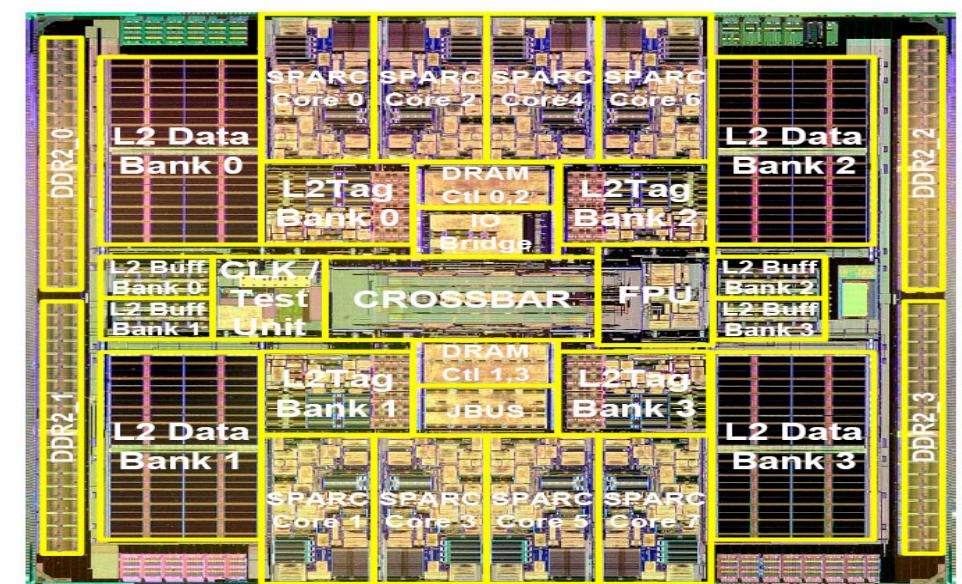
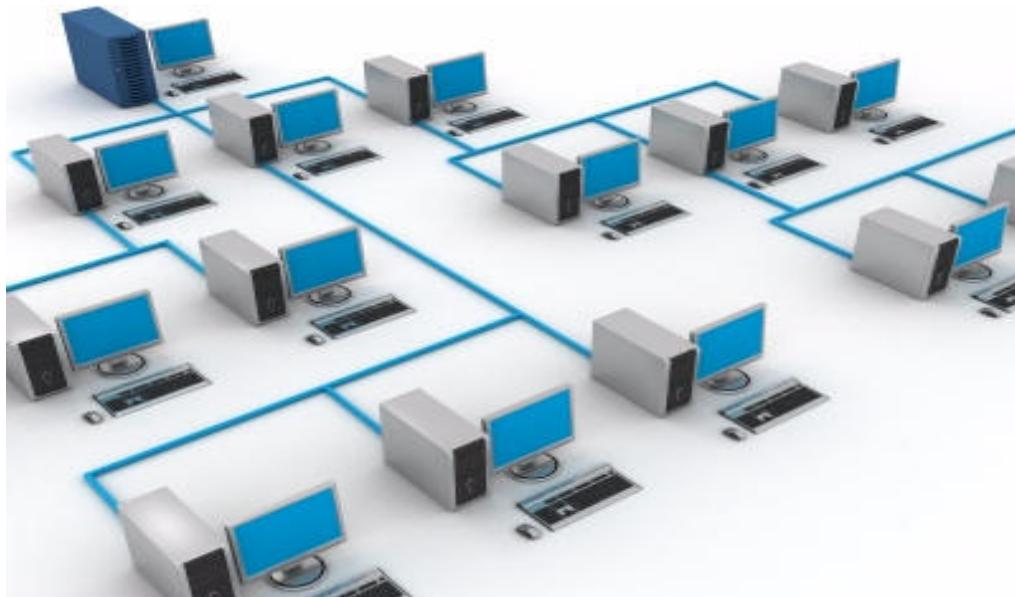
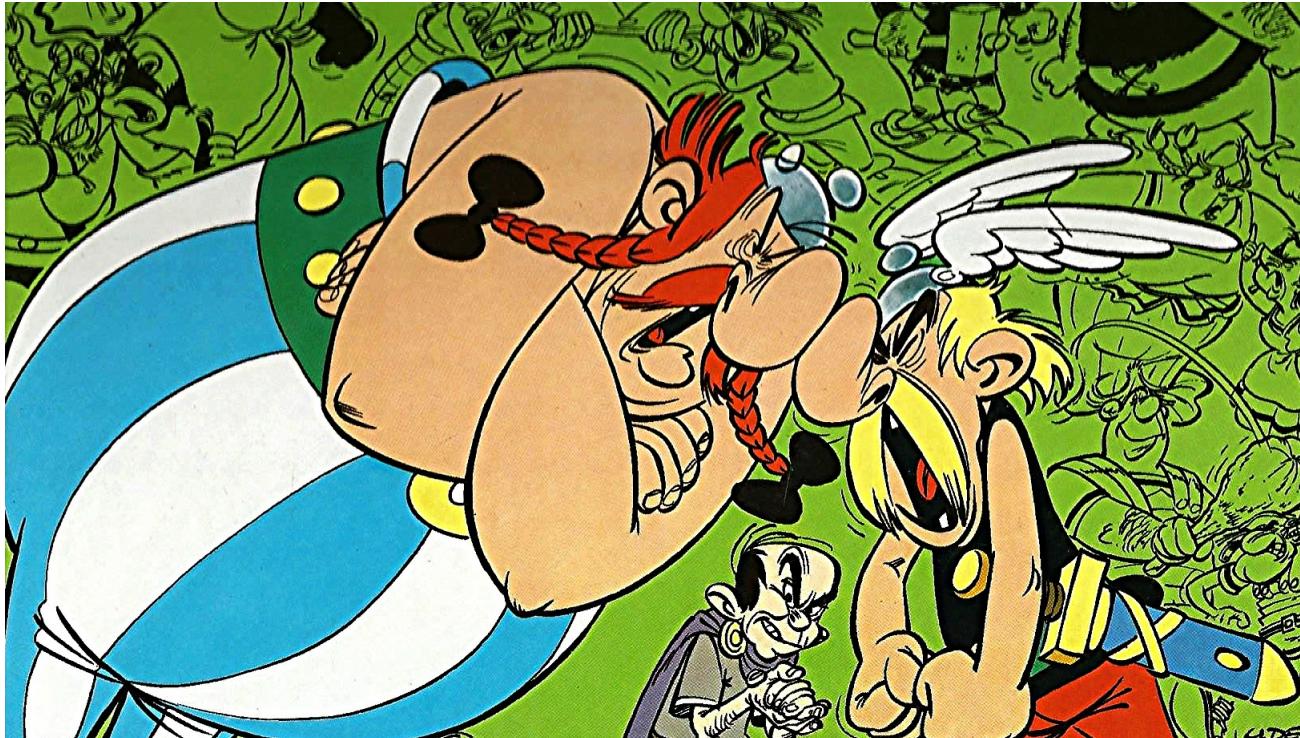


Figure 1 Diagram of a Turing Machine

Lost Universality



Impossibility of Consensus

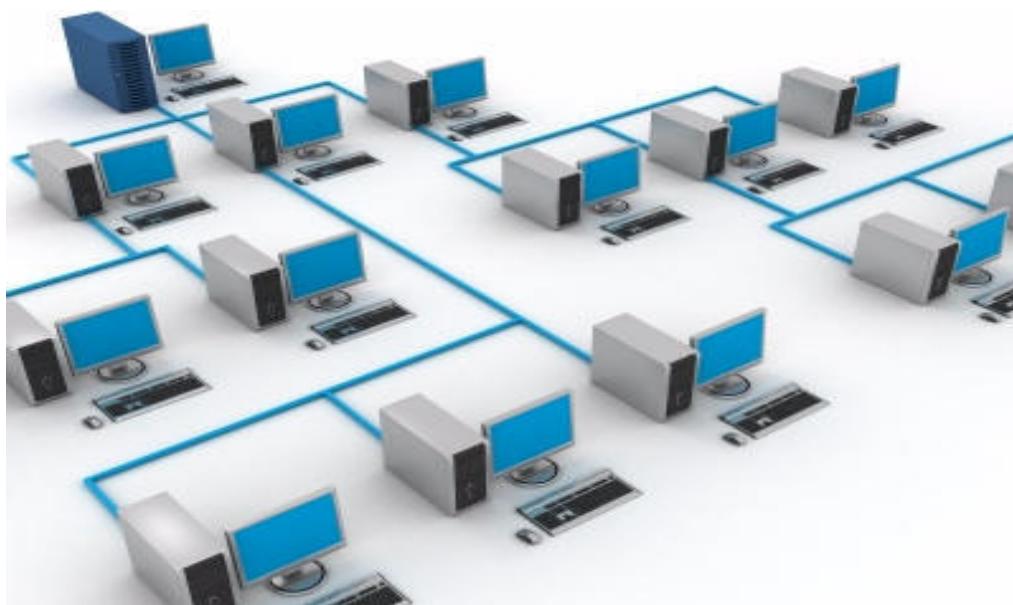


Adversary

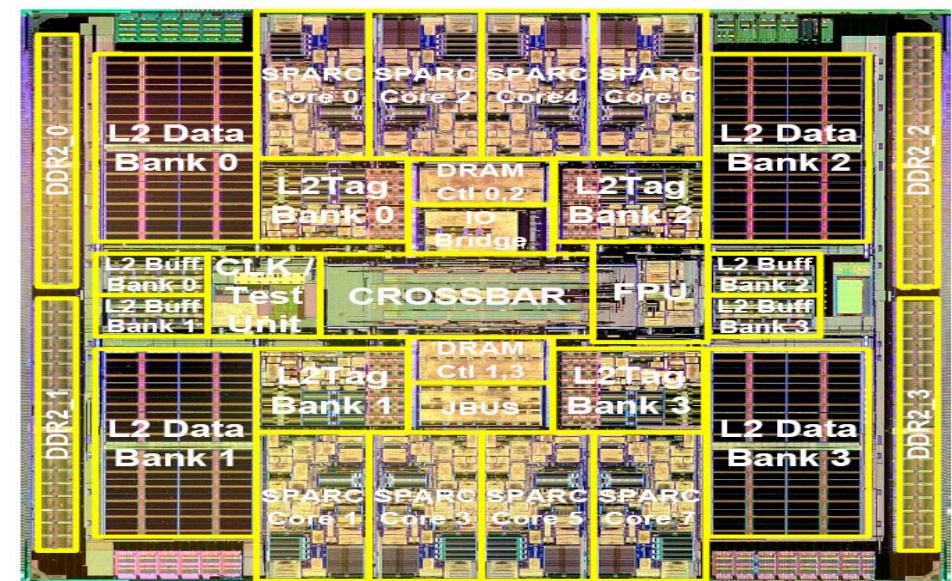


Distributed Computing

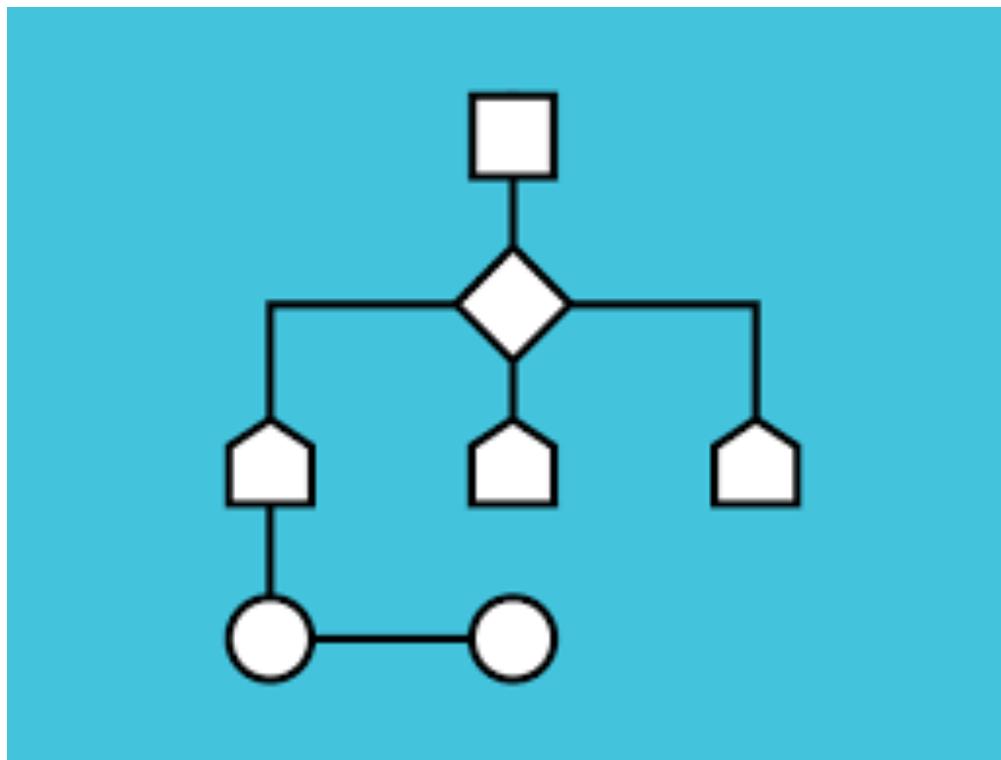
Distributed Algorithms

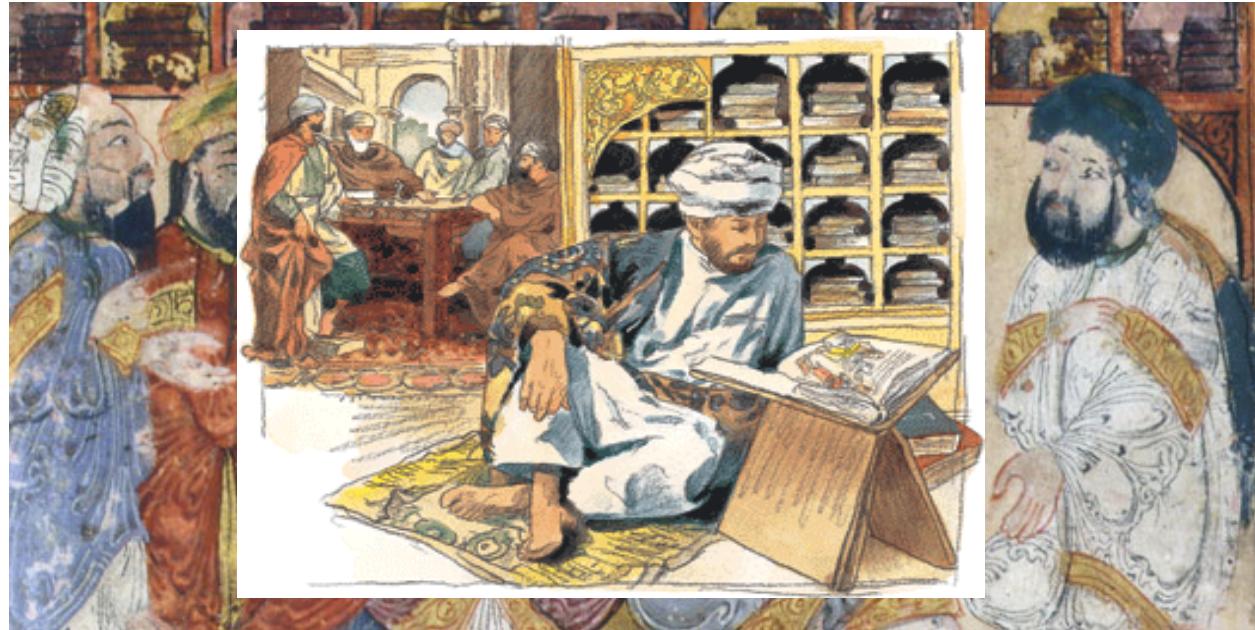


Concurrent Algorithms



$$\begin{array}{r} & 1 & 1 \\ & 5 & 4 & 8 & 5 & 3 \\ + & 2 & 9 & 5 & 1 & 4 \\ \hline & 8 & 4 & 3 & 6 & .7 \end{array}$$





Euclide

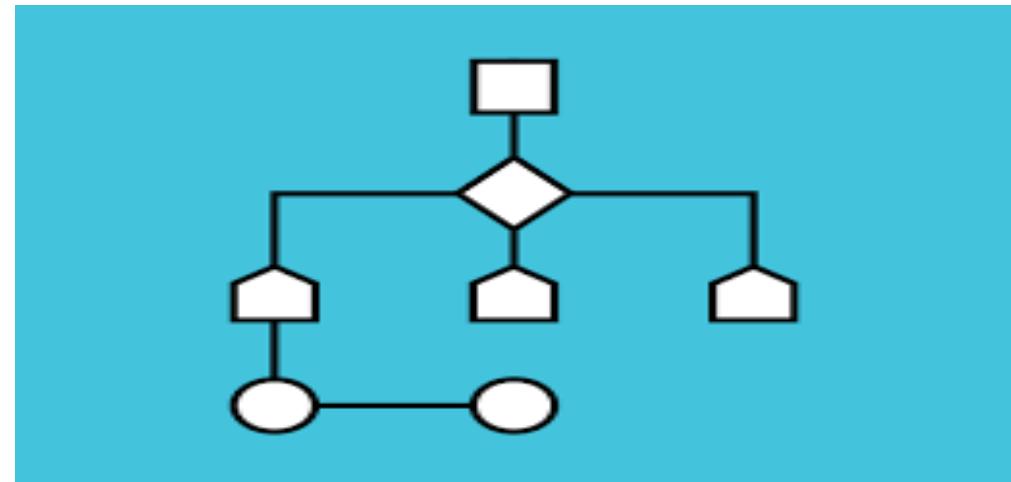


Mohammed



Muhammad Al-Khawarizmi

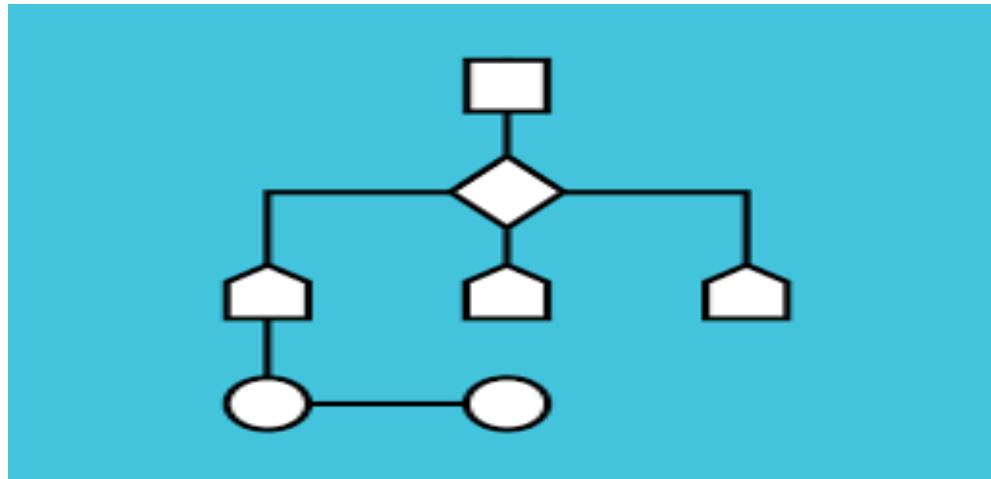
ca. 780 - 850



$$\begin{array}{r} & 1 & 1 \\ & 5 & 4 & 8 & 5 & 3 \\ + & 2 & 9 & 5 & 1 & 4 \\ \hline & 8 & 4 & 3 & 6 & 7 \end{array}$$

What is an Algorithm? (800)

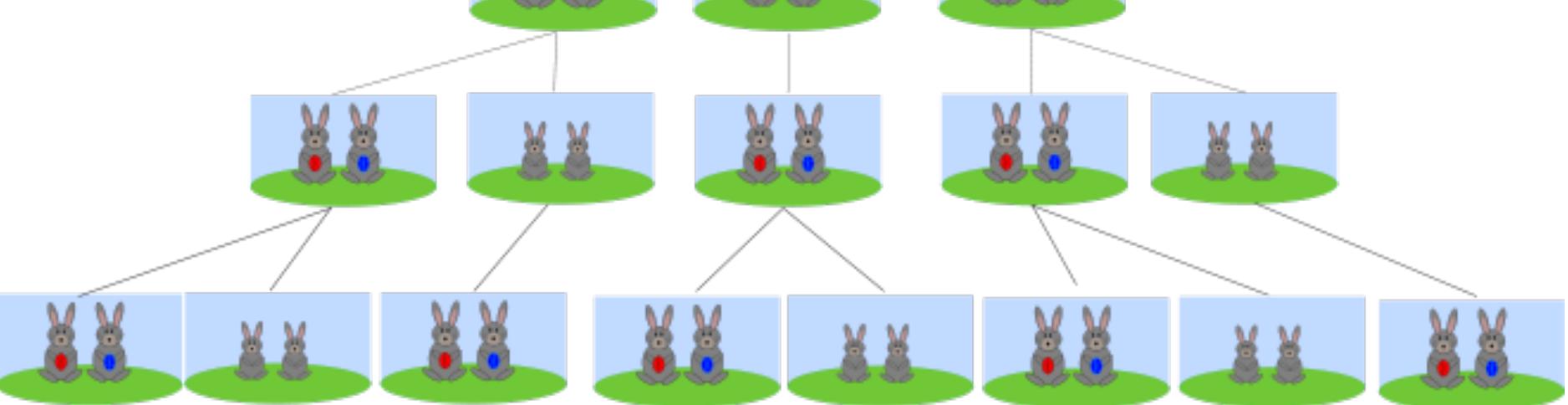
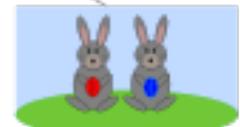
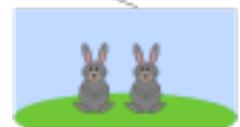
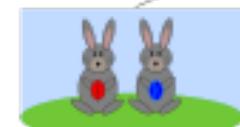
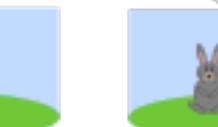
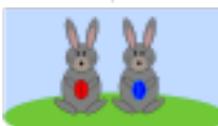
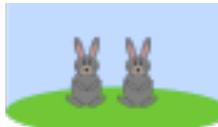
- ☞ An ordered set of elementary instructions



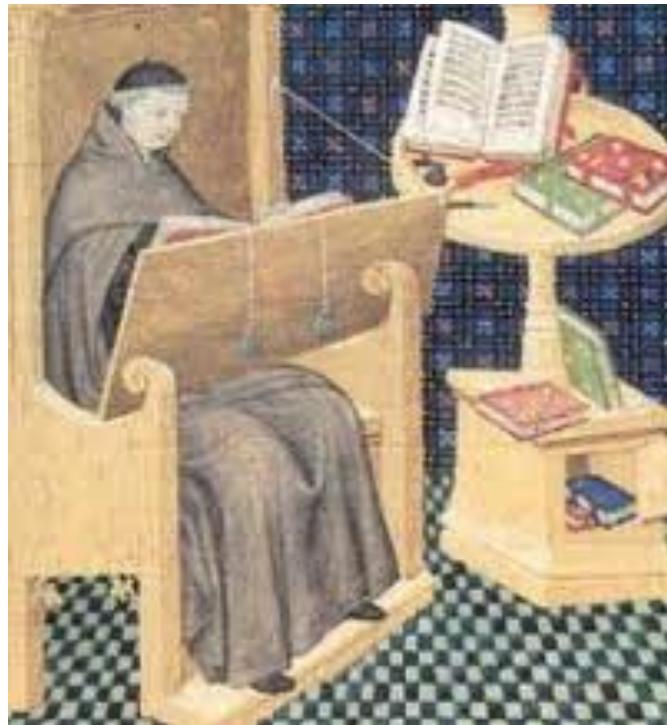
- ☞ Executed by a human

Fibonacci

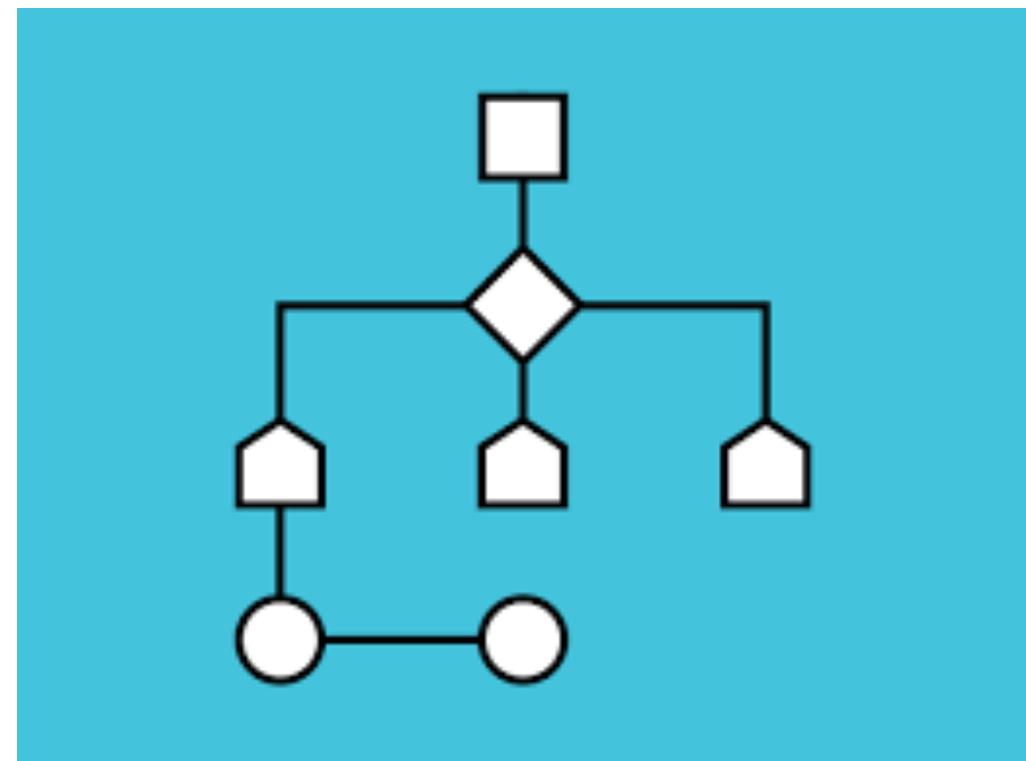
$$F(n) = F(n-1) + F(n-2)$$

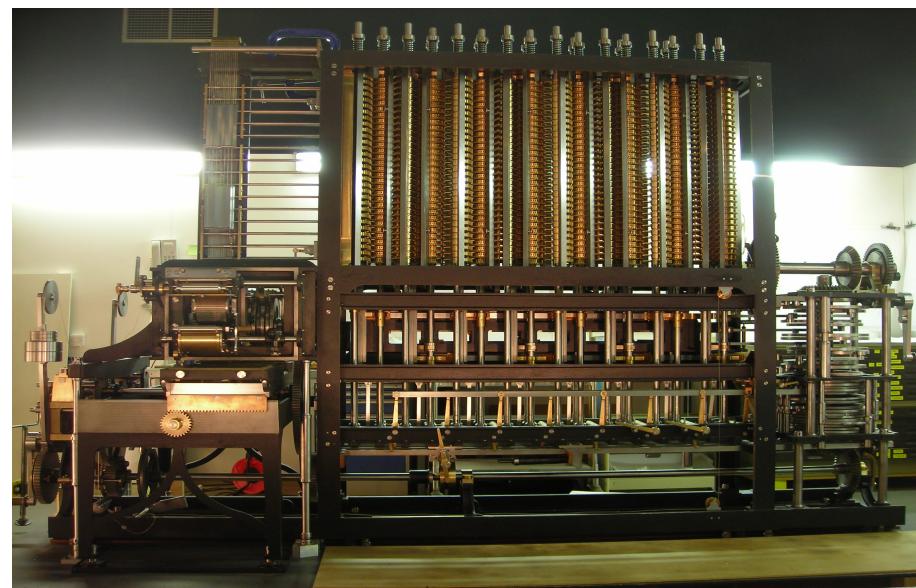
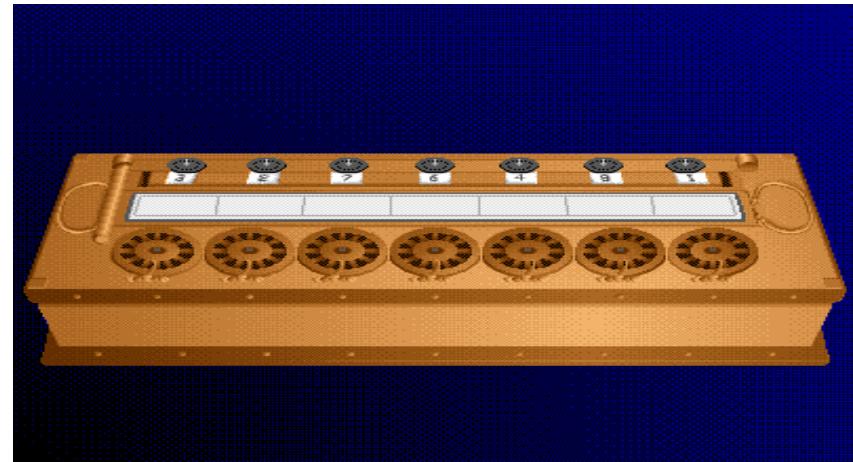


Adelard of Bath



Algorithm





Alan Turing

1912-1936-1954

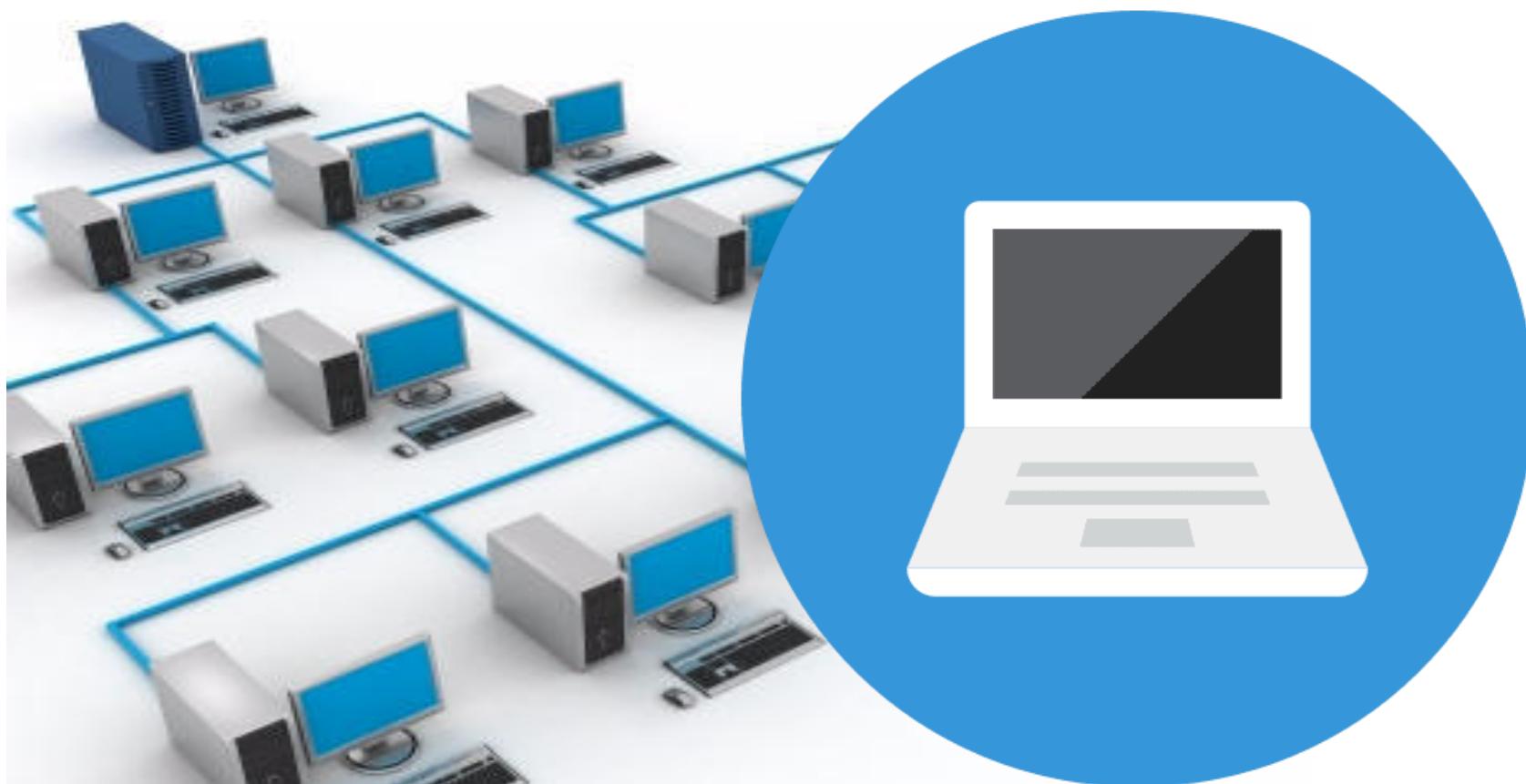


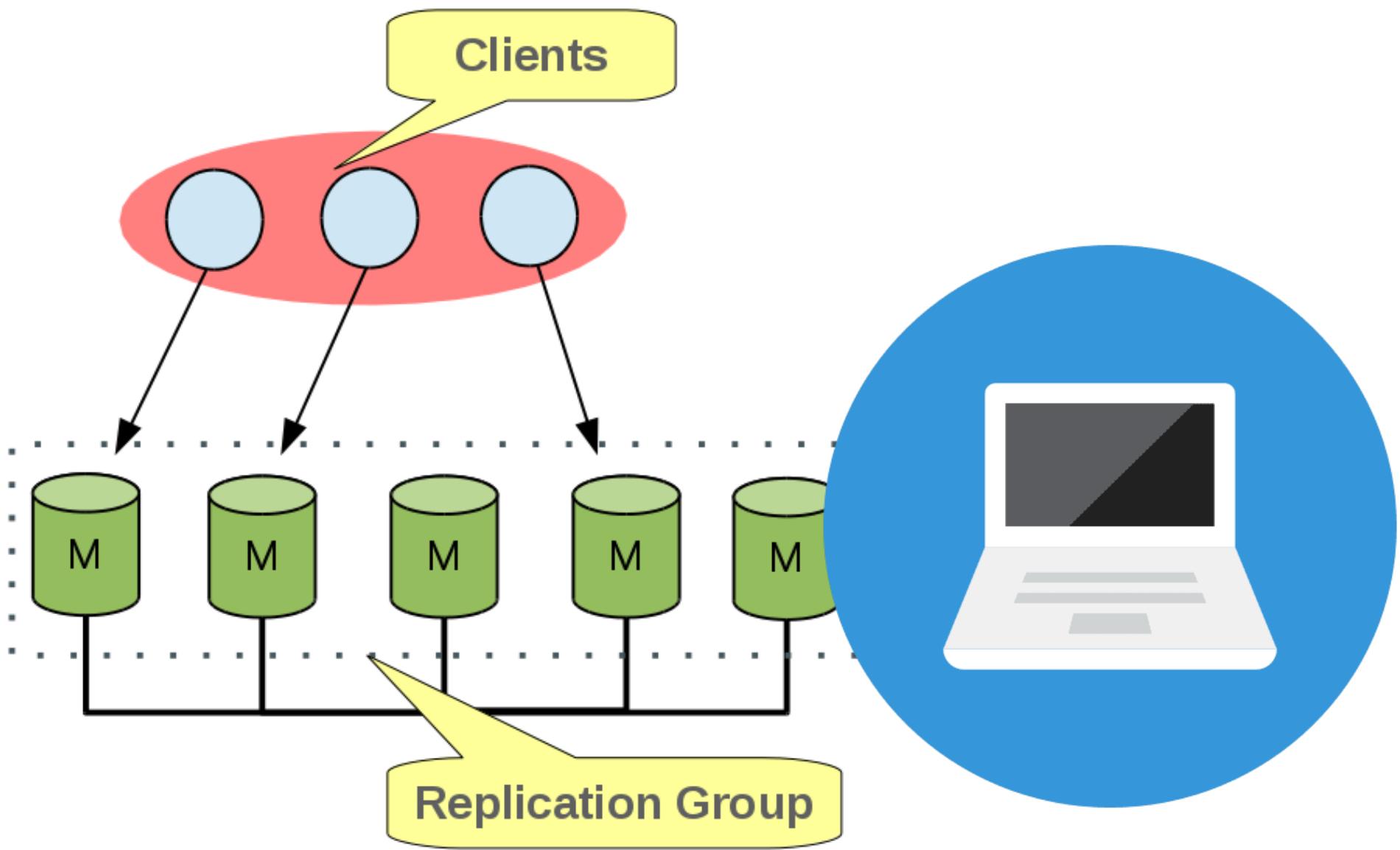
1954 : 1st IBM650

What is an Algorithm? (1936)

- ➊ An ordered set of elementary instructions
- ➋ All execute on the same Turing machine
- ➌ Complexity measures the number of instructions (variables)

1960 : Ultra-Robust Distributed Machine



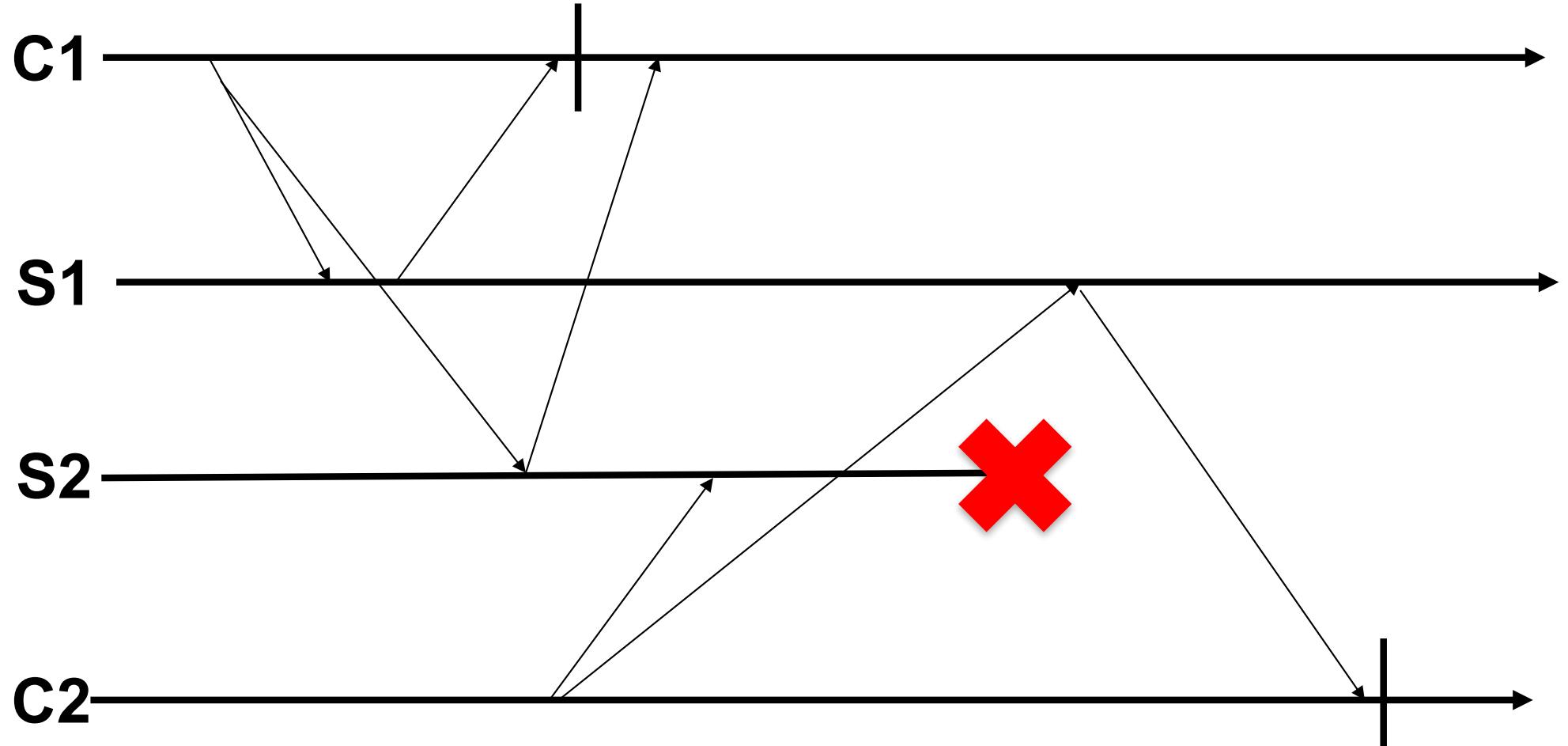


The distributed machine looks like a single machine (atomicity) that tolerates the failure of individual machines

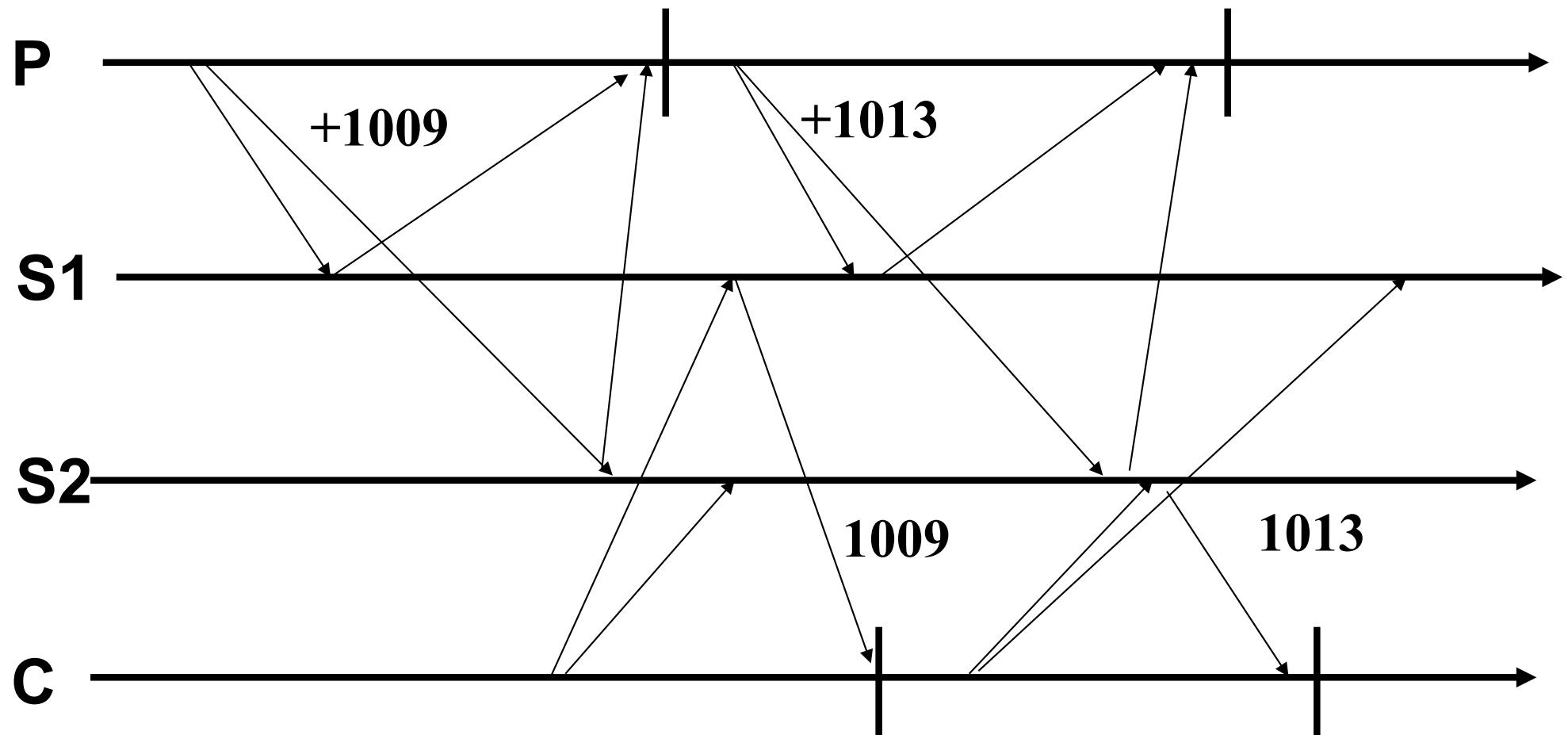
Prime Numbers

1	2	3	5	7	9
11		13	15	17	19
21		23	25	27	29
31		33	35	37	39
41		43	45	47	49

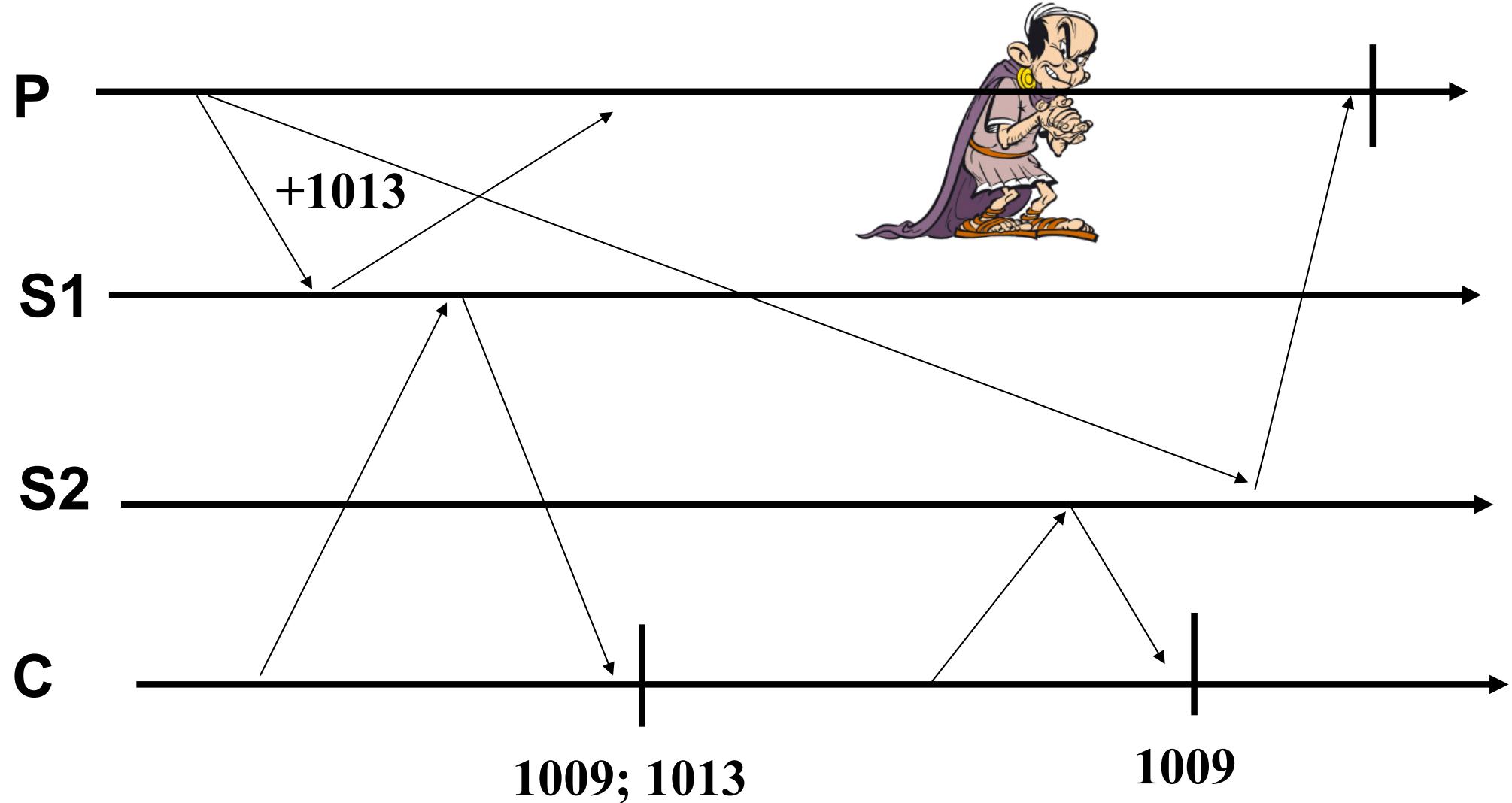
Robustness



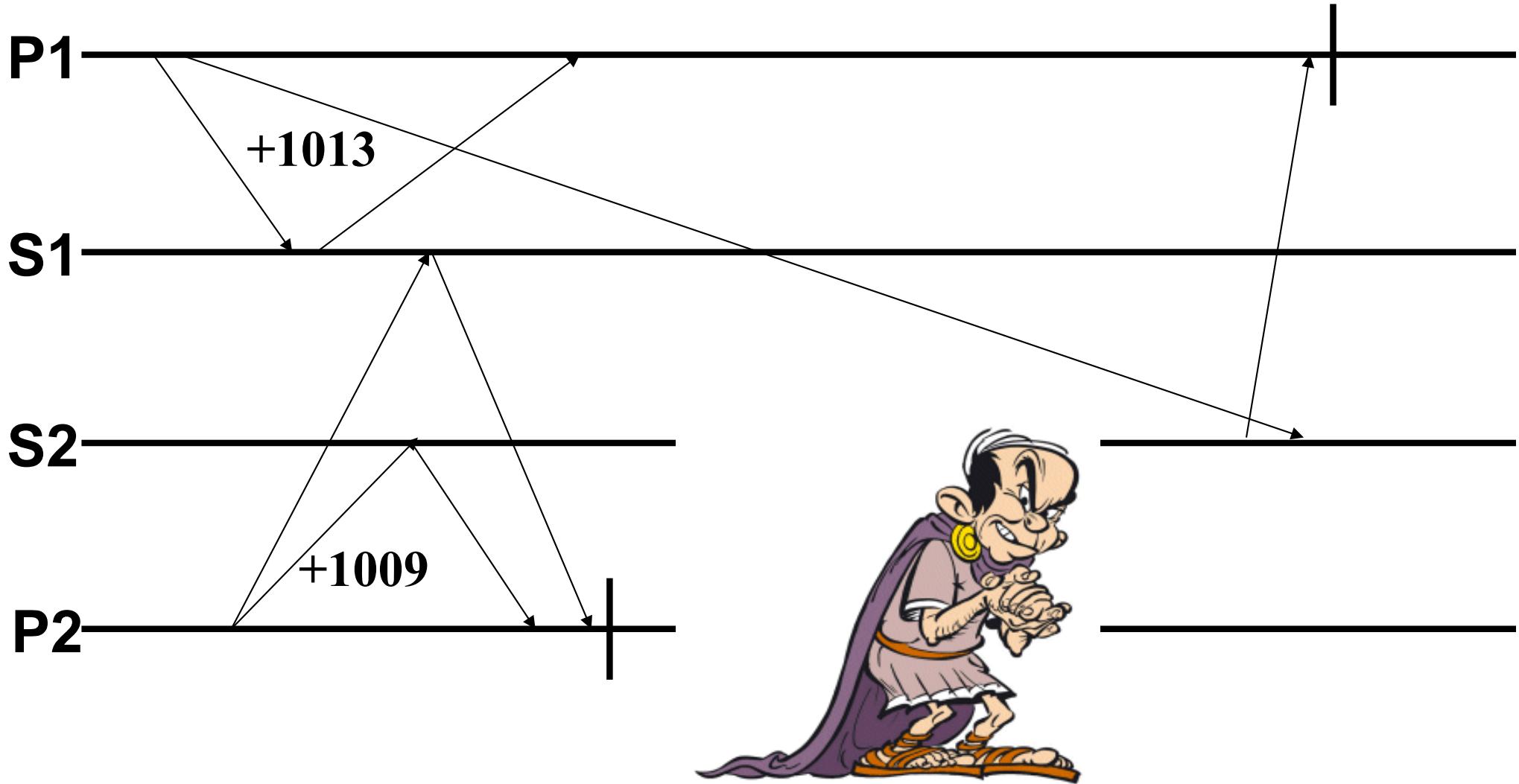
Adding Numbers



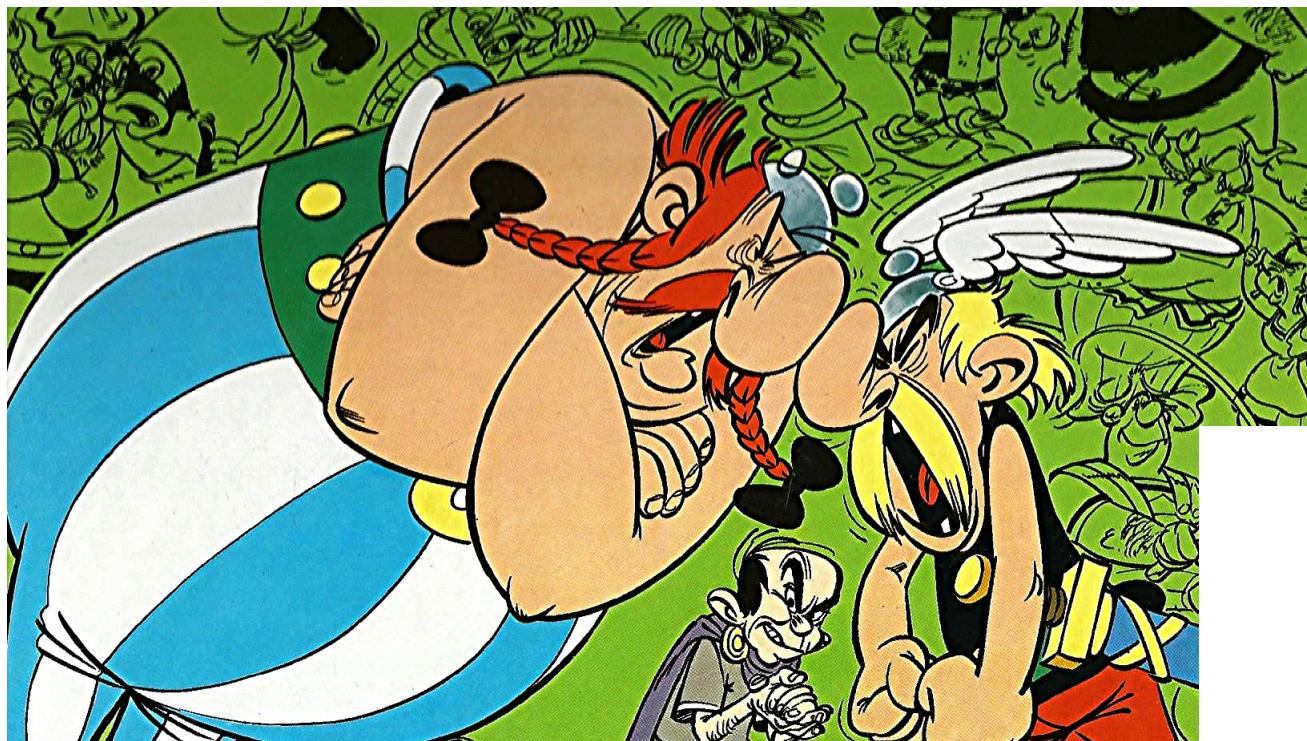
1^{er} Atomicity Problem (Solvable)



2nd Atomicity Problem (Impossible)

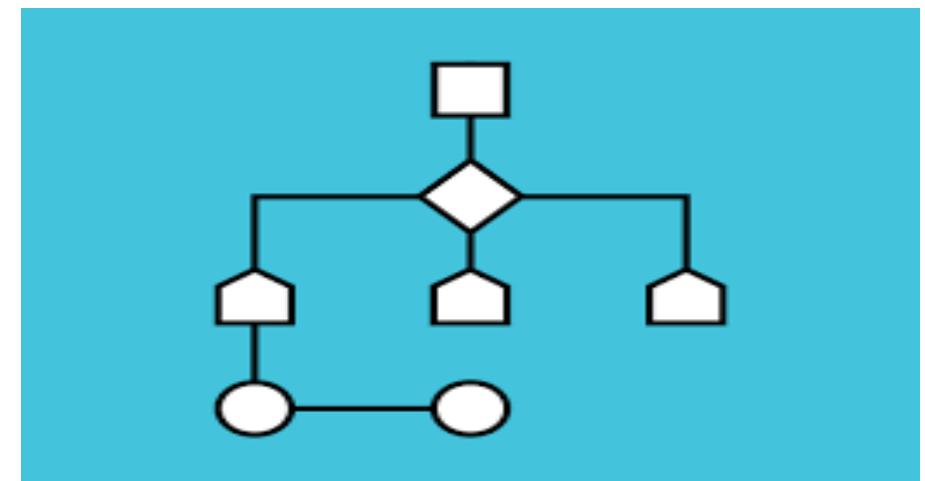
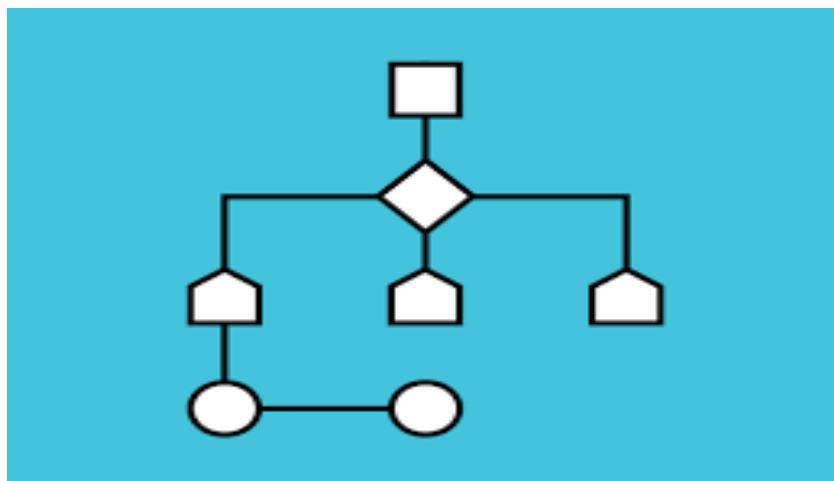


Impossibility of Consensus



What is an Algorithm? (Today)

- An ordered set of elementary instructions + communication instructions
- Executes on several Turing machines



Distributed Algorithms

- ↙ E. Dijkstra (concurrent os) ~60's
- ↙ L. Lamport: "a distributed system is one that stops your application because a machine you have never heard from crashed" ~70's
- ↙ J. Gray (transactions) ~70's
- ↙ N. Lynch (consensus) ~80's
- ↙ Birman, Schneider, Toueg – Cornell – (this course) ~90's

In short

- ➊ We study algorithms for ***distributed*** systems
- ➋ A new way of thinking about algorithms and their complexity

Important

- This course is complementary to the course (concurrent algorithms)
- We study here ***message passing*** based algorithms whereas the other course focuses on ***shared memory*** based algorithms

Overview

- ➊ (1) **Why?** Motivation
- ➋ (2) **Where?** Between the network and the application
- ➌ (3) **How?** (3.1) Specifications, (3.2) assumptions, and (3.3) algorithms

A Distributed System



A



B



C

Clients-Server



Client B



Client A



Server

Multiple Servers (genuine distribution)



Server A



Server B



Server C

Applications

- ➊ Traffic control
- ➋ Reservation systems
- ➌ Banking/Bitcoin
- ➍ Pretty much everything in the cloud

The Optimistic View

- ➊ Concurrency => speed (load-balancing)
- ➋ Partial failures => high-availability

The Pessimistic View

- Concurrency (interleaving) => incorrectness
- Partial failures => incorrectness

Distributed Algorithms

(Today: Google)

- ☞ Hundreds of thousands of machines connected
- ☞ A Google job involves 2000 machines
- ☞ 10 machines go down per day

Satoshi Nakamoto (2008) Nick Szabo

2009: 0.005 \$

2016: 600 \$

2017: 3000 \$

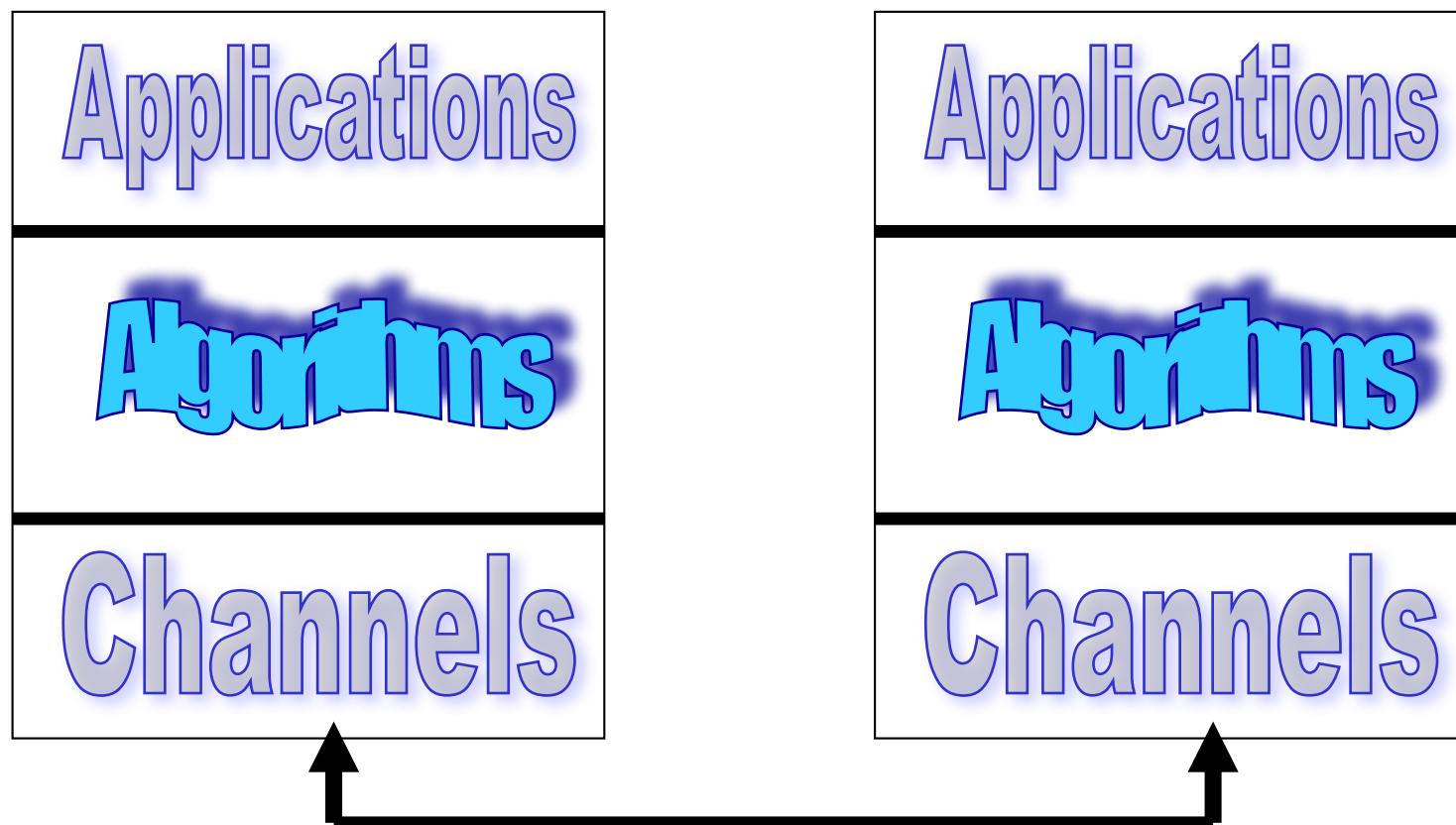
2018: 6000 \$



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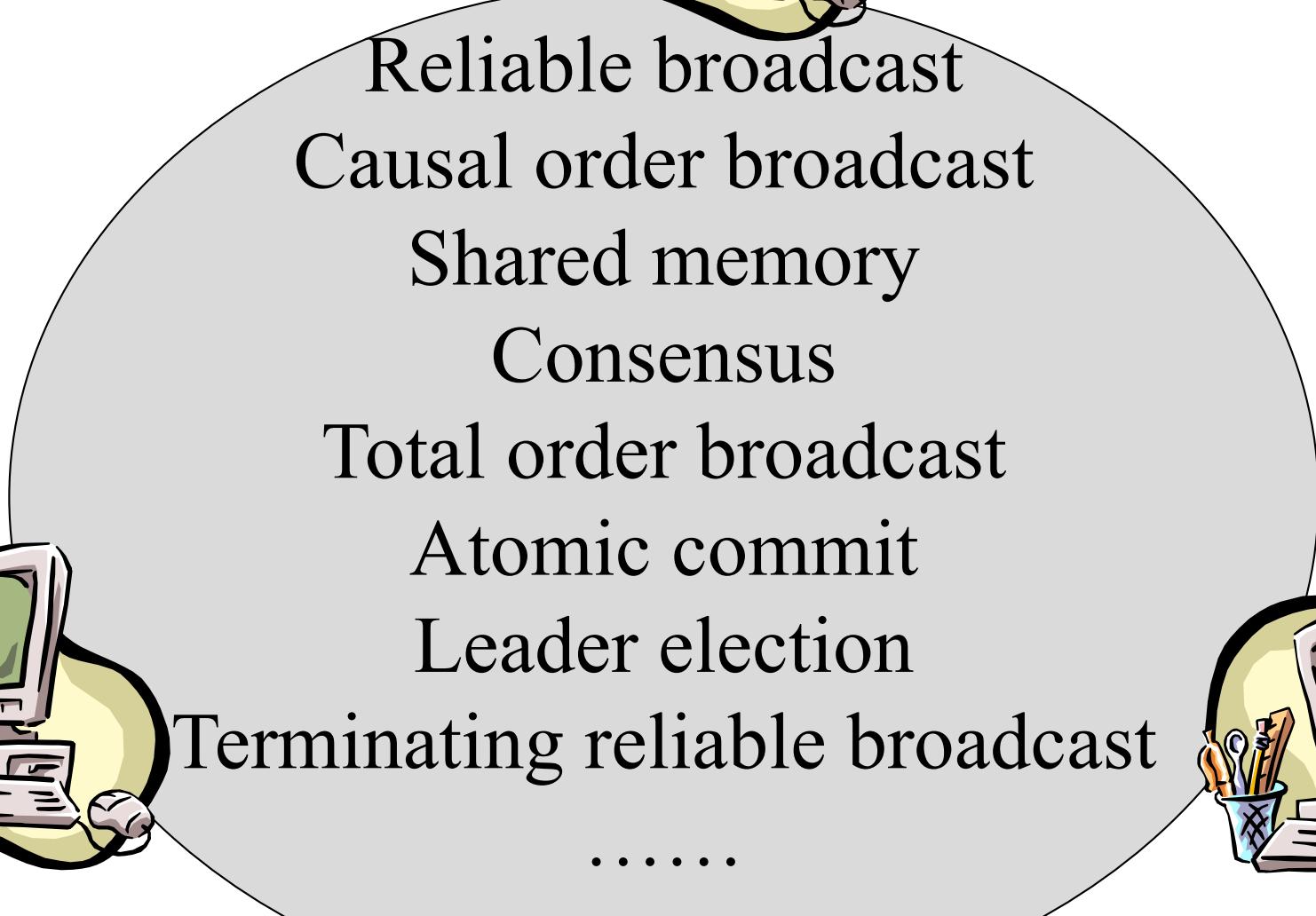
Distributed Systems



Distributed Systems

- ➊ The application needs underlying services for distributed interaction
- ➋ The network is not enough
 - ➌ Reliability guarantees (e.g., TCP) are only offered for communication among pairs of processes, i.e., *one-to-one* communication (*client-server*)

Content of this Course



- Reliable broadcast
- Causal order broadcast
- Shared memory
- Consensus
- Total order broadcast
- Atomic commit
- Leader election
- Terminating reliable broadcast

.....

Reliable Distributed Services

- ➊ Example 1: ***reliable broadcast***
 - ➋ Ensure that a message sent to a group of processes is received (delivered) by all or none
- ➋ Example 2: ***atomic commit***
 - ➋ Ensure that the processes reach a common decision on whether to commit or abort a transaction

Underlying Services

- ➊ (1): ***processes*** (abstracting computers)
- ➋ (2): ***channels*** (abstracting networks)
- ➌ (3): ***failure detectors*** (abstracting time)

Processes

- The distributed system is made of a finite set of processes: each process models a sequential program
- Processes are denoted by $p_1,..p_N$ or p, q, r
- Processes have unique identities and know each other
- Every pair of processes is connected by a link through which the processes exchange messages

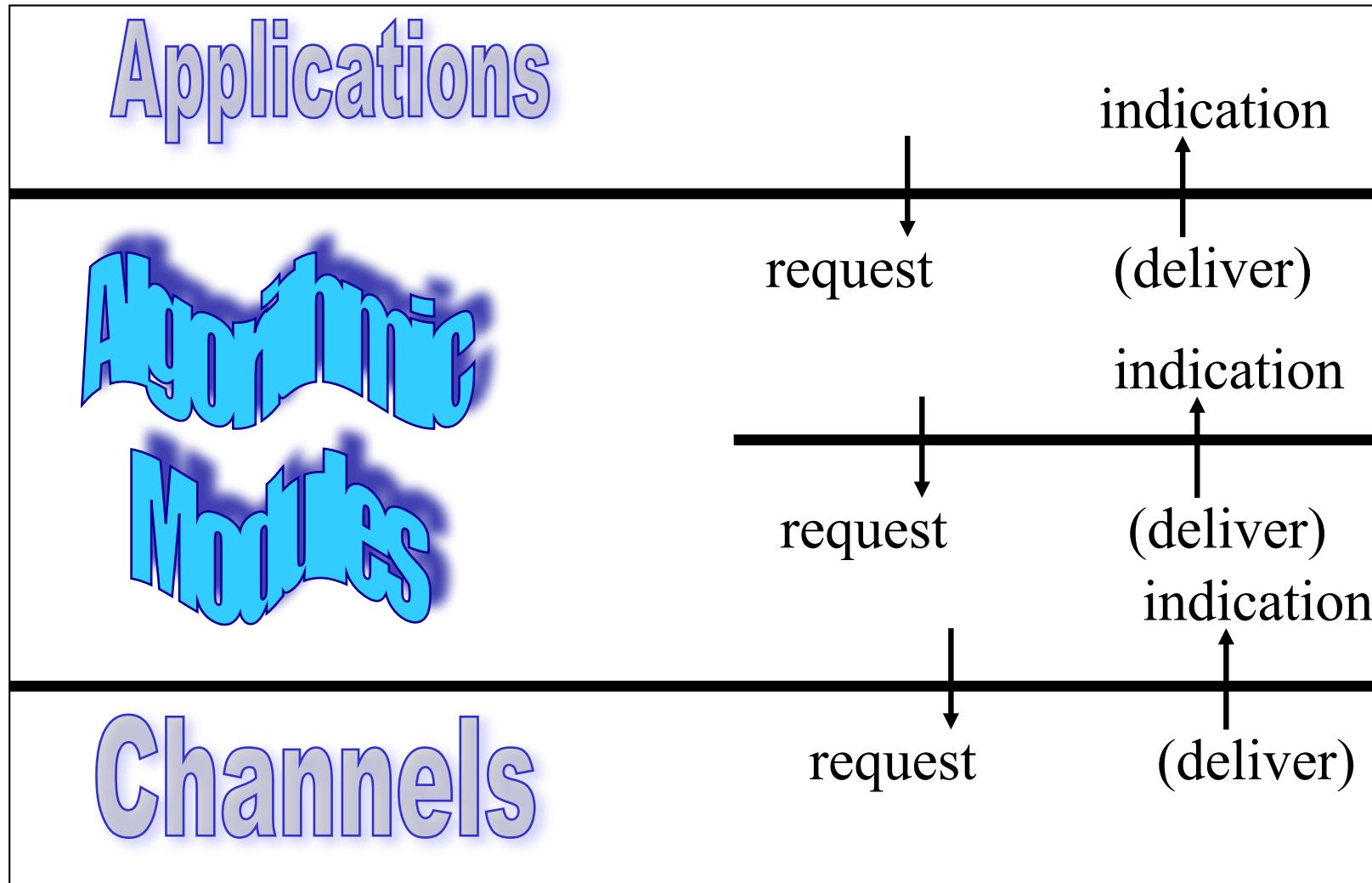
Processes

- ➊ A process executes a step at every tick of its local clock: a step consists of
 - ➋ A local computation (local event) and message exchanges with other processes (global event)
- ➋ NB. One message is delivered from/sent to a process per step

Processes

- ➊ The program of a process is made of a finite set of modules (or components) organized as a software stack
- ➋ Modules within the same process interact by exchanging events
- ➌ **upon event** < Event1, att1, att2,..> do
 - ➍ // something
 - ➎ **trigger** < Event2, att1, att2,..>

Modules of a Process



Overview

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Approach

- ➊ ***Specifications:*** What is the service?
i.e., the problem \sim liveness + safety
- ➋ ***Assumptions:*** What is the model, i.e.,
the power of the adversary?
- ➌ ***Algorithms:*** How do we implement the
service? Where are the bugs (proof)?
What cost?

Overview

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Liveness and Safety

- ➊ **Safety** is a property which states that nothing bad should happen
- ➋ **Liveness** is a property which states that something good should happen
- ➌ Any specification can be expressed in terms of liveness and safety properties (Lamport and Schneider)

Liveness and Safety

- ➊ Example: *Tell the truth*
- ➋ Having to say something is *liveness*
- ➌ Not lying is *safety*

Specifications

- ➊ Example 1: ***reliable broadcast***
 - ➋ Ensure that a message sent to a group of processes is received by all or none
- ➋ Example 2: ***atomic commit***
 - ➋ Ensure that the processes reach a common decision on whether to commit or abort a transaction

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 - ➍ 3.2.1 Assumptions on processes and channels
 - ➎ 3.2.2 Failure detection

Processes

- A process either executes the algorithm assigned to it (steps) or fails
 - Two kinds of failures are mainly considered:
 - ✓ **Omissions:** the process omits to send messages it is supposed to send (distracted)
 - ✓ **Arbitrary:** the process sends messages it is not supposed to send (malicious or Byzantine)
- Many models are in between

Processes

- ☞ ***Crash-stop:*** a more specific case of omissions
 - A process that omits a message to a process, omits all subsequent messages to all processes (permanent distraction): it crashes

Processes

- ➊ By default, we shall assume a ***crash-stop*** model throughout this course; that is, unless specified otherwise: processes fail only by crashing (no recovery)
- ➋ A ***correct*** process is a process that does not fail (that does not crash)

Processes/Channels

Processes communicate by message passing through communication channels

Messages are uniquely identified and the message identifier includes the sender's identifier

Fair-Loss Links

- ☞ **FL1. Fair-loss:** If a message is sent infinitely often by p_i to p_j , and neither p_i or p_j crashes, then m is delivered infinitely often by p_j
- ☞ **FL2. Finite duplication:** If a message m is sent a finite number of times by p_i to p_j , m is delivered a finite number of times by p_j
- ☞ **FL3. No creation:** No message is delivered unless it was sent

Stubborn Links

- ☞ ***SL1. Stubborn delivery:*** if a process p_i sends a message m to a correct process p_j , and p_i does not crash, then p_j delivers m an infinite number of times
- ☞ ***SL2. No creation:*** No message is delivered unless it was sent

Algorithm (sl)

- ☞ **Implements:** StubbornLinks (sp2p).
- ☞ **Uses:** FairLossLinks (flp2p).
- ☞ **upon event** < sp2pSend, dest, m> **do**
 - ☞ **while** (true) **do**
 - ☞ **trigger** < flp2pSend, dest, m>;
- ☞ **upon event** < flp2pDeliver, src, m> **do**
 - ☞ **trigger** < sp2pDeliver, src, m>;

Reliable (Perfect) Links

Properties

- **PL1. Validity:** If p_i and p_j are correct, then every message sent by p_i to p_j is eventually delivered by p_j
- **PL2. No duplication:** No message is delivered (to a process) more than once
- **PL3. No creation:** No message is delivered unless it was sent

Algorithm (pl)

- ☞ **Implements:** PerfectLinks (pp2p).
- ☞ **Uses:** StubbornLinks (sp2p).
- ☞ **upon event** < Init> **do** delivered := \emptyset ;
- ☞ **upon event** < pp2pSend, dest, m> **do**
 - ☞ **trigger** < sp2pSend, dest, m>;
- ☞ **upon event** < sp2pDeliver, src, m> **do**
 - ☞ **if** m \notin delivered **then**
 - ☞ **trigger** < pp2pDeliver, src, m>;
 - ☞ add m **to** delivered;

Reliable Links

- ➊ We shall assume reliable links (also called perfect) throughout this course (unless specified otherwise)
- ➋ Roughly speaking, reliable links ensure that messages exchanged between correct processes are not lost

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 - ➍ 3.2.1 Processes and links
 - ➎ **3.2.2 Failure Detection**

Failure Detection

- ➊ A ***failure detector*** is a distributed oracle that provides processes with suspicions about crashed processes
- ➋ It is implemented using (i.e., it encapsulates) ***timing assumptions***
- ➌ According to the timing assumptions, the suspicions can be accurate or not

Failure Detection

- ➊ A failure detector module is defined by events and properties
- ➋ ***Events***
 - ➌ Indication: <crash, p>
- ➌ ***Properties:***
 - ➍ Completeness
 - ➍ Accuracy

Failure Detection

Perfect:

- ⌚ *Strong Completeness:* Eventually, every process that crashes is permanently suspected by every correct process
- ⌚ *Strong Accuracy:* No process is suspected before it crashes

Eventually Perfect:

- ⌚ *Strong Completeness*
- ⌚ *Eventual Strong Accuracy:* Eventually, no correct process is ever suspected

Failure detection

Algorithm:

- ↙ (1) Processes periodically send heartbeat messages
- ↙ (2) A process sets a timeout based on worst case round trip of a message exchange
- ↙ (3) A process suspects another process if it timeouts that process
- ↙ (4) A process that delivers a message from a suspected process revises its suspicion and doubles its time-out

Timing Assumptions

Synchronous:

- ⌚ *Processing:* the time it takes for a process to execute a step is bounded and known
- ⌚ *Delays:* there is a known upper bound limit on the time it takes for a message to be received
- ⌚ *Clocks:* the drift between a local clock and the global real time clock is bounded and known

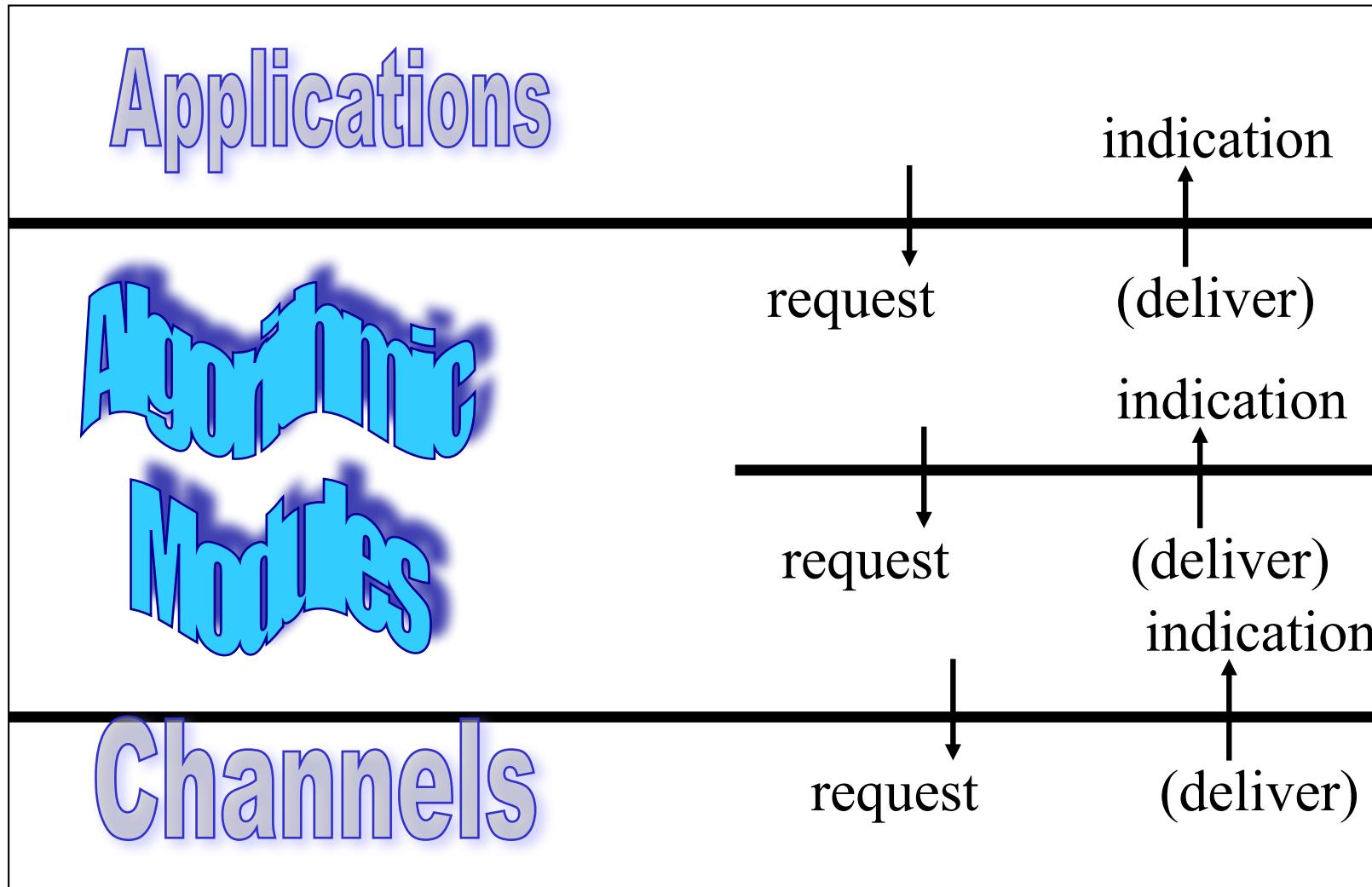
Eventually Synchronous: the timing assumptions hold eventually

Asynchronous: no assumption

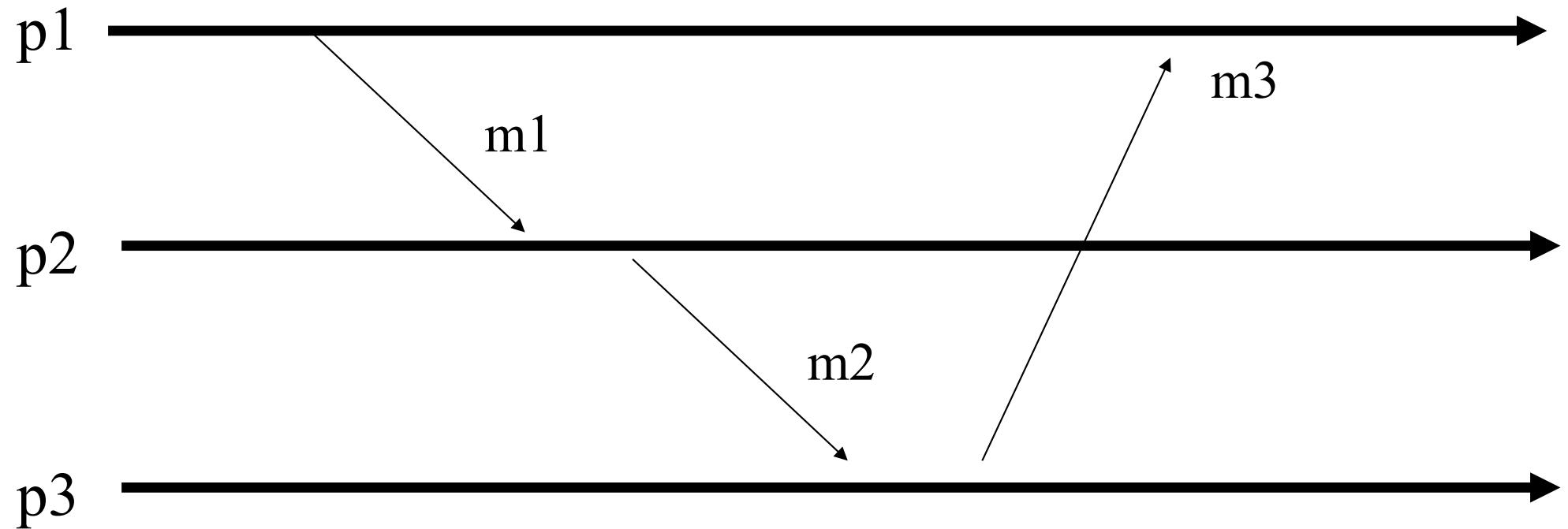
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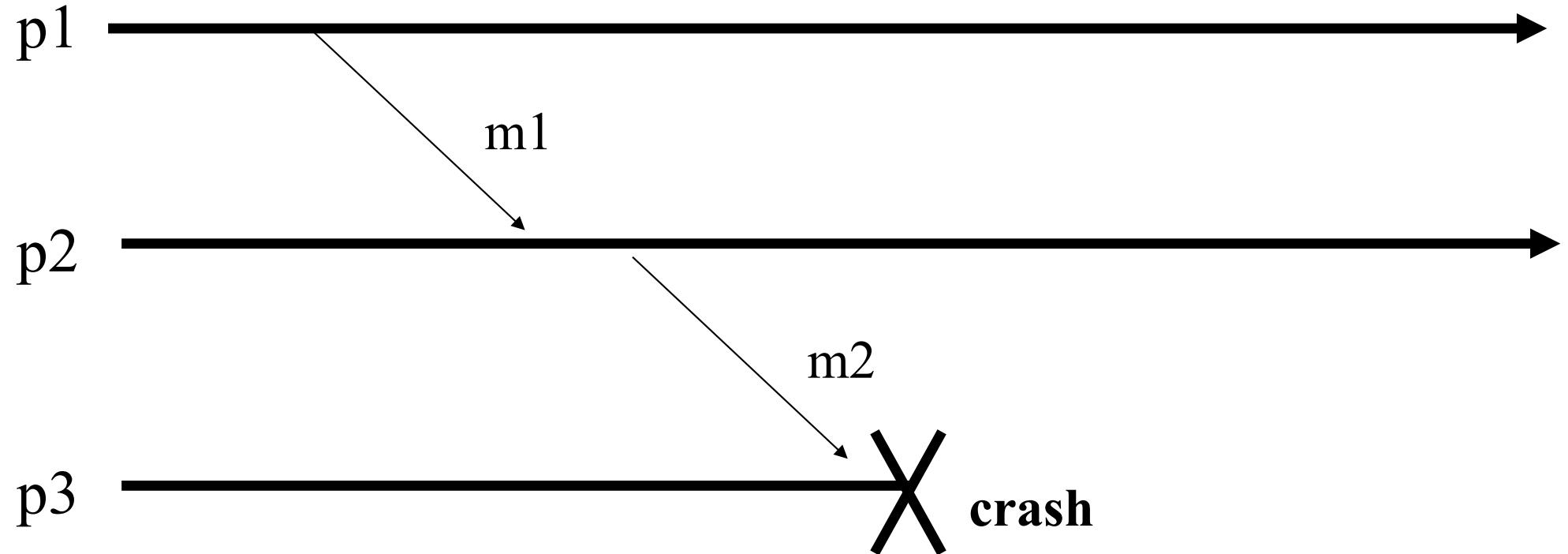
Algorithms Modules of a Process



Algorithms



Algorithms



For every Abstraction

- ↙ (A) We assume a crash-stop system with a perfect failure detector (fail-stop)
 - ↙ We give algorithms
- ↙ (B) We try to make a weaker assumption
 - ↙ We revisit the algorithms

Content of this Course

Reliable broadcast

Causal order broadcast

Shared memory

Consensus

Total order broadcast

Atomic commit

Leader election

Terminating reliable broadcast

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