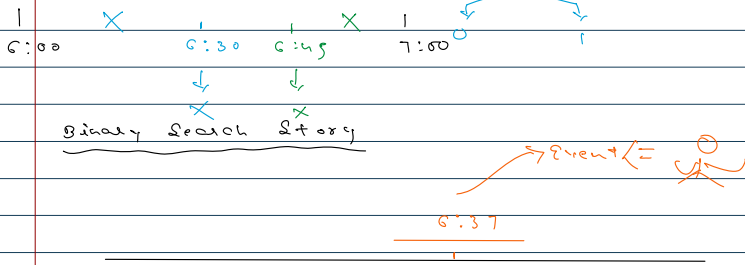
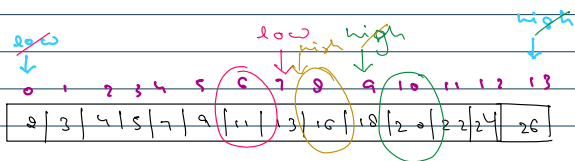
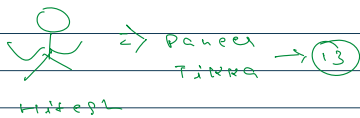
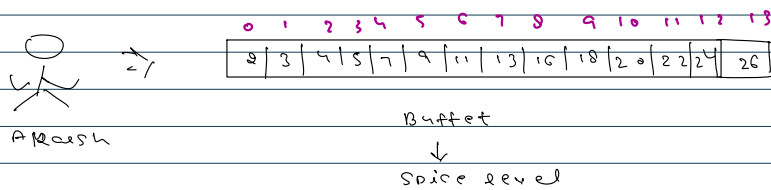


Searching algorithms

- Linear (Sequential)
- Binary search



It is an algorithm for finding an element in a sorted array by dividing the search range in half.



$$\text{mid} = \frac{\text{low} + \text{high}}{2}$$

$$\text{low} \rightarrow 0 \quad \text{mid} + 1 \rightarrow 6 + 1 \rightarrow 7$$

$$\text{high} \rightarrow 13 \quad \text{mid} - 1 \rightarrow 10 - 1 \rightarrow 9$$

$$\text{key} \rightarrow 13$$

$$\text{mid} - 1 \Rightarrow 9$$

$$\frac{\text{mid} = (0 + 13)}{2} = 6 \quad \text{arr[mid]} < \text{key}$$

$$11 < 13$$

$$\text{if (arr[mid] == key)}$$

$$\text{return mid;}$$

$$\text{else if (arr[mid] > key)} \quad \text{high} = \text{mid} - 1 \quad \} \rightarrow \text{1st array}$$

$$\text{else if (arr[mid] < key)} \quad \text{low} = \text{mid} + 1; \quad \} \rightarrow \text{2nd array}$$

$$\text{low} = 7 \quad \text{mid} = \frac{(7 + 13)}{2} \quad \text{arr[mid]} > \text{key}$$

$$\text{high} = 13 \quad 20 > 13$$

$$\text{mid} = 10$$

$$\text{low} = 7 \quad \text{mid} = \frac{(7 + 9)}{2} \quad \text{arr[mid]} > \text{key}$$

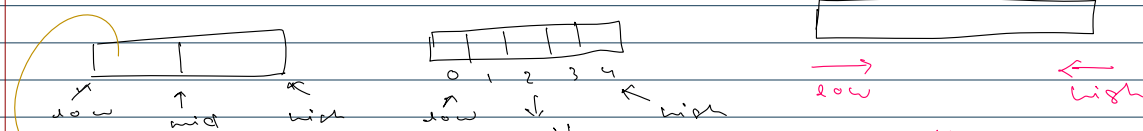
$$\text{high} = 9 \quad 16 > 13$$

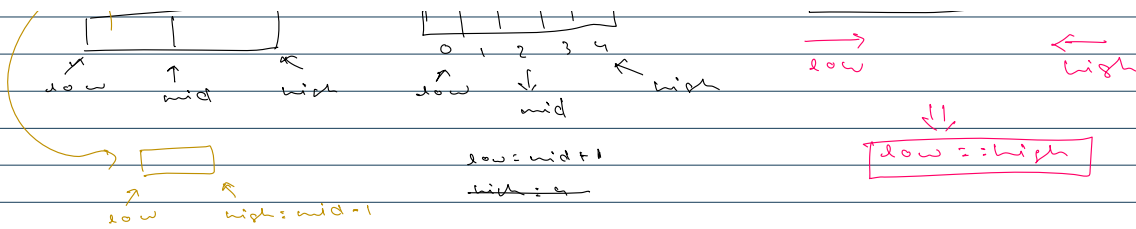
$$\text{mid} = 8$$

$$\text{low} = 7 \quad \text{mid} = \frac{(7 + 7)}{2} \quad \text{arr[mid]} = \text{key}$$

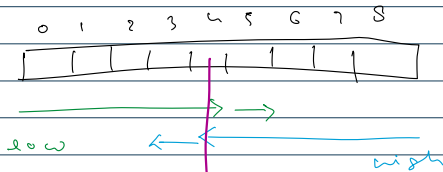
$$\text{high} = 7 \quad 13 = 13$$

$$\text{mid} = 7$$





Exit condition \Rightarrow while (low <= high)



$low == high \Rightarrow low < high \Rightarrow low \leq high$

// "static void main" must be defined in a public class.

```
public class Main {
    public static void main(String[] args) {

        int[] arr = {2, 3, 4, 5, 6, 7, 8, 11, 13, 16, 17};
        int item = 13;
        System.out.println(binarySearch(arr, item));
    }
}
```

```
public static int binarySearch(int[] arr, int item){
    int n = arr.length;
    int low = 0;
    int high = n-1;

    while(low <= high){

        int mid = (low+high)/2;

        if(arr[mid] == item){
            return mid;
        }
        else if(arr[mid] > item){
            high = mid - 1;
        }
        else if(arr[mid] < item){
            low = mid + 1;
        }
    }

    return -1;
}
```

How to identify when to use Binary Search

1. array sorted \Rightarrow asc, desc.

1. array sorted \Rightarrow asc, desc.
2. data is static
3. less insertion/deletion

Find the floor of the kth root

$x^3 \leq 149 \Rightarrow$ find largest value of x

$$\begin{array}{lcl} 5^3 = 125 & \leq 149 & \checkmark \Rightarrow x=5 \\ 6^3 = 216 & > 149 & \times \end{array}$$

$$x^k \leq n$$

$k \rightarrow$ power
 $n \rightarrow$ number
 find x ?

$\left. \begin{array}{l} \text{Input} \\ \text{Output} \end{array} \right\}$

```

public class Main {
    public static void main(String[] args) {

        int n = 149;
        int k = 3;
        System.out.println(kthRootLinear(n, k));
    }

    public static int kthRootLinear(int n, int k){
        int ans = 0;

        for(int i=1; i<=n; i++){
            double power = Math.pow(i, k);

            if(power <= n){
                ans = i;
            }
            else{
                break;
            }
        }
        return ans;
    }
}
  
```

Binary search solution

$x^3 \leq 149 \Rightarrow x \rightarrow ?$

n | low | $high$ | mid | ans
 1 | 1 | 149 | 75 |
 1 | 36 | 74 | 75 |
 $mid = (1+149)/2 = 75$
 $75^3 \leq 149 \rightarrow \times$
 $75^3 > 149 \rightarrow \checkmark$
 $low = mid + 1$
 $mid = (1+74)/2 = 37$
 $37^3 \leq 149 \rightarrow \times$

$low = 1$
 $high = 149$
 $mid = 36$

```

if (mid^k <= n) {
    ans = mid;
    low = mid + 1;
}
  
```

$n = 149$

$<$

$75^3 > 149 \rightarrow \checkmark$

$ans = mid$;
 $low = mid + 1$;

$l = 1$ $m = \frac{(1+74)}{2} = 37$
 $n = 74$

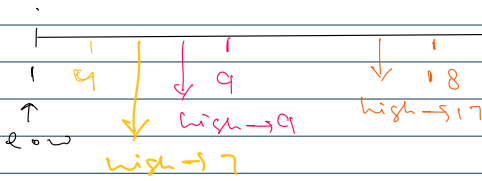
$37^3 \leq 149 \rightarrow \times$
 $37^3 > 149 \rightarrow \checkmark$

}

else {

$high = mid - 1$;

}



$l = 1$ $m = \frac{(1+36)}{2} = 18$
 $n = 36$

$18^3 \leq 149 \rightarrow \times$
 $18^3 > 149 \rightarrow \checkmark$

$l = 1$ $h = 36$
 $h = 17$ $h = 8$ $h = 4$ $h = 3$ $h = 1$

$ans = 1$

$l = 1$ $m = \frac{(1+17)}{2} = 9$
 $n = 17$

$9^3 \leq 149 \rightarrow \times$
 $9^3 > 149 \rightarrow \checkmark$

$l = 1$ $m = \frac{(1+8)}{2} = 4$
 $n = 8$

$4^3 \leq 149 \rightarrow \checkmark$

$l = 5$ $m = \frac{(5+8)}{2} = 6$
 $n = 8$

$6^3 \leq 149 \rightarrow \times$
 $6^3 > 149 \rightarrow \checkmark$

$l = 5$ $m = \frac{(5+5)}{2} = 5$
 $n = 5$

$5^3 < 149 \rightarrow \checkmark$

```
public class Main {  
    public static void main(String[] args) {  
        int n = 149;  
        int k = 3;  
        System.out.println(kthRootLinear(n, k));  
        System.out.println(kthRootBinary(n, k));  
    }  
}
```

```
public static int kthRootLinear(int n, int k){  
    int ans = 0;
```

```
    for(int i=1; i<=n; i++){  
        double power = Math.pow(i, k);
```

```
        if(power <= n){  
            ans = i;
```

```
        }  
        else{  
            break;
```

```
        }  
    }  
    return ans;
```

```
}  
  
public static int kthRootBinary(int n, int k){  
    int ans = 0;  
    int low = 1;
```

```
int high = n;
```

```
while(low <= high){  
    int mid = (low + high) / 2;  
    if(Math.pow(mid, k) <= n){  
        ans = mid;  
        low = mid + 1;  
    }  
    else{  
        high = mid - 1;  
    }  
}  
return ans;
```

```
}
```

```
}
```

278. First Bad Version

Solved ✓

Easy Topics Companies

You are a product manager and currently leading a team to develop a new product. Unfortunately, the latest version of your product fails the quality check. Since each version is developed based on the previous version, all the versions after a bad version are also bad.

Suppose you have n versions $[1, 2, \dots, n]$ and you want to find out the first bad one, which causes all the following ones to be bad.

You are given an API `bool isBadVersion(version)` which returns whether `version` is bad. Implement a function to find the first bad version. You should minimize the number of calls to the API.

Example 1:

Input: $n = 5$, $bad = 4$

Output: 4

Explanation:

call `isBadVersion(3)` → false

call `isBadVersion(5)` → true

call `isBadVersion(4)` → true

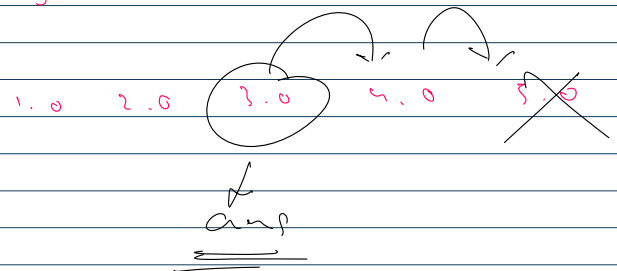
Then 4 is the first bad version.

Example 2:

Input: $n = 1$, $bad = 1$

Output: 1

Rajesh



$n = 5$



low: 1
high: 5

$$l = 1 \quad m = \frac{(1 + 5)}{2} = 3$$
$$h = 5$$

```
mid = (low + high) / 2  
if (isBadVersion(mid)) {  
    ans = mid;  
    high = mid - 1;  
}  
else {  
    low = mid + 1;  
}
```

manager
leq
manager
[isBadVersion]

constraint

$$1 \leq \text{bad} \leq n \leq 2^{31} - 1$$

$$\text{max value of } n = 2^{31} - 1$$

$$l = 2^{31} - 6$$

$$\text{mid} = \frac{\text{low} + \text{high}}{2} = \frac{2^{31} - 6 + 2^{31} - 1}{2}$$

$$h = 2^{31} - 1$$

$$2$$

$$= \frac{2^{31} + 2^{31} - 7}{2}$$

$$2^2 + 2^2 = 2^3$$

$$\downarrow$$
$$2 \cdot (2^2) = 2^3$$

$$= \frac{\begin{matrix} 32 \\ 2 \end{matrix}}{2} \rightarrow \text{out of range}$$

$$\text{mid} = \frac{\text{low} + (\text{high} - \text{low})}{2}$$

$$\frac{2 \cdot \text{low} + \text{high} - \text{low}}{2} = \frac{\text{low} + \text{high}}{2}$$

/* The isBadVersion API is defined in the parent class VersionControl.

boolean isBadVersion(int version); */

public class Solution extends VersionControl {

public int firstBadVersion(int n) {

int low = 1;

int high = n;

int ans = -1;

while(low <= high){

// int mid = (low+high)/2;

int mid = low + (high-low)/2;

// int mid = low/2 + high/2; // -->X

if(isBadVersion(mid)){

ans = mid;

high = mid-1;

}

else{

low = mid + 1;

}

}

return ans;

}

}