# Tree Implementation

## Today's Plan



Recap

BST Implementation

```
#ifndef BST H
#define BST H
#include <memory>
using namespace std;
template<typename ItemType>
class BST
public:
   BST(); // constructor
   BST(const BST<ItemType>& tree); // copy constructor
   ~ BST(); // destructor
   bool isEmpty() const;
   size t getHeight() const;
   size t getNumberOfNodes() const;
   void add(const ItemType& new item);
   void remove(const ItemType& new item);
   ItemType find(const ItemType& item) const;
   void clear();
   void preorderTraverse(Visitor<ItemType>& visit) const;
   void inorderTraverse(Visitor<ItemType>& visit) const;
   void postorderTraverse(Visitor<ItemType>& visit) const;
   BST& operator= (const BST<ItemType>& rhs);
                                                      Let's try something new
private:
                                                       and use shared ptr:
   shared ptr<BinaryNode<ItemType>> root ptr ;
                                                       A bit of extra syntax at
}; // end BST
                                                      declaration but then you
#include "BST.cpp"
                                                        use them as regular
#endif // BST H
                                   3
```

To implement this as a linked structure what do we need to change in our previous implementation ???

## BinaryNode



```
#ifndef BinaryNode H
#define BinaryNode H
                              For shared ptr
#include <memory> _
using namespace std;
template<typename ItemType>
class BinaryNode
public:
   BinaryNode();
   BinaryNode(const ItemType& an item);
   void setItem(const ItemType& an item);
   ItemType getItem() const;
   bool isLeaf() const;
   auto getLeftChildPtr() const;
   auto getRightChildPtr() const;
   void setLeftChildPtr(shared ptr<BinaryNode<ItemType>> left ptr);
   void setRightChildPtr(shared_ptr<BinaryNode<ItemType>> right ptr);
private:
   ItemType item ; // Data portion
   shared ptr<BinaryNode<ItemType>> left ;  // Pointer to left child
   shared ptr<BinaryNode<ItemType>> right ; // Pointer to right child
}; // end BST
#include "BinaryNode.cpp"
#endif // BinaryNode H
                                      6
```

### Lecture Activity

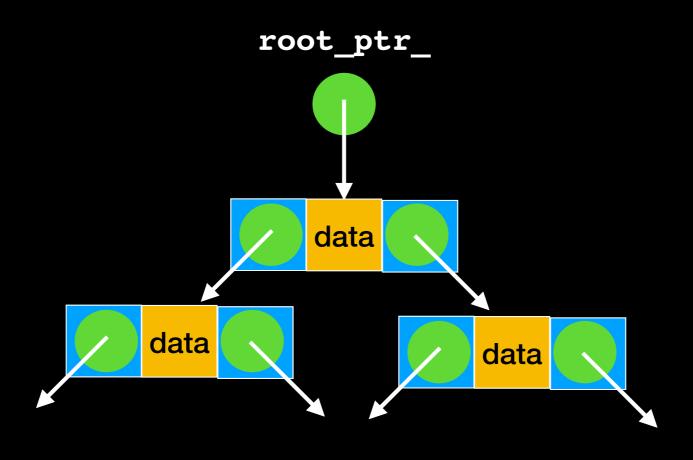
#### Implement:

```
BinaryNode(const ItemType& an_item);
bool isLeaf() const;

void setLeftChildPtr(shared_ptr<BinaryNode<ItemType>> left_ptr);
```

```
template<typename ItemType>
BinaryNode<ItemType>::BinaryNode(const ItemType& an item)
                                : item (an item){ }//end constructor
template<typename ItemType>
bool BinaryNode<ItemType>::isLeaf() const
{
   return ((left_ == nullptr) && (right_ == nullptr));
} // end isLeaf
template<typename ItemType>
void BinaryNode<ItemType>::setLeftChildPtr(
                           shared ptr<BinaryNode<ItemType>> left ptr)
  left = left ptr;
   // end setLeftChildPtr
```

## BST



```
#ifndef BST H
#define BST H
#include <memory>
using namspace std;
template<typename ItemType>
class BST
public:
   BST(); // constructor
   BST(const BST<ItemType>& tree); // copy constructor
   ~ BST(); // destructor
   bool isEmpty() const;
   size t getHeight() const;
   size t getNumberOfNodes() const;
   void add(const ItemType& new item);
   void remove(const ItemType& new item);
   ItemType find(const ItemType& item) const;
   void clear();
   void preorderTraverse(Visitor<ItemType>& visit) const;
   void inorderTraverse(Visitor<ItemType>& visit) const;
   void postorderTraverse(Visitor<ItemType& visit) const;</pre>
   BST& operator= (const BST<ItemType>& rhs);
private:
   shared_ptr<BinaryNode<ItemType>> root_ptr_;
}; // end BST
#include "BST.cpp"
                                  10
#endif // BST H
```

We want our interface to be generic and not tied to implementation. Many of these will therefore use helper functions, which should be private (or protected if you envision inheritance). I do not include them here in the interface for lack of space.

## Copy Constructor

```
root_ptr of
this object

templa re<typename ItemType>
BST<ItemType>::BST(const BST<ItemType>& tree)
{
   root_ptr of tree: the
   object I'm going to copy

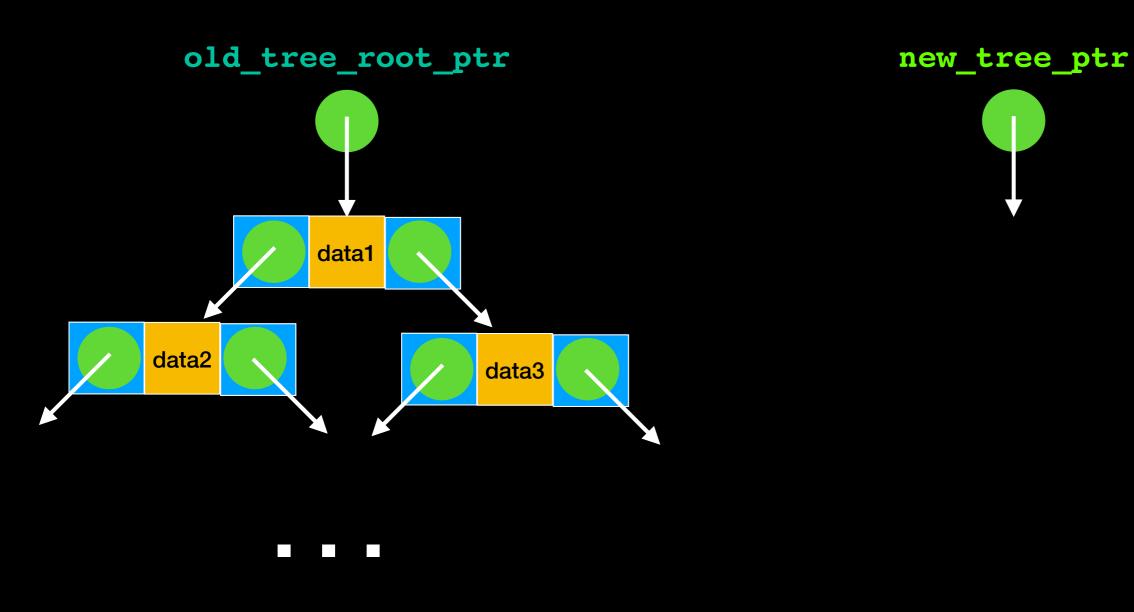
templa re<typename ItemType>
BST<ItemType>& tree)
{
   root_ptr = copyTree(tree.root_ptr_); // Call helper function
} // end copy constructor
```

Safe programming: the public method does not take pointer parameter.

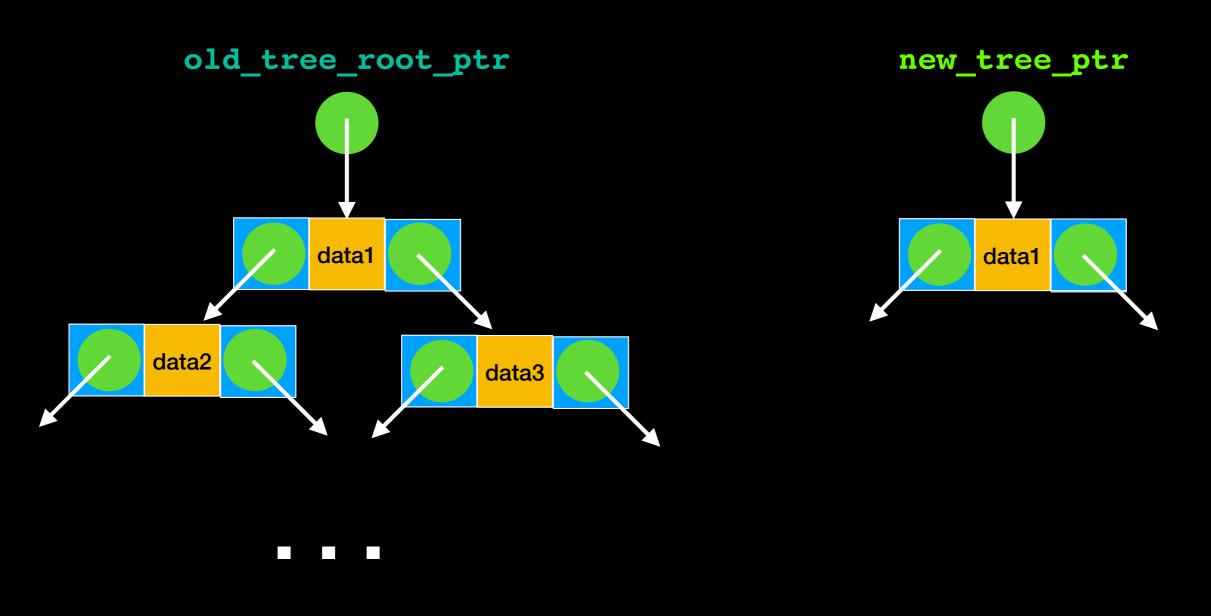
Only protected/private methods have access to pointers and may modify tree structure

I can use the . operator to access a private member variable because it is s within the class definition.

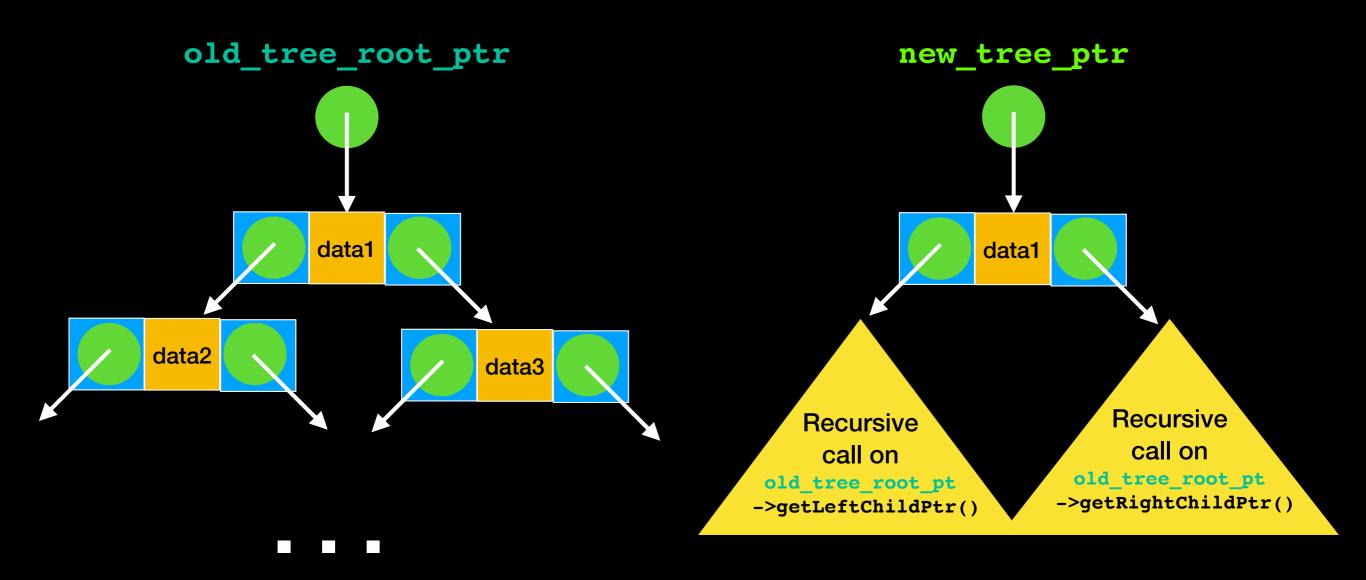
#### copyTree(old\_tree\_root\_ptr)



#### copyTree(old\_tree\_root\_ptr)



### copyTree(old\_tree\_root\_ptr)



Returning shared ptr, cleaner to use auto return type: -std=c++14

## Copy Constructor Helper Function

```
template<typename ItemType>
auto BST<ItemType>::copyTree(const
shared ptr<BinaryNode<ItemType>> old tree root ptr) const
                                                         Recall: this is the syntax
   shared ptr<BinaryNode<ItemType>> new tree ptr;
                                                          for allocating a "new"
   // Copy tree nodes during a preorder traversal
                                                         object with shared ptr
   if (old tree root ptr != nullptr)
                                                             pointing to it
      // Copy node
      new tree ptr = make shared<BinaryNode<ItemType>>
                     (old tree root ptr->getItem(), nullptr, nullptr);
      new tree ptr->setLeftChildPtr(copyTree(old tree root ptr
                                                    ->getLeftChildPtr());
      new tree ptr->setRightChildPtr(copyTree(old_tree_root_ptr
                                                     >getRightChildPtr()));
                                 Recursive Calls:
   } // end if
                              Don't want to tie interface
                                                           Preorder Traversal
   return new tree ptr;
                                   to recursive
                                                         Scheme: copy each node
   // end copyTree
                                 implementation:
                                                         as soon as it is visited to
                                Use helper function
```

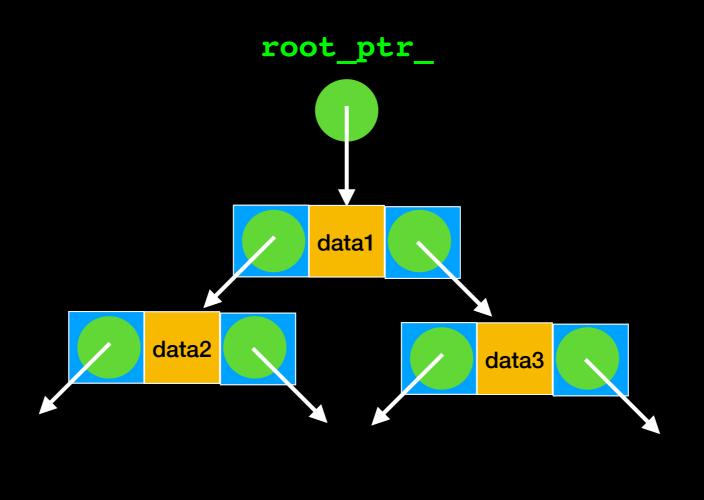
make exact copy

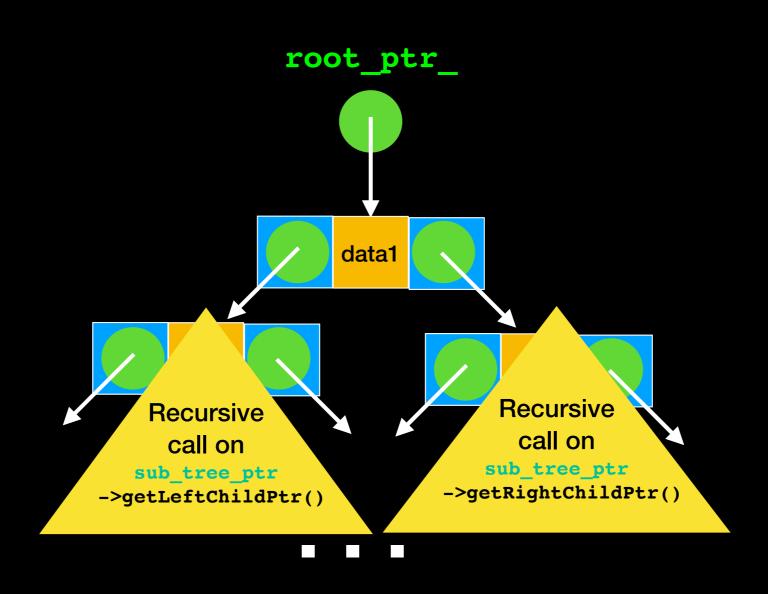
### Destructor

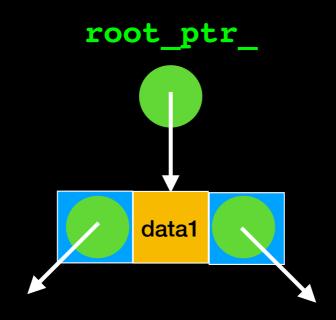
```
template<typename ItemType>
BST<ItemType>::~BST()
{
   destroyTree(root_ptr_); // Call helper function
} // end destructor
```

Safe programming: the public method does not take pointer parameter.

Only protected/private methods have access to pointers and may modify tree structure







root\_ptr\_.reset()



## Destructor Helper Function

Notice: all we have to do is set the shared\_ptr to nullptr with reset() and it will take care of deleting the node.

PostOrder Traversal Scheme:
Delete node only after deleting
both of its subtrees

#### clear

```
template<typename ItemType>
void BST<ItemType>::clear()
{
    destroyTree(root_ptr_); // Call helper method
} // end clear
```

Safe programming: the public method does not take pointer parameter.

Only protected/private methods have access to pointers and

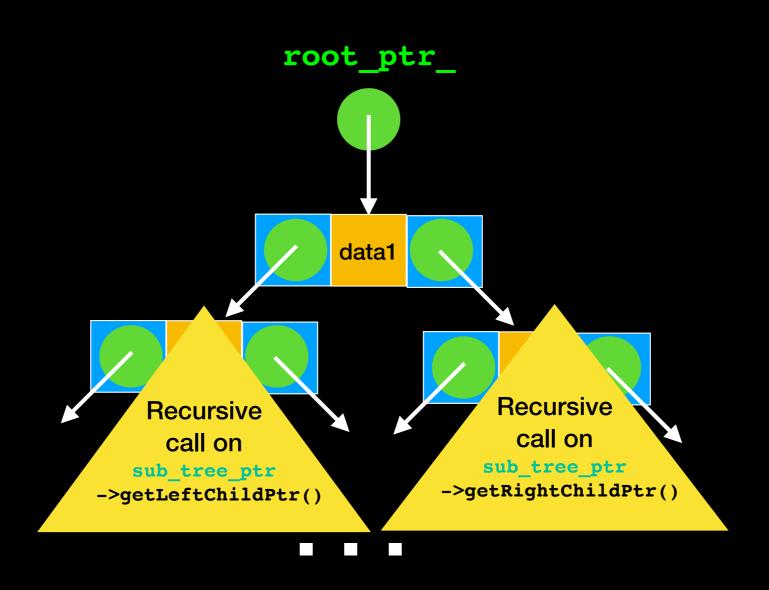
may modify tree structure

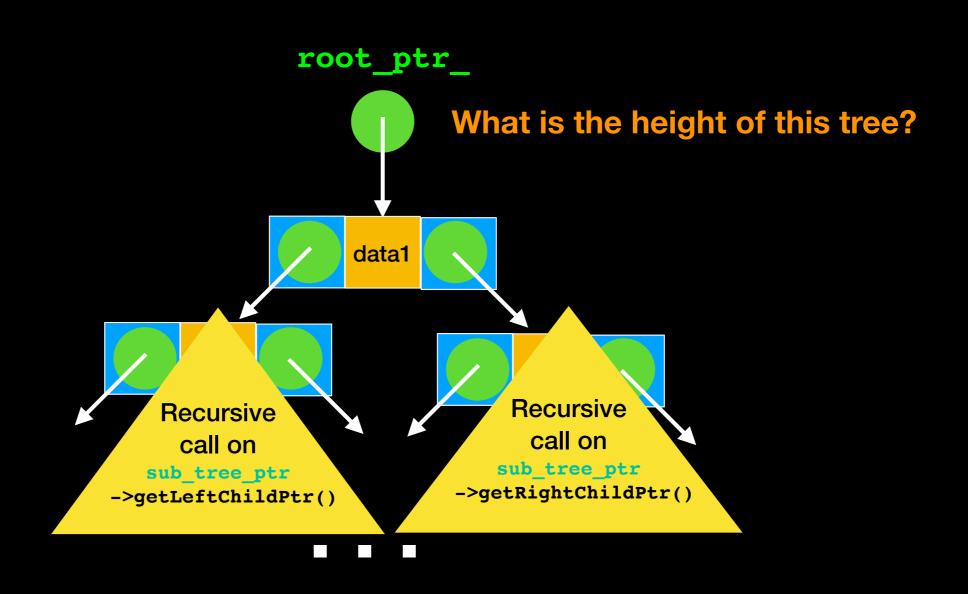
## getHeight

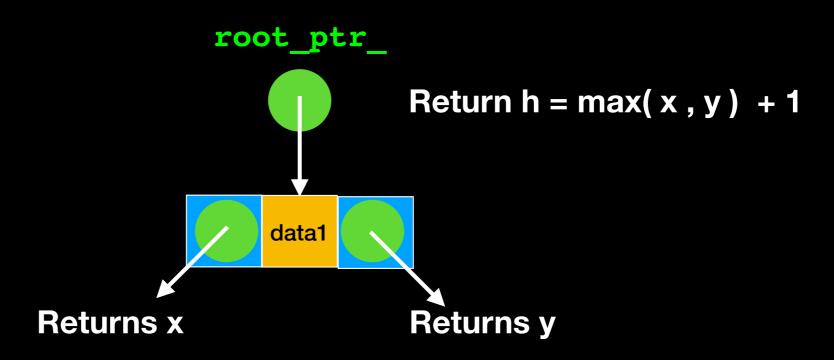
```
template<typename ItemType>
int BST<ItemType>::getHeight() const
{
    return getHeightHelper(root_ptr_);
} // end getHeight
```

Safe programming: the public method does not take pointer parameter.

Only protected/private methods have access to pointers and may modify tree structure









#### Similarly: implement these at home!!!

### add and remove

Key methods: determine order of data

Distinguish between different types of Binary Trees

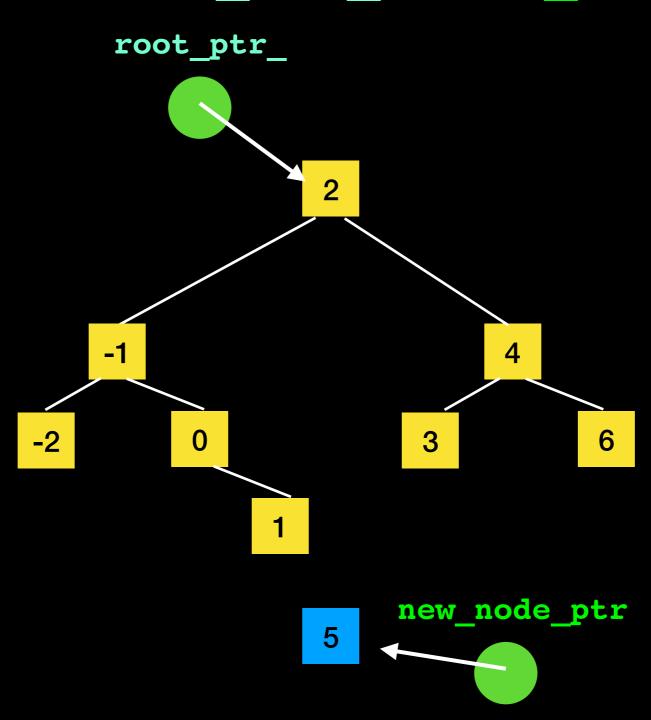
Implement the BST structural property

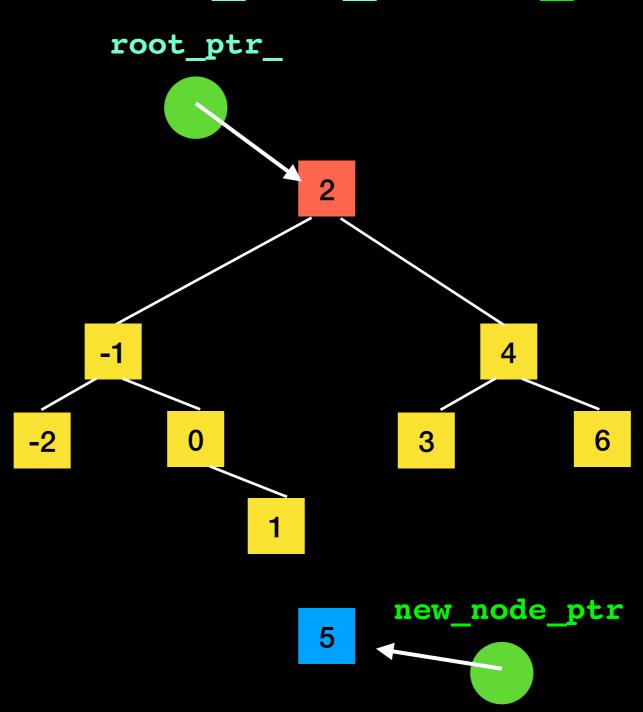
#### add

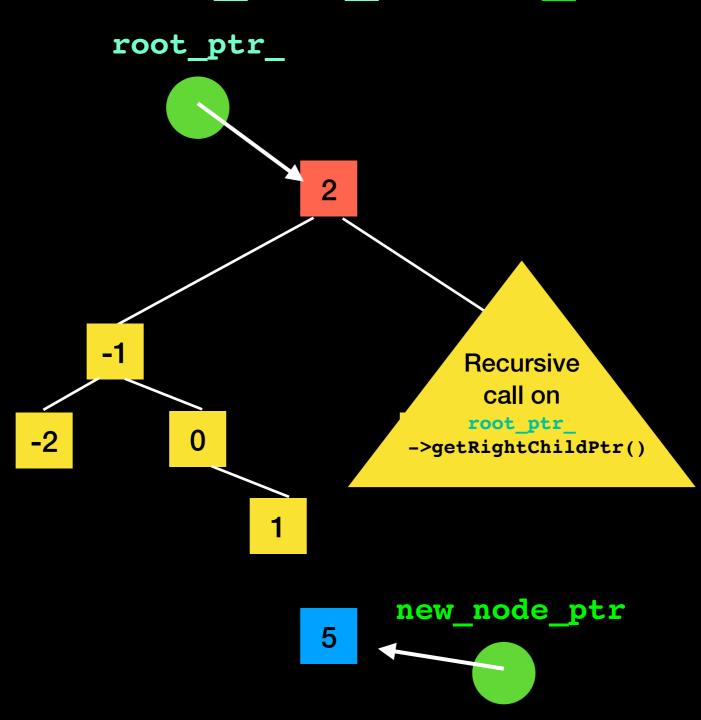
```
using namespace std;

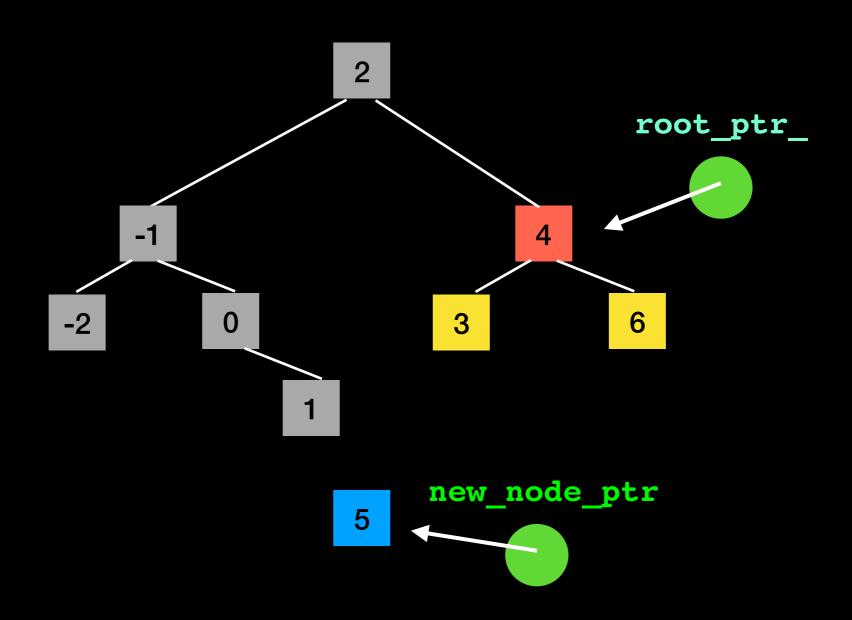
template<typename ItemType>
void BST<ItemType>::add(const ItemType& new_item)
{
    auto new_node_ptr =
        make_shared<BinaryNode<ItemType>>(new_item);
    placeNode(root_ptr_, new_node_ptr);
} // end add
```

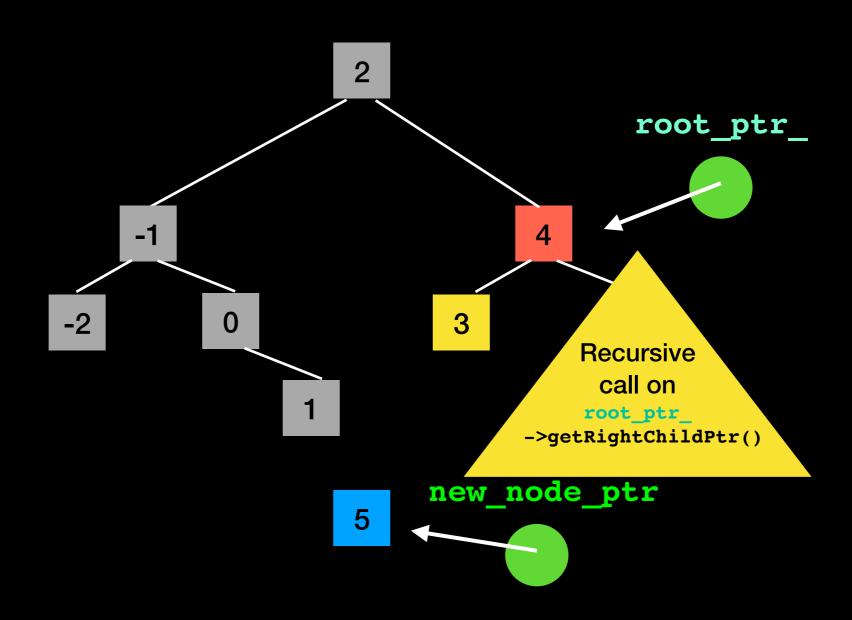
Safe programming: the public method does not take pointer parameter.
Only protected/private methods have access to pointers and may modify tree structure

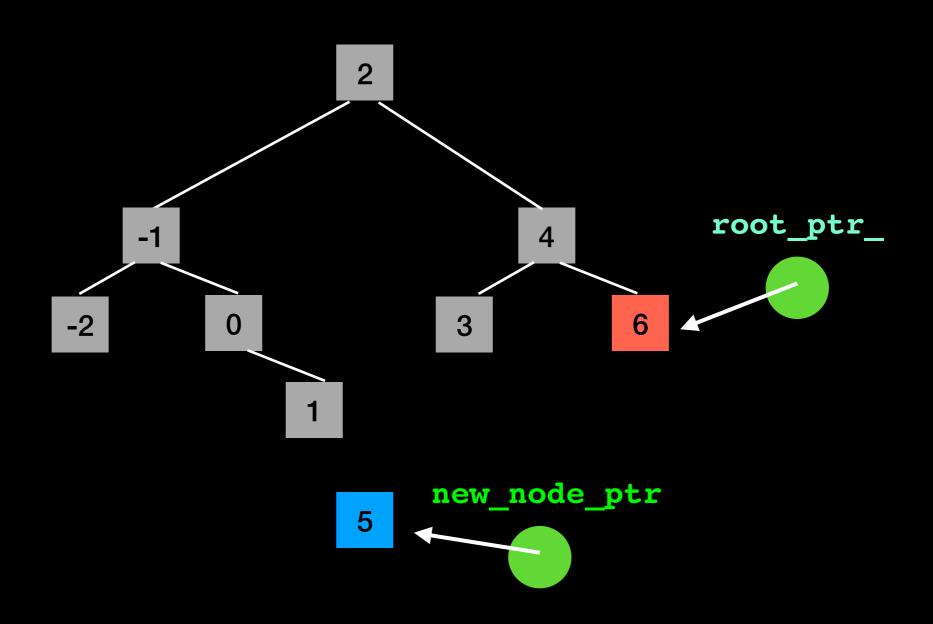


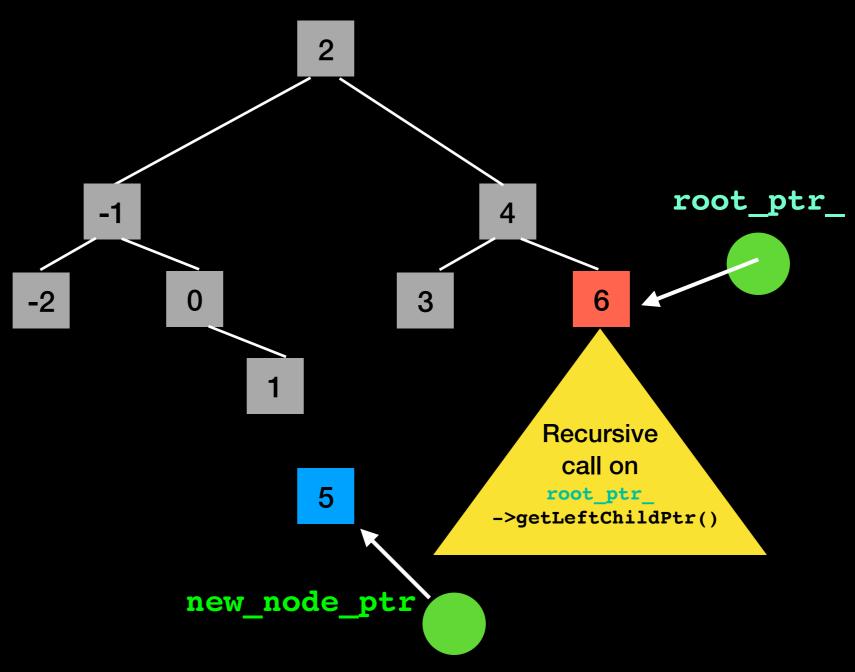


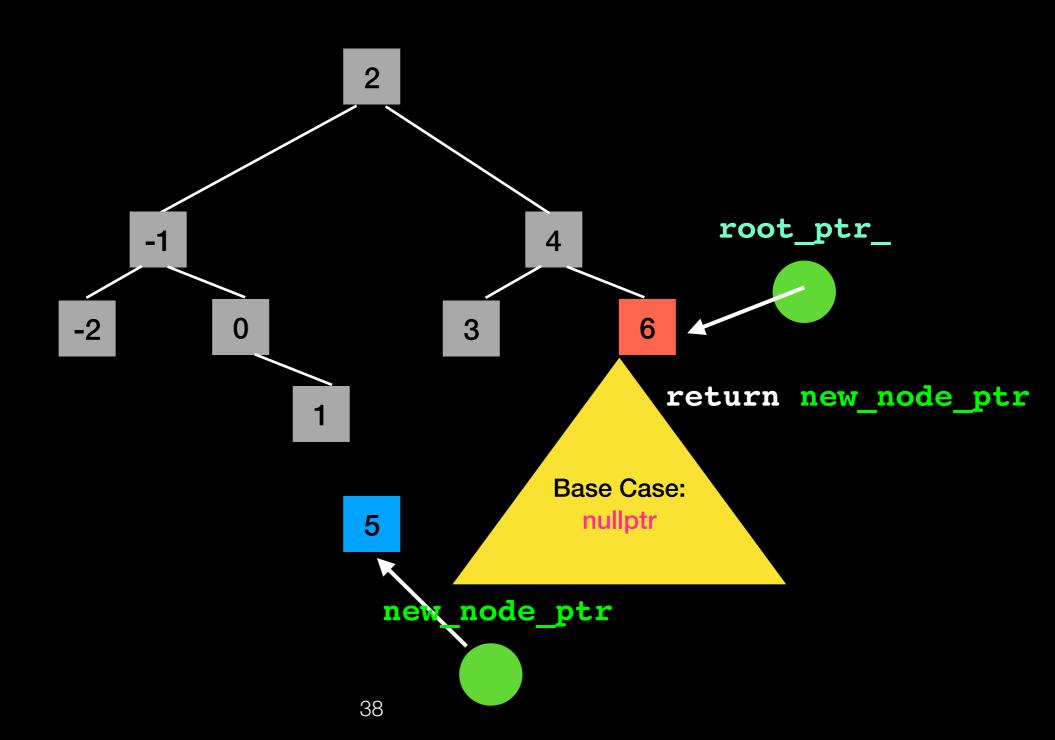


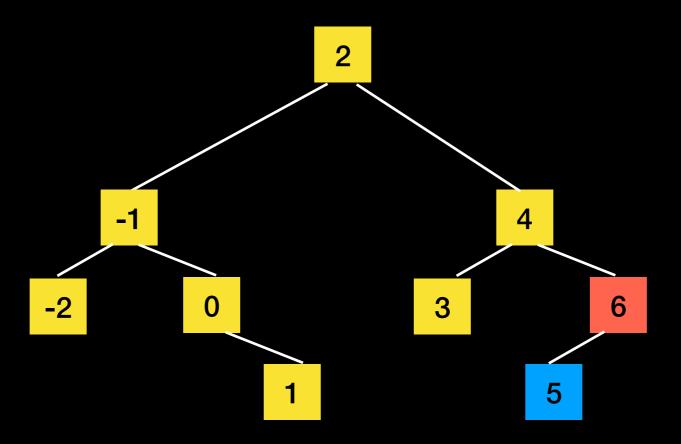


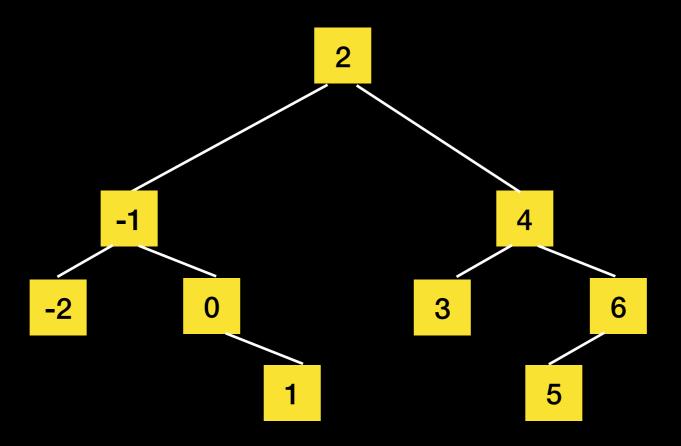












## add helper function

```
template<typename ItemType>
auto BST<template<typename ItemType>::placeNode(
     shared ptr<BinaryNode<template<typename ItemType>>> subtree ptr,
     shared_ptr<BinaryNode<template<typename ItemType>>> new_node_ptr)
   if (subtree ptr == nullptr)
      return new_node_ptr; //base case
   else
   {
      if (subtree ptr->getItem() > new node ptr->getItem())
          subtree_ptr->setLeftChildPtr(placeNode(subtree ptr
          ->getLeftChildPtr(), new_node_ptr));
      else
         subtree ptr->setRightChildPtr(placeNode(subtree ptr
         ->getRightChildPtr(), new_node_ptr));
      return subtree ptr;
   } // end if
} // end placeNode
```

using namespace std;

### remove

```
template<typename ItemType>
bool BST<ItemType>::remove(const ItemType& target)
{
   bool is_successful = false;
   // call may change is_successful
   root_ptr_ = removeValue(root_ptr_, target, is_successful);
   return is_successful;
} // end remove
```

Only protected/private methods have access to pointers and may modify tree structure

Safe programming: the public

method does not take pointer

parameter.

# remove helper function

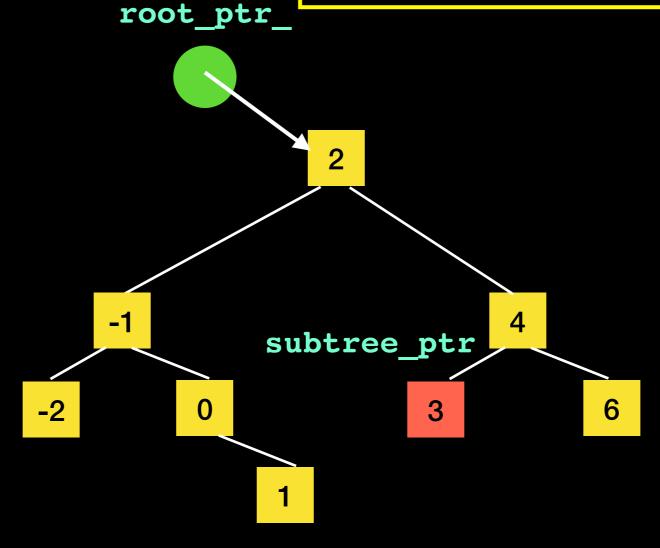
Looks for the value to remove

```
template<typename ItemType>
auto BST<ItemType>::removeValue(std::shared ptr<BinaryNode<ItemType>>
                                  subtree ptr, const ItemType target,
                                  bool& success)
   if (subtree ptr == nullptr)
                                                 target not in tree
      // Not found here
      success = false;
      return subtree ptr;
                                                        Found target now
                                                        remove the node
      (subtree ptr->getItem() == target)
      // Item is in the root of this subtree
      subtree ptr = removeNode(subtree ptr);
      success = true;
      return subtree ptr;
```

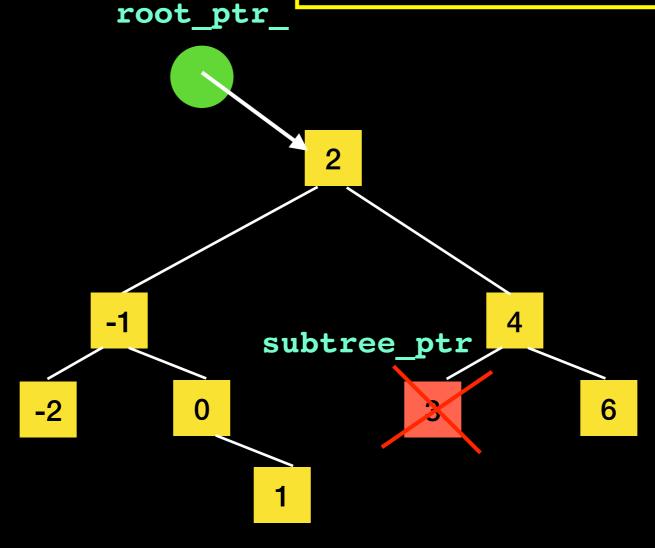
# remove helper function continued

```
else
                                                  Search for target in
   if (subtree ptr->getItem() > target)
                                                    left subtree
      // Search the left subtree
      subtree ptr->setLeftChildPtr(removeValue(subtree ptr
                             ->getLeftChildPtr(), target, success));
                                                  Search for target in
   else
                                                    right subtree
      // Search the right subtree
      subtree ptr->setRightChildPtr(removeValue(subtree ptr
                             ->getRightChildPtr(), target, success));
   return subtree ptr;
  // end if
   end removeValue
```

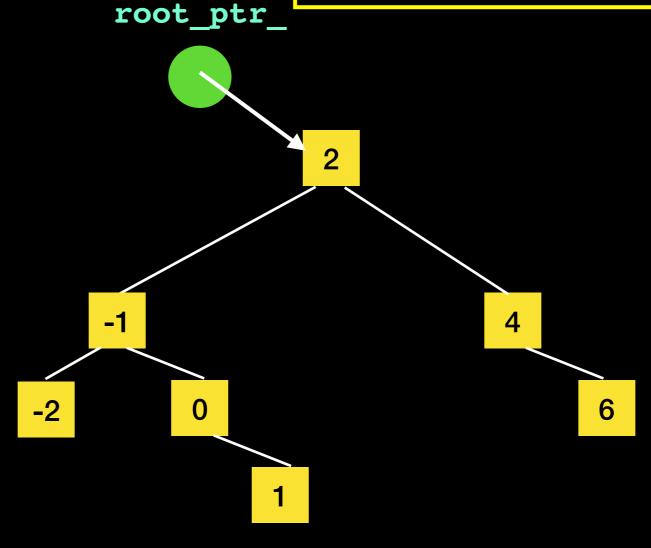
**Case 1: target is a leaf** 



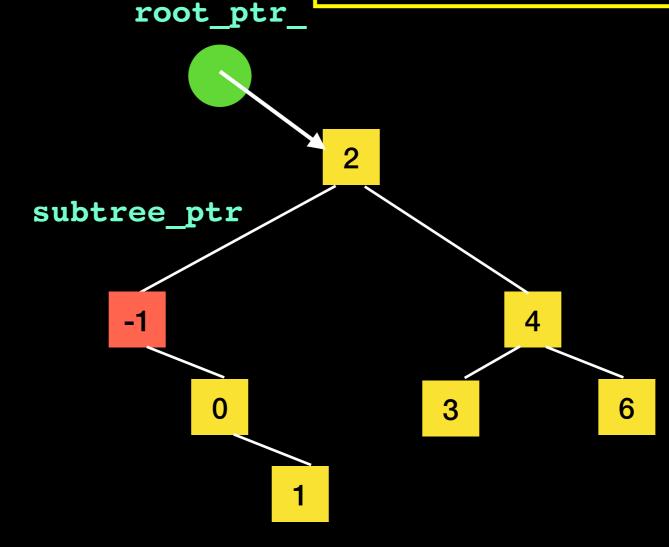
Case 1: target is a leaf



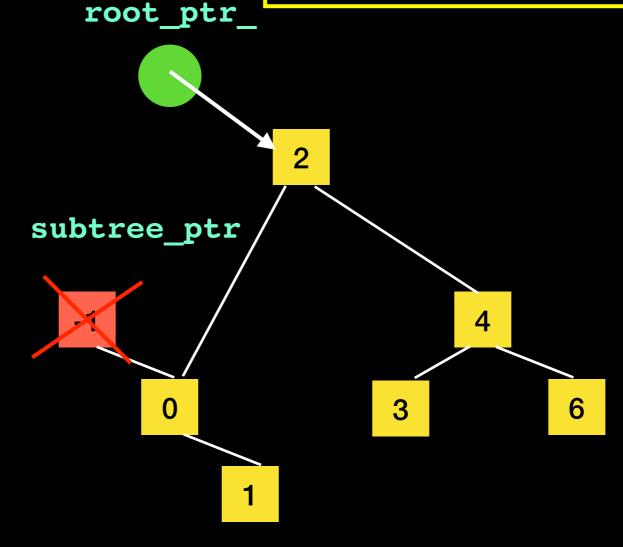
Case 1: target is a leaf



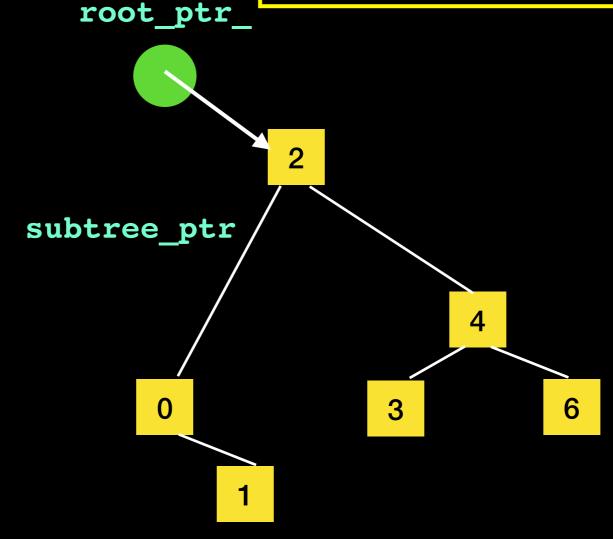
Case 2: target has 1 child Left and right case are symmetric



Case 2: target has 1 child Left and right case are symmetric



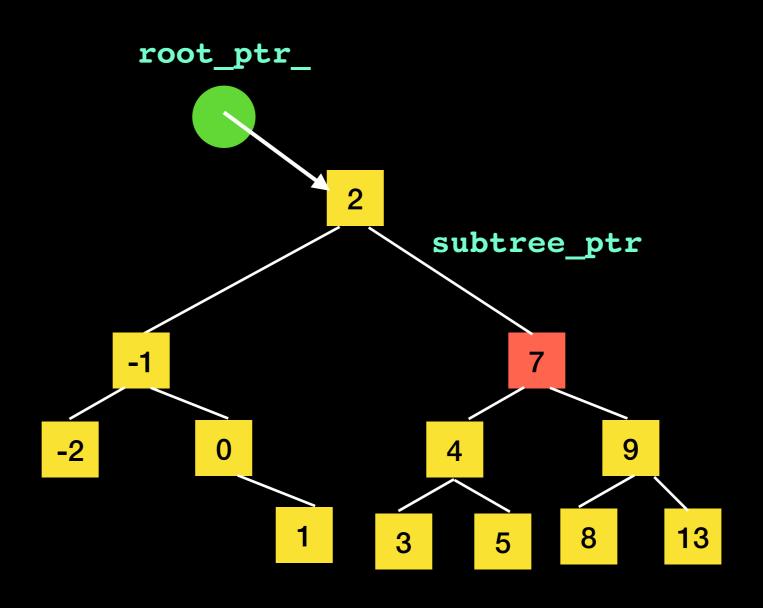
Case 2: target has 1 child Left and right case are symmetric



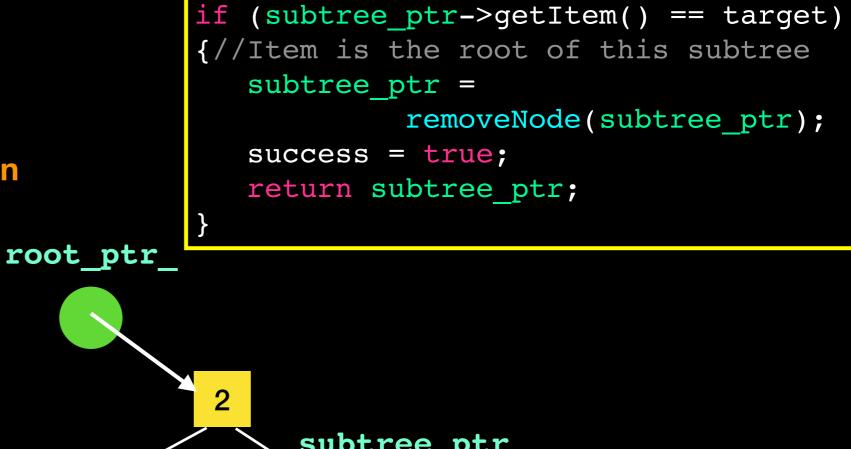
## Lecture Activity

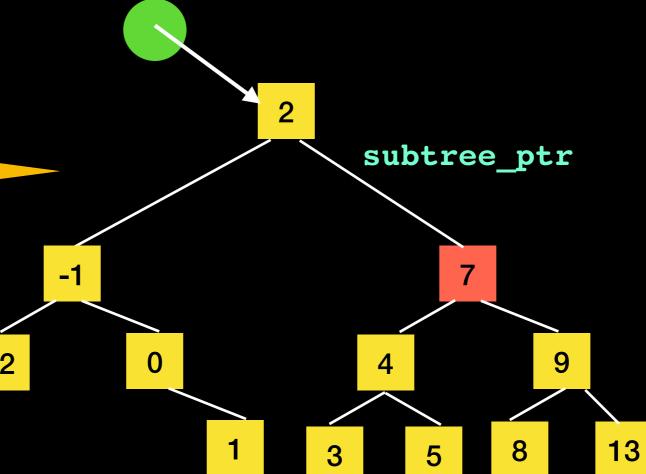
### How would you remove node 7?

Case 3: target has 2 children

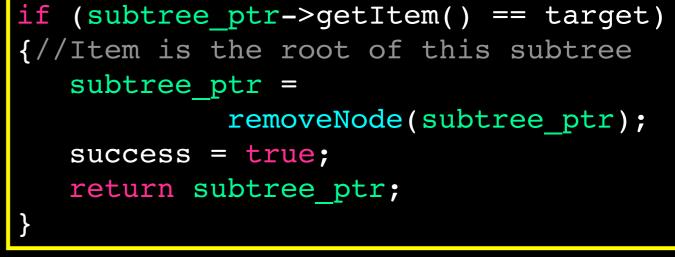


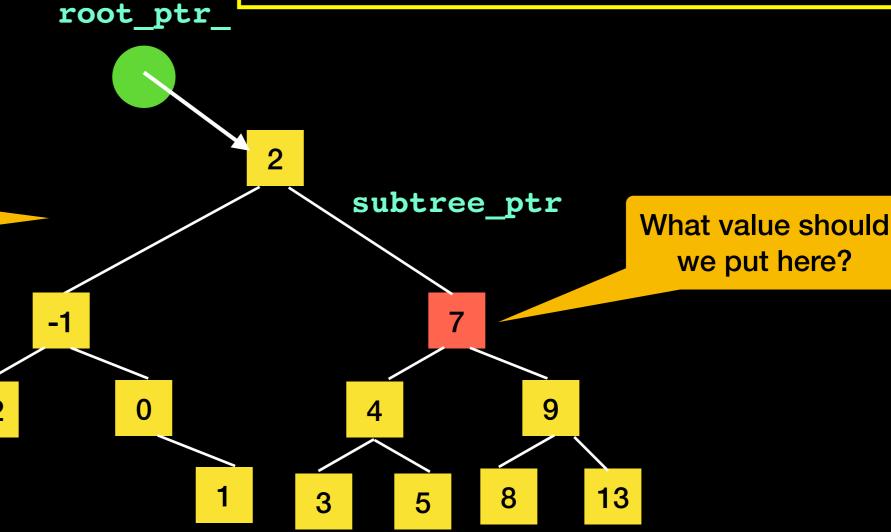
#### Case 3: target has 2 children



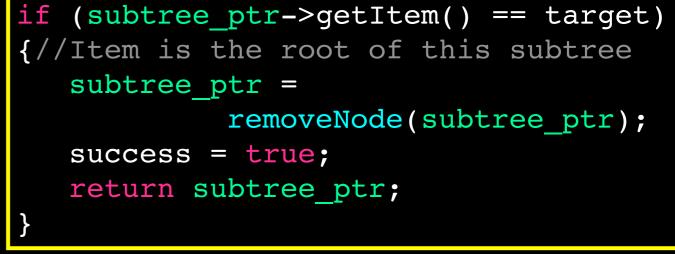


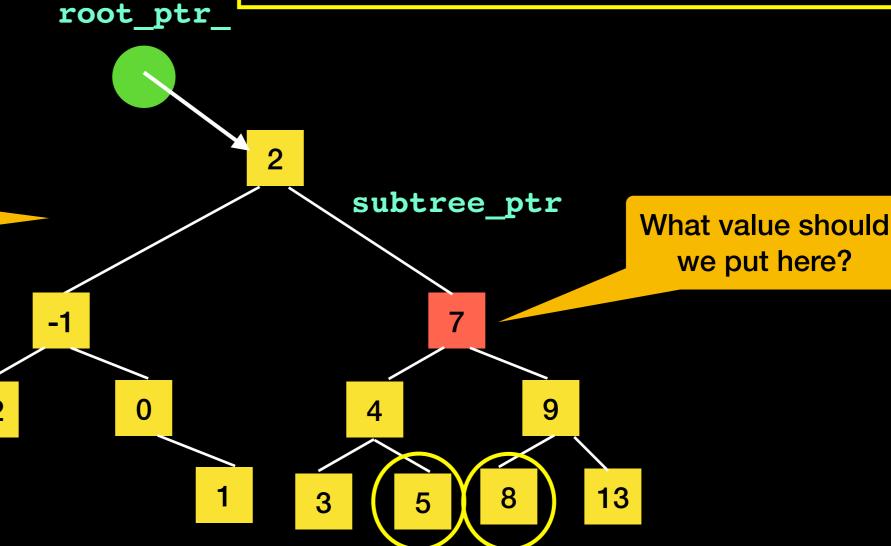
#### Case 3: target has 2 children



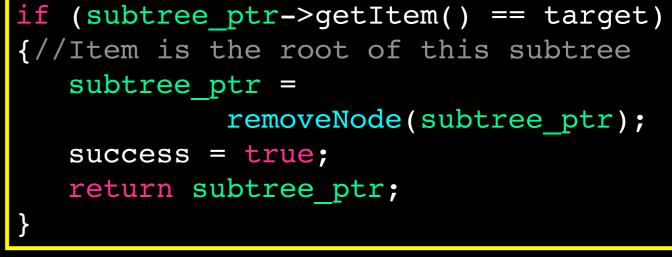


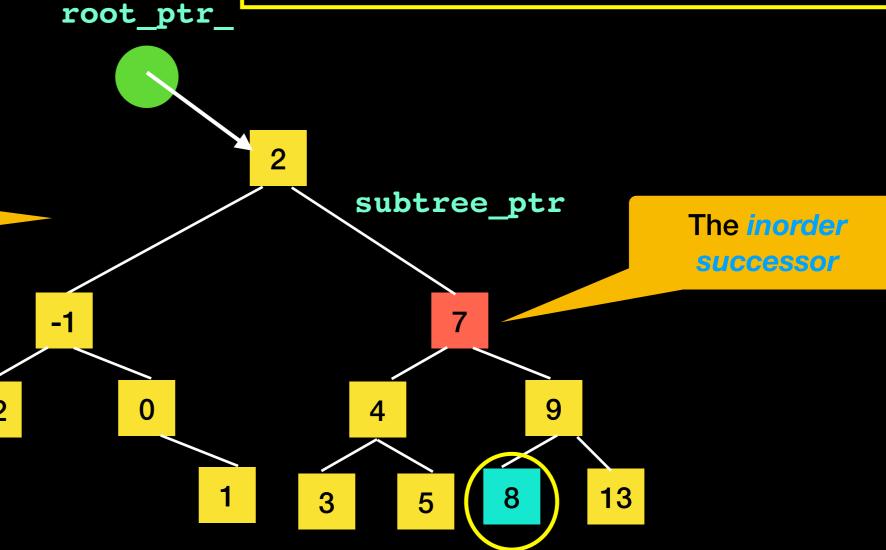
#### Case 3: target has 2 children



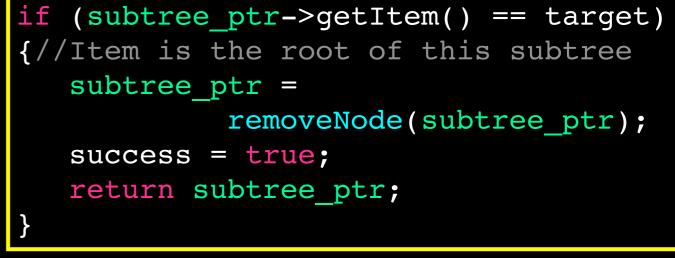


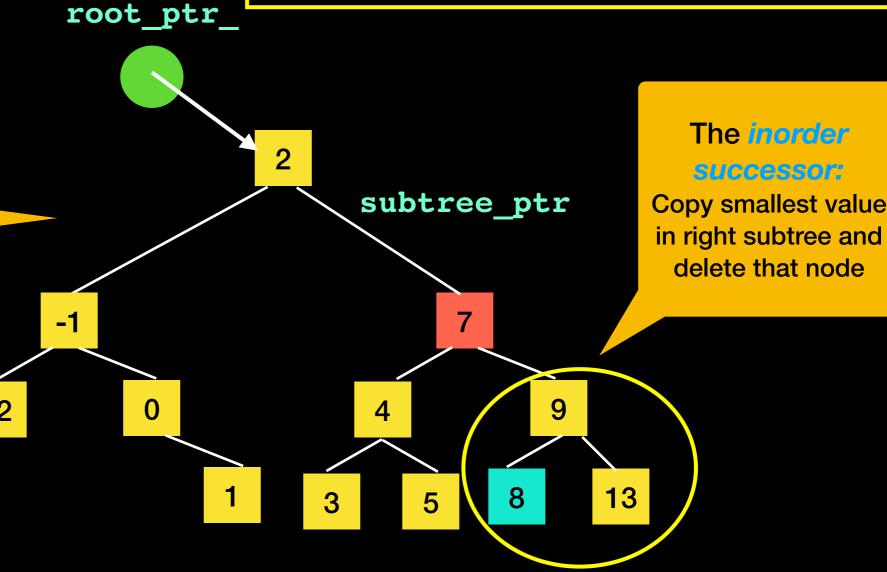
#### Case 3: target has 2 children



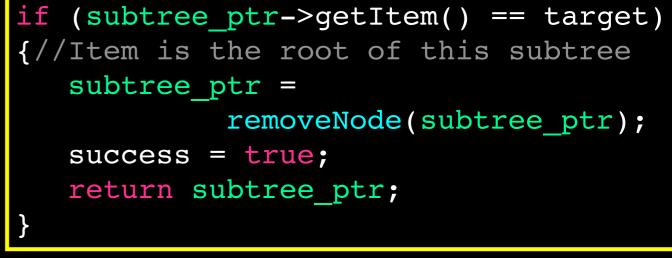


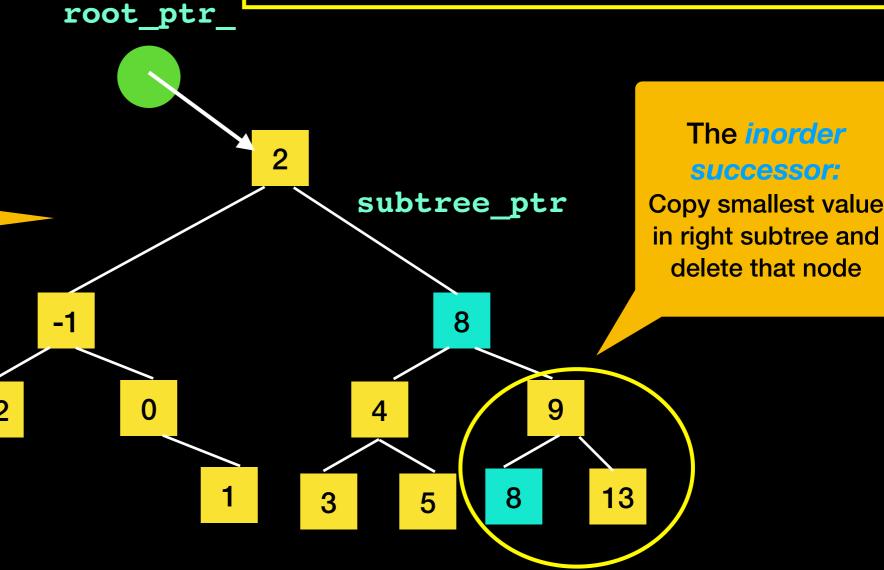
#### Case 3: target has 2 children



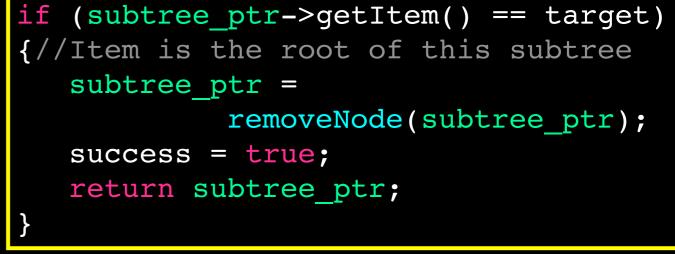


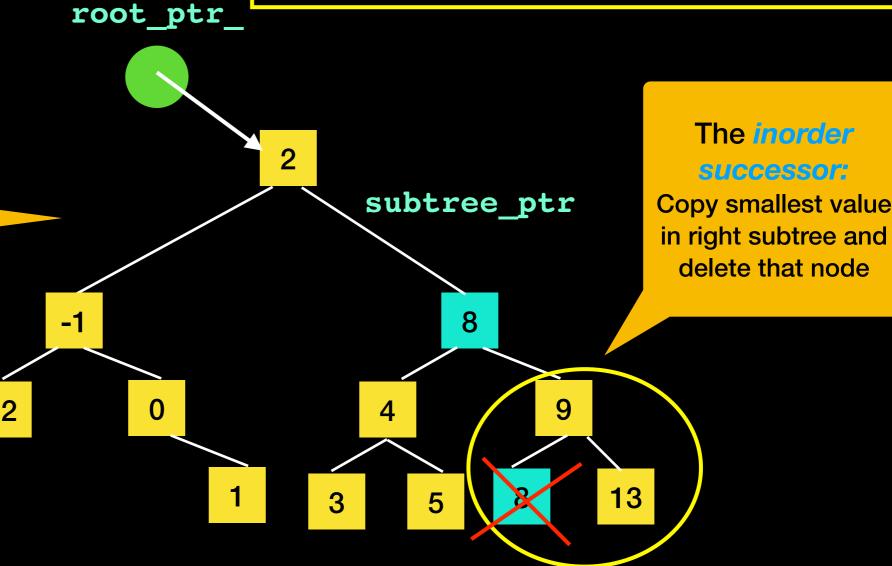
#### Case 3: target has 2 children





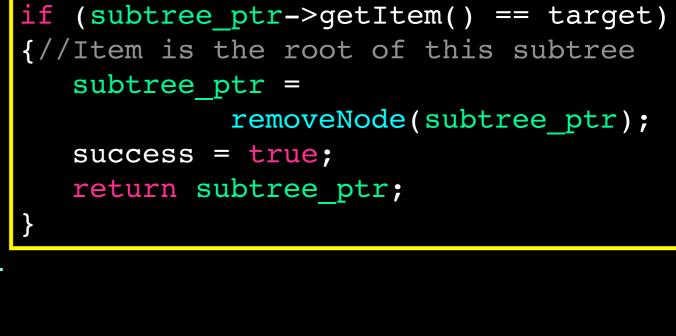
#### Case 3: target has 2 children

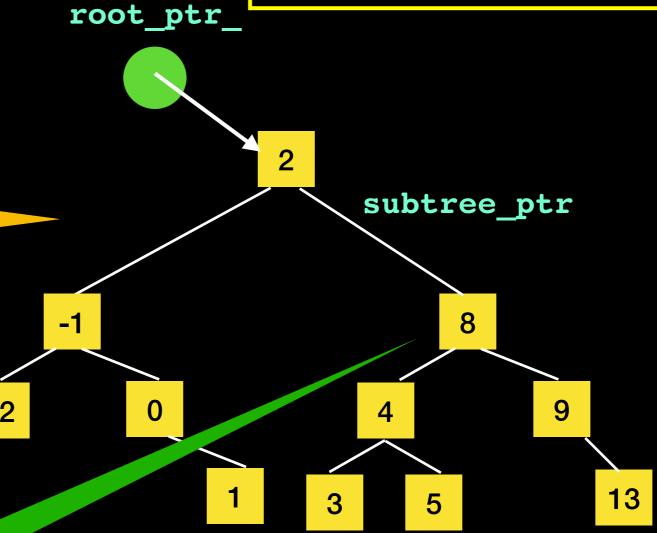




#### Case 3: target has 2 children

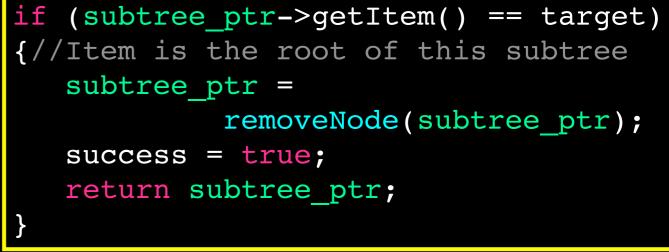
Find a node that is easy to remove and remove that one instead.

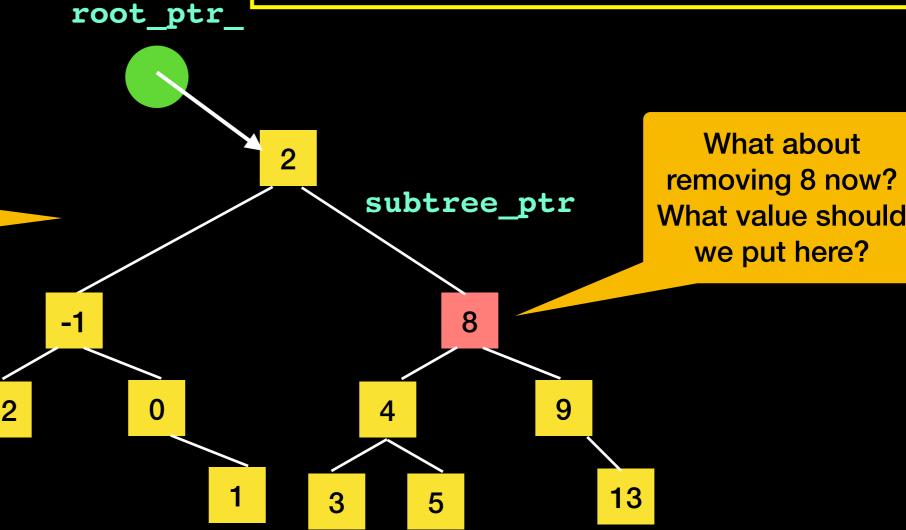




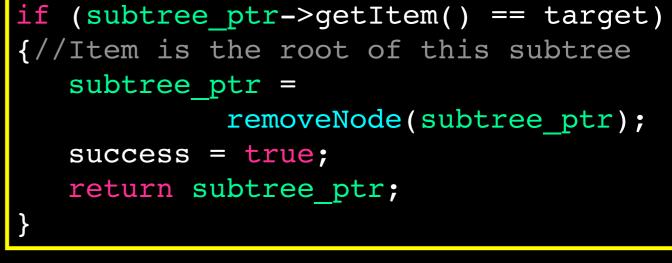
This operation will actually "reorganize" the tree

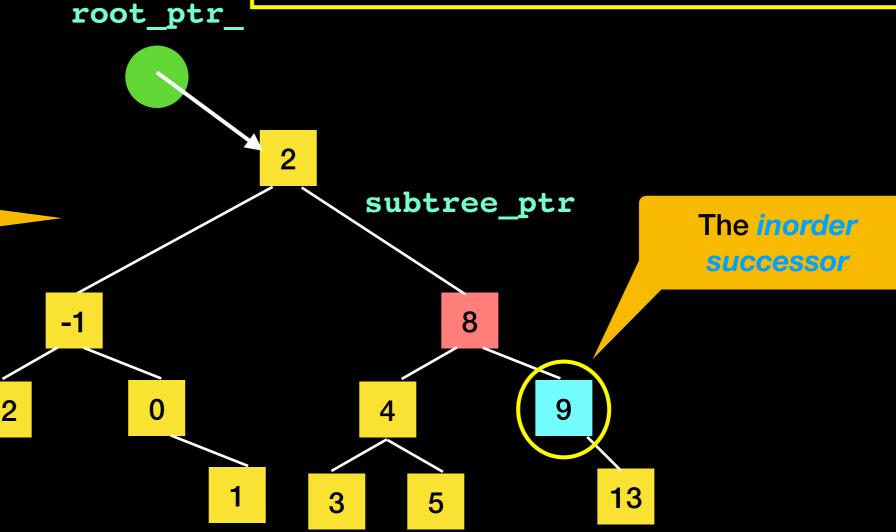
#### Case 3: target has 2 children



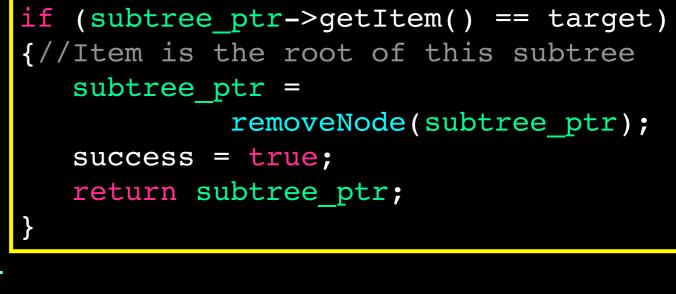


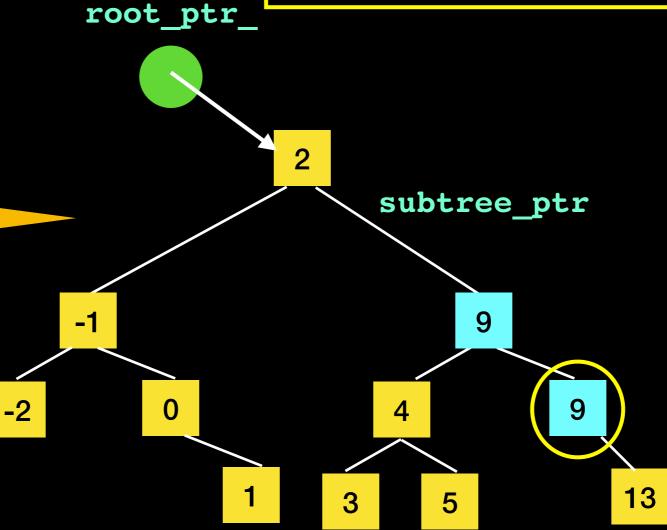
#### Case 3: target has 2 children



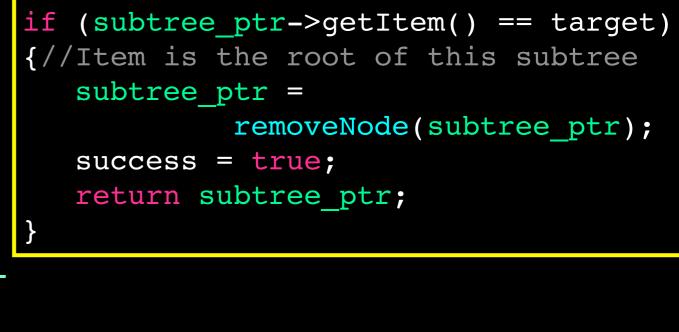


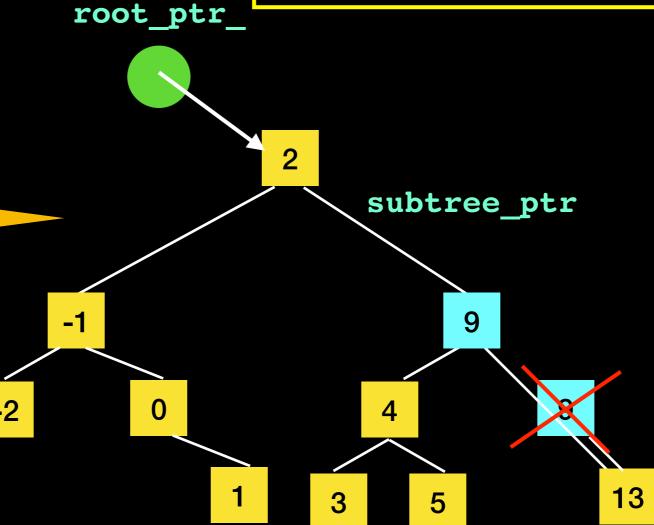
#### Case 3: target has 2 children



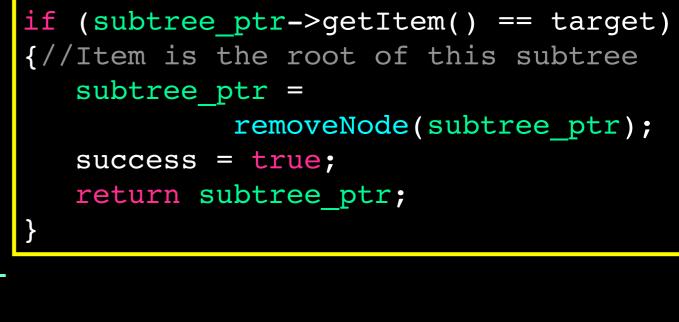


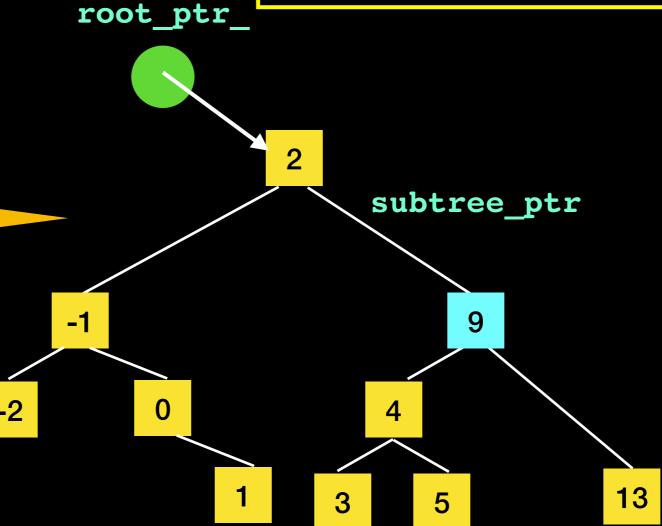
#### Case 3: target has 2 children





#### Case 3: target has 2 children





### removeNode(node\_ptr);

```
using namespace std;
template<typename ItemType>
auto BST<ItemType>::removeNode(std::shared ptr<BinaryNode<ItemType>>
node ptr)
   //Case 1) Node is a leaf - it is deleted:
                                                             Node is leaf
   if (node ptr->isLeaf())
      node ptr.reset();
                                                                    Node has 1 child
      return node ptr; // delete and return nullptr
   }//Case 2) Node has one child - parent adopts child:
   else if (node ptr->getLeftChildPtr() == nullptr) // Has rightChild only
      return node ptr->getRightChildPtr();
   else if (node ptr->getRightChildPtr() == nullptr) // Has left child only
                                                Node has 2 children
      return node ptr->getLeftChildPtr();
   }//Case 3) Node has two children:
                                                              Will find leftmost leaf in right
   else
                                                                 subtree, save value in
                                                                new node value and
                                                                   delete leaf node
      ItemType new node value;
      node ptr->setRightChildPtr(removeLeftmostNode()
                              node ptr->getRightChildPtr(), new node value));
      node ptr->setItem(new node value);
                                                               Safe Programming:
      return node ptr;
                                                           reference parameter is local to
      // end if
                                                             the private calling function
      end removeNode
```

### removeLeftmostNode

```
using namespace std;
template<typename ItemType>
auto BST<ItemType>::removeLeftmostNode(shared_ptr<BinaryNode<ItemType>>
                                         nodePtr, ItemType& inorderSuccessor)
      (nodePtr->getLeftChildPtr() == nullptr)
      inorderSuccessor = nodePtr->getItem();
      return removeNode(nodePtr);
   else
      nodePtr->setLeftChildPtr(removeLeftmostNode(nodePtr->getLeftChildPtr(),
                                                 inorderSuccessor));
      return nodePtr;
     // end if
   // end removeLeftmostNode
```

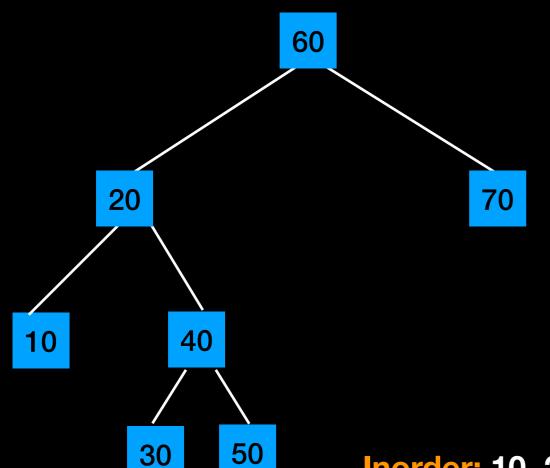
## Traversals

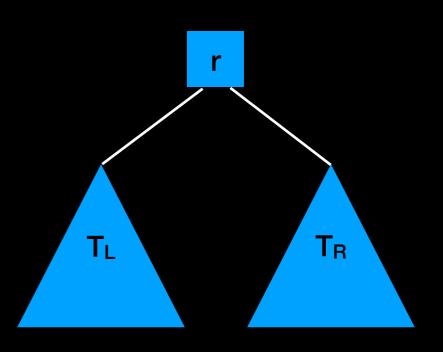
Let's focus on the traversal for now, we will find out what Visitor does next

```
template<typename ItemType>
void BST<ItemType>::preorderTraverse(Visitor<ItemType>& visit) const
   preorder(visit, root_ptr_);
   // end preorderTraverse
template<class ItemType>
void BST<ItemType>::inorderTraverse(Visitor<ItemType& visit) const</pre>
   inorder(visit, root ptr );
   // end inorderTraverse
template<class ItemType>
void BST<ItemType>::postorderTraverse(Visitor<ItemType>& visit) const
   postorder(visit, root_ptr_);
   // end postorderTraverse
```

```
Visit (retrieve, print, modify ...) every node in the tree Inorder Traversal:
```

```
\label{eq:traverse} \begin{tabular}{ll} \textbf{($T$ is not empty) //implicit base case} \\ \textbf{(} \\ \textbf{traverse $T_L$} \\ \textbf{visit the root r} \\ \textbf{traverse $T_R$} \\ \end{tabular}
```



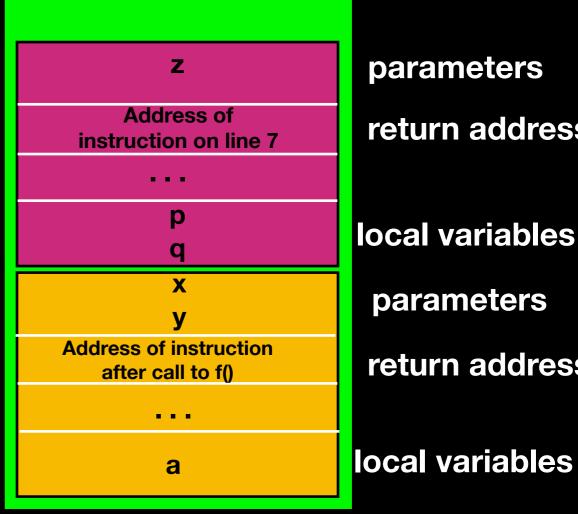


**Inorder:** 10, 20, 30, 40, 50, 60, 70

## inorderTraverse Helper Function

# Recall: Program Stack

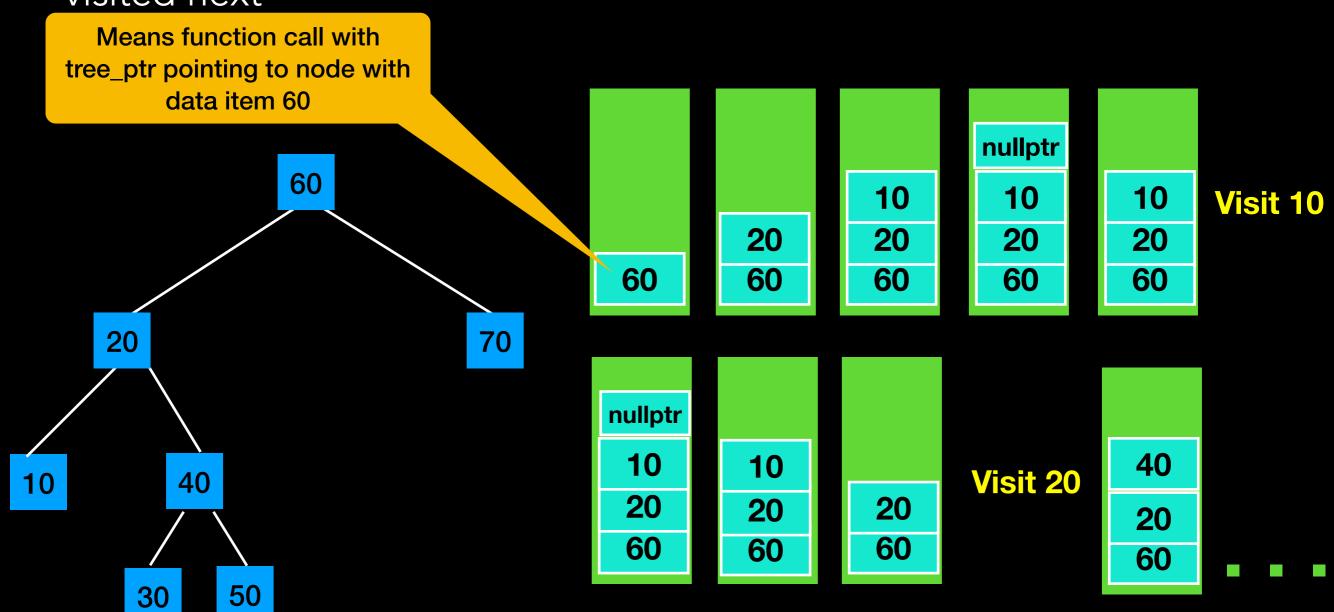
```
1
   void f(int x, int y)
2
3
     int a;
4
    // stuff here
5
   if(a<13)
6
        a = g(a);
7
   // stuff here
                      Stack Frame
8
                        for g()
9
   int g(int z)
10
11
     int p ,q;
                     Stack Frame
12 // stuff here
                        for f()
13 return q;
14 }
```



return address local variables parameters return address

## Recursive Traversal

In recursive solution program stack keeps track of what node must be visited next



## Recursive Traversal

#### With recursion:

- program stack implicitly finds node traversal must visit next
- If traversal backs up to node *d* from right subtree it backs up further to *d*'s parent as a consequence of the recursive program execution

### Non-recursive Traversal

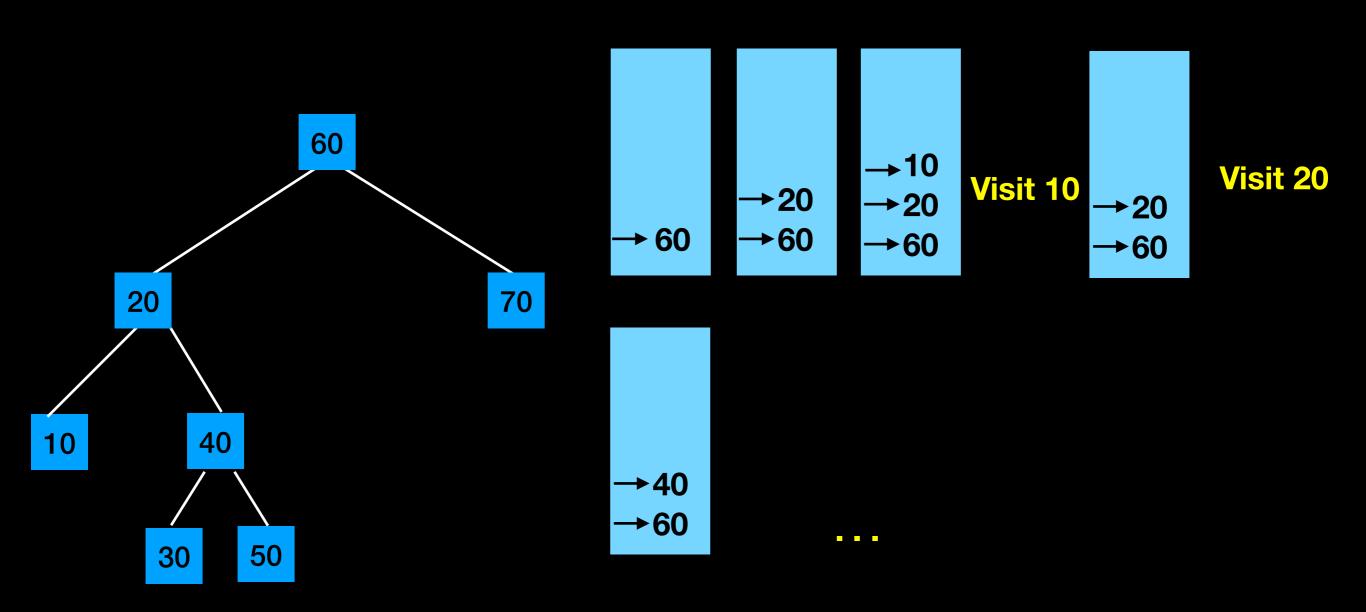
Optimize: Implement iterative approach that maintains an explicit stack to keep track of nodes that must be visited

Place pointer to node on stack **only** before traversing it's left subtree but **NOT** before traversing right subtree

This will also save some "steps" that were unnecessary but implicit in recursive implementation

## Non-recursive Traversal

Iterative solution explicitly maintains a stack of pointers to nodes to keep track of what node must be visited next



### Non-recursive Traversal

```
template<typename ItemType>
void BST<ItemType>::inorder(Visitor<ItemType>& visit) const
    std::stack<ItemType> node stack;
    std::shared ptr<BinaryNode<ItemType>> current_ptr = root ptr ;
    bool done = false;
   while(!done)
        if(current ptr != nullptr)
            node stack.push(current_ptr);
            //traverse left subtree
            current ptr = current ptr->getLeftChildPtr();
```

### Non-recursive Traversal cont.

```
//backtrack from empt subtree and visit the node at top of
  //stack, but if stack is empty traversal is completed
  else{
      done = node stack.isEmpty();
      if(!done)
      {
          current ptr = node stack.top();
          visit(current_ptr->getItem());
          node stack.pop();
          //traverse right subtree of node just visited
          current ptr = current ptr->getRightChildPtr();
end inorder
```

The last cool trick for you this semester

#### Traversals

```
template<typename ItemType>
void BST<ItemType>::preorderTraverse(Visitor<ItemType>& visit) const
   preorder(visit, root ptr );
   // end preorderTraverse
template<class ItemType>
void BST<ItemType>::inorderTraverse(Visitor<ItemType>& visit) const
   inorder(visit, root ptr );
  // end inorderTraverse
template<class ItemType>
void BST<ItemType>::postorderTraverse(Visitor<ItemType>& visit)
const
   postorder(visit, root_ptr_);
   // end postorderTraverse
```

### Functors

Objects that by overloading operator() can be "called" like a function

#### POLYMORPHISM! ABSTRACT CLASS!!!

```
#ifndef Visitor hpp
#define Visitor_hpp
#include <string>
template<typename ItemType>
class Visitor
public:
    virtual void operator()(ItemType&) = 0;
    virtual void operator()(ItemType&, ItemType&) = 0;
};
#endif /* Visitor hpp */
```

```
#ifndef StringPrinter hpp
#define StringPrinter hpp
#include "Visitor.hpp"
#include <iostream>
#include <string>
using namespace std;
class StringPrinter: public Visitor<string>
public:
    void operator()(string&) override;
    void operator()(string&, string&) override;
#endif /* StringPrinter hpp */
```

```
#include "StringPrinter.hpp"
using namespace std;

void StringPrinter::operator()(string& x)
{
    cout << x << endl;
}

void StringPrinter::operator()(string& a, string& b)
{
    cout << a << b << endl;
}</pre>
```

```
#ifndef Inverter hpp
#define Inverter hpp
#include "Visitor.hpp"
#include <iostream>
#include <string>
#include <algorithm>
using namespace std;
class Inverter: public Visitor<string>
public:
    void operator()(string&) override;
    void operator()(string&, string&) override;
};
#endif /* Inverter hpp */
```

```
#include "Inverter.hpp"
using namespace std;
void Inverter::operator()(string& x)
{
    reverse(x.begin(), x.end());
    cout << x << endl;</pre>
void Inverter::operator()(string& a, string& b)
{
    a.swap(b);
    cout << a << b << endl;</pre>
```

# Traversal with Functor parameter

```
using namespace std;
template<typename ItemType>
void BST<ItemType>::inorder(Visitor<ItemType>& visit,
                          shared ptr<BinaryNode<ItemType>> tree ptr) const
    if (tree ptr != nullptr)
        inorder(visit, tree ptr->getLeftChildPtr());
        ItemType the item = tree ptr->getItem();
        visit(the_item);
        inorder(visit, tree ptr->getRightChildPtr());
       // end if
   // end inorder
```

```
using namespace std;
int main() {
    string a string = "a string";
    string anoter string = "o string";
    BST<string> a tree(a string);
    a tree.add(anoter string);
    StringPrinter p;
    Inverter i;
    a tree.inorderTraverse(p);
    cout << endl;</pre>
    a_tree.inorderTraverse(i);
    return 0;
```

```
root_ptr_

"a string"

"o string"
```

```
a string
o string
gnirts a
gnirts o
Program ended with exit code: 0
```

```
root_ptr_
using namespace std;
int main() {
    string a string = "a string";
                                                        "a string"
    string anoter string = "o string";
    BST<string> a tree(a string);
    a tree.add(anoter string);
    StringPrinter p;
                                                  TA-DAH!
    Inverter i;
    a tree.inorderTraverse(p);
    cout << endl;</pre>
    a_tree.inorderTraverse(i);
                                     a string
                                     o string
    return 0;
                                     gnirts a
                                     gnirts o
                                     Program ended with exit code: 0
```

"o string"