# Tree Implementation

## Today's Plan



Recap

BST Implementation

```
#ifndef BST H
#define BST H
#include <memory>
using namespace std;
template<typename ItemType>
class BST
public:
   BST(); // constructor
   BST(const BST<ItemType>& tree); // copy constructor
   ~ BST(); // destructor
   bool isEmpty() const;
   size t getHeight() const;
   size t getNumberOfNodes() const;
   void add(const ItemType& new item);
   void remove(const ItemType& new item);
   ItemType find(const ItemType& item) const;
   void clear();
   void preorderTraverse(Visitor<ItemType>& visit) const;
   void inorderTraverse(Visitor<ItemType>& visit) const;
   void postorderTraverse(Visitor<ItemType>& visit) const;
   BST& operator= (const BST<ItemType>& rhs);
                                                      Let's try something new
private:
                                                       and use shared ptr:
   shared ptr<BinaryNode<ItemType>> root ptr ;
                                                       A bit of extra syntax at
}; // end BST
                                                      declaration but then you
#include "BST.cpp"
                                                        use them as regular
#endif // BST H
                                   3
```

To implement this as a linked structure what do we need to change in our previous implementation ???

## BinaryNode



```
#ifndef BinaryNode H
#define BinaryNode H
                              For shared ptr
#include <memory> _
using namespace std;
template<typename ItemType>
class BinaryNode
public:
   BinaryNode();
   BinaryNode(const ItemType& an item);
   void setItem(const ItemType& an item);
   ItemType getItem() const;
   bool isLeaf() const;
   auto getLeftChildPtr() const;
   auto getRightChildPtr() const;
   void setLeftChildPtr(std::shared ptr<BinaryNode<ItemType>> left ptr);
   void setRightChildPtr(std::shared ptr<BinaryNode<ItemType>> right ptr);
private:
   ItemType item ; // Data portion
   shared ptr<BinaryNode<ItemType>> left ;  // Pointer to left child
   shared ptr<BinaryNode<ItemType>> right ; // Pointer to right child
}; // end BST
#include "BinaryNode.cpp"
#endif // BinaryNode H
                                      6
```

## Lecture Activity

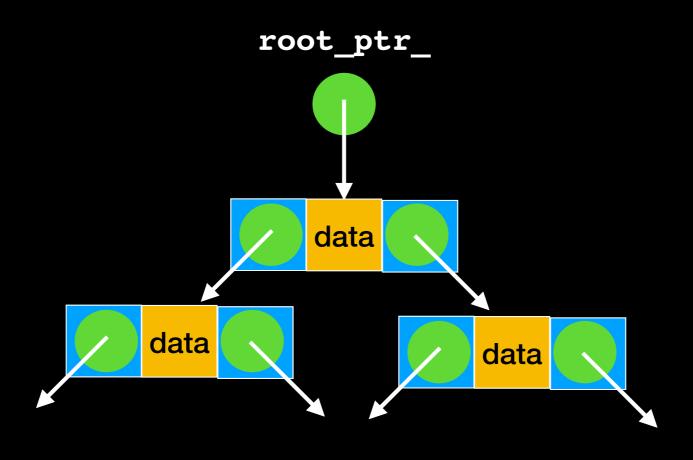
#### Implement:

```
BinaryNode(const ItemType& an_item);
bool isLeaf() const;

void setLeftChildPtr(shared_ptr<BinaryNode<ItemType>> left_ptr);
```

```
template<typename ItemType>
BinaryNode<ItemType>::BinaryNode(const ItemType& an item)
      : item (an item){ } // end constructor
template<typename ItemType>
bool BinaryNode<ItemType>::isLeaf() const
   return ((left == nullptr) && (right == nullptr));
} // end isLeaf
template<typename ItemType>
void
BinaryNode<ItemType>::setLeftChildPtr(std::shared ptr<BinaryNode<Ite</pre>
mType>> left ptr)
   left = left ptr;
  // end setLeftChildPtr
```

## BST



```
#ifndef BST H
                                              We want our interface to be generic
                                              and not tied to implementation. Many
#define BST H
                                                of these will therefore use helper
#include <memory>
                                               functions, which should be private
template<typename ItemType>
                                                  (or protected if you envision
class BST
                                               inheritance). I do not include them
                                                 here in the interface for lack of
public:
                                                          space.
   BST(); // constructor
   BST(const BST<ItemType>& tree); // copy constructor
   ~ BST(); // destructor
   bool isEmpty() const;
   size t getHeight() const;
   size t getNumberOfNodes() const;
   void add(const ItemType& new item);
   void remove(const ItemType& new item);
   ItemType find(const ItemType& item) const;
   void clear();
   void preorderTraverse(Visitor<ItemType>& visit) const;
   void inorderTraverse(Visitor<ItemType>& visit) const;
   void postorderTraverse(Visitor<ItemType& visit) const;</pre>
   BST& operator= (const BST<ItemType>& rhs);
private:
   std::shared ptr<BinaryNode<ItemType>> root ptr ;
}; // end BST
#include "BST.cpp"
#endif // BST H
                                   10
```

## Copy Constructor

```
root_ptr of
this object

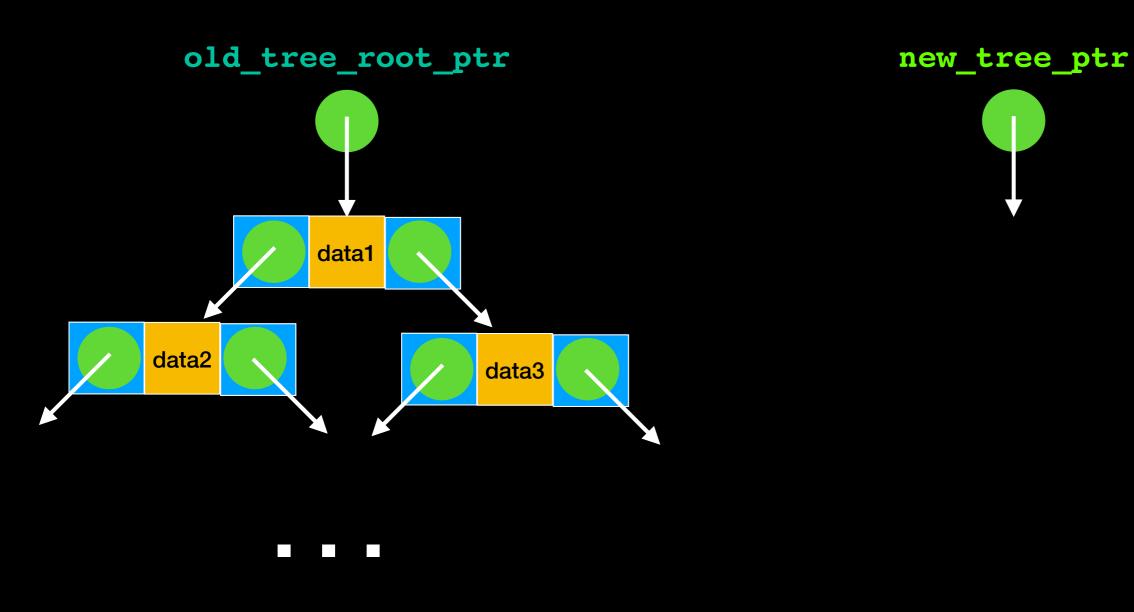
templa re<typename ItemType>
BST<ItemType>::BST(const BST<ItemType>& tree)
{
   root_ptr_ = copyTree(tree.root_ptr_); // Call helper function
} // end copy constructor
```

Safe programming: the public method does not take pointer parameter.

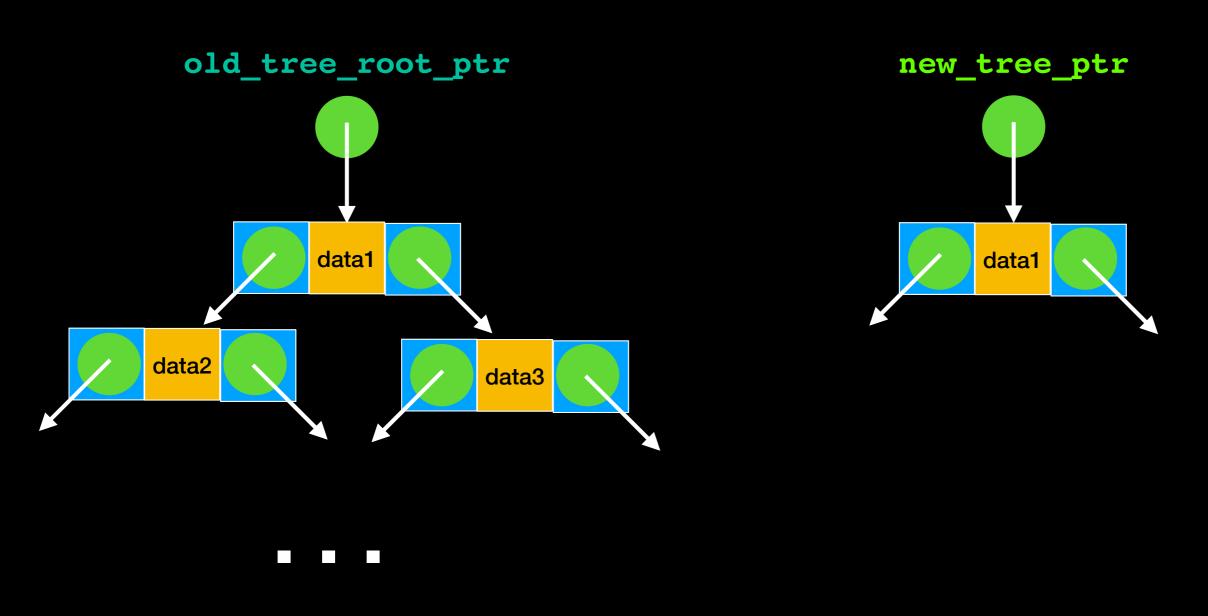
Only protected/private methods have access to pointers and may modify tree structure

I can use the . operator to access a private member variable because it is s within the class definition.

