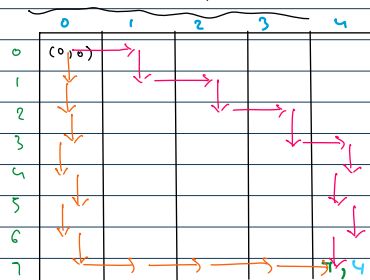


## Grid Path finder



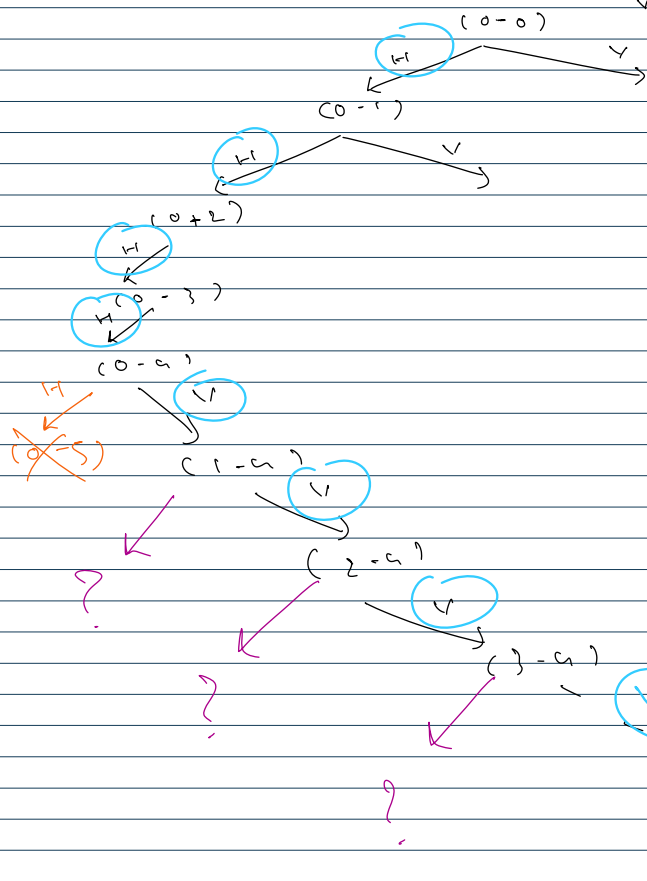
move  $\begin{cases} \rightarrow \text{right (horizontally)} \\ \rightarrow \text{down (vertically)} \end{cases}$

V H V H V H V H H H H H  
H H H H H H H H V V V V

H and V  
should be swapped  
omission

options  $\rightarrow$  movement  $\begin{cases} \rightarrow \text{right} \\ \rightarrow \text{down} \end{cases} \rightarrow \text{choices} \rightarrow \text{decision} \rightarrow \text{Recursion}$

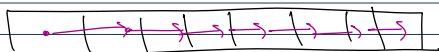
H  $\rightarrow$  col + 1  
V  $\rightarrow$  row + 1



H H H H V V V V

final destination

Grid  $\rightarrow$



H H H H H H H H

```
public class Main {
    public static void main(String[] args) {
        int n = 1; // rows -> r
        int m = 7; // cols -> c

        int cr = 0; // current row
        int cc = 0; // current col

        String ans = "";
        paths(n-1, m-1, cr, cc, ans);
    }
}
```

```
public static void paths(int r, int c, int cr, int cc, String ans){
    if(r==cr && c==cc){
        System.out.println(ans + " STOP");
        return;
    }
}
```

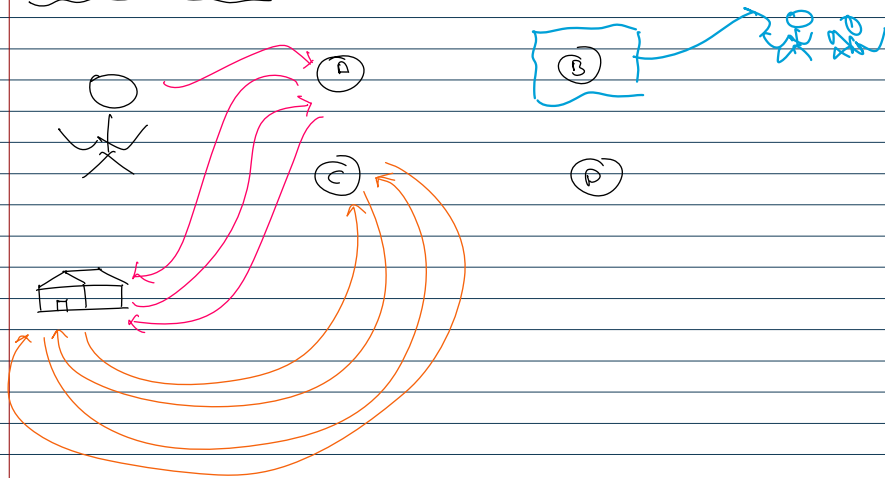
1 2 3 4 5

```

}
if(cr > r || cc > c){
    return;
}
paths(r, c, cr, cc+1, ans + "H->");
paths(r, c, cr+1, cc, ans + "V->");
}
}

```

### Backtracking



### Queen Permutation

arrangement matters

$n=4$   
 $q_2=2$   
 $a_0$   $b_0$   $b_1$   $b_2$   $b_3$

$a_1$   $a_0$   
 $a_0$   $a_1$   
 $b_0$   $b_1$

$a_1$   $a_0$   
 $a_0$   $a_1$   
 $b_1$   $b_2$

$a_1$   $a_0$   
 $a_0$   $a_1$   
 $b_0$   $b_2$

$a_1$   $a_0$   
 $a_0$   $a_1$   
 $b_1$   $b_3$

$a_1$   $a_0$   
 $a_0$   $a_1$   
 $b_0$   $b_3$

$a_1$   $a_0$   
 $a_0$   $a_1$   
 $b_2$   $b_3$

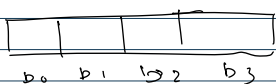
Combinations =  ${}^4C_2 = 6$

Permutations =  ${}^4P_2 = 12$



$\begin{cases} A B C \\ B A C \\ C A B \\ A C B \\ B C A \\ C B A \end{cases} \Rightarrow 3!$   
 $\sim 1$

Combinations  $\times$   $q!$   
 Permutations



accept  $\begin{cases} \rightarrow a_0 \\ \rightarrow a_1 \end{cases}$

### Combinations

$\begin{cases} a_0 & a_1 \\ b_0 & b_1 \end{cases}$

$\begin{cases} a_0 & a_1 \\ b_1 & b_2 \end{cases}$

2 permutations

$\begin{cases} a_0 & a_1 \\ b_0 & b_2 \end{cases}$

$\begin{cases} a_0 & a_1 \\ b_1 & b_3 \end{cases}$

$\begin{cases} a_0 & a_1 \\ b_0 & b_1 \end{cases}$

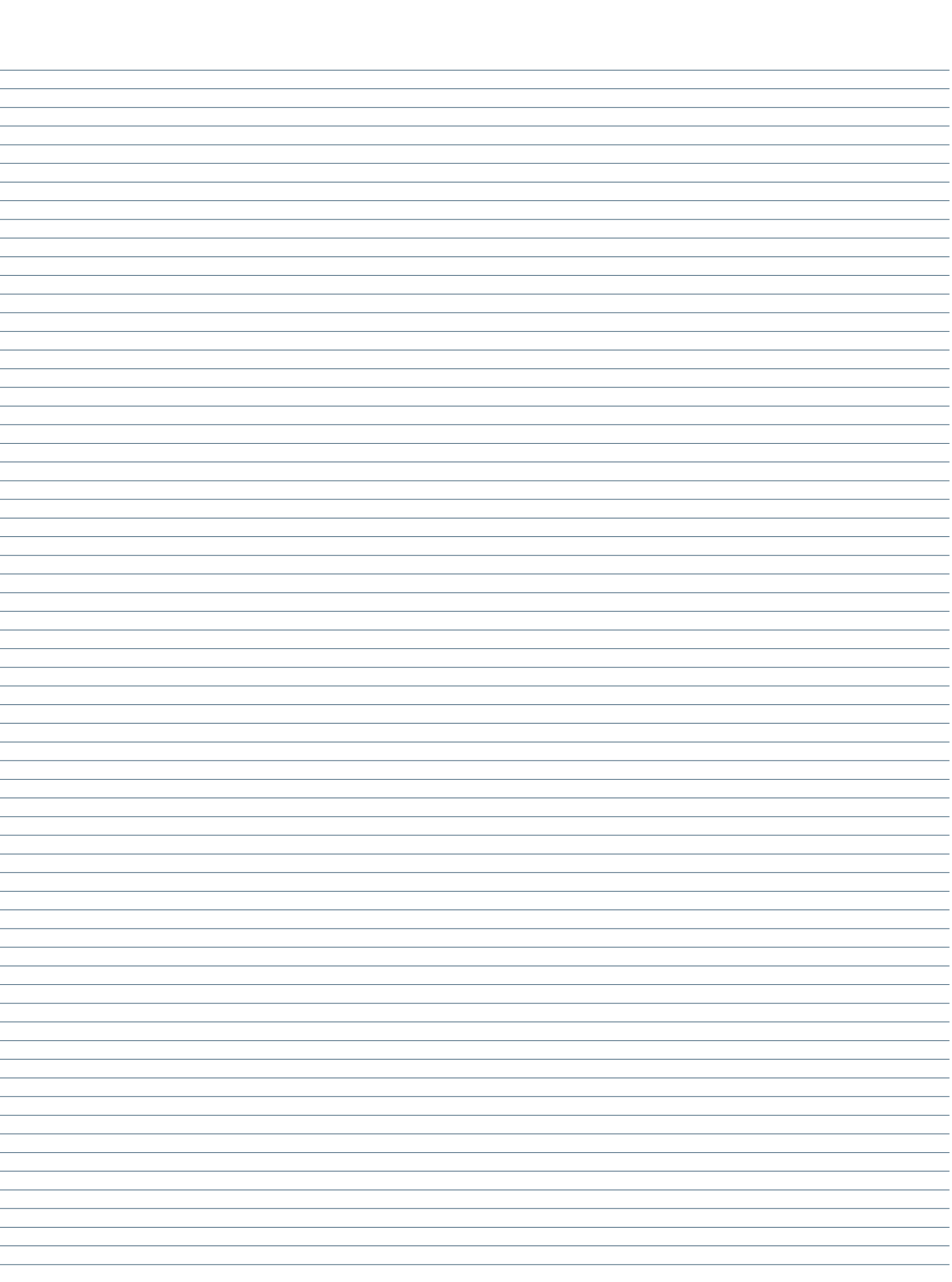
$\begin{cases} a_0 & a_1 \\ b_0 & b_3 \end{cases}$

$\begin{cases} a_0 & a_1 \\ b_2 & b_3 \end{cases}$

$\Rightarrow 6$

Permutations

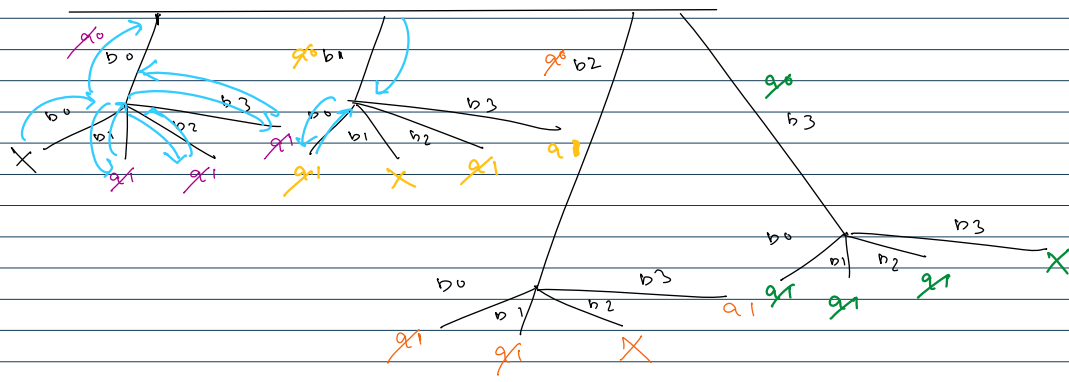
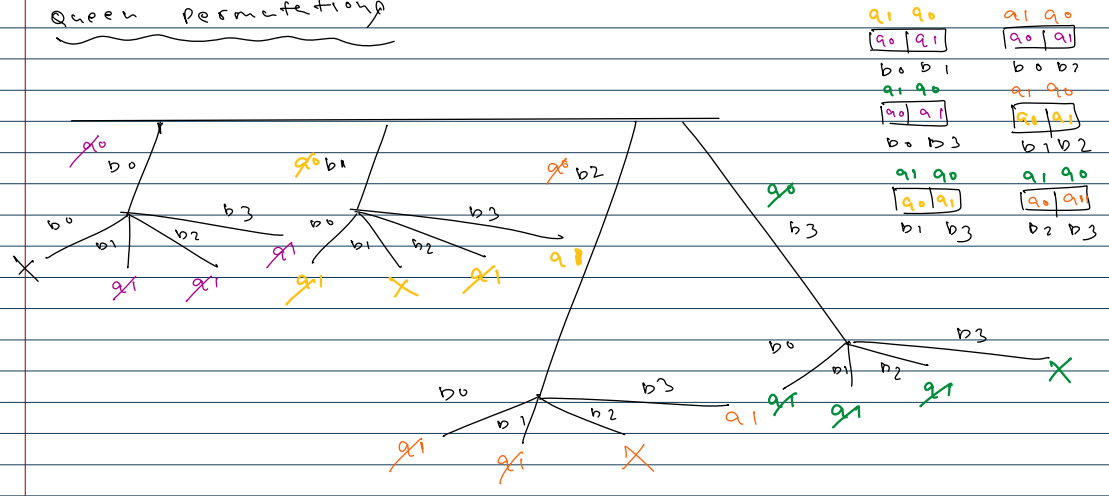
$\Rightarrow 6 \times 2!$





