

Statistic with pandas

Presented to you by

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Sample Data

```
import pandas as pd

data = {'name': ['Jason', 'Molly', 'Tina', 'Jake', 'Amy'],
        'age': [42, 52, 36, 24, 73],
        'preTestScore': [4, 24, 31, 2, 3],
        'postTestScore': [25, 94, 57, 62, 70]}
df = pd.DataFrame(data, columns = ['name', 'age', 'preTestScore', 'postTestScore'],
index=[0,1,2,3,4])
df=df.sort_index()

print()
print(df)
```

| | name | age | preTestScore | postTestScore |
|---|-------|-----|--------------|---------------|
| 0 | Jason | 42 | 4 | 25 |
| 1 | Molly | 52 | 24 | 94 |
| 2 | Tina | 36 | 31 | 57 |
| 3 | Jake | 24 | 2 | 62 |
| 4 | Amy | 73 | 3 | 70 |

Sum, Cumulative Sum

| | name | age | preTestScore | postTestScore |
|---|-------|-----|--------------|---------------|
| 0 | Jason | 42 | 4 | 25 |
| 1 | Molly | 52 | 24 | 94 |
| 2 | Tina | 36 | 31 | 57 |
| 3 | Jake | 24 | 2 | 62 |
| 4 | Amy | 73 | 3 | 70 |

```
sum_age=df['age'].sum()  
print('sum_age=', sum_age)
```

sum_age=227

```
cumsum_age=df['age'].cumsum()  
print('cumsum_age:')  
print(cumsum_age)
```

```
cumsum_age:  
0      42  
1      94  
2     130  
3     154  
4     227  
Name: age, dtype: int64
```

Min,Max,Mean

| | name | age | preTestScore | postTestScore |
|---|-------|-----|--------------|---------------|
| 0 | Jason | 42 | 4 | 25 |
| 1 | Molly | 52 | 24 | 94 |
| 2 | Tina | 36 | 31 | 57 |
| 3 | Jake | 24 | 2 | 62 |
| 4 | Amy | 73 | 3 | 70 |

```
min_age=df['age'].min()  
print('min_age:', min_age)
```

min_age=24

```
max_age=df['age'].max()  
print('max_age:', max_age)
```

max_age=73

```
mean_age=df['age'].mean()  
print('mean_age:', mean_age)
```

mean_age=45.4

Shape Dataframe, Count

| | name | age | preTestScore | postTestScore |
|---|-------|-----|--------------|---------------|
| 0 | Jason | 42 | 4.0 | 25.0 |
| 1 | Molly | 52 | 24.0 | 94.0 |
| 2 | Tina | 36 | NaN | 57.0 |
| 3 | Jake | 24 | 2.0 | 62.0 |
| 4 | Amy | 73 | 3.0 | NaN |

```
print('shape:',df.shape)
```

```
shape=(5,4)
```

```
count_preTestScore=df['preTestScore'].count()  
print('count_preTestScore:',count_preTestScore)
```

```
count_preTestScore: 4
```

Median

| | name | age | preTestScore | postTestScore |
|---|-------|-----|--------------|---------------|
| 0 | Jason | 42 | 4 | 25 |
| 1 | Molly | 52 | 24 | 94 |
| 2 | Tina | 36 | 31 | 57 |
| 3 | Jake | 24 | 2 | 62 |
| 4 | Amy | 73 | 3 | 70 |

```
median_age=df['age'].median()  
print('median_age:',median_age)
```

median_age: 42.0

Median

| | name | age | preTestScore | postTestScore |
|---|---------|-----|--------------|---------------|
| 0 | Jason | 42 | 4 | 25 |
| 1 | Molly | 52 | 24 | 94 |
| 2 | Tina | 36 | 31 | 57 |
| 3 | Jake | 24 | 2 | 62 |
| 4 | Amy | 73 | 3 | 70 |
| 5 | Carsten | 10 | 5 | 75 |

```
median_age=df['age'].median()  
print('median_age:',median_age)
```