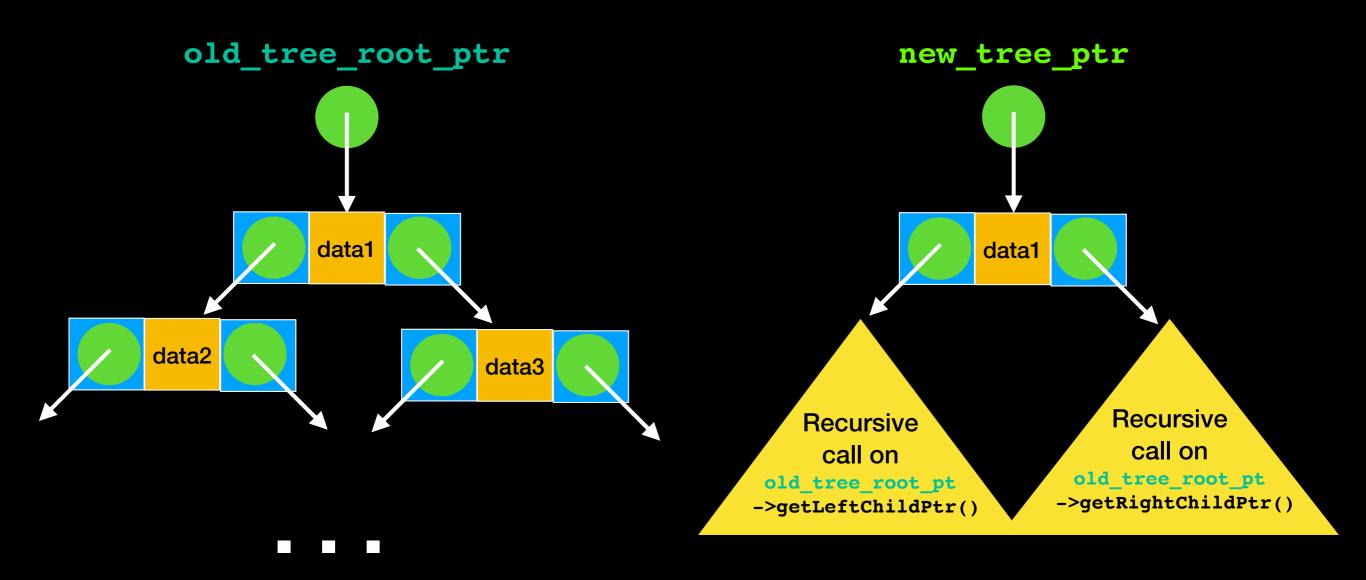
#### copyTree(old\_tree\_root\_ptr)



#### copyTree(old\_tree\_root\_ptr)



### copyTree(old\_tree\_root\_ptr)



Returning shared ptr, cleaner to use auto return type: -std=c++14

## Copy Constructor Helper Function

```
template<typename ItemType>
auto BST<ItemType>::copyTree(const
shared ptr<BinaryNode<ItemType>> old tree root ptr) const
                                                         Recall: this is the syntax
   shared ptr<BinaryNode<ItemType>> new tree ptr;
                                                          for allocating a "new"
   // Copy tree nodes during a preorder traversal
                                                         object with shared ptr
   if (old tree root ptr != nullptr)
                                                             pointing to it
      // Copy node
      new tree ptr = make shared<BinaryNode<ItemType>>
                     (old tree root ptr->getItem(), nullptr, nullptr);
      new tree ptr->setLeftChildPtr(copyTree(old tree root ptr
                                                    ->getLeftChildPtr());
      new tree ptr->setRightChildPtr(copyTree(old_tree_root_ptr
                                                     >getRightChildPtr()));
                                 Recursive Calls:
   } // end if
                              Don't want to tie interface
                                                           Preorder Traversal
   return new tree ptr;
                                   to recursive
                                                         Scheme: copy each node
   // end copyTree
                                 implementation:
                                                         as soon as it is visited to
                                Use helper function
```

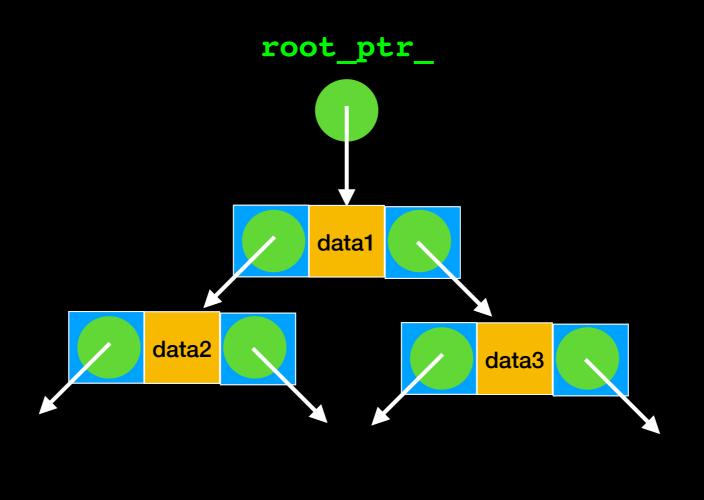
make exact copy

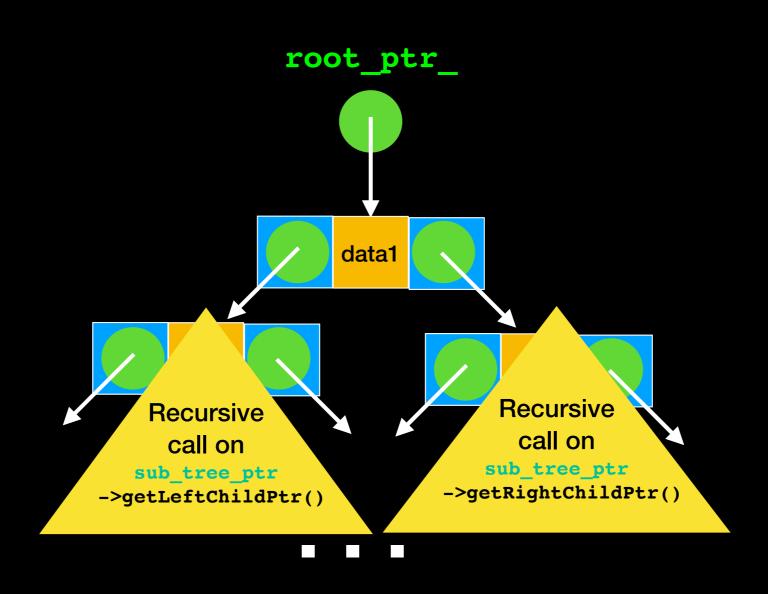
### Destructor

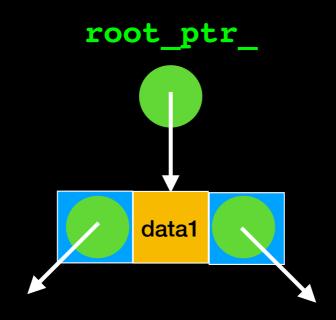
```
template<typename ItemType>
BST<ItemType>::~BST()
{
   destroyTree(root_ptr_); // Call helper function
} // end destructor
```

Safe programming: the public method does not take pointer parameter.

Only protected/private methods have access to pointers and may modify tree structure







root\_ptr\_.reset()



## Destructor Helper Function

Notice: all we have to do is set the shared\_ptr to nullptr with reset() and it will take care of deleting the node.

PostOrder Traversal Scheme:
Delete node only after deleting
both of its subtrees

#### clear

```
template<typename ItemType>
void BST<ItemType>::clear()
{
    destroyTree(root_ptr_); // Call helper method
} // end clear
```

Safe programming: the public method does not take pointer parameter.

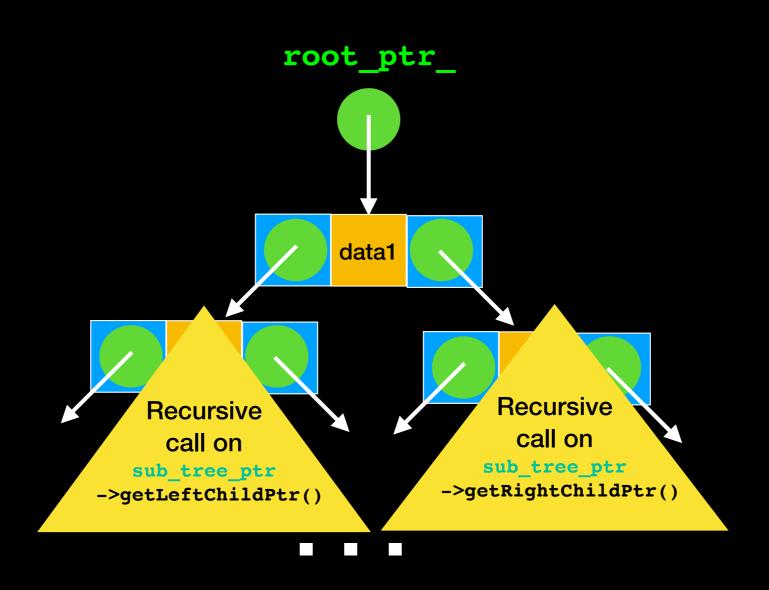
Only protected/private methods have access to pointers and may modify tree structure

