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In[933]:= Clear["Global`*"];
(*Define the Following;
x0=; y0=;
x1=; y1=;
θ=;*)

(*Reference To Origin*)
x1o = Abs[x1 - x0];
y1o = Abs[y1 - y0];

(*Equation for Radius*)
R =  $\sqrt{x1o^2 + y1o^2}$ ;

(*Defining Y variable of the second vector, R= $\sqrt{x2o^2+y2o^2}$  *)
(*Since Solving for square + or - is the output*)
y2o1 =  $\sqrt{R^2 - x2o^2}$ ;
y2o2 =  $-\sqrt{R^2 - x2o^2}$ ;

(*Defining the x variable using angle formula*)
(*Cos[θ] =  $\frac{x1o \cdot x2o + y1o \cdot y2o}{\sqrt{x1o^2 + y1o^2} \cdot \sqrt{x2o^2 + y2o^2}}$  *)
(*4 Outputs, 2 different Y produces 4 different X*)
(*Using y2o1 or positive y2o*)
x2o11 =  $\frac{1}{x1o^2 + y1o^2} \left( x1o \left( \sqrt{R^2} + \sqrt{x1o^2 + y1o^2} \right) \cos[\theta] - \sqrt{y1o^2 \left( R^2 (x1o^2 + y1o^2) - \left( R^2 + x1o^2 + y1o^2 + 2 \sqrt{R^2} \sqrt{x1o^2 + y1o^2} \right) \cos[\theta]^2 \right)} \right);$ 
x2o12 =  $\frac{1}{x1o^2 + y1o^2} \left( x1o \left( \sqrt{R^2} + \sqrt{x1o^2 + y1o^2} \right) \cos[\theta] + \sqrt{y1o^2 \left( R^2 (x1o^2 + y1o^2) - \left( R^2 + x1o^2 + y1o^2 + 2 \sqrt{R^2} \sqrt{x1o^2 + y1o^2} \right) \cos[\theta]^2 \right)} \right);$ 

(*Using y2o2 or negative y2o*)
x2o21 =  $\frac{1}{x1o^2 + y1o^2} \left( x1o \left( \sqrt{R^2} + \sqrt{x1o^2 + y1o^2} \right) \cos[\theta] - \sqrt{y1o^2 \left( R^2 (x1o^2 + y1o^2) - \left( R^2 + x1o^2 + y1o^2 + 2 \sqrt{R^2} \sqrt{x1o^2 + y1o^2} \right) \cos[\theta]^2 \right)} \right);$ 
x2o22 =  $\frac{1}{x1o^2 + y1o^2} \left( x1o \left( \sqrt{R^2} + \sqrt{x1o^2 + y1o^2} \right) \cos[\theta] + \sqrt{y1o^2 \left( R^2 (x1o^2 + y1o^2) - \left( R^2 + x1o^2 + y1o^2 + 2 \sqrt{R^2} \sqrt{x1o^2 + y1o^2} \right) \cos[\theta]^2 \right)} \right);$ 

(*Appears to be the same exact equation for positive or negative Y. Look

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at the bottom of the page for derived equations.*)

(*Solving for the four different Ys*)
y2o11 =  $\sqrt{R^2 - x2o11^2}$ ;
y2o12 =  $\sqrt{R^2 - x2o12^2}$ ;
y2o21 =  $-\sqrt{R^2 - x2o21^2}$ ;
y2o22 =  $-\sqrt{R^2 - x2o22^2}$ ;

(*Adding the Origin offset*)
x211 = x2o11 + x0;
y211 = y2o11 + y0;

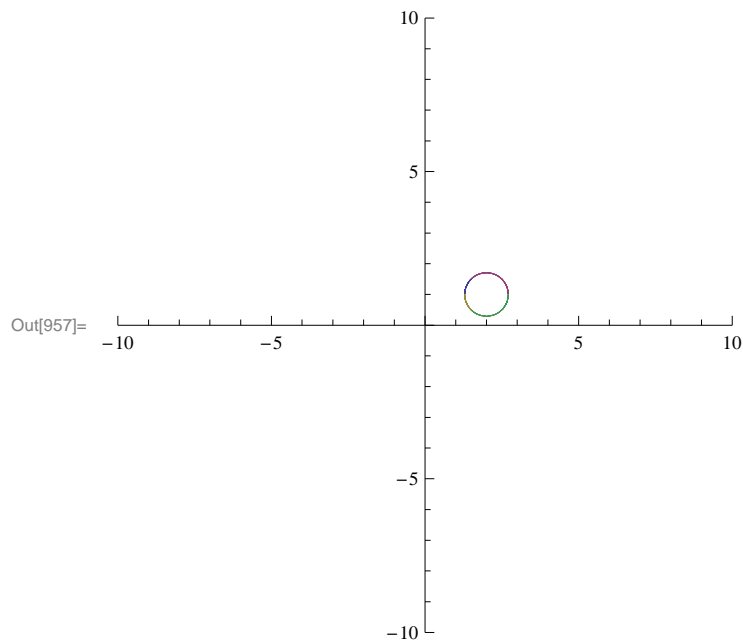
x212 = x2o12 + x0;
y212 = y2o12 + y0;

x221 = x2o21 + x0;
y221 = y2o21 + y0;

x222 = x2o22 + x0;
y222 = y2o22 + y0;

(*And finally plotting the thing*)
x0 = 2; y0 = 1;
x1 = 1.5; y1 = 1.5;
ParametricPlot[{ {x211, y211}, {x212, y212}, {x221, y221}, {x222, y222} },
{ $\theta$ , 0, 2 Pi}, PlotRange -> 10]

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In[436]:= Clear["Global`*"];
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$$y2o1 = \sqrt{R^2 - x2o1^2};$$

$$\text{Solve}\left[\cos[\theta] == \frac{x1o * x2o1 + y1o * y2o1}{\sqrt{x1o^2 + y1o^2} + \sqrt{x2o1^2 + y2o1^2}}, x2o1\right] // \text{FullSimplify}$$

$$y2o2 = \left(-\sqrt{R^2 - x2o2^2}\right);$$

$$\text{Solve}\left[\cos[\theta] == \frac{x1o * x2o2 + y1o * y2o2}{\sqrt{x1o^2 + y1o^2} + \sqrt{x2o2^2 + y2o2^2}}, x2o2\right] // \text{FullSimplify}$$

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Clear["Global`*"];
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$$\begin{aligned} \text{Out[438]} = & \left\{ \left\{ x2o1 \rightarrow \frac{1}{x1o^2 + y1o^2} \left(x1o \left(\sqrt{R^2} + \sqrt{x1o^2 + y1o^2} \right) \cos[\theta] - \right. \right. \right. \\ & \left. \left. \left. \sqrt{y1o^2 \left(R^2 (x1o^2 + y1o^2) - \left(R^2 + x1o^2 + y1o^2 + 2 \sqrt{R^2} \sqrt{x1o^2 + y1o^2} \right) \cos[\theta]^2 \right)} \right) \right\}, \right. \\ & \left. \left\{ x2o1 \rightarrow \frac{1}{x1o^2 + y1o^2} \left(x1o \left(\sqrt{R^2} + \sqrt{x1o^2 + y1o^2} \right) \cos[\theta] + \right. \right. \right. \\ & \left. \left. \left. \sqrt{y1o^2 \left(R^2 (x1o^2 + y1o^2) - \left(R^2 + x1o^2 + y1o^2 + 2 \sqrt{R^2} \sqrt{x1o^2 + y1o^2} \right) \cos[\theta]^2 \right)} \right) \right\} \right\} \end{aligned}$$

$$\begin{aligned} \text{Out[440]} = & \left\{ \left\{ x2o2 \rightarrow \frac{1}{x1o^2 + y1o^2} \left(x1o \left(\sqrt{R^2} + \sqrt{x1o^2 + y1o^2} \right) \cos[\theta] - \right. \right. \right. \\ & \left. \left. \left. \sqrt{y1o^2 \left(R^2 (x1o^2 + y1o^2) - \left(R^2 + x1o^2 + y1o^2 + 2 \sqrt{R^2} \sqrt{x1o^2 + y1o^2} \right) \cos[\theta]^2 \right)} \right) \right\}, \right. \\ & \left. \left\{ x2o2 \rightarrow \frac{1}{x1o^2 + y1o^2} \left(x1o \left(\sqrt{R^2} + \sqrt{x1o^2 + y1o^2} \right) \cos[\theta] + \right. \right. \right. \\ & \left. \left. \left. \sqrt{y1o^2 \left(R^2 (x1o^2 + y1o^2) - \left(R^2 + x1o^2 + y1o^2 + 2 \sqrt{R^2} \sqrt{x1o^2 + y1o^2} \right) \cos[\theta]^2 \right)} \right) \right\} \right\} \end{aligned}$$