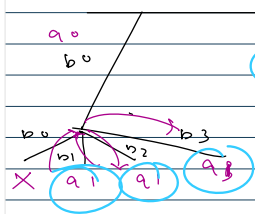
$\Rightarrow$  ABC  
 $\Rightarrow$  ACB  
 $\Rightarrow$  BAC  
 $\Rightarrow$  BCA  
 $\Rightarrow$  CAB  
 $\Rightarrow$  CBA

Queen permutations



$q_0 b_0$   $q_1 b_1$   
 $q_0 b_0$   $q_1 b_2$   
 $q_0 b_0$   $q_1 b_3$

trace	trace	trace	trace
false	false	false	false
b0	b1	b2	b3



```

public class Main {
    public static void main() {
        int n = 4;
        int tq = 2; // total queens
        int qpsf = 0; // queens placed so far
        boolean[] board = new boolean[n];
        String ans = "";
        perm(board, tq, 0);
    }
}

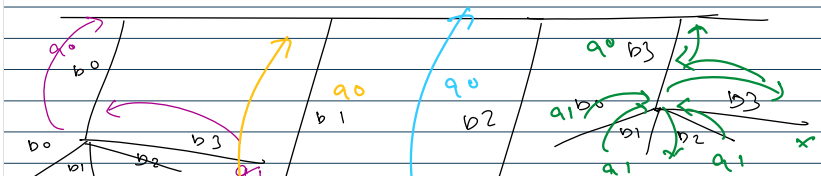
```



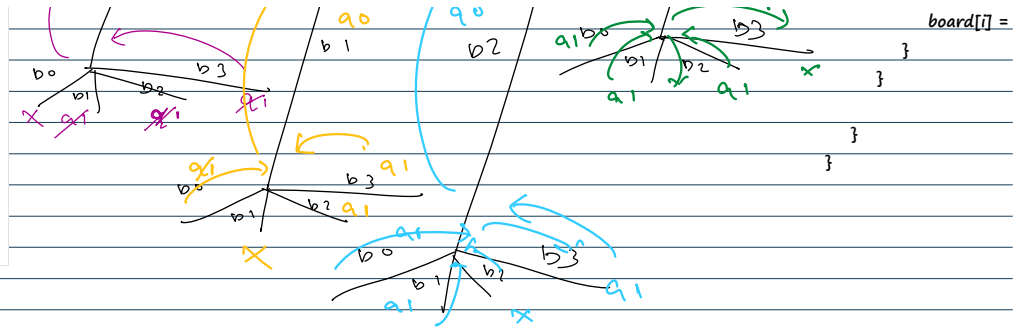
```

public static void perm(boolean[] board, int tq, int qpsf) {
    if (qpsf == tq) {
        System.out.println(ans);
        return;
    }
    for (int i = 0; i < board.length; i++) {
        if (board[i] == false) {
            board[i] = true;
            perm(board, tq, qpsf + 1);
            board[i] = false;
        }
    }
}

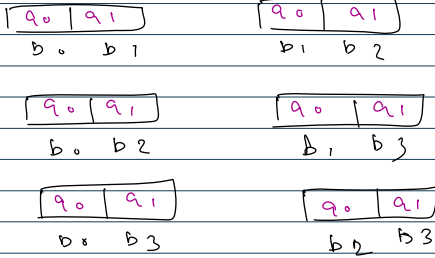
```



```
main(String[] args) {  
    // total queens  
    // queen placed so far  
    boolean[] board = new boolean[n];  
  
    dfs(0, ans);  
  
    return ans;  
}  
  
private void dfs(boolean[] board, int tq, int qpsf, String ans){  
    if(tq == n){  
        ans += "b" + tq + "q" + qpsf + " ";  
        return;  
    }  
    for(int i = 0; i < n; i++){  
        if(board[i] == true){  
            continue;  
        }  
        board[i] = true;  
        dfs(board, tq+1, ans + "b" + i + "q" + qpsf + " ");  
        board[i] = false;  
    }  
}
```