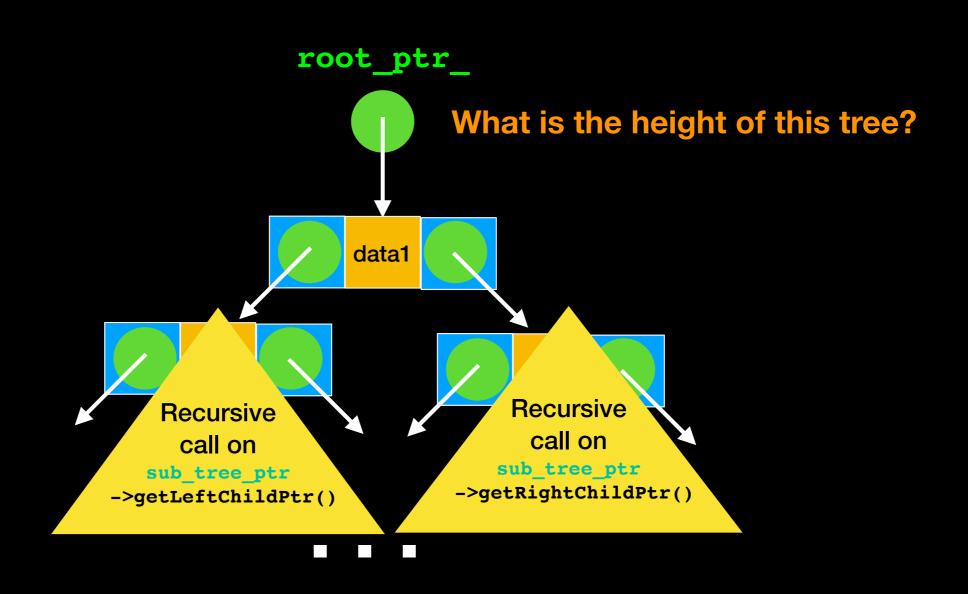
## getHeight

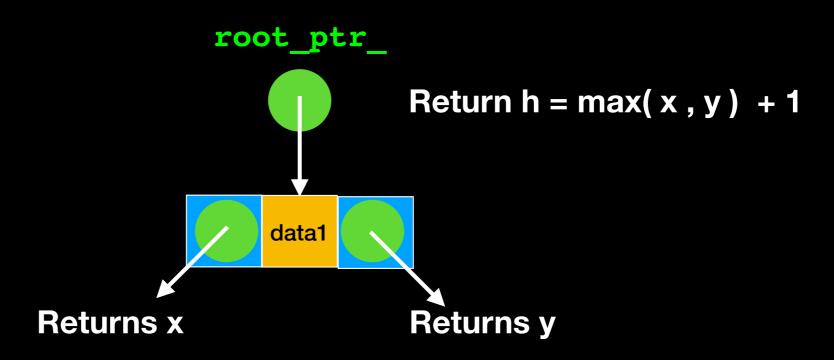
```
template<typename ItemType>
int BST<ItemType>::getHeight() const
{
    return getHeightHelper(root_ptr_);
} // end getHeight
```

Safe programming: the public method does not take pointer parameter.

Only protected/private methods have access to pointers and may modify tree structure









#### Similarly: implement these at home!!!

```
int BST<T>::getNumberOfNodes() const
{    //try it at home!!!!}

int BST<T>::getNumberOfNodesHelper(std::shared_ptr
<BinaryNode<T>> sub_tree_ptr) {//try it at home!!!!}
```

### add and remove

Key methods: determine order of data

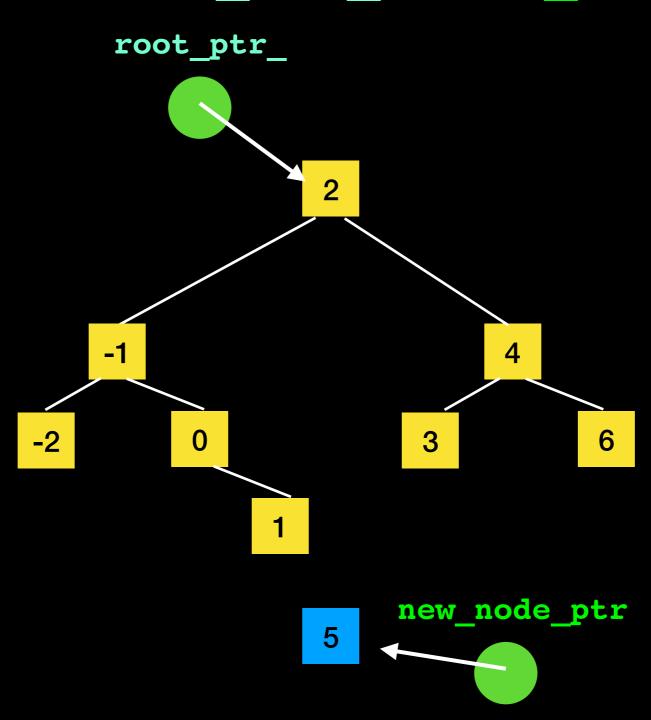
Distinguish between different types of Binary Trees

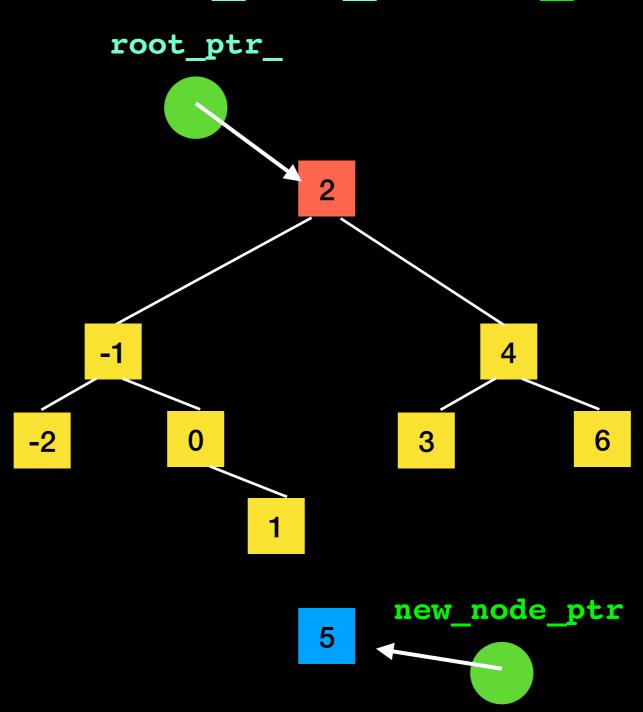
Implement the BST structural property

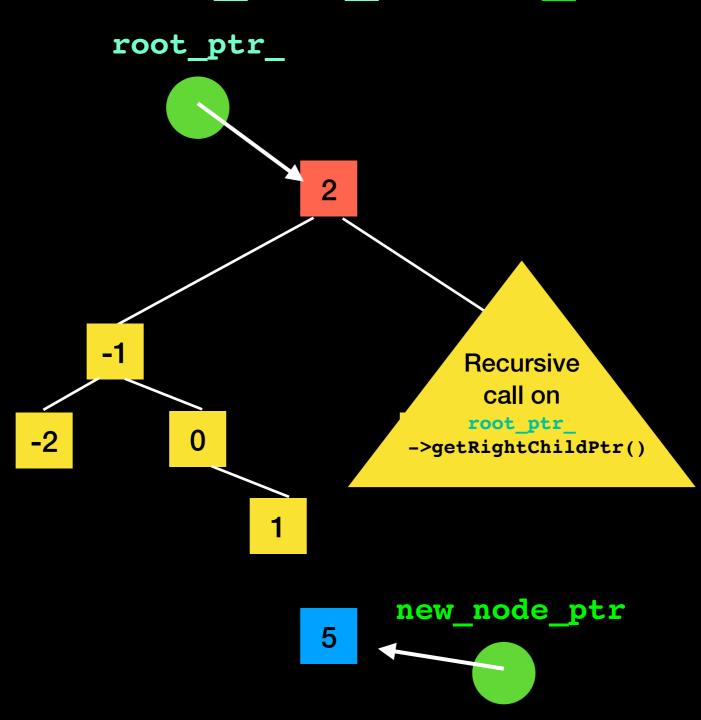
#### add

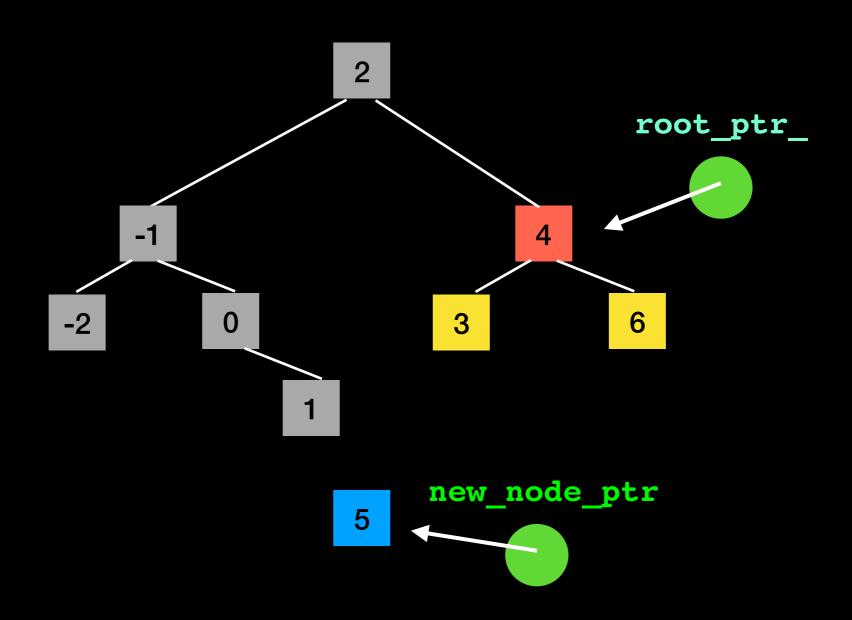
```
template<typename ItemType>
void BST<ItemType>::add(const ItemType& new_item)
{
    auto new_node_ptr =
        std::make_shared<BinaryNode<ItemType>>(new_item);
    placeNode(root_ptr_, new_node_ptr);
} // end add
```

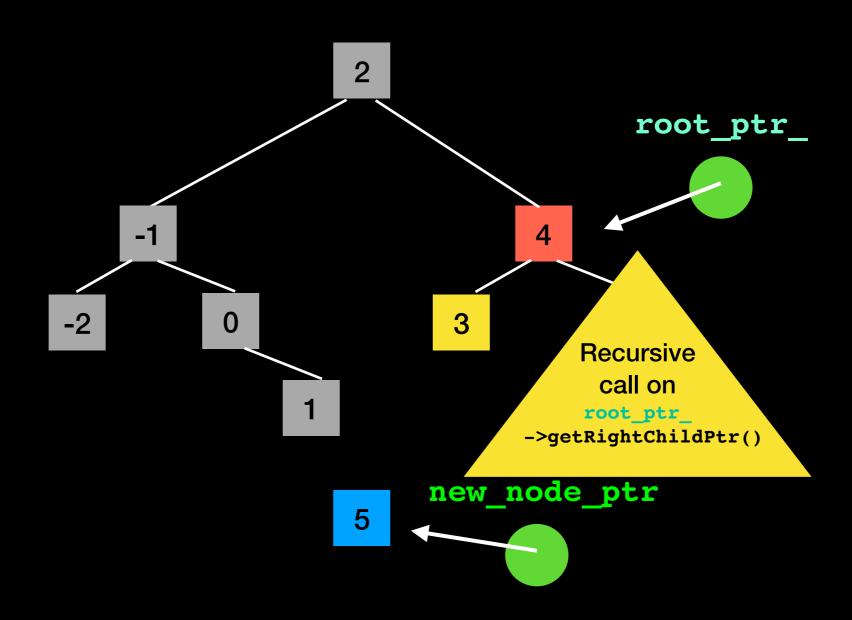
Safe programming: the public method does not take pointer parameter.
Only protected/private methods have access to pointers and may modify tree structure

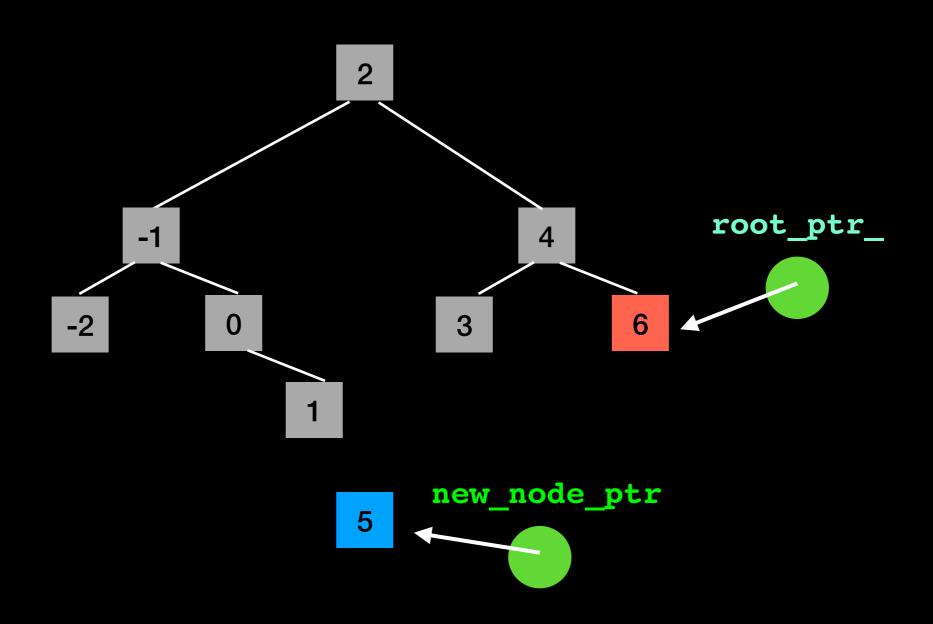


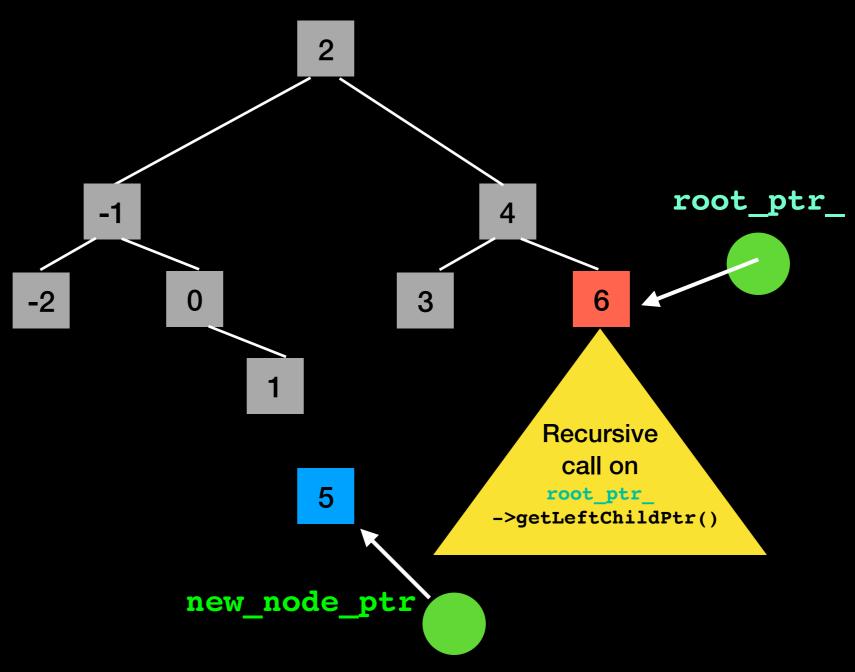


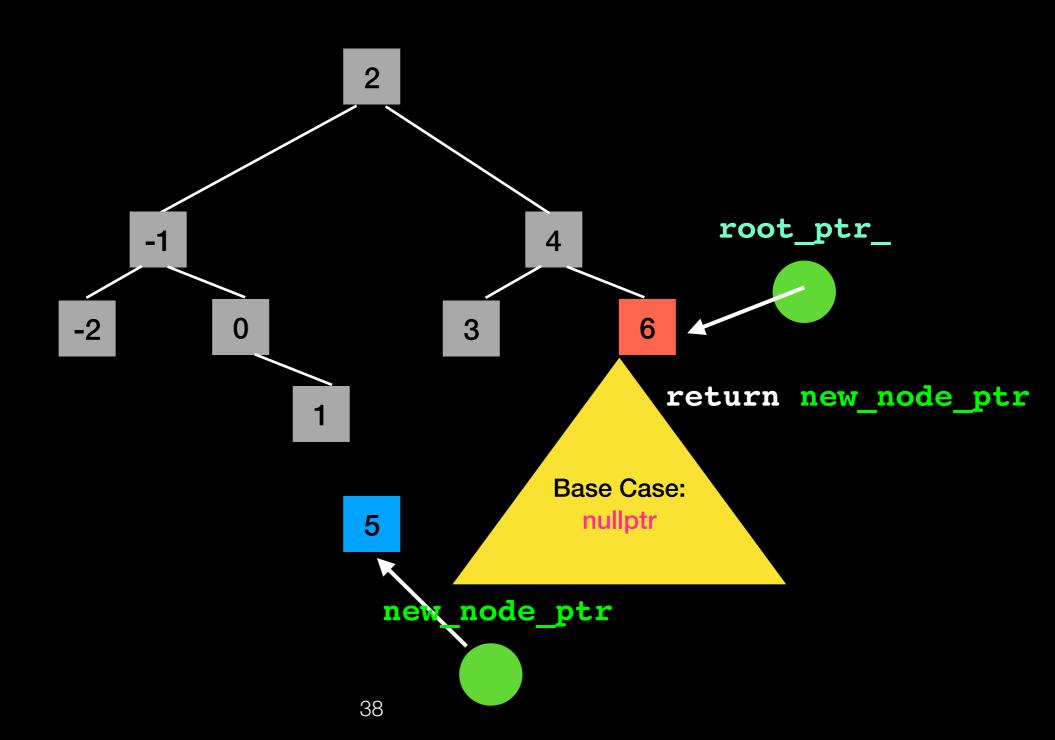


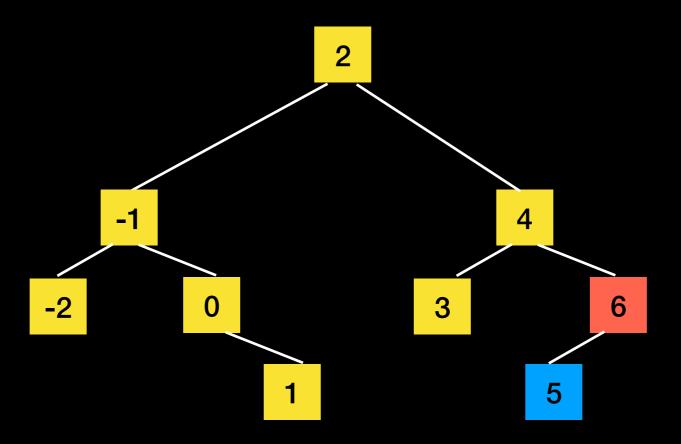


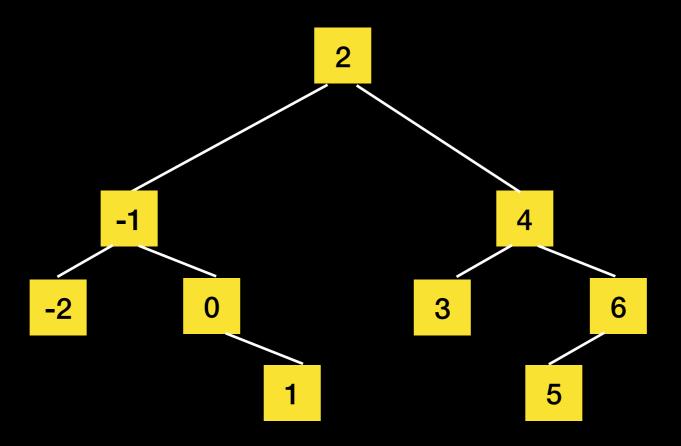












## add helper function

```
template<typename ItemType>
auto BST<template<typename ItemType>::placeNode(
std::shared ptr<BinaryNode<template<typename ItemType>>>
subtree ptr, std::shared ptr<BinaryNode<template<typename</pre>
ItemType>>> new node ptr)
{
   if (subtree ptr == nullptr)
      return new node ptr; //base case
   else
      if (subtree ptr->getItem() > new node ptr->getItem())
          subtree ptr->setLeftChildPtr(placeNode(subtree ptr
          ->getLeftChildPtr(), new node ptr));
      else
         subtree ptr->setRightChildPtr(placeNode(subtree ptr
         ->getRightChildPtr(), new node ptr));
      return subtree ptr;
   // end if
 // end placeNode
```

### remove

```
template<typename ItemType>
bool BST<ItemType>::remove(const ItemType& target)
{
   bool is_successful = false;
   // call may change is_successful
   root_ptr_ = removeValue(root_ptr_, target, is_successful);
   return is_successful;
} // end remove
```

method does not take pointer parameter.
Only protected/private methods have access to pointers and may modify tree structure

Safe programming: the public

# remove helper function

Looks for the value to remove

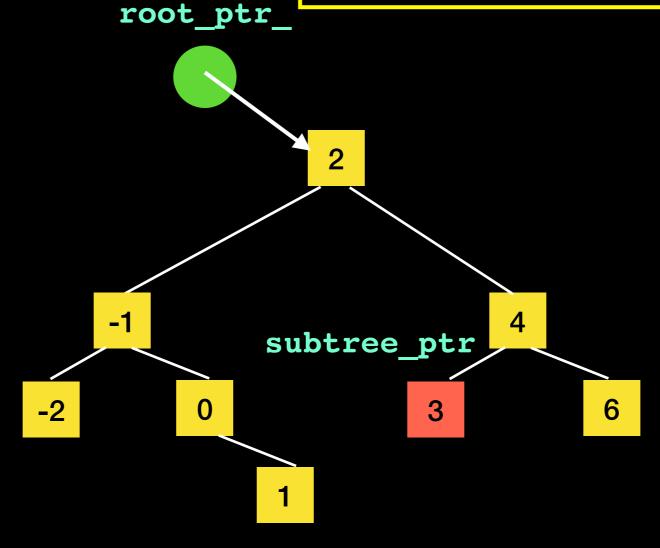
```
template<typename ItemType>
auto BST<T>::removeValue(std::shared ptr<BinaryNode<T>>
      subtree ptr, const T target, bool& success)
   if (subtree ptr == nullptr)
                                               target not in tree
      // Not found here
      success = false;
      return subtree ptr;
      (subtree ptr->getItem() == target)
      // Item is in the root of this subtree
      subtree ptr = removeNode(subtree ptr);
      success = true;
      return subtree ptr;
```

Found target now remove the node

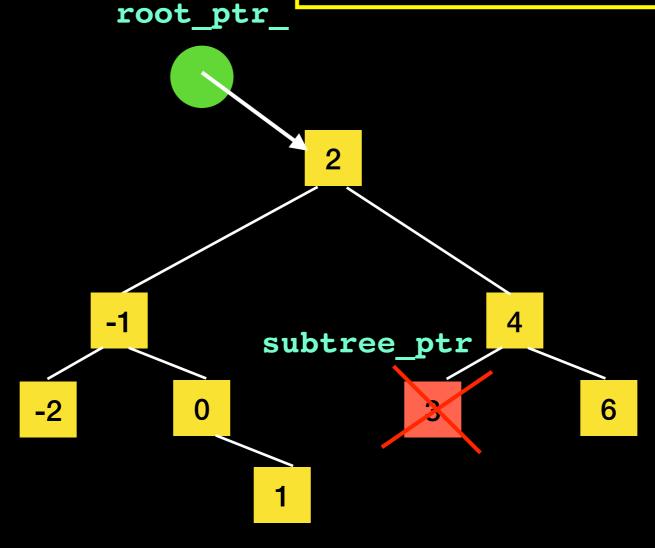
# remove helper function cont.ed

```
else
                                                    Search for target in
   if (subtree ptr->getItem() > target)
                                                        left subtree
      // Search the left subtree
      subtree ptr->setLeftChildPtr(removeValue(subtree ptr
                                 ->qetLeftChildPtr(), target, success));
                                                      Search for target in
   else
                                                         right subtree
      // Search the right subtree
      subtree ptr->setRightChildPtr(removeValue(subtree ptr
                                 ->getRightChildPtr(), target, success));
   return subtree ptr;
   // end if
   end removeValue
```

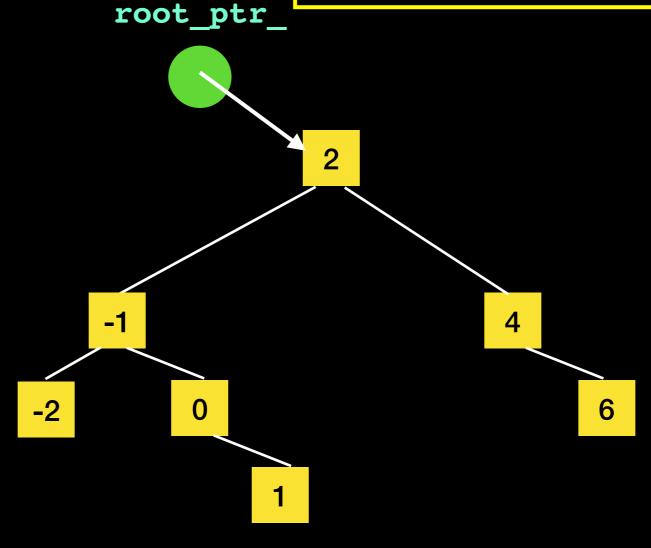
**Case 1: target is a leaf** 



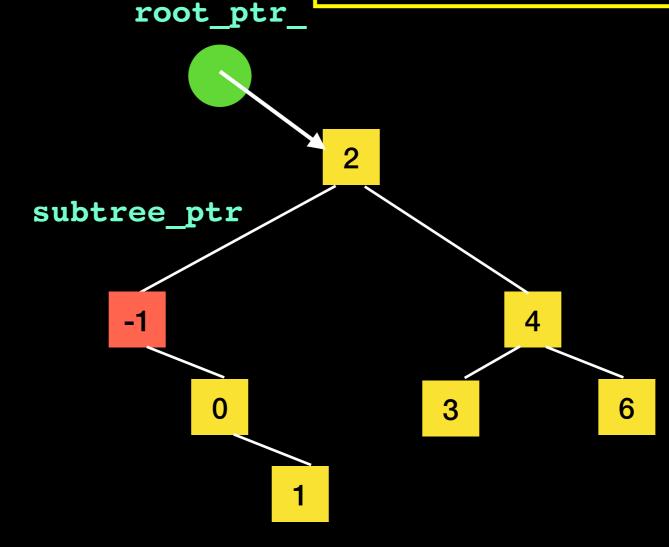
Case 1: target is a leaf



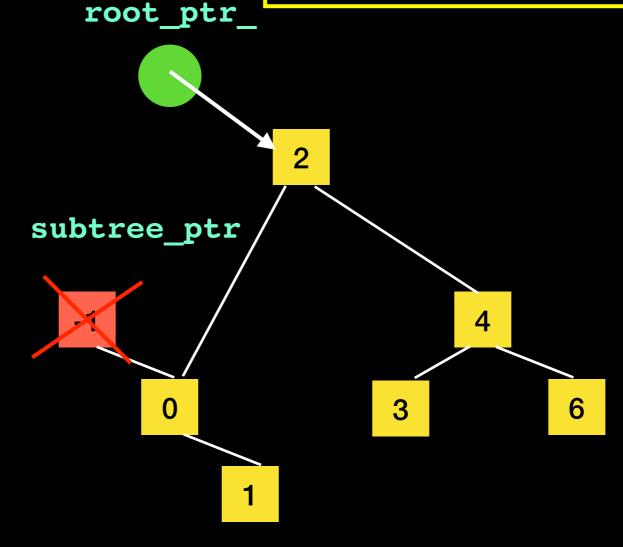
Case 1: target is a leaf



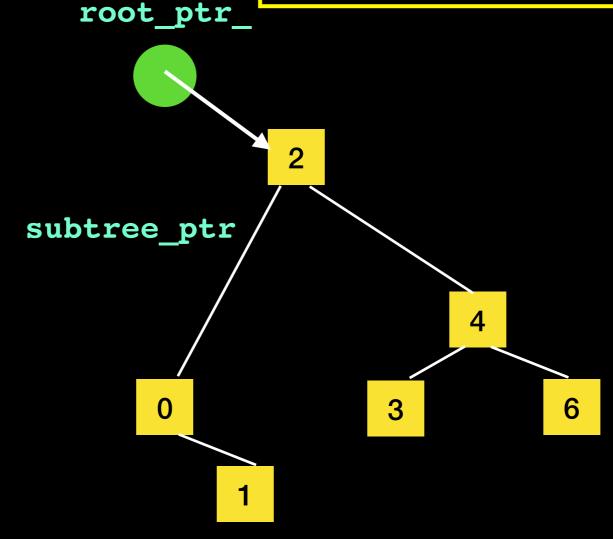
Case 2: target has 1 child Left and right case are symmetric



Case 2: target has 1 child Left and right case are symmetric



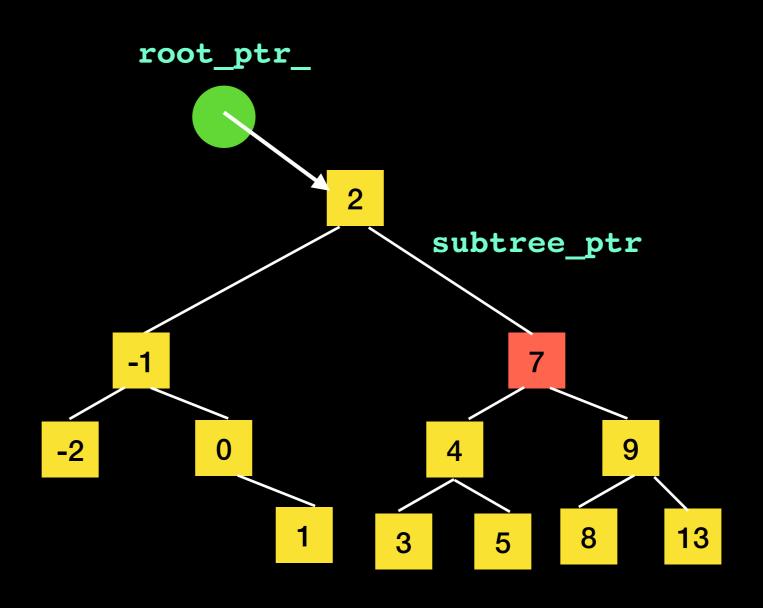
Case 2: target has 1 child Left and right case are symmetric



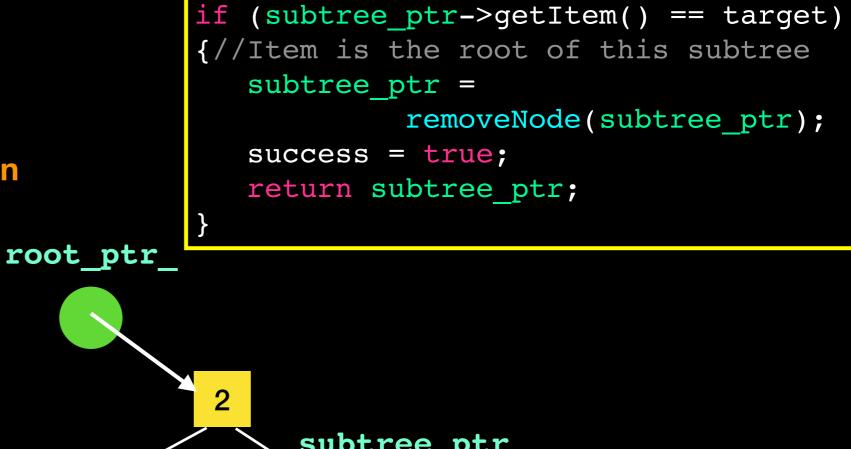
## Lecture Activity

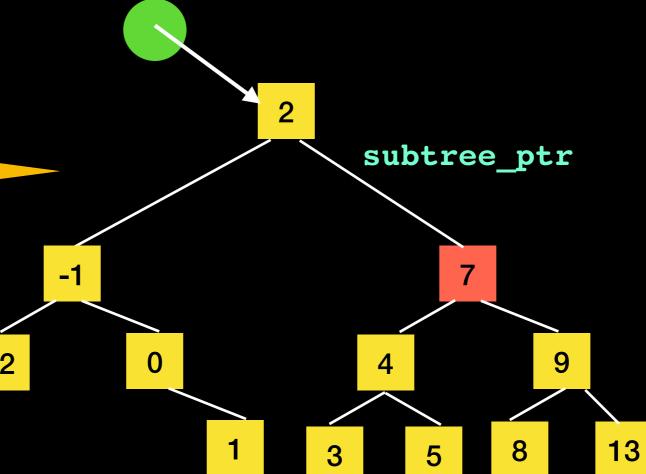
### How would you remove node 7?

Case 3: target has 2 children

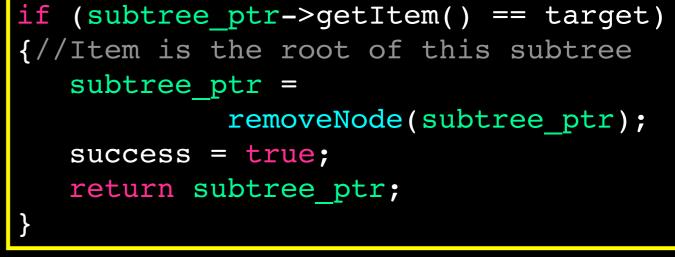


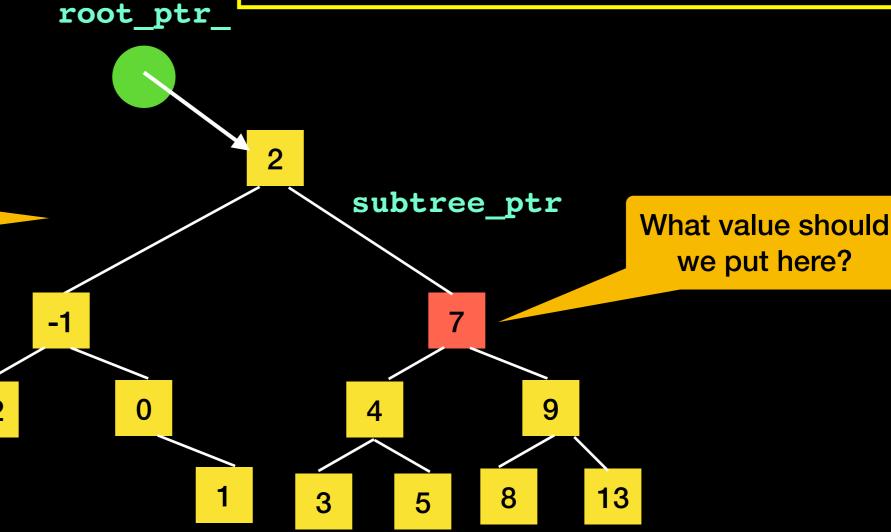
#### Case 3: target has 2 children



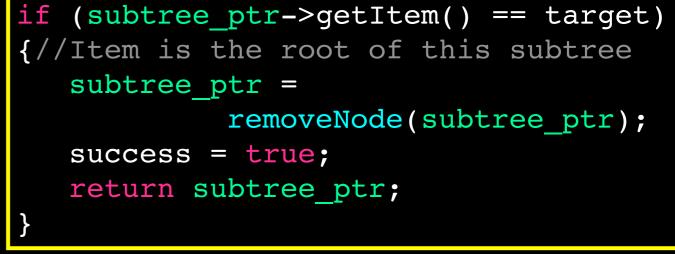


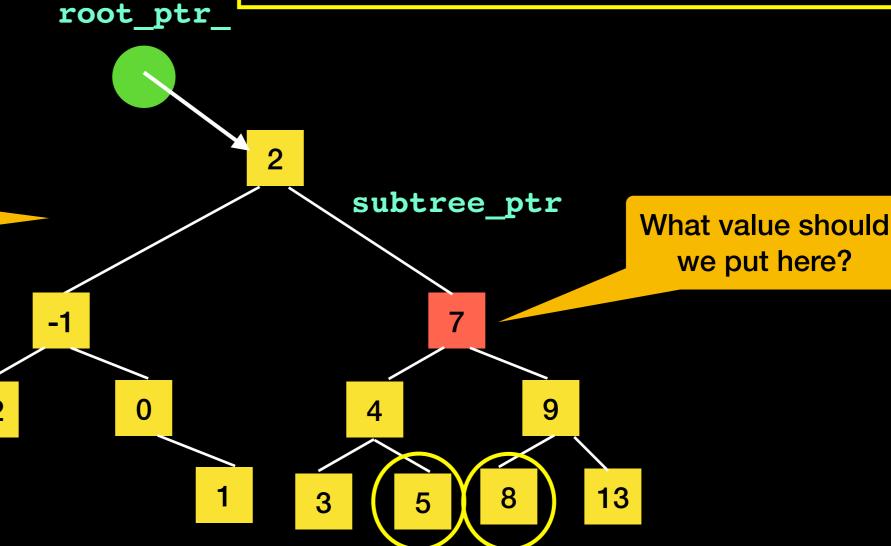
#### Case 3: target has 2 children



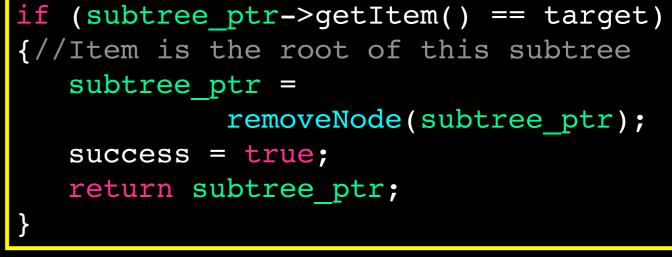


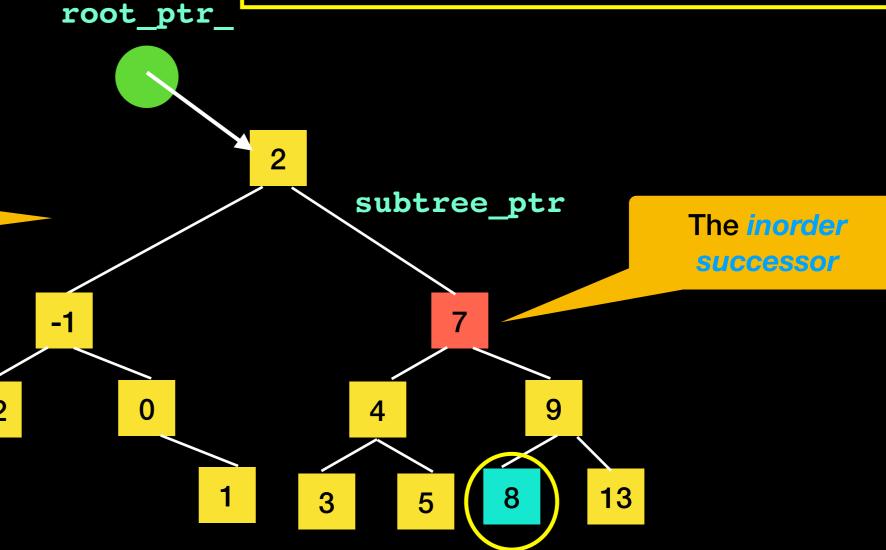
#### Case 3: target has 2 children



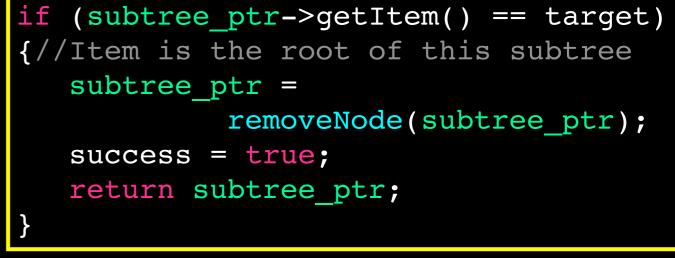


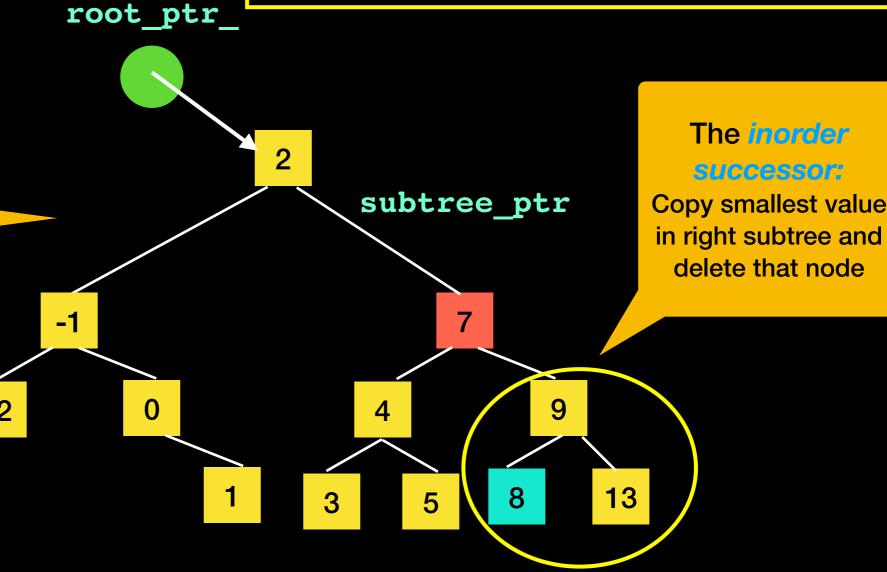
#### Case 3: target has 2 children



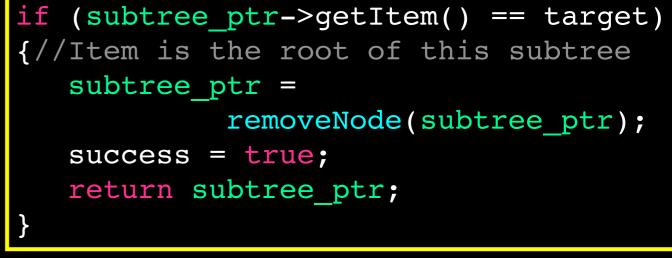


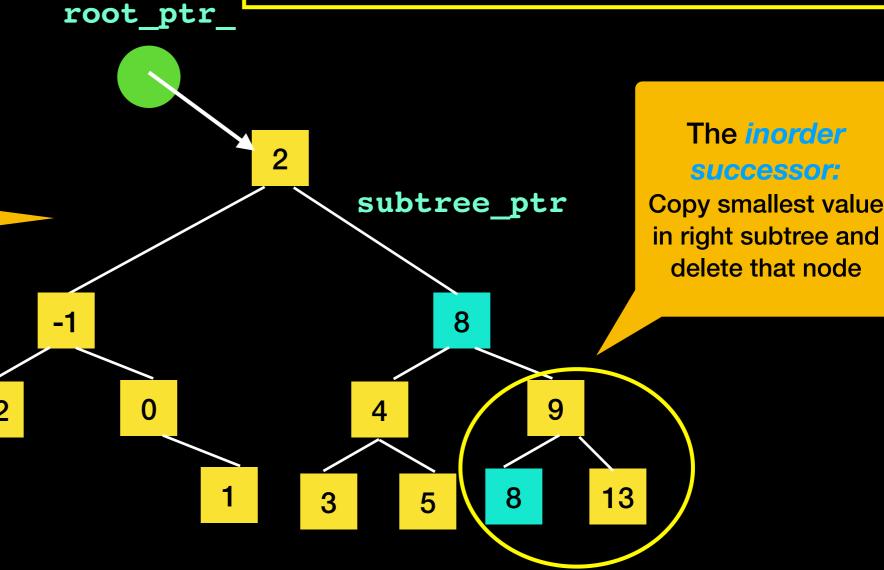
#### Case 3: target has 2 children



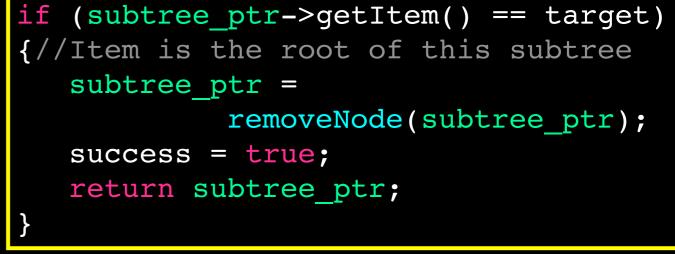


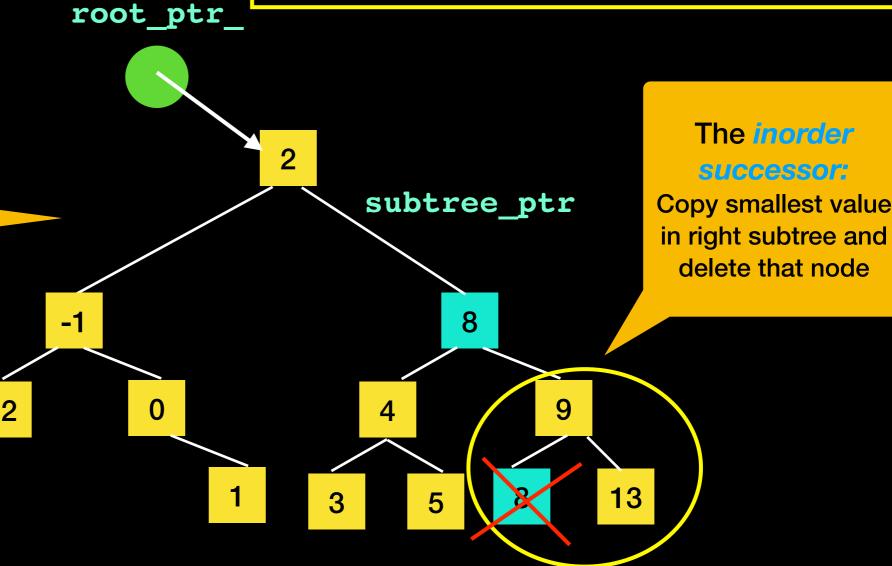
#### Case 3: target has 2 children





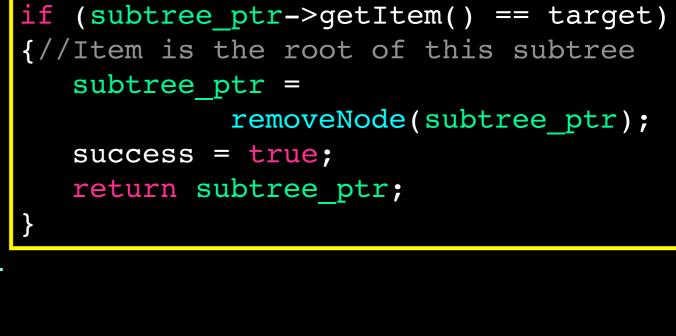
#### Case 3: target has 2 children

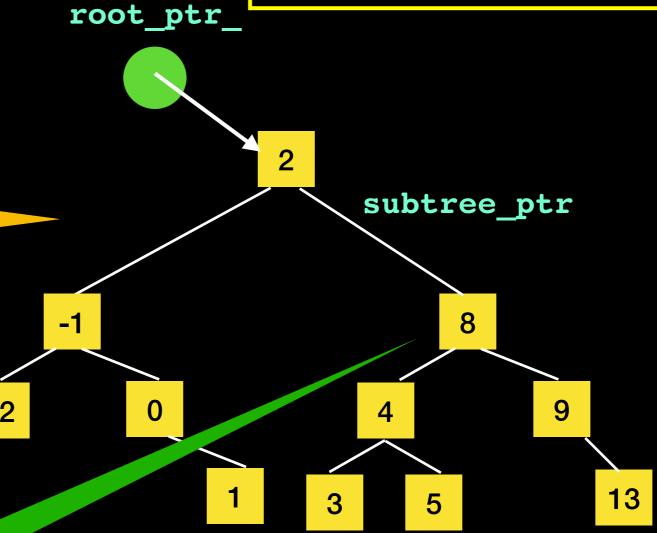




#### Case 3: target has 2 children

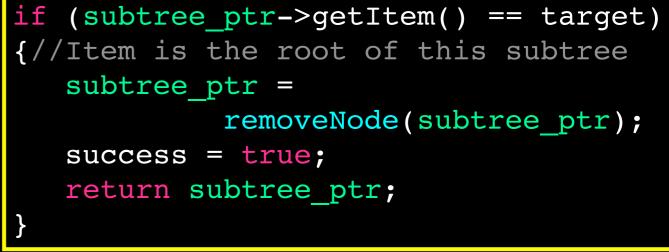
Find a node that is easy to remove and remove that one instead.

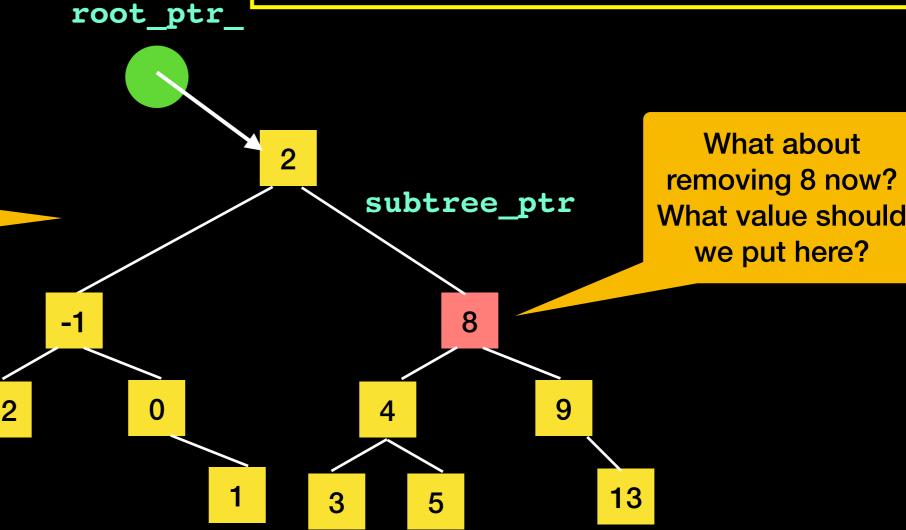




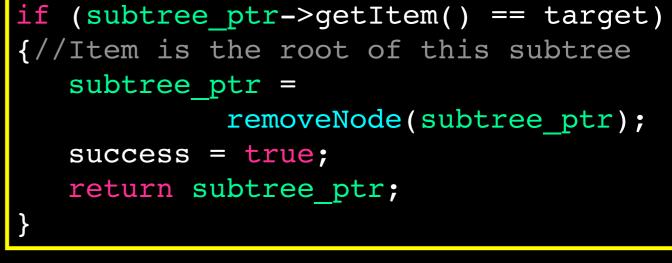
This operation will actually "reorganize" the tree

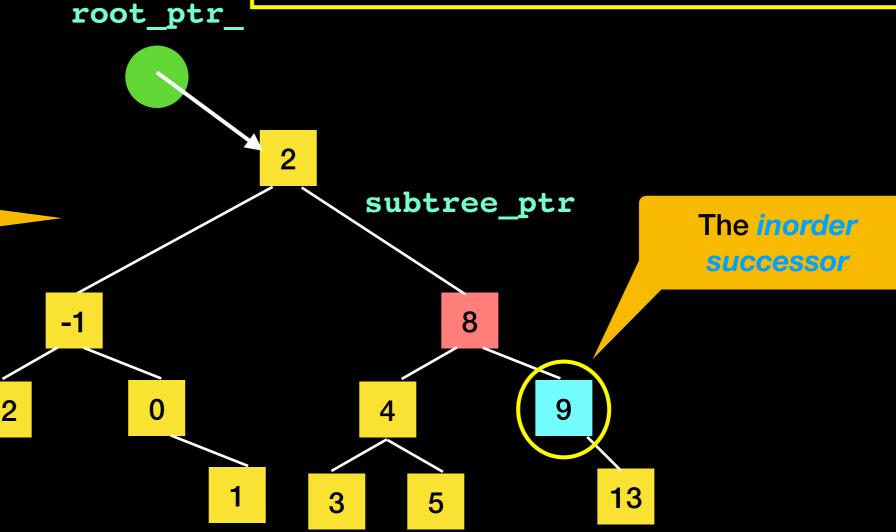
#### Case 3: target has 2 children



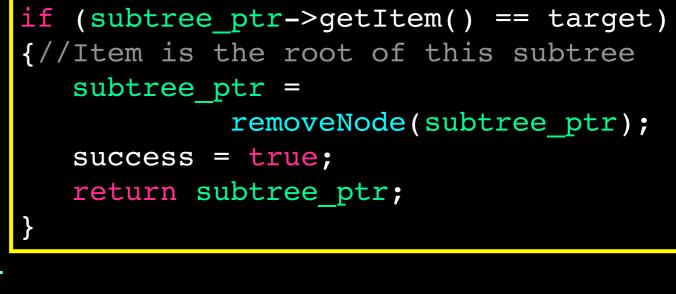


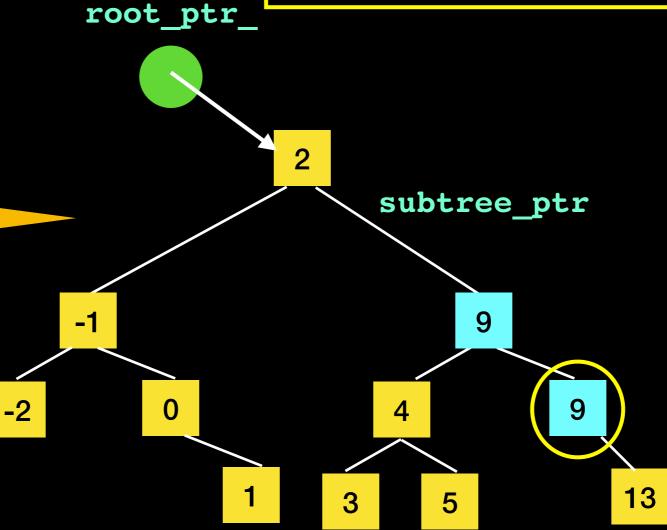
#### Case 3: target has 2 children



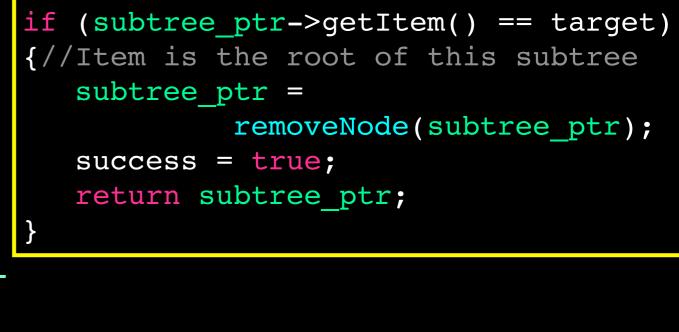


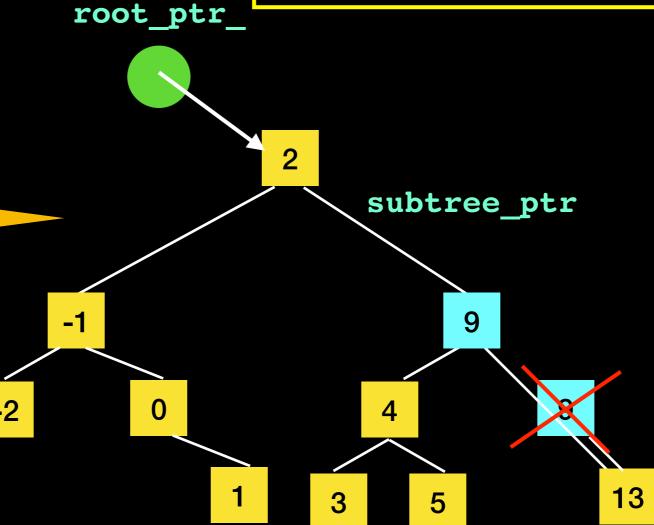
#### Case 3: target has 2 children



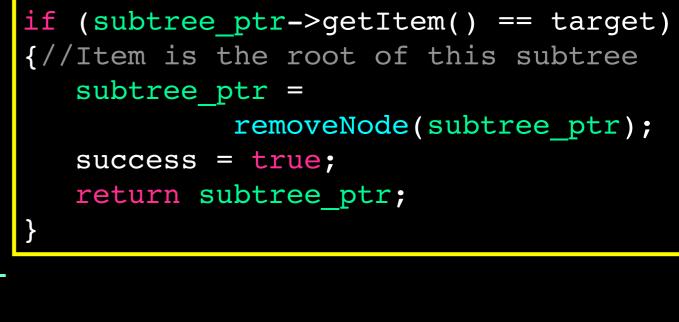


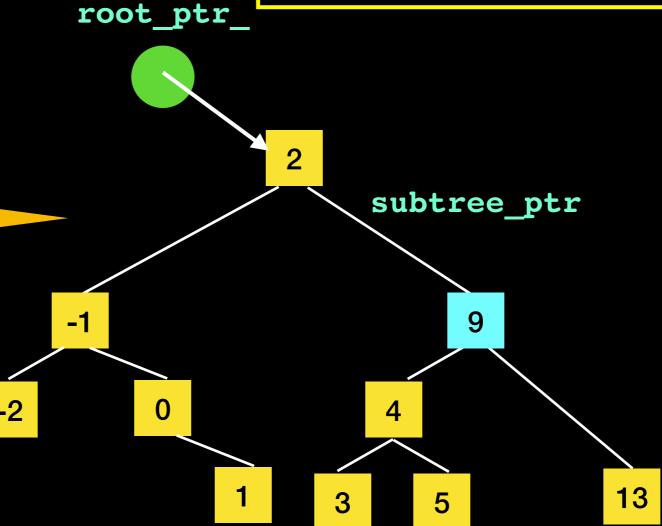
#### Case 3: target has 2 children





#### Case 3: target has 2 children





### removeNode(node\_ptr);

```
template<typename ItemType>
auto BST<ItemType>::removeNode(std::shared ptr<BinaryNode<ItemType>>
node ptr)
   //Case 1) Node is a leaf - it is deleted:
   if (node ptr->isLeaf())
                                          Node is leaf
      node ptr.reset();
      return node ptr; // delete and return nullptr
                                                                   Node has 1 child
   }//Case 2) Node has one child - parent adopts child:
   else if (node_ptr->getLeftChildPtr() == nullptr) // Has rightChild only
      return node ptr->getRightChildPtr();
   else if (node ptr->getRightChildPtr() == nullptr) // Has left