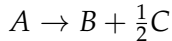
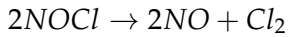


ChE445_Seminar5_Winter2020_Solution

February 11, 2020

Q 1. Again review of 345: conversion in an ideal PFR. 20 pts

(adapted from Fogler's 4th Ed. Elements of Chemical Reaction engineering). $2\text{NOCl} \rightarrow 2\text{NO} + \text{Cl}_2$ The second-order gas-phase reaction is carried out in a steady-state isothermal isobaric ideal PFR. Pure NOCl is fed with an inlet flow rate of $2.26 \times 10^{-5} \frac{\text{mol}}{\text{s}}$ and initial concentration of $0.283 \frac{\text{mol}}{\text{L}}$. The rate constant with respect to A is $267 \text{L}/(\text{mol.s})$. Find reactor volume to decrease the exit molar flow rate of NOCl to $0.339 \times 10^{-5} \frac{\text{mol}}{\text{s}}$.



Stoichiometry Table where $X = X_A = \frac{F_{A0} - F_A}{f_{A0}} = \frac{2.26 - 0.339}{2.26} = 0.85$

Species	Initial	Change	Final
A	F_{A0}	$-F_{A0}X$	$F_A = F_{A0}(1 - X)$
B	0	$F_{A0}X$	$F_B = F_{A0}X$
C	0	$0.5F_{A0}X$	$F_C = 0.5F_{A0}X$
Total	$F_{T0} = F_{A0}$	$\frac{1}{2}F_{A0}X$	$F_{A0}(1 + \frac{1}{2}X)$

At $P, T = \text{cte}$, $Q = Q_0 \frac{F_T}{F_{T0}} = Q_0(1 + \frac{1}{2}X)$

rate law for 2nd order reaction:

$$-r_A = k_A C_A^2$$

$$C_A = \frac{F_A}{Q} = \frac{F_{A0}(1-X)}{Q_0(1+\frac{1}{2}X)} = C_{A0} \frac{1-X}{1+\frac{1}{2}X}$$

Therefore:

$$-r_A = k_A (C_{A0} \frac{1-X}{1+\frac{1}{2}X})^2$$

Mole Balance for an ideal PFR:

$$V = F_{A0} \int_0^X \frac{dX}{-r_A}$$

$$V = F_{A0} \int_0^X \frac{(1+0.5X)^2}{k C_{A0}^2 (1-X)^2} dX$$

Integration rule: $\int_0^X \frac{(1+\epsilon X)^2 dX}{(1-X)^2} = 2\epsilon(1+\epsilon)\ln(1-x) + \epsilon^2 X + \frac{(1+\epsilon)^2 X}{1-X}$

$$V = \frac{2.26 \times 10^{-5}}{267 \times 0.283^2} (2 \times 0.5 \times 1.5 \times \ln(1 - 0.85) + 0.5^2 \times 0.85 + \frac{(1.5)^2 \times 0.85}{1 - 0.85}) = 1.07 \times 10^{-5} \text{ L (microreactor)}$$

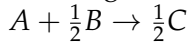
0.0.1 CH E 445, Midterm Exam Fall 2018. 45 minutes. Weight: 24/100.

Q1. A gas-phase irreversible reaction $2A + B \rightarrow C$ occurs in an ideal isobaric isothermal PFR and 80% conversion of A is reached. The feed contains $1 \frac{\text{mol}}{\text{m}^3}$ of A, $5 \frac{\text{mol}}{\text{m}^3}$ of B and $4 \frac{\text{mol}}{\text{m}^3}$ of inerts. The reaction is 2^{nd} order to A and 0^{th} order to B. Rate constant is $3 \frac{\text{m}^3}{\text{mol.s}}$.

1a. Calculate mean residence time.

1b. Is the space time higher or lower than the mean residence time? Explain.

Limiting reactant is A so:



Stoichiometry Table where $X = X_A$

Species	Initial	Change	Final
A	F_{A0}	$-F_{A0}X$	$F_A = F_{A0}(1 - X)$
B	$5F_{A0}$	$-0.5F_{A0}X$	$F_B = F_{A0}(5 - 0.5X)$
C	0	$0.5F_{A0}X$	$F_C = 0.5F_{A0}X$
I	$4F_{A0}$	0	$4F_{A0}X$
Total	$F_{T0} = 10F_{A0}$	$-F_{A0}X$	$F_{A0}(10 - X)$

$$\frac{F_T}{F_{T0}} = \frac{10-X}{10} = 1 - 0.1X$$

$$\text{At } P, T = cte: \frac{Q}{Q_0} = 1 - 0.1X$$

$$\text{At } P, T = cte: \bar{t} = C_{A0} \int_0^X \frac{dX}{-r_A(1+\epsilon X)}$$

$$\text{Rate law: } -r_A = kC_A^2C_B^0 = kC_A^2 = k\frac{F_A^2}{Q^2} = k\frac{F_{A0}^2(1-X)^2}{Q_0^2(1-0.1X)^2} = k\frac{C_{A0}^2(1-X)^2}{(1-0.1X)^2}$$

$$\bar{t} = \frac{C_{A0}}{kC_{A0}^2} \int_0^X \frac{(1-0.1X)^2}{(1-X)^2(1-0.1X)} dX$$

$$\bar{t} = \frac{1}{kC_{A0}} \int_0^X \frac{1-0.1X}{(1-X)^2} dX$$

$$\bar{t} = \frac{1}{3 \times 1} \frac{0.9}{1-0.8} + 0.1 \ln \frac{1}{1-0.8} = \frac{3.76}{3} = 1.25 \text{ s}$$

$$\tau = V/Q_0 =$$

since $Q < Q_0$, ($Q = Q_0(1 - 0.1X)$) then $\tau < \bar{t}$

Q2. 25/100 pts

What fraction of the material spends between 2 and 8 minutes in a liquid-phase ideal CSTR with space time of 4 minutes?

Cumulative function for an ideal CSTR:

$$F = 1 - e^{-t/\tau}$$

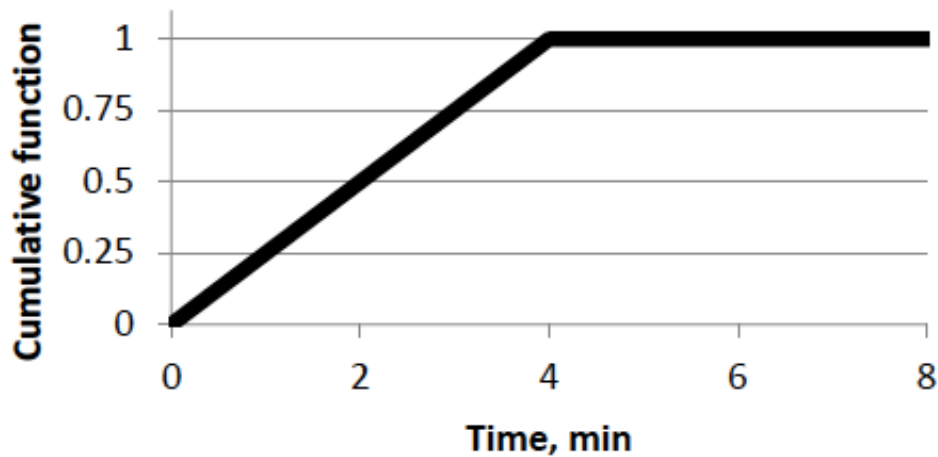
$$\text{up to 8 min: } F = 1 - e^{-8/4} = 0.865$$

$$\text{up to 2 min: } F = 1 - e^{-2/4} = 0.393$$

$$\text{Between: } F(10) - F(2) = 0.472$$

Q3. 25/100 pts

Predict conversion using segregation model for a zero-order liquid phase reaction $A \rightarrow B$ with rate constant of $5 \text{ mol} / (\text{Lmin})$, C_{A0} of $10 \text{ mol} / \text{L}$ using the given cumulative distribution function:



S5Q3.png

Answer

$$\bar{X} = \int_0^{\infty} X(t)E(t)dt$$

$$-r_A = k$$

$$X \text{ from CVBR: } \frac{dX}{dt} = \frac{-r_A}{C_{A0}} = \frac{k}{C_{A0}}$$

$$\int_0^X dX = \frac{k}{C_{A0}} \int_0^t dt$$

$$X = \frac{k}{C_{A0}} t$$

From the plot: $F(t) = 0.25t \quad 0 \leq t \leq 4$ else = 0.

$$F(t) = \frac{dF(t)}{dt}$$

$$E(t) = 0.25 \quad 0 \leq t \leq 4 \text{ else} = 0.$$

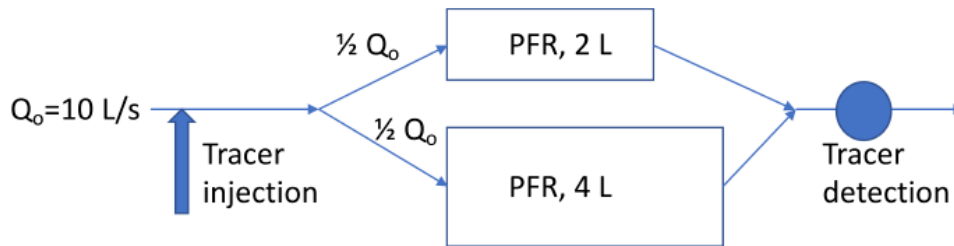
$$\bar{X} = \int_0^4 \frac{0.25k}{C_{A0}} t dt = \frac{0.25 \cdot 5}{10} \frac{1}{2} t^2 [0 \rightarrow 4] = 1$$

Q 4. 25/100 pts

A pulse of tracer is injected in a liquid flow which is equally divided between two ideal PFRs:

4a. Plot the tracer concentration at the point of detection as a function of time.

4b. Plot cumulative distribution function at the point of detection as a function of time. For both graphs in 4a and 4b, clearly indicate relevant numerical values and how they were calculated.



S5Q4.png

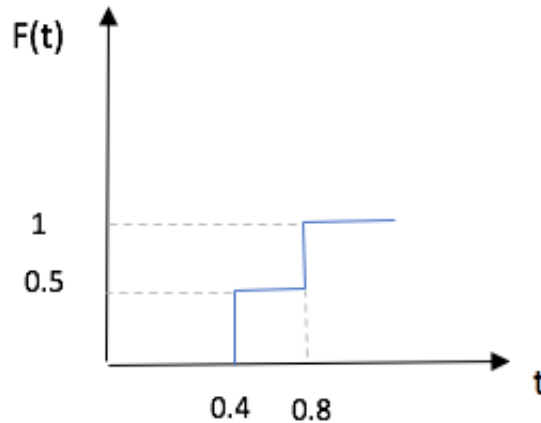
Answer

Ideal PFR

$$2L \text{ PFR: } \tau = \frac{V}{Q_0} = \frac{2L}{5L/s} = 0.4 \text{ s}$$

4L PFR: $\tau = \frac{V}{Q_0} = \frac{4}{5} = 0.8 \text{ s}$

b) since flow is divided in 50% half of the tracer will leave at 0.4s and the rest at 0.8s.



S5Q4-2.png

0.0.2 CH E 445, Midterm Exam Fall 2019. 45 minutes.

Q1. 25/100 pts.

A gas-phase 1st-order irreversible reaction $A \rightarrow 2B$ occurs in an ideal isobaric isothermal CSTR at 5s space-time. 80% conversion of A is reached. The feed contains 7 mol/m^3 of A, 1 mol/m^3 of B and 2 mol/m^3 of inerts.

Calculate mean residence time in this ideal reactor.

Answer.

Stoichiometry Table where $X = X_A$

Species	Initial	Change	Final
A	F_{A0}	$-F_{A0}X$	$F_A = F_{A0}(1 - X)$
B	$\frac{1}{7}F_{A0}$	$2F_{A0}X$	$F_B = F_{A0}(\frac{1}{7} + 2X)$
I	$\frac{2}{7}F_{A0}$	0	$\frac{2}{7}F_{A0}X$
Total	$F_{T0} = \frac{10}{7}F_{A0}$	$F_{A0}X$	$F_{A0}(\frac{10}{7} + X)$

$$Q = Q_0 \frac{F_T}{F_{T0}} = \frac{Q_0(\frac{10}{7} + X)}{\frac{10}{7}}$$

$$\bar{t} = \int_0^V \frac{dV}{Q} = \frac{V}{Q_{exit}} = \frac{V}{Q_0} \frac{10/7}{10/7 + X} = 3.205 \text{ s}$$

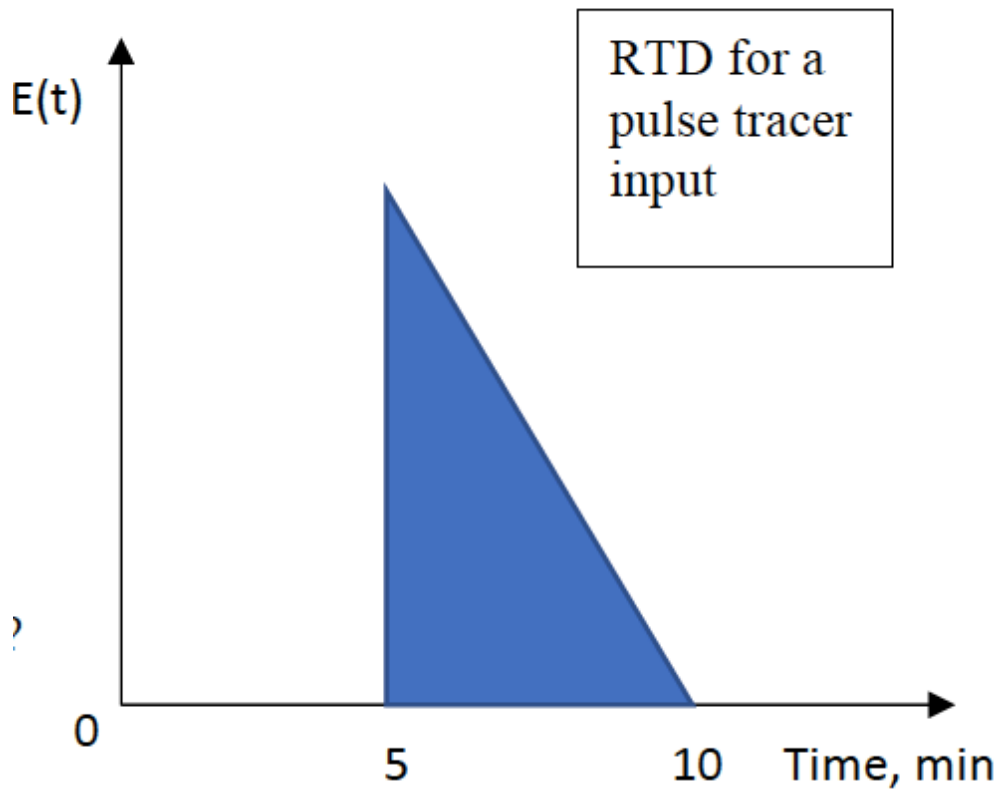
Q2. 25/100 pts

A pulse tracer input was used to determined RTD function in a constant-density flow reactor (see the Figure). All tracer has left by 10 minutes.

2a). Calculate the maximum value of the $E(t)$ function. **10 pts**

2b). What is the maximum achieved value of $F(t)$ function? Explain. **5 pts**

2c). Sketch the exit tracer concentration vs. time if a step tracer input is performed on the same reactor at the same volumetric flow rate. Mark all known numerical values. **10 pts**



S5Q119.png

Answer

2a). $\int_0^{\infty} E(t) dt = 1$ so area under the graph = 1

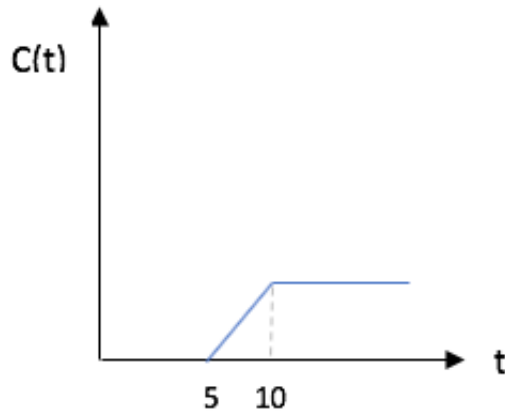
$$1 = \frac{1}{2}X(10 - 5)$$

$$X = 0.4$$

2b). Since all tracer has left the reactor, $F(t)_{max} = 1$

2c). Step tracer input:

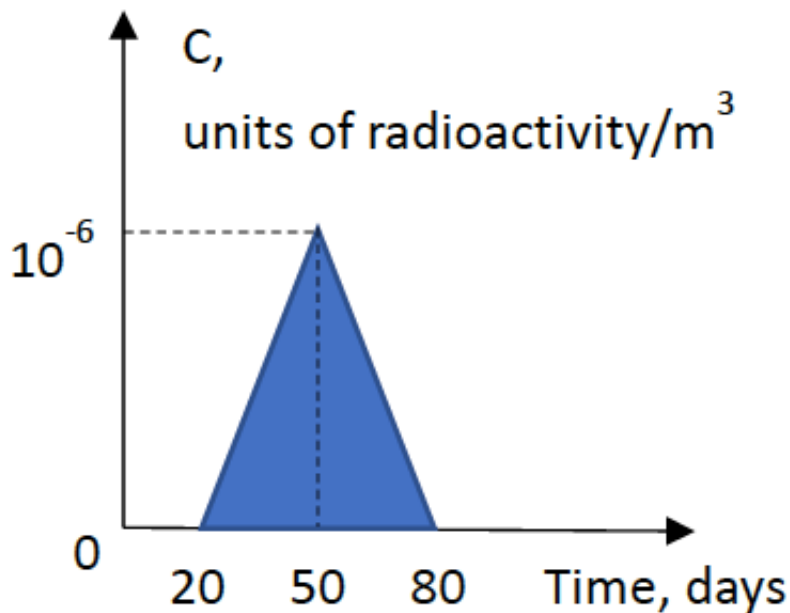
The $F(t)$ plot would be as :



S5Q219.png

no tracer upto 5 min. The tracer reaches its maximum value by 10 min

Q3. 20/100 pts A radioactive waste with half-life time of 100 years was dumped into a river. The flowing waters ($200 \times 10^6 \text{ m}^3/\text{day}$) are monitored downstream for this particular radioisotope. The data are shown in the Figure below:



S5Q319.png

3a). How many radioactive units of this isotope were dumped? 5 pts

3b). What is the volume of the river between the monitoring point and the point of introduction of the waste? 10 pts

3c). Why is the half-life time of the isotope is mentioned? (1-sentence answer). 5 pts

Answer

$$3a) \int_0^{\infty} C(t) dt = \text{Area under the triangle} = 30 \times 10^{-6} \frac{\text{u.r.}}{\text{m}^3} \text{ days}$$

$$30 \times 10^{-6} \times Q = 30 \times 10^{-6} \frac{\text{u.r.}}{\text{m}^3} \text{ days} \times 200 \times 10^6 \frac{\text{m}^3}{\text{day}} = 6000 \text{ u.r.}$$

3b) $\tau = \frac{V}{Q_0}$ here $\tau = \bar{t} = 50 \text{ days}$

$$V = 50 * 200 * 10^6 = 10^{10} \text{ m}^3$$

3c) It does not convert within this time of 80 days, so it can be considered as a non-reactive tracer.

Q4. 30/100 pts

Based on RTD measurements, a real flow reactor can be modelled as a combination of one ideal PFR (8L) followed by one ideal CSTR (4L) in series. The volumetric flow rate of the liquid feed is 2L/s.

4a). Sketch the RTD function of the real reactor. Show and justify all known numerical values on both axes. **15 pts**

4b). Find mean residence time in the real reactor. **5 pts**

4c). Imagine now if 25% of the PFR volume is "dead zones". Sketch the RTD function of the real reactor. Show and justify all known numerical values on both axes. **10 pts**

Answer

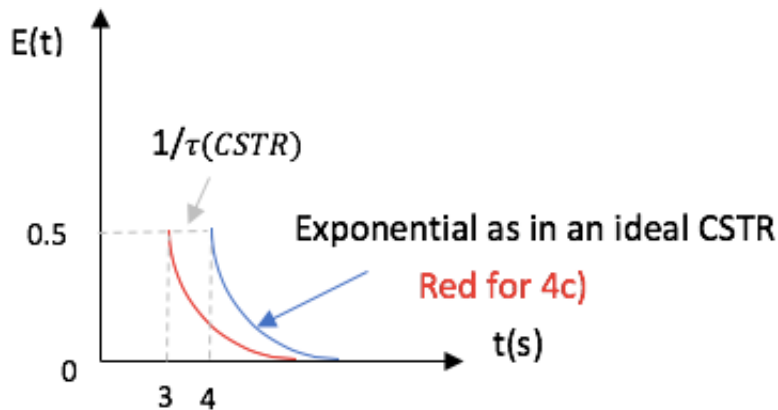
4a) $\tau_{PFR} = \frac{V}{Q_0} = \frac{8}{2} = 4 \text{ s}$

$\tau_{CSTR} = \frac{4}{2} = 2 \text{ s}$

PFR only delays the ideal exit from CSTR.

4b) $\bar{t} = \tau = 4 + 2 = 6 \text{ s}$

4c) For PFR $\tau_{new,PFR} = \frac{0.75*8L}{2L/s} = 3 \text{ s}$ τ_{CSTR} the same.



S5Q419.png

[]: