Computer Lab 1

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Question 1 (Be Careful When Comparing)

1

 $\mathbf{2}$

Instead of writing if(x1 - x2 == 1/12) it should be written if(isTRUE(all.equal(x1-x2,1/12))). In this case this equation will return TRUE. We can use all.equal function, or we can use all.equal.numeric function too.

Question 2 (Derivative)

1

Write your own R function to calculate the derivative of f(x) = x in this way with $e = 10^-15$.

```
derivative <- function(x,e){
  f <- function(x){
   return(x)
}
  return((f(x+e)-f(x))/e)
}</pre>
```

 $\mathbf{2}$

Evaluate your derivative function at x = 1 and x = 100000

```
e <- 10^(-15)
x <- 1

derivative(x,e)

## [1] 1.110223

e <- 10^(-15)
x <- 100000

derivative(x,e)</pre>
```

```
## [1] 0
```

3

when x = 1, derivative = 1.110223, when x = 100000, derivative = 0

However, true values for both cases should be 1.

The smallest positive computer number is epsilon that here we considered it 10^{-15} When x=100000 the derivative function showed 0, in equation((x+e)-x), difference between large numbers dominates epsilon, in other words the smallest positive number is added to the large number. Hence the epsilon would be ignored. But when x=1, the effect of epsilon can not be ignored the result would be 1.110223.

Question 3 (Variance)

1

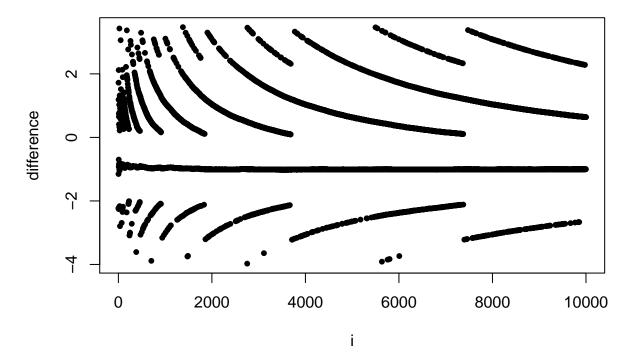
```
myvar <- function(x){
  n <- length(x)
  xSq <- sum(x^2)
  sumXSq <- sum(x)^2
  part2 <- sumXSq/n
  return((xSq - part2)* (1/(n-1)))
}</pre>
```

2

```
x <- rnorm(10000, 10<sup>8</sup>, 1)
```

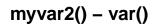
3

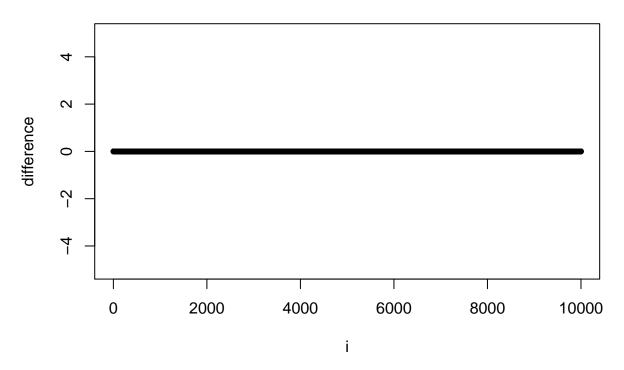
myvar() - var()



The function does not work good. It can be noted that the oscillation pattern in the produced response (myVar(Xi) - var(Xi)) decreases as the value of terms involved increases. Squaring big numbers result in losing precision (point). As a result first squaring and summing might be less than first summing and later squaring. that is why function will not produce correct answers.

4





Question 4 (Binomial coeficient)

1

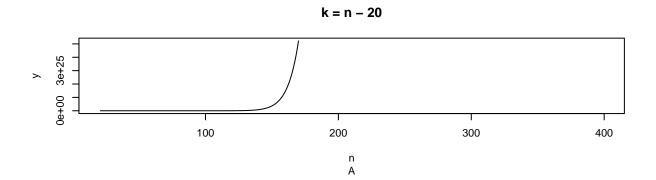
A: n, k and n - k cant be zero

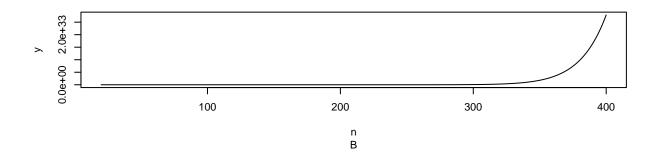
B: n and n - k cant be zero

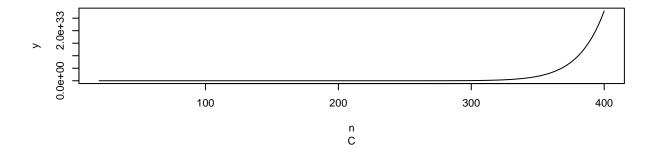
C: same as B

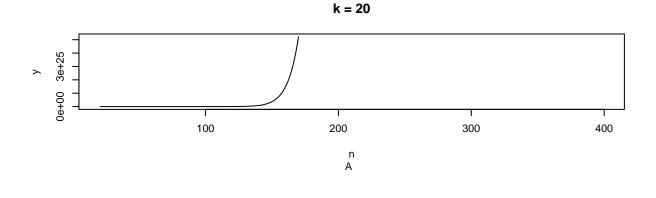
because prod(0) = 0 and 0 / 0 will be NaN

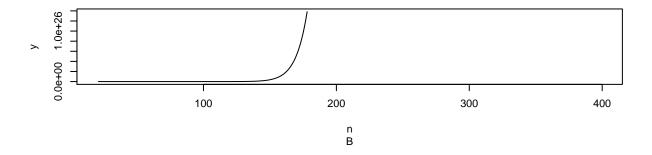
 $\mathbf{2}$

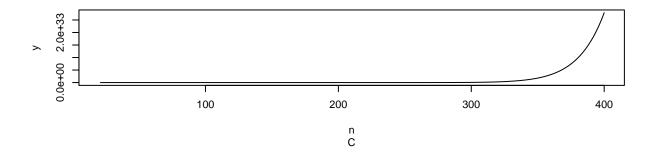












3

expression A and B, because with large numbers method prod() will overflow.

In expression A we calculate product of vector from 1 to n and later divide it by other products with smaller vectors. However in this case first operation (prod(1:n)) will overflow (=Inf) and other operations wont matter as the result will be Inf or Nan (if denominator will be also Inf).

In expression B overflow will depend on k, if k is close to n it wont overflow.

In expression C, as first vectors are divided, the final vector for product will have smaller values and that is why prod() method wont overflow.