median_age: 39.0

Mode

```
import pandas as pd
```

```
data = {'name': ['Jason', 'Molly', 'Tina', 'Jake', 'Amy', 'Carsten'],  
        'age': [42, 52, 36, 24, 73, 10],  
        'preTestScore': [4, 24, 31, 2, 3, 5],  
        'postTestScore': [25, 60, 70, 70, 70, 60]}  
df = pd.DataFrame(data, columns = ['name', 'age', 'preTestScore', 'postTestScore'],  
index=[0,1,2,3,4,5])
```

```
print()  
print(df)
```

| | name | age | preTestScore | postTestScore |
|---|---------|-----|--------------|---------------|
| 0 | Jason | 42 | 4 | 25 |
| 1 | Molly | 52 | 24 | 60 |
| 2 | Tina | 36 | 31 | 70 |
| 3 | Jake | 24 | 2 | 70 |
| 4 | Amy | 73 | 3 | 70 |
| 5 | Carsten | 10 | 5 | 60 |

```
mode_postTestScore=df['postTestScore'].mode()
```

mode:

0 70

dtype: int64

Variance, Standard Deviation

$$\text{variance} = \sigma^2 = \frac{\sum (x_r - \mu)^2}{n}$$

$$\text{standard deviation } \sigma = \sqrt{\frac{\sum (x_r - \mu)^2}{n}}$$

μ = mean

Variance, Standard Deviation

```
import pandas as pd
```

```
data = {'name': ['Jason', 'Molly', 'Tina', 'Jake', 'Amy'],  
        'age': [42, 52, 36, 24, 73],  
        'preTestScore': [4, 24, 31, 2, 3],  
        'postTestScore': [25, 94, 57, 62, 70]}  
df = pd.DataFrame(data, columns = ['name', 'age', 'preTestScore', 'postTestScore'],  
index=[0,1,2,3,4])  
df=df.sort_index()
```

```
print()  
print(df)
```

| | name | age | preTestScore | postTestScore |
|---|-------|-----|--------------|---------------|
| 0 | Jason | 42 | 4 | 25 |
| 1 | Molly | 52 | 24 | 94 |
| 2 | Tina | 36 | 31 | 57 |
| 3 | Jake | 24 | 2 | 62 |
| 4 | Amy | 73 | 3 | 70 |

```
var_postTestScore=df['postTestScore'].var()  
print('var postTestScore=', var_postTestScore)
```

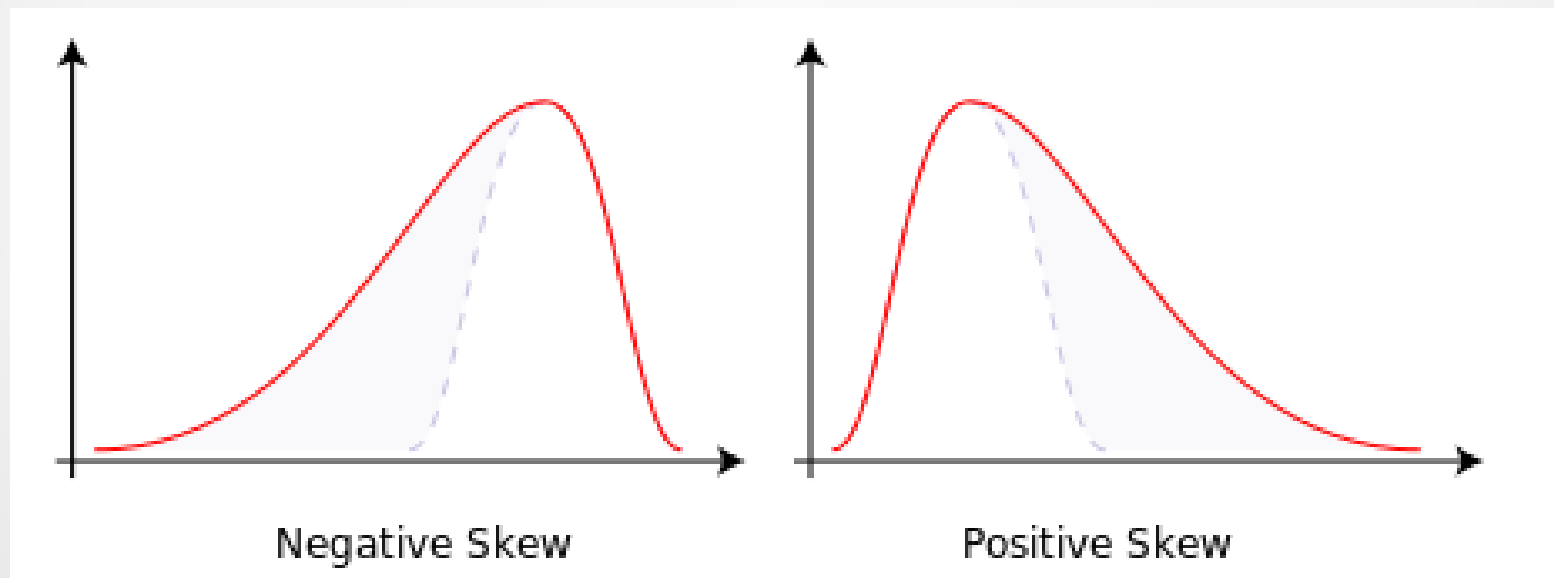
```
var postTestScore= 620.3
```

```
std_postTestScore=df['postTestScore'].std()  
print('std postTestScore=', std_postTestScore)
```

```
std postTestScore= 24.90582261239327
```

Skewness

$$\gamma_1 = \mathbf{E} \left[\left(\frac{X - \mu}{\sigma} \right)^3 \right]$$



Skewness

```
data = {'name': ['Jason', 'Molly', 'Tina', 'Jake', 'Amy'],
        'age': [40, 50, 30, 20, 60],
        'preTestScore': [4, 5, 40, 2, 3],
        'postTestScore': [10, 90, 85, 80, 75]}
df = pd.DataFrame(data, columns = ['name', 'age', 'preTestScore', 'postTestScore'],
index=[0,1,2,3,4])
df=df.sort_index()

print()
print(df)
print()
sk_age=df['age'].skew()
print('skewness age=', sk_age)
print()
sk_preTestScore=df['preTestScore'].skew()
print('skewness preTestScore=', sk_preTestScore)
print()
sk_postTestScore=df['postTestScore'].skew()
print('skewness postTestScore=', sk_postTestScore)
print()
```

Skewness

| | name | age | preTestScore | postTestScore |
|---|-------|-----|--------------|---------------|
| 0 | Jason | 40 | 4 | 10 |
| 1 | Molly | 50 | 5 | 90 |
| 2 | Tina | 30 | 40 | 85 |
| 3 | Jake | 20 | 2 | 80 |
| 4 | Amy | 60 | 3 | 75 |

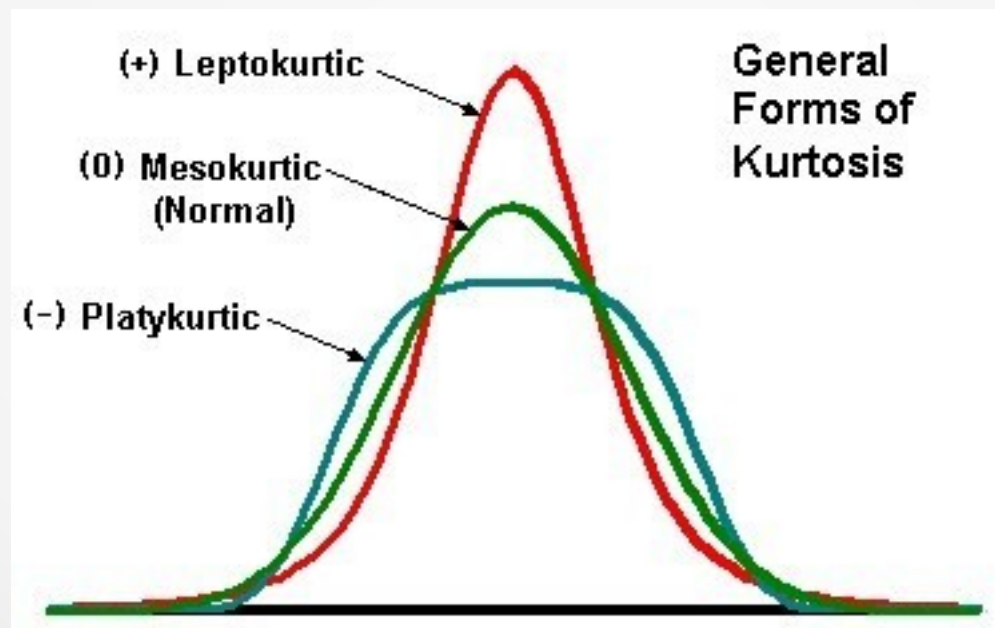
skewness age= 0.0

skewness preTestScore= 2.2100079064682228

skewness postTestScore= -2.0763297220115997

Kurtosis

$$\text{Kurt}[X] = E \left[\left(\frac{X - \mu}{\sigma} \right)^4 \right] :$$



Kurtosis

```
import pandas as pd
```

```
data = {'name': ['Jason', 'Molly', 'Tina', 'Jake', 'Amy', 'Lukas', 'Jony'],  
        'age': [10, 22, 27, 30, 33, 38, 50],  
        'preTestScore': [5, 18, 19, 20, 21, 22, 35],  
        'postTestScore': [35, 40, 45, 50, 55, 60, 65]}
```

```
df = pd.DataFrame(data, columns = ['name', 'age', 'preTestScore', 'postTestScore'],  
index=[0,1,2,3,4,5,6])  
df=df.sort_index()
```

```
print()  
print(df)  
print()  
kurt_age=df['age'].kurtosis()  
print('kurtosis age=', kurt_age)  
print()  
kurt_preTestScore=df['preTestScore'].kurtosis()  
print('kurtosis preTestScore=', kurt_preTestScore)  
print()  
kurt_postTestScore=df['postTestScore'].kurtosis()  
print('kurtosis postTestScore=', kurt_postTestScore)  
print()
```

Kurtosis

| | name | age | preTestScore | postTestScore |
|---|-------|-----|--------------|---------------|
| 0 | Jason | 10 | 5 | 35 |
| 1 | Molly | 22 | 18 | 40 |
| 2 | Tina | 27 | 19 | 45 |
| 3 | Jake | 30 | 20 | 50 |
| 4 | Amy | 33 | 21 | 55 |
| 5 | Lukas | 38 | 22 | 60 |
| 6 | Jony | 50 | 35 | 65 |

```
kurtosis age= 0.7640949541632951
```

```
kurtosis preTestScore= 2.64145179584121
```

```
kurtosis postTestScore= -1.2000000000000002
```


Correlation

Correlation coefficients are used in statistics to measure how strong a relationship is between two variables.

Pearson Correlation Coefficient

$$r = \frac{\text{cov}(x, y)}{\sigma_x \cdot \sigma_y}$$

$$r = \frac{\sum x \cdot y}{\sqrt{\sum x^2 \cdot \sum y^2}}$$

Where

$$x = X - \bar{X}$$

and

$$y = Y - \bar{Y}$$

Spearman's correlation

Spearman's correlation is a measure of monotonic relationship. It can be used for ordinal variables. It is less sensitive to outliers. If spearman correlation coefficient of a variable is close to 0, it means there is no monotonic relationship between variables.

Hoeffding's D Correlation

Hoeffding's D correlation is a measure of linear, monotonic and non-monotonic relationship. It has values between -0.5 to 1 . The signs of Hoeffding coefficient has no interpretation.

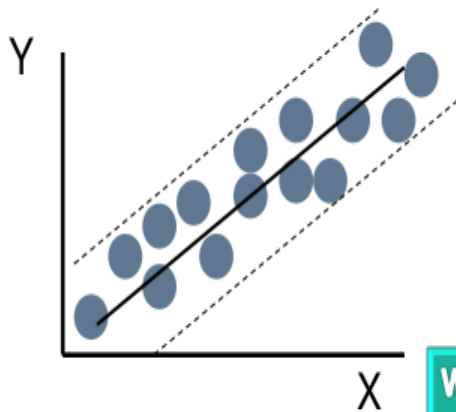
If a variable has a very low rank for Spearman (coefficient - close to 0) and a very high rank for Hoeffding indicates a non-monotonic relationship.

If a variable has a very low rank for Pearson (coefficient - close to 0) and a very high rank for Hoeffding indicates a non-linear relationship.

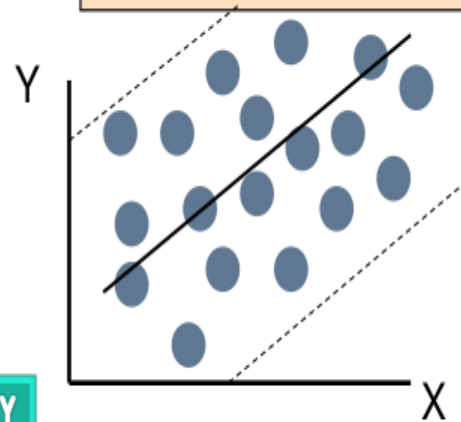
If a variable has poor rank on both the spearman and hoeffding correlation metrics, it means the relationship between the variables is random.

Type of relationship

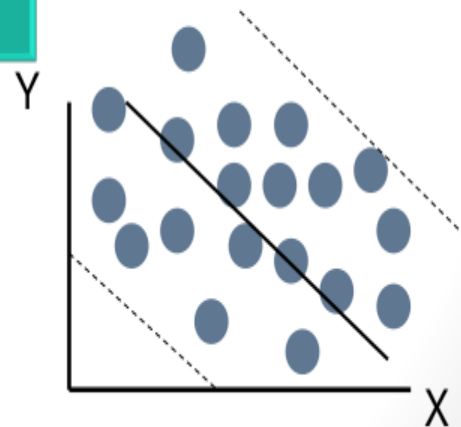
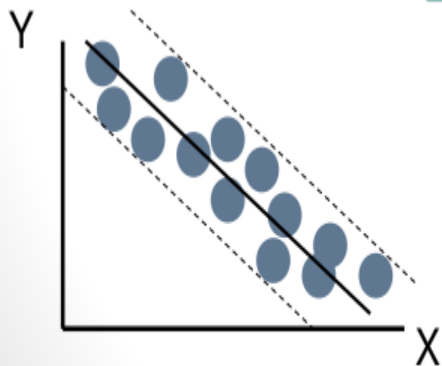
Strong relationships



Weak relationships

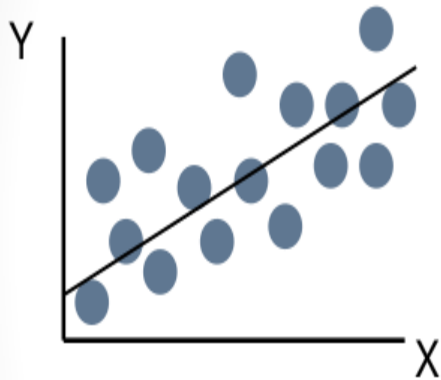


What is happening to Y when X is increasing?

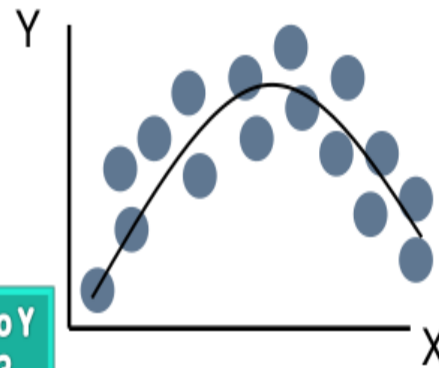


Type of relationship

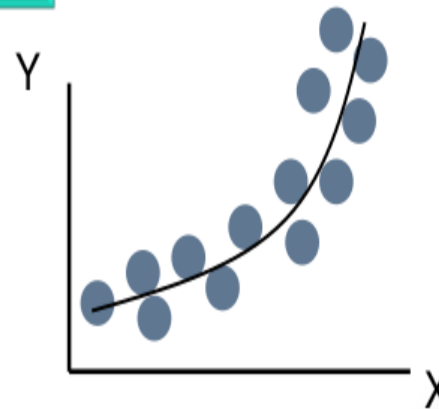
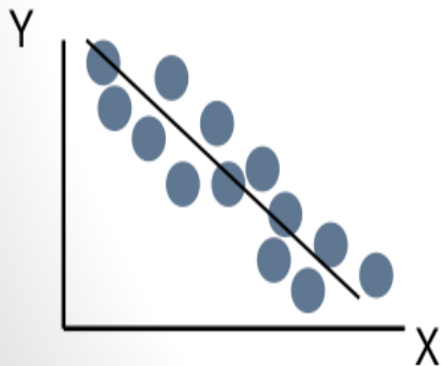
Linear relationships



Curvilinear relationships



What is happening to Y
when X is increasing?



Correlation

High
positive
correlation

Zero
correlation

High
negative
correlation

stronger



weaker

weaker



stronger

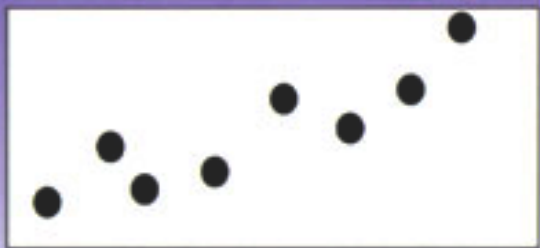
+1.00

perfect positive
as one event increases,
the second exactly
increases



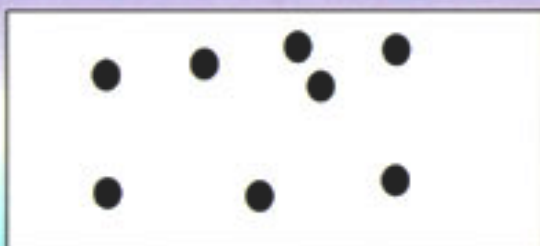
+.50

positive
as one event increases,
the second sometimes
increases



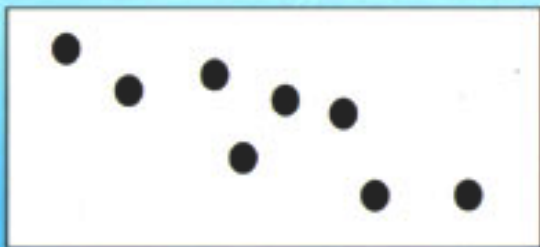
0

zero correlation
no relationship between
the events



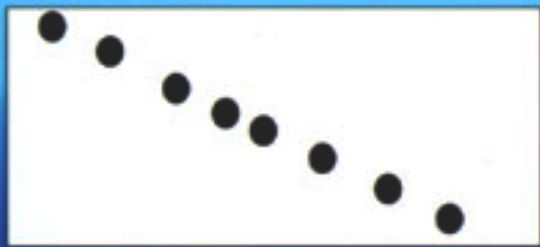
-.50

negative
as one event increases,
the second sometimes
decreases



-1.00

perfect negative
as one event increases,
the second exactly
decreases



Correlation matrix example code

```
import pandas as pd

data = {'name': ['Jason', 'Molly', 'Tina', 'Jake', 'Amy', 'Lukas', 'Jony'],
        'age': [10, 20, 30, 40, 50, 60, 70],
        'glucose_level': [100, 105, 120, 130, 140, 150, 160],
        'preTestScore': [5, 10, 19, 3, 21, 4, 6],
        'postTestScore': [100, 95, 93, 70, 67, 60, 55]}
df = pd.DataFrame(data,
                  columns = ['name', 'age', 'glucose_level', 'preTestScore', 'postTestScore'],
                  index=[0,1,2,3,4,5,6])
df=df.sort_index()

print()
print(df)
print()
corr_coefs=df.corr(method='pearson')
print('correlation matrix')
print(corr_coefs)
```

Correlation matrix example

| | name | age | glucose_level | preTestScore | postTestScore |
|---|-------|-----|---------------|--------------|---------------|
| 0 | Jason | 10 | 100 | 5 | 100 |
| 1 | Molly | 20 | 105 | 10 | 95 |
| 2 | Tina | 30 | 120 | 19 | 93 |
| 3 | Jake | 40 | 130 | 3 | 70 |
| 4 | Amy | 50 | 140 | 21 | 67 |
| 5 | Lukas | 60 | 150 | 4 | 60 |
| 6 | Jony | 70 | 160 | 6 | 55 |

correlation matrix

| | age | glucose_level | preTestScore | postTestScore |
|---------------|-----------|---------------|--------------|---------------|
| age | 1.000000 | 0.997041 | -0.073107 | -0.968709 |
| glucose_level | 0.997041 | 1.000000 | -0.071814 | -0.968581 |
| preTestScore | -0.073107 | -0.071814 | 1.000000 | 0.194108 |
| postTestScore | -0.968709 | -0.968581 | 0.194108 | 1.000000 |