

Water Jug Problem.Aim:

To implement the water jug problem using bfs and state-space (bfs).

Algorithm:

- \* Start
- \* Read the capacities of jug<sub>1</sub>, jug<sub>2</sub> and final capacity of water needed.
- \* Call the function water-jug-bfs().
- \* In function, water-jug-bfs(), add the target values & if the target list is in current list, break the loop in function.
- \* Fill both the jugs and empty both the jugs based on the rule.
- \* If at any instant, the x gallon jug becomes empty, fill it with water.
- \* If at any instant, the y gallon jug becomes empty, fill it with water.
- \* Do steps 5, 6 & 7 till any of the jugs among the x gallon and y gallon jugs contains exactly z liters of water using rules.
- \* Stop

Problem:

We have 2 water jugs, one measure  $x$  gallon & other one measure  $y$  gallon. But there is no measuring label on either of these jugs. (ie) we can't know the exact amount filled in the jug.

i) There is infinite amount of water supply.

ii) We can empty / fill the jugs completely.

iii) We can transfer water from 1 jug to another.

→ Fill 2G of water into anyone of this jug.

Using BFS:

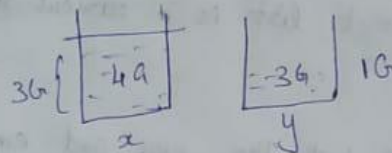
$$x=0 \quad y=0$$

$$x=0 \quad y=3$$

$$x=3 \quad y=0$$

$$x=3 \quad y=3$$

$$x=4 \quad y=2$$

Using State-Space (BFS):

The state space for this problem can be described as the set of ordered pairs of integers  $(x, y)$

$x \rightarrow$  The quantity of water in 4G Jug.

$y \rightarrow$  The quantity of water in 3G Jug.

State space =  $(0, 0)$

Goal state =  $(2, 0)$

# Production Rule:

18CW2

Rule	State	Process
1	$(x, y / x < 4)$	$(4, y)$ {fill The 4G Jug}
2	$(x, y / y < 3)$	$(x, 3)$ {fill The 3G Jug}
3	$(x, y / x > 0)$	$(0, y)$ {empty The 4-gallon jug}
4	$(x, y / y > 0)$	$(x, 0)$ {empty 3G Jug}
5	$(x, y / x + y > 4 \text{ \& } y > 0)$	$(4, y - (4 - x))$ {Pour water from 3 to 4 gallon Jug until 4 gallon jug is full}
6	$(x, y / x + y > 3, x > 0)$	$(x - (3 - y), 3)$ {Pour water from 4 to the other 3G Jug until 3G is full}
7	$(x, y / x + y \leq 4 \text{ \& } y > 0)$	$(x + y, 0)$ {Pour all the water from 3 to 4G Jug}
8	$(x, y / x + y \leq 4)$	$(0, x + y)$ {Pour all the water from 4 to 3G Jug}

Gallon in 4 G Jug (x)	Gallon in 3G Jug (y)	Rule Applied
0	0	1
4	0	6
1	3	4
1	0	8
0	1	1
4	1	6
2	3	4
2	0	Goal achieved.

## **Program:**

### **Breadth First Search:**

```
from collections import deque
```

```
def printPath(target, parent):
```

```
    res = []
```

```
    curr = target
```

```
    src = (-1, -1)
```

```
    while(curr != src):
```

```
        res.append(curr)
```

```
        curr = parent[curr]
```

```
    print()
```

```
    while(len(res) != 0):
```

```
        print(res.pop(), end = " -> ")
```

```
    print("GOAL")
```

```
# Available operations:
```

```
# 1. Fill the jug
```

```
# 2. Empty the jug
```

```
# 3. Transfer jug contents
```

```
def water_jug_bfs(j1, j2, water):
```

```
    visited = set()
```

```
    # To hold the already visited nodes
```

```
    q = deque()
```

```
    # To hold the bfs queue
```

```
    parent = dict()
```

```
    # To store parent of any node
```

```
    q.append((0, 0))
```

```
    # initially we start with (0, 0) as the starting state
```

```
    visited.add((0, 0))
```

```
    parent[(0, 0)] = (-1, -1)
```

```
    # the starting state has no parent
```

```
    isSolvable = False
```

```
    # Sometimes problem cant be solved
```

```
    target = [(0, water), (water, 0)] # required target state
```

```
    while(len(q) != 0):
```

```

curr = q.popleft();
if(curr in target):
    isSolvable = True
    break

curr_j1, curr_j2 = curr[0], curr[1]
possibilities = []

possibilities.append((j1, curr_j2)) # 1a) Fill jug1
possibilities.append((curr_j1, j2)) # 1b) Fill jug2

possibilities.append((0, curr_j2)) # 2a) Empty jug1
possibilities.append((curr_j1, 0)) # 2b) Empty jug2

# 3a) Jug-1 to Jug-2
# cant transfer when jug-1 is empty and jug-2 is already full
if(curr_j1 != 0 and curr_j2 != j2):
    total_water = curr_j1 + curr_j2
    # when total capacity is less than jug-2 capacity
    if(total_water <= j2): possibilities.append((0, total_water))
    # when total capacity is greater than jug-2 capacity
    else: possibilities.append((total_water-j2, j2))

# 3b) Jug-2 to Jug-1
# cant transfer when jug-2 is empty and jug-1 is already full
if(curr_j1 != j1 and curr_j2 != 0):
    total_water = curr_j1 + curr_j2
    # when total capacity is less than jug-1 capacity
    if(total_water <= j1): possibilities.append((total_water, 0))
    # when total capacity is greater than jug-1 capacity
    else: possibilities.append((j1, total_water-j1))

for poss in possibilities:
    if(poss not in visited):
        x, y = poss[0], poss[1]
        q.append((x, y))
        visited.add((x, y))
        parent[(x, y)] = curr

```

```

if(isSolvable):
    printPath(curr, parent)
else:
    print("Not possible to work with these inputs")

```

```

if __name__ == "__main__":

```

```

    jug1 = int(input("Enter jug 1 capacity : "))
    jug2 = int(input("Enter jug 2 capacity : "))
    water = int(input("Enter final capacity of water needed : "))
    water_jug_bfs(jug1, jug2, water)

```

### **Output:**

```

Enter jug 1 capacity : 4
Enter jug 2 capacity : 3
Enter final capacity of water needed : 2
(0, 0) -> (0, 3) -> (3, 0) -> (3, 3) -> (4, 2) -> (0, 2) -> GOAL

```

### **Using State Space (BFS):**

```

from collections import deque

```

```

def water_jug_bfs(j1, j2, water):

```

```

    visited = set()           # To hold the already visited nodes
    q = deque()              # To hold the bfs queue
    q.append((0, 0))         # initially we start with (0, 0) as the starting state
    print("\n", (0, 0))
    visited.add((0, 0))
    isSolvable = False       # Sometimes problem cant be solved

```

```
target = [(0, water), (water, 0)] # required target state
```

```
while(len(q) != 0):
```

```
    size = len(q)
```

```
    print("\n\n *** \n")
```

```
    for _ in range(size):
```

```
        curr = q.popleft();
```

```
        if(curr in target):
```

```
            isSolvable = True
```

```
            break
```

```
        curr_j1, curr_j2 = curr[0], curr[1]
```

```
        possibilities = []
```

```
        possibilities.append((j1, curr_j2)) # 1a) Fill jug1
```

```
        possibilities.append((curr_j1, j2)) # 1b) Fill jug2
```

```
        possibilities.append((0, curr_j2)) # 2a) Empty jug1
```

```
        possibilities.append((curr_j1, 0)) # 2b) Empty jug2
```

```
        # 3a) Jug-1 to Jug-2
```

```
        # cant transfer when jug-1 is empty and jug-2 is already full
```

```
        if(curr_j1 != 0 and curr_j2 != j2):
```

```
            total_water = curr_j1 + curr_j2
```

```
            # when total capacity is less than jug-2 capacity
```

```
            if(total_water <= j2): possibilities.append((0, total_water))
```

```
            # when total capacity is greater than jug-2 capacity
```

```
            else: possibilities.append((total_water-j2, j2))
```

```
        # 3b) Jug-2 to Jug-1
```

```
        # cant transfer when jug-2 is empty and jug-1 is already full
```

```
        if(curr_j1 != j1 and curr_j2 != 0):
```

```
            total_water = curr_j1 + curr_j2
```

```
            # when total capacity is less than jug-1 capacity
```

```
            if(total_water <= j1): possibilities.append((total_water, 0))
```

```
# when total capacity is greater than jug-1 capacity
else: possibilities.append((j1, total_water-j1))
```

```
for poss in possibilities:
    if(poss not in visited):
        x, y = poss[0], poss[1]
        q.append((x, y))
        print((x, y), end= " ")
        visited.add((x, y))
```

```
if(isSolvable == False):
    print("Not possible to work with these inputs")
```

```
if __name__ == "__main__":
```

```
jug1 = int(input("Enter jug 1 capacity : "))
jug2 = int(input("Enter jug 2 capacity : "))
water = int(input("Enter final capacity of water needed : "))
water_jug_bfs(jug1, jug2, water)
```



### **Output:**

```
Enter jug 1 capacity : 4
Enter jug 2 capacity : 3
Enter final capacity of water needed : 2

(0, 0)

***

(4, 0) (0, 3)

***

(4, 3) (1, 3) (3, 0)

***

(1, 0) (3, 3)

***

(0, 1) (4, 2)

***

(4, 1) (0, 2)

***

(2, 3)

***

(2, 0)
```

### **Result:**

Thus the rule based system (i.e) Water Jug Problem is implemented using bfs and State\_space (bfs).