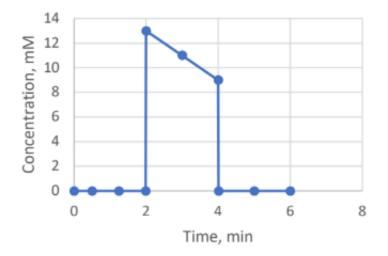
Seminar_1

January 14, 2020

Q1. A pulse tracer input into a PFR showed the following outlet concentration: The experimental data between 2 and 4 min were fit into the line equation $C_{out} = -2t + 17$, with C_{out} in [mM]* and t in [min].

- a) Find the RTD function.
- b) Find mean residence time.
- c) Find variance.
- d) What is the fraction of material that spends in the reactor 3 minutes and longer?
 - [M] means [mol/L] it is a molar concentration in a fluid (gas or liquid)

Exiting tracer concentration (pulse input)



```
[1]: import numpy as np
t=np.linspace(0.,8.,100)
C=np.zeros(len(t))

for i in range(0,len(t)):
    if 0<t[i]<2:
        C[i]=0
    elif 2<=t[i]<=4:</pre>
```

```
C[i] = -2*t[i] + 17
         else:
             C[i]=0
    import matplotlib.pyplot as plt
    plt.plot(t,C)
    plt.ylabel('Concentration, mM')
    plt.xlabel('Concentration, mM')
[1]: Text(0.5, 0, 'Concentration, mM')
      \int_0^\infty C(t)dt = 0 + \int_2^4 (-2*t + 17)dt + 0 = -2\int_2^4 tdt + 17\int_2^4 dt = 22
[2]: import numpy as np
    import scipy.integrate as integrate
    t=np.linspace(0.,8.,10000)
    C=np.zeros(len(t))
    for i in range(0,len(t)):
         if 0<t[i]<2:</pre>
             C[i]=0
         elif 2<=t[i]<=4:
             C[i] = -2*t[i] + 17
         else:
```

22.003

RTD function : $E(t) = \frac{C(t)}{\int_0^\infty C(t)dt}$

I = integrate.cumtrapz(C, t, initial=0)
print ("{0:.3f}".format(I[len(I)-1]))

C[i]=0

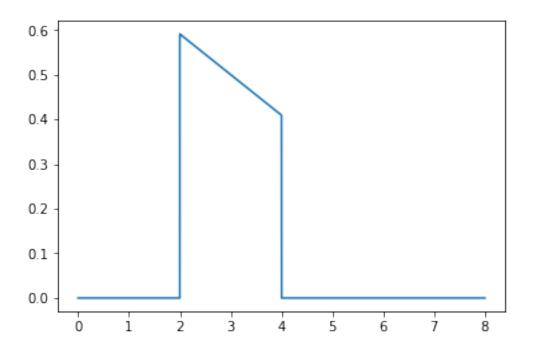
```
[3]: import numpy as np
import matplotlib.pyplot as plt
E=np.zeros(len(t))

for i in range(0,len(t)):
    # if 0<t[i]<2:
    # E[i]=0
    # elif 2<=t[i]<=4:
    # E[i]=(-2*t[i]+17)/22
# else:
    # E[i]=0

    E[i]=C[i]/I[len(I)-1]
E</pre>
```

plt.plot(t,E)

[3]: [<matplotlib.lines.Line2D at 0x7f5654104438>]



b. Mean residence time $\bar{t} = \int_0^\infty t E(t) dt = 0 + \int_2^4 t E(t) dt + 0 = \int_2^4 \left(t \frac{-2t+17}{22}\right) dt = -\frac{2}{22} \left(\frac{4^3}{3} - \frac{2^3}{3}\right) + \frac{17}{22} \left(\frac{4^2}{2} - \frac{2^2}{2}\right) = 2.9 min$

```
[4]: t_r=np.zeros(len(t))
for i in range(0,len(t)):
    t_r[i]=t[i]*E[i]

tr = integrate.trapz(t_r, t)

print ("mean residence time ={0:.3f}".format(tr))
```

mean residence time =2.939

c. Find the varience $\sigma^2 = \int_0^\infty t^2 E(t) dt - \bar{t}^2 = \int_2^4 t^2 (\frac{-2t+17}{22}) dt - 2.9^2 = \frac{-1}{11} (\frac{4^4}{4} - \frac{2^4}{4}) + \frac{17*4^3}{22*3} - \frac{17*2^3}{22*3} - 2.9^2 = 0.56 min^2$ [13]: v = np.zeros(len(t))for i in range(0,len(t)): v[i] = t[i] * t[i] * E[i]

