

Recursion

Fibonacci Series

1st term $\rightarrow 0$ 2nd term $\rightarrow 1$ 

$$\text{fib}(3) = \text{fib}(2) + \text{fib}(1)$$

$$\text{fib}(4) = \text{fib}(3) + \text{fib}(2)$$

$$\text{fib}(5) = \text{fib}(4) + \text{fib}(3)$$

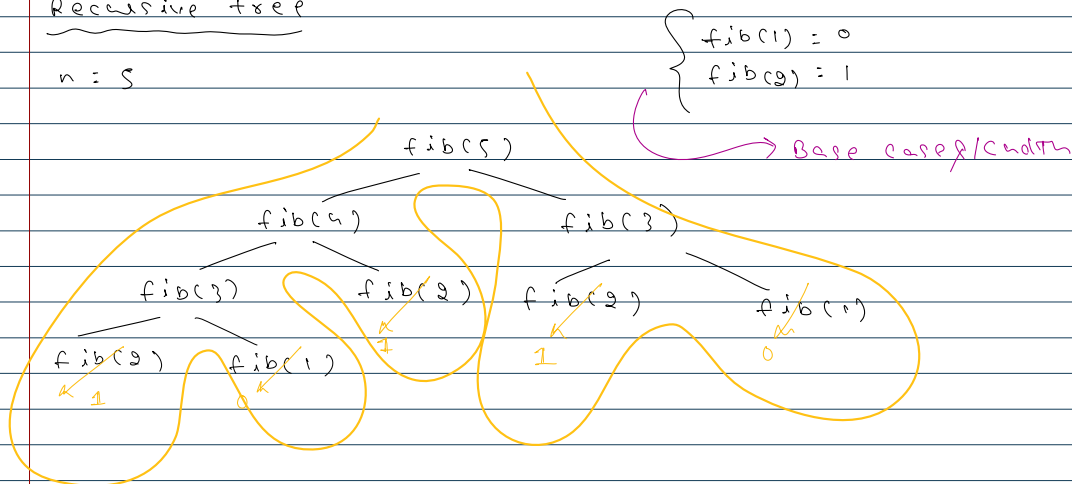
$$\text{fib}(n) = \text{fib}(n-1) + \text{fib}(n-2)$$

$$\text{fib}(87) = \text{fib}(86) + \text{fib}(85)$$

\downarrow
87th term of the
fibonacci series

Recurrence $\Rightarrow \text{fib}(n) = \text{fib}(n-1) + \text{fib}(n-2)$
relation

Recursive tree

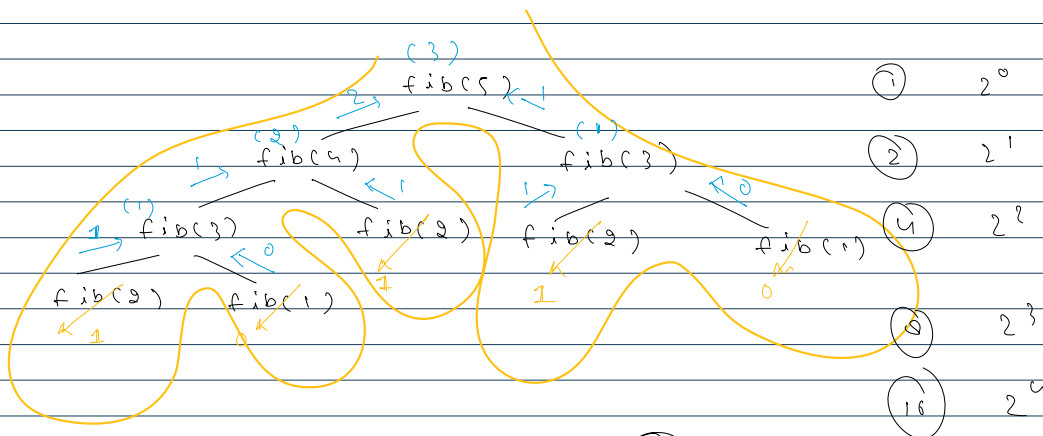
 $n = 5$


```
public class Main {
    public static void main(String[] args) {
        int n = 5;
        System.out.println(fib(n));
    }
}
```

```
public static int fib(int n){
    // if(n == 1){
    //     return 0;
    // }
    // if(n == 2){
    //     return 1;
    // }

    if(n==1 || n==2){
        return n-1;
    }

    return fib(n-1) + fib(n-2);
}
```



$$\text{Time} \Rightarrow 2^0 + 2^1 + 2^2 + 2^3 + 2^4 \dots (2^5)$$

Subsequence

Subarray?

$$\begin{aligned} 288 &\rightarrow [1, 2, 3] \quad \neq / \quad [1] \\ &\quad [1, 2] \\ &\quad [2, 3] \\ &\quad [3] \\ &\quad [1, 2, 3] \\ &\quad [2, 3] \\ &\quad [1, 2, 3] \end{aligned}$$

Subset ?

a	b	c	\rightarrow	a	a	b	a	b	c	a
				b		b		c		
				c						

Subsequence ?

$a b c$	\rightarrow	a	$a b$	$a b c$	$b c$
		b	$b c$		c
		c	$a c$		c

Print all subsequence

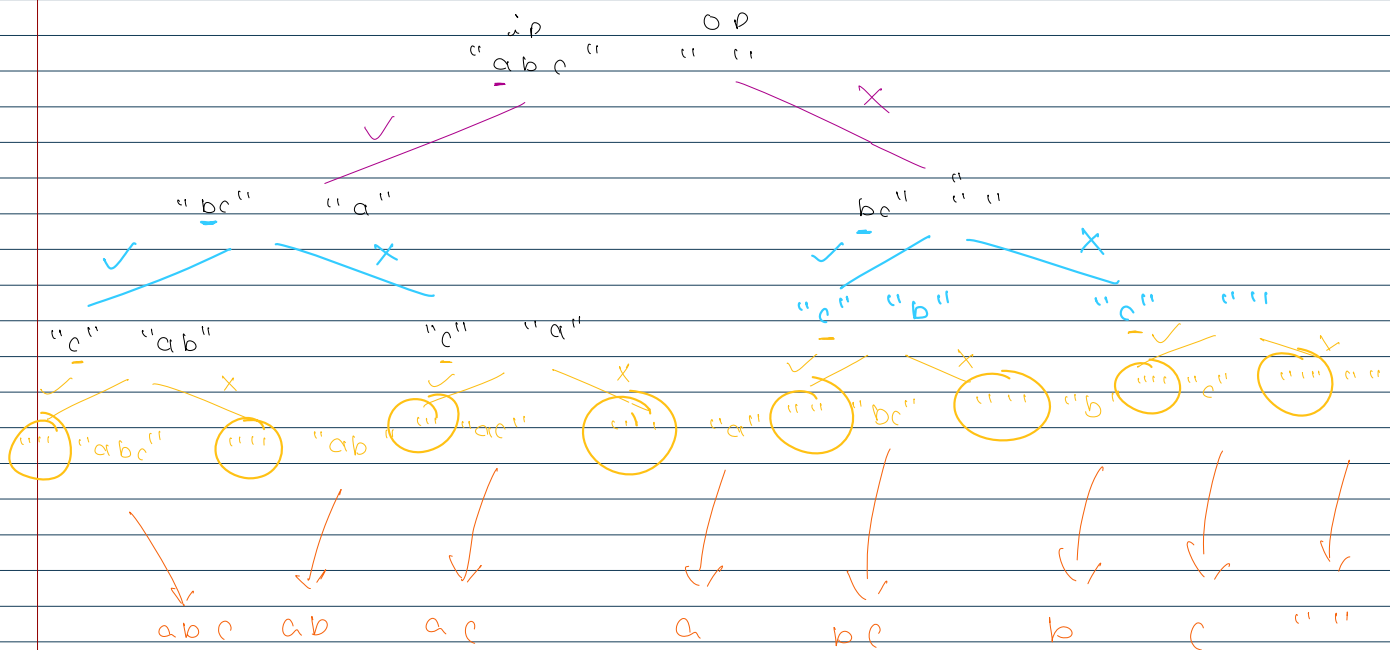
recursion \rightarrow ?

$abc \Rightarrow a$

- include this
- don't include this

answer

choice \rightarrow Recursion
↓
decision



```

public class Main {
    public static void main(String[] args) {
        String ip = "abc";
        String op = "";
        subsequence(ip, op);
    }

    public static void subsequence(String ip, String op){
        if(ip.length() == 0){
            System.out.println(op);
            return;
        }
        char ch = ip.charAt(0);
        subsequence(ip.substring(1), op+ch); //Include
        subsequence(ip.substring(1), op); //Not include
    }
}

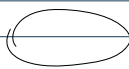
```

ip: bc	sub()
ip: abc op: "" sub("a") sub("bc")	sub()
ip: "abc" op: "" sub("abc", "")	main

abc \Rightarrow ip.substring(1)

bc

Print count of all subsequence

coin \Rightarrow  \Rightarrow $\frac{\text{Head}}{\text{Tail}}$ \Rightarrow flip \Rightarrow 2 possibilities

\swarrow Head \searrow Tail

Print all possible outcomes of a coin flip

n = 2

HT
 HT
 TH
 TT

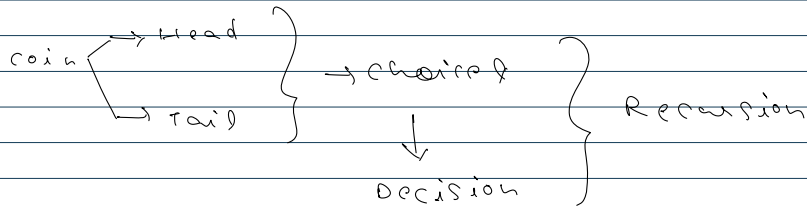
n = 3

HHT
 HHT
 HTH
 HTT
 THT
 THT
 TTH
 TTT

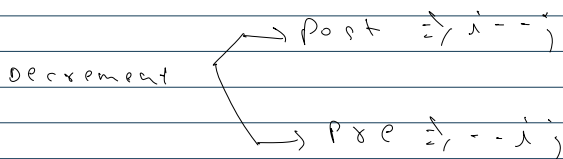
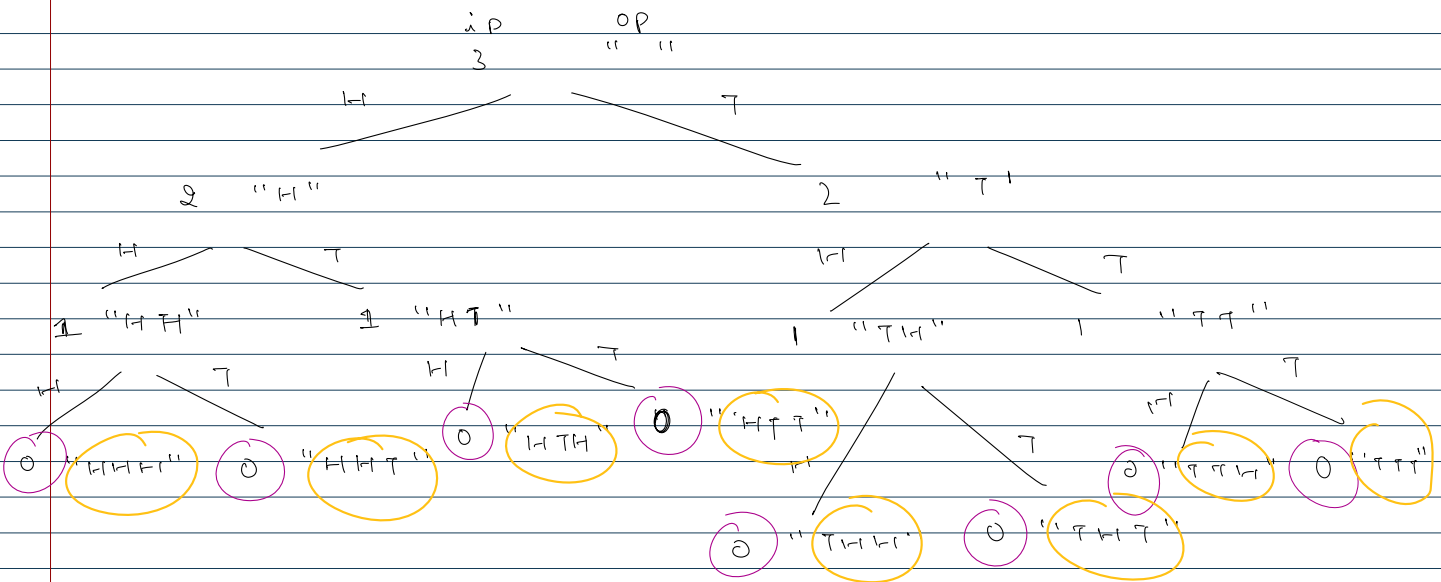
T H T

T T H

T T T



Recursive Tree



784. Letter Case Permutation

Medium Topics Companies

Given a string `s`, you can transform every letter individually to be lowercase or uppercase to create another string.

Return a list of all possible strings we could create. Return the output in **any order**.

Example 1:

Input: `s = "a1b2"`

Output: `["a1b2", "a1B2", "A1b2", "A1B2"]`

Example 2:

Input: `s = "3z4"`

Output: `["3z4", "3Z4"]`