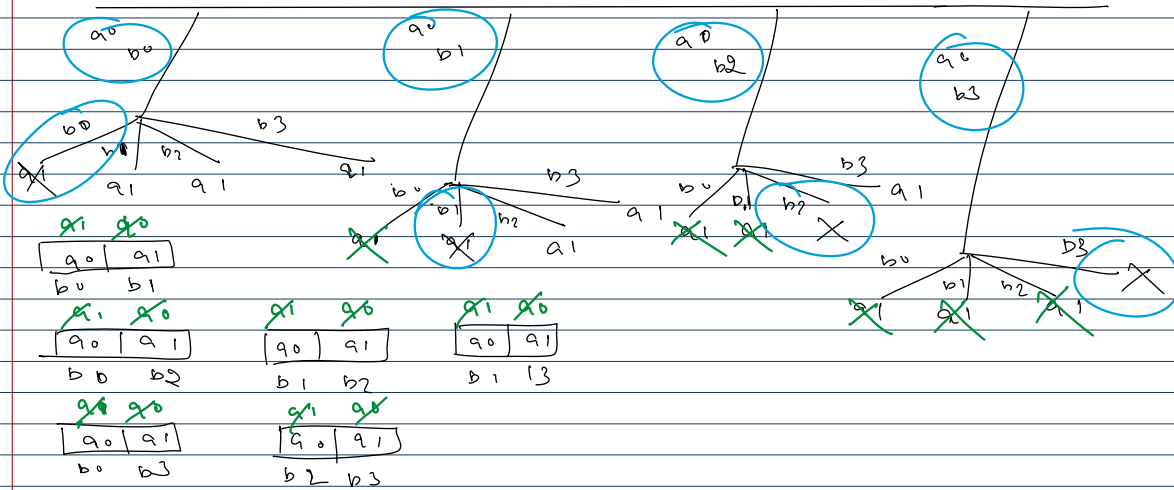


Combinations



Queen combinations

n = 4  
q = 2

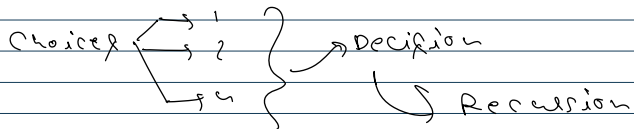


```
public class Main {
    public static void main(String[] args) {
        int n = 4;
        int tq = 2; // total queens
        int qpsf = 0; // queen placed
        boolean[] board = new boolean[n];
        String ans = "";
        int idx = 0;
        perm(board, tq, qpsf, ans, idx);
    }

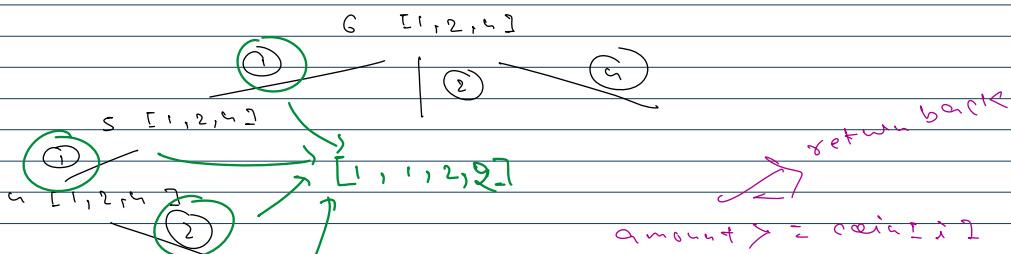
    public static void perm(boolean[] board, int tq, int qpsf, String ans, int idx) {
        if (qpsf == tq) {
            System.out.println(ans);
            return;
        }
        for (int i = idx; i < board.length; i++) {
            if (board[i] == false) {
                board[i] = true;
                perm(board, tq, qpsf + 1, ans + "Q", i + 1);
                board[i] = false;
            }
        }
    }
}
```

coin change - Permutations

coins = [1, 2, 4]  
amount = 6



2 \* 4 = 8  
1 + 1 + 2 + 2 = 6  
1 + 1 + 4 = 6  
1 + 1 + 1 + 1 + 2 = 6



```
false;
```

```
[] args) {
```

```
ed so far  
ean[n];
```

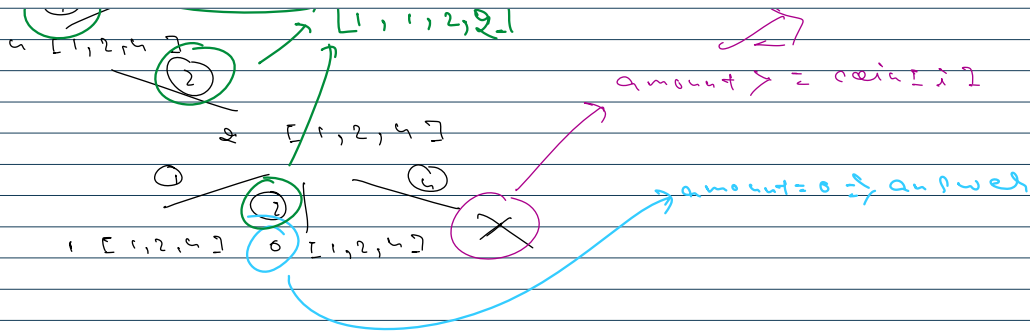
```
idx);
```

```
n[] board, int tq, int qpsf, String ans, int idx){
```

```
; i++){
```

```
i+1, ans+ "b"+ i+ "q" + qpsf+" ", i+1);
```





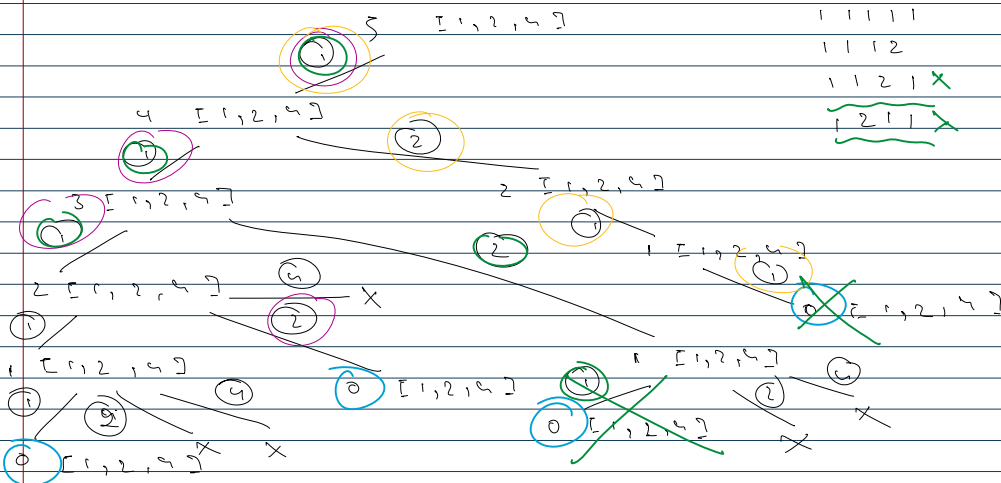
Permutation  $\rightarrow$  2 4 } different  
 4 2 } arrangement  
 radical  
 both

```
public class Main {
    public static void main(String[] args) {
        int[] coins = {1, 2, 4};
        int amount = 6;
        String ans = "";
        perm(coins, amount, ans);
    }

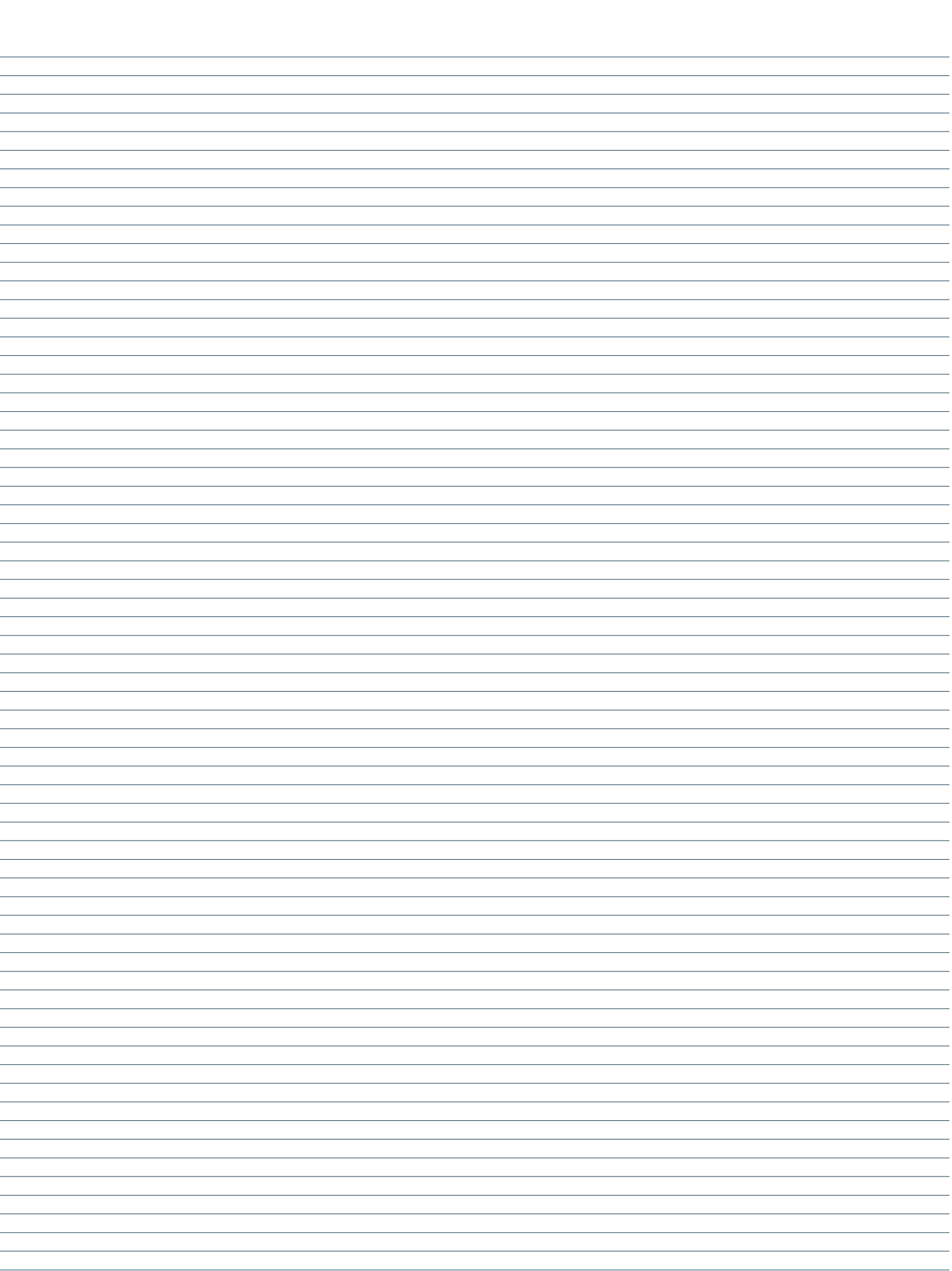
    public static void perm(int[] coins, int amount, String ans){
        if(amount==0){
            System.out.println(ans);
            return;
        }

        for(int i=0; i<coins.length; i++){
            if(amount >= coins[i]){
                perm(coins, amount - coins[i], ans+" "+coins[i]);
            }
        }
    }
}
```

coin change - combination



```
public class Main {
    public static void main(String[] args) {
        int[] coins = {1, 2, 4};
        int amount = 5;
        String ans = "";
        int idx = 0;
    }
}
```



```

perm(coins, amount, ans, idx);
}

public static void perm(int[] coins, int amount, String ans, int idx){
    if(amount==0){
        System.out.println(ans);
        return;
    }

    for(int i=idx; i<coins.length; i++){
        if(amount >= coins[i]){
            perm(coins, amount - coins[i], ans+coins[i], i);
        }
    }
}
}
}

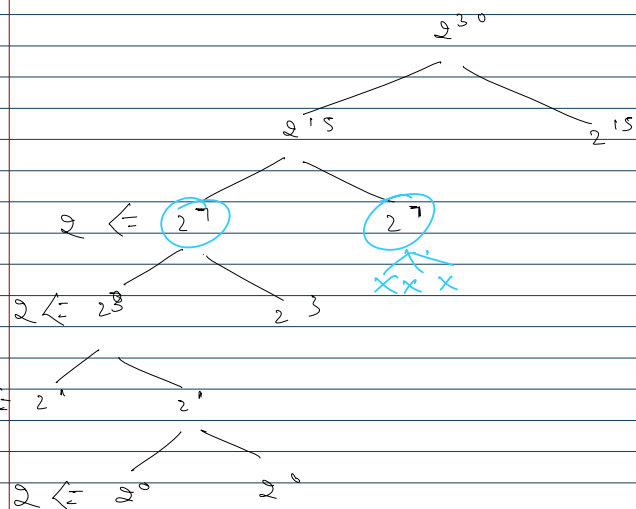
```

Power function

$$2^5 = 2 \times 2 \times 2 \times 2 \times 2 = 32$$

$\text{pow}(2, 5)$

$$2^3 = 2 \times 2 \times 2 = 8$$



$$x^0 = 1$$

$$2^0 = 1$$

$\text{pow}(2, 5)$

→ calculate once

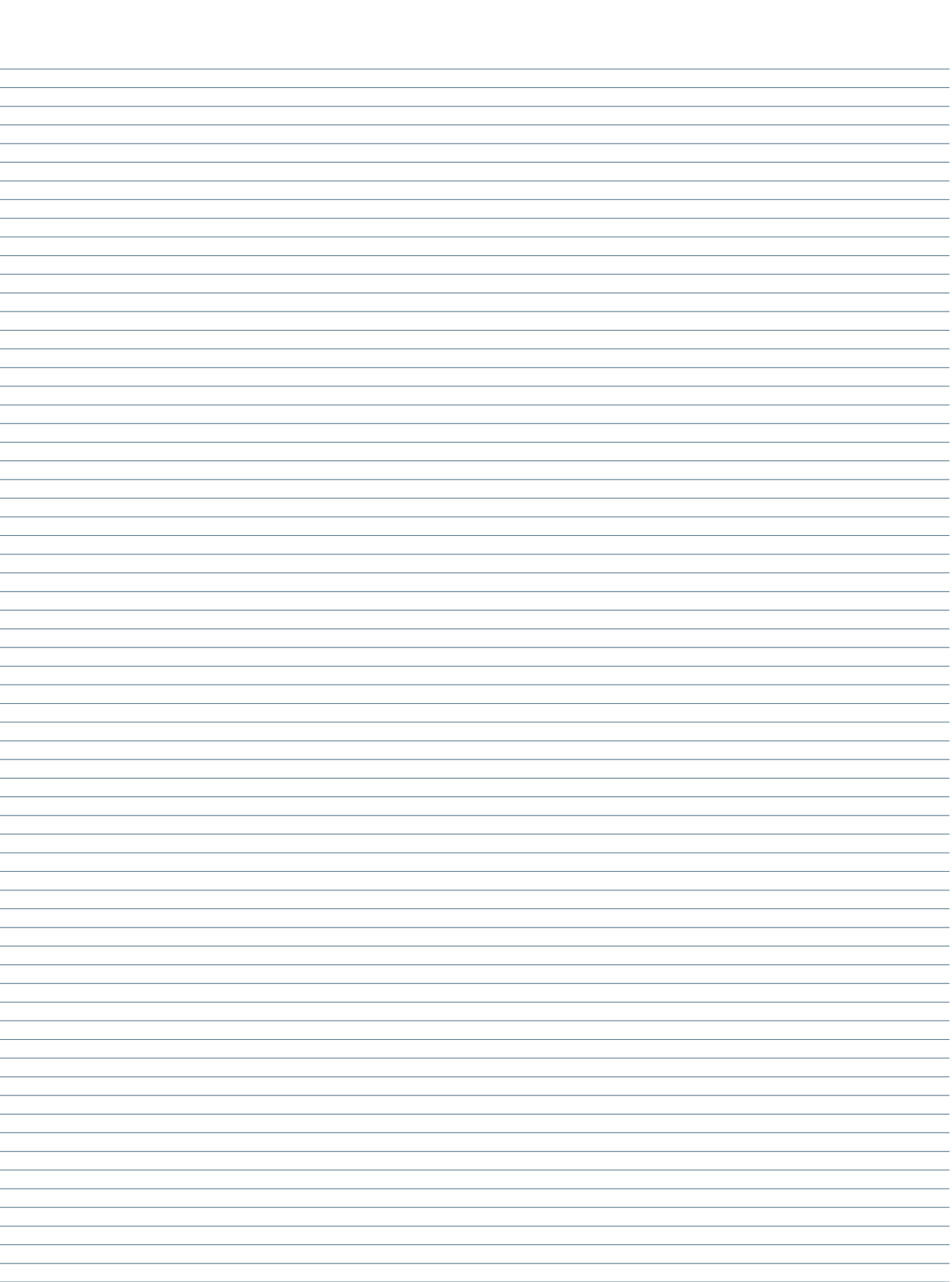
```

public class Main {
    public static void main(String[] args) {
        int a = 2;
        int b = 10;
        System.out.println(pow(a, b));
        System.out.println(pow1(a, b));
    }

    public static int pow(int a, int b){
        if(b==0){
            return 1;
        }
        if(b%2==0){
            return pow(a, b/2)*pow(a, b/2);
        }
        else{
            return 2*pow(a, b/2)*pow(a, b/2);
        }
    }
}

public static int pow1(int a, int b){
    if(b==0){
        return 1;
    }
}

```



```
int half = pow1(a, b/2);  
if(b%2==0){  
    return half*half;  
}  
else{  
    return 2*half*half;  
}  
}  
}
```