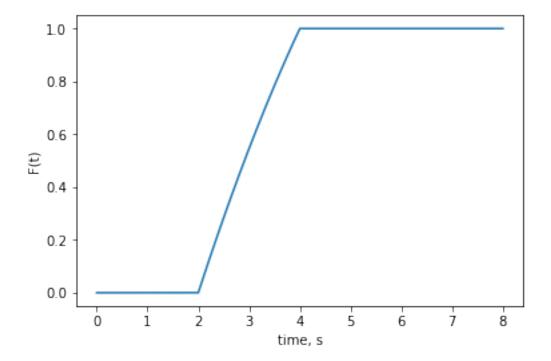
Varience of residence times =0.330 min^2 vs 0.559 min^2

d. Fraction of the material spends in the reactor longer than 3 min.

We use cumulative distribution function, $F(t) = \int_0^t E(t)dt$.

```
\begin{array}{l} 1-F(t)?\\ F(3)=\int_0^3 t dt + \frac{17}{22} \int_2^3 dt = \frac{-2}{22} (\frac{3^2}{2} - \frac{2^2}{2}) + \frac{17}{22} (3-2) = 0.545\\ 1\text{-F(3)} = 0.455 \end{array}
```

Fraction spends in the reactor less than 3 min = 0.545 Fraction spends in the reactor greater than 3 min = 0.455



Q2. Residence time distribution in real reactors and its characteristics. From Chapter 13, 4th Ed. Fogler

The following data were obtained from a pulse tracer test to a real flow reactor:

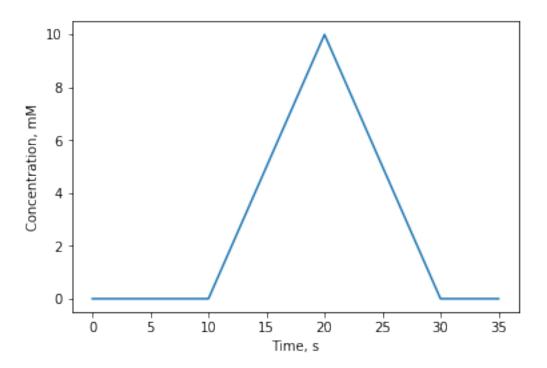
t(s)	0	5	10	15	20	25	30	35
C(mg/dm ³)	0	0	0	5	10	5	0	0

- a) Plot RTD function
- b) Find the fraction of material that spends between 15 and 20 seconds in the reactor
- c) Plot cumulative distribution function F(t)
- d) What fraction of the material spends 25 seconds or less in the reactor?
- e) Find mean residence time.

a. RTD function is $E(t) = \frac{C(t)}{\int_0^\infty C(t)dt}$ To find the total concentration in the denominator, we plot C(t) vs. time and evaluate the area:

```
C_{t}
O_{t}
O_{t
```

[20]: Text(0.5, 0, 'Time, s')



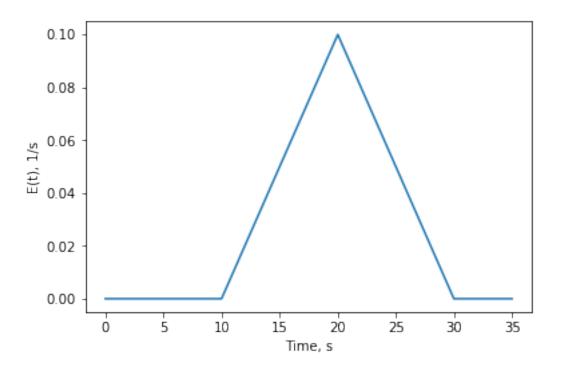
```
[24]: I2 = integrate.cumtrapz(C2, t2, initial=0) print ("The total concentration in denominator ={0:.3f}".format(I[len(I)-1]), 

→"mg.s/dm^3")
```

The total concentration in denominator =22.003 mg.s/dm³

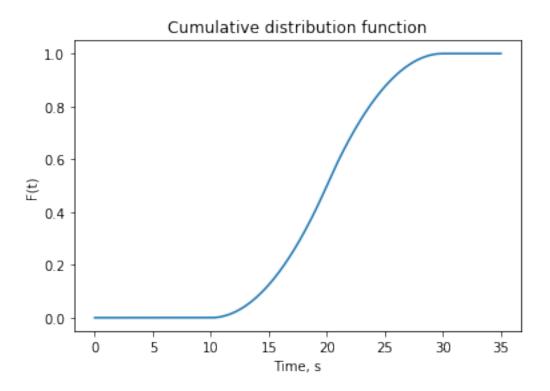
```
RTD function is () = () \int_0^\infty ()
```

[27]: Text(0.5, 0, 'Time, s')



b. Fraction of material spending between 15 and 20 s. $\int_{15}^{20} E(t) dt$

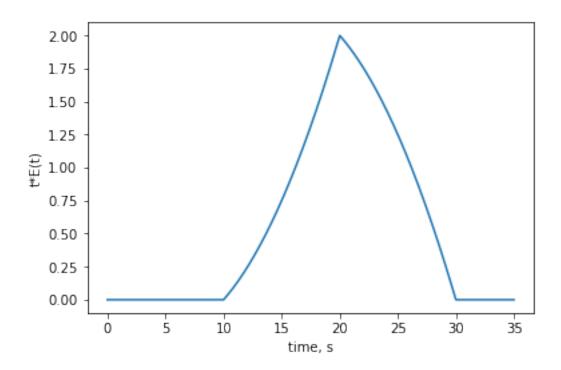
37.051~% of material spends between 15-20 seconds in the reactor



```
[75]: k3=0
     k4=0
     k5=0
     k6=0
     for i in range(0,len(t2)):
         if 14.99 < t2[i] < 15.03:</pre>
              k3=i
         if 19.99 < t2[i] < 20.02:</pre>
              k4=i
         if 24.99 < t2[i] < 25.02:</pre>
              k5=i
         if 29.99 < t2[i] < 30.02:</pre>
              k6=i
     print ("Fraction spends in the reactor:")
     print ("
                      less than 10 s = ", 0)
                      less than 15 s = \{0:.3f\}".format(y2[k3-1]))
     print ("
                      less than 20 s = \{0:.3f\}".format(y2[k4-1]))
     print ("
     print ("
                      less than 25 s = \{0:.3f\}".format(y2[k5-1]))
                      less than 30 s = \{0:.3f\}".format(y2[k6-1]))
     print ("
     print ("
                      less than 35 s = \{0:.3f\}".format(y2[len(y2)-1]))
```

```
print ("{0:.1f}".format(y2[k5-1]*100), "% of material spends 25 seconds or less_
      →in the reactor")
    Fraction spends in the reactor:
             less than 10 s = 0
             less than 15 s = 0.123
             less than 20 s = 0.497
             less than 25 s = 0.874
             less than 30 s = 1.000
             less than 35 s = 1.000
    87.4 \% of material spends 25 seconds or less in the reactor
       e. mean residence time. \bar{t} = \int_0^\infty t \cdot E(t) dt
[76]: t_r2=np.zeros(len(t2))
     for i in range(0,len(t2)):
         t_r2[i]=t2[i]*E2[i]
     tr2 = integrate.trapz(t_r2, t2)
     print ("mean residence time ={0:.1f}".format(tr2), 's')
     plt.plot(t2,t_r2)
     plt.ylabel('t*E(t)')
     plt.xlabel('time, s')
     k33=0
     k44=0
     k55=0
     k66=0
     for i in range(0,len(t2)):
         if 14.99 < t2[i] < 15.03:</pre>
             k33=i
         if 19.99 < t2[i] < 20.02:
             k44=i
         if 24.99 < t2[i] < 25.02:</pre>
             k55=i
         if 29.99 < t2[i] < 30.02:</pre>
             k66=i
```

mean residence time =20.0 s



[]: