Computer Lab 1

Martynas Lukosevicius, Alejo Perez Gomez, Zahra Jalil Pour

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Question 1 (Be Careful When Comparing)

1

 $\mathbf{2}$

Instead of writing if(x1 - x2 == 1/12) it should be written if(isTRUE(all.equal(x1-x2,1/12))). In this case this equation will return TRUE. We can use all.equal function, or we can use all.equal.numeric function too.

Question 2 (Derivative)

1

Write your own R function to calculate the derivative of f(x) = x in this way with $e = 10^-15$.

```
f <- function(x){
  return(x)
}

derivative <- function(x,e){
  return((f(x+e)-f(x))/e)
}</pre>
```

 $\mathbf{2}$

Evaluate your derivative function at x = 1 and x = 100000

```
e <- 10^(-15)
x <- 1
derivative(x,e)</pre>
```

```
## [1] 1.110223
```

```
e <- 10^(-15)
x <- 100000
derivative(x,e)</pre>
```

[1] 0

3

When x = 1, derivative = 1.110223 and when x = 100000, derivative = 0

However, true values for both cases should be 1.

The smallest positive computer number is epsilon that here we considered it to be10 $^(-15)$. When x=100000 the derivative function showed 0, in the equation((x+e)-x), the difference between large numbers dominates over epsilon, in other words the smallest positive number is added to the large number. Hence the epsilon would be ignored. However, when x=1, the effect of epsilon cannot be ignored the result would be 1.110223.

Question 3 (Variance)

1.

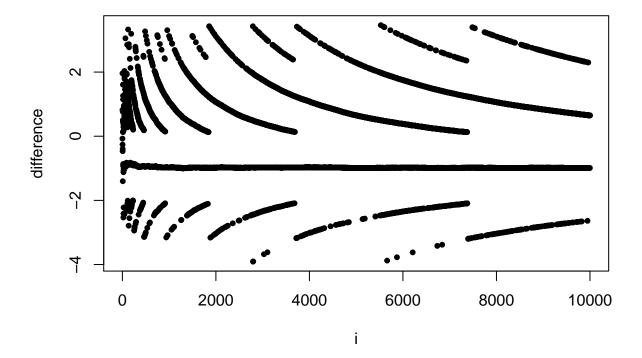
```
myvar <- function(x){
  n <- length(x)
  xSq <- sum(x^2)
  sumXSq <- sum(x)^2
  part2 <- sumXSq/n
  return((xSq - part2)* (1/(n-1)))
}</pre>
```

 $\mathbf{2}$

```
x <- rnorm(10000, 10<sup>8</sup>, 1)
```

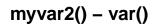
3

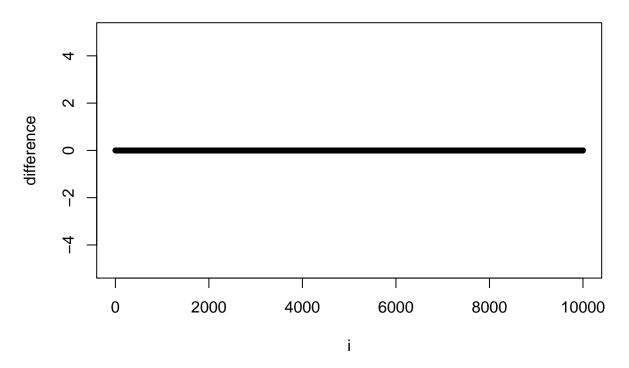
myvar() - var()



The function does not work properly. It oscillates primarily when a smaller set of values is involved in the variances calculation. It can also be noted that the oscillation pattern in the produced response (myVar(Xi) - var(Xi)) decreases as the value of terms involved increases. Squaring big numbers result in overflow, since the computer is not able to handle such a large number correctly. That is because the numbers are so big that the computer cannot destine the right amount of bytes for them. Moreover, first squaring and summing might be less than first summing and later squaring. This is why our function will not produce correct answers.

4





Question 4 (Binomial coeficient)

1

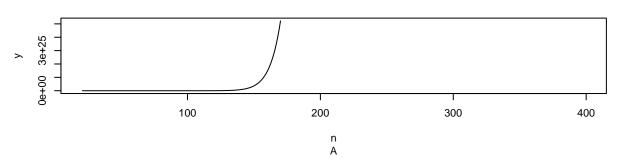
A: n , k and n - k cant be zero

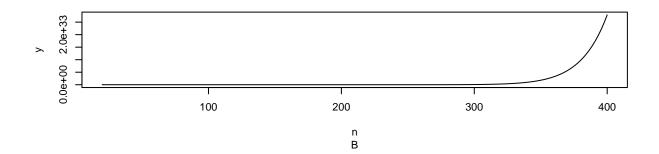
B: n and n - k cant be zero

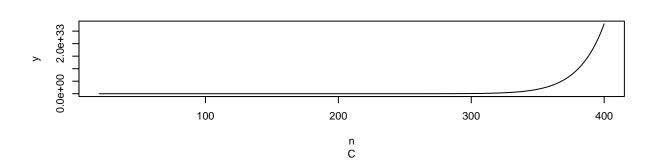
C: same as B

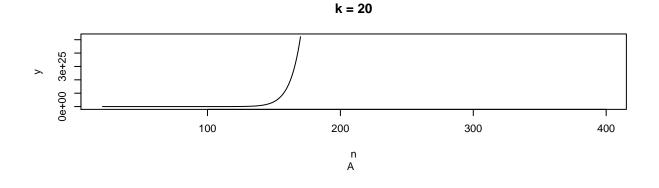
because prod(0) = 0 and 0 / 0 will be NaN

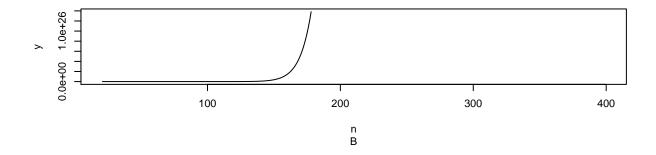


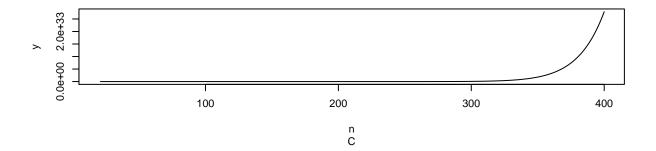












3

The expressions A and B, because with large numbers method prod() will overflow.

In expression A we calculate product of vector from 1 to n and later divide it by other products with smaller vectors. However in this case first operation (prod(1:n)) will overflow (= Inf) and other operations won't matter as the result will be Inf or Nan (if denominator will be also Inf).

In expression B overflow will depend on k, if k is close to n it won't overflow.

In expression C, as first vectors are divided, the final vector for product will have smaller values and that is why prod() method won't overflow.

Appendix

```
#1
# all.equal.numeric() and isTRUE() function
x1 < -1/3
x2 < -1/4
if (isTRUE(all.equal.numeric(x1-x2, 1/12))) {
  print ("Subtraction is correct" )
} else {
 print ("Subtraction is wrong")
#2
f <- function(x){</pre>
 return(x)
derivative <- function(x,e){</pre>
  return((f(x+e)-f(x))/e)
e < 10^{(-15)}
x <- 1
derivative(x,e)
e <- 10<sup>(-15)</sup>
x <- 100000
derivative(x,e)
#3
myvar <- function(x){</pre>
 n <- length(x)
  xSq \leftarrow sum(x^2)
  sumXSq <- sum(x)^2
  part2 <- sumXSq/n</pre>
  return((xSq - part2)* (1/(n-1)))
x <- rnorm(10000, 10<sup>8</sup>, 1)
result <- list()</pre>
options(digits = 22 )
for (i in 1:length(x)) {
 temp <- x[1:i]
 y <- myvar(temp) - var(temp)
  result <- append(result, y)</pre>
plot(c(1:length(x)), result, main = "myvar() - var()",
     xlab = "i",type = "p", pch = 20 , ylab = "difference")
```

```
myvar2 <- function(x){</pre>
 n \leftarrow length(x)
  return((sum((x - mean(x))^2))/(n-1))
result <- list()
options(digits = 22 )
for (i in 1:length(x)) {
  temp \leftarrow x[1:i]
 y <- myvar2(temp) - var(temp)
 result <- append(result, y)</pre>
plot(c(1:length(x)), result, main = "myvar2() - var()", xlab = "i",type = "p",
     pch = 20, ylab = "difference", ylim = c(-5,5))
#4
n <- 0
k <- 0
prod(1:n) / (prod(1:k) * prod(1:(n-k)))
prod((k+1):n) / prod(1:(n-k))
prod(((k+1):n) / (1:(n-k)))
#n < - c(20:100)
calc1 <- function(n,k){</pre>
k \leftarrow n - k
return(prod(1:n) / (prod(1:k) * prod(1:(n-k))))
calc2 <- function(n,k){</pre>
 k <- n - k
return(prod((k+1):n) / prod(1:(n-k)))
calc3 <- function(n,k){</pre>
 k <- n - k
return(prod(((k+1):n) / (1:(n-k))))
n < -c(20:400)
k <- 20
y \leftarrow sapply(n, calc1, k = k)
y2 \leftarrow sapply(n, calc2, k = k)
y3 \leftarrow sapply(n, calc3, k = k)
par(mfrow=c(3,1))
plot(n,y, type = "l", main = "k = n - 20", sub = "A", ylab = "y")
plot(n,y2, type = "l", sub = "B", ylab = "y")
plot(n, y3, type = "1", sub = "C" , ylab = "y")
calc1 <- function(n,k){</pre>
return(prod(1:n) / (prod(1:k) * prod(1:(n-k))))
```

```
} calc2 <- function(n,k){
    return(prod((k+1):n) / prod(1:(n-k)))
}
calc3 <- function(n,k){
    return(prod(((k+1):n) / (1:(n-k))))
}

n <- c(20:400)
k <- 20

y <- sapply(n, calc1, k = k)
    y2 <- sapply(n, calc2, k = k)
    y3 <- sapply(n, calc3, k = k)
    par(mfrow=c(3,1))

plot(n,y, type = "l", main = "k = 20", sub = "A " , ylab = "y")
    plot(n,y2, type = "l", sub = "B", ylab = "y")
    plot(n, y3, type = "l", sub = "C", ylab = "y")
</pre>
```