Pagerank mit Markov-Chains

Severin Kaderli Marius Schär

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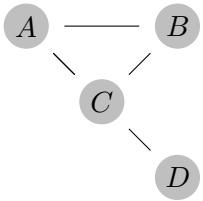
Material

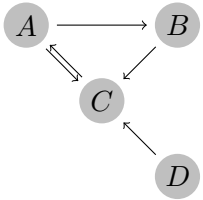
markov.mariusschaer.ch Link

Markov Chains

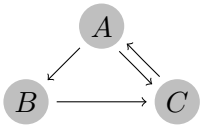
The PageRank example



Manual



Graph



There's nothing here:

PageRank Formula

$$PR(X) = (1 - d) + d(\frac{PR(T_1)}{C(T_1)} + ... + \frac{PR(T_n)}{C(T_n)})$$

Table

Iteration	$PR(A)$	$PR(B)$	$PR(C)$
0	1	1	1
1	1	0.75	1.125
2	1.0625	0.7656	1.1484
⋮	⋮	⋮	⋮
12	1.0769	0.7692	1.1538

System of Equations

$$\left|\begin{array}{rcrcrcl} x & & & - & 0.5z & = & 0.5 \\ - & 0.25x & & & & = & 0.5 \\ - & 0.25x & - & 0.5y & + \quad z & = & 0.5 \end{array}\right|$$

Probability Matrix

$$\text{Probability Matrix } A = \begin{array}{c} \\ A \\ B \\ C \end{array} \begin{array}{c} \begin{array}{ccc} A & B & C \end{array} \\ \begin{pmatrix} 0 & 0.5 & 0.5 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix} \end{array}$$

Equations

$V =$ PageRank Vektor

$\lambda =$ Eigenwert. Immer 1 bei Markov-Matricies

$$A \cdot V = \lambda \cdot V$$

$$\downarrow$$

$$\begin{bmatrix} 0 & 0.5 & 0.5 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{bmatrix} \cdot \begin{vmatrix} x \\ y \\ z \end{vmatrix} = \begin{vmatrix} x \\ y \\ z \end{vmatrix}$$

Solving

$$\begin{bmatrix} -1 & 0.5 & 0.5 \\ 0 & -1 & 1 \\ 1 & 0 & -1 \end{bmatrix} = A - \lambda \cdot E \rightarrow A - 1 \cdot E$$

Solving

$$\left[\begin{array}{ccc|c} -1 & 0.5 & 0.5 & 0 \\ 0 & -1 & 1 & 0 \\ 1 & 0 & -1 & 0 \end{array}\right] = A - \lambda \cdot E \rightarrow A - 1 \cdot E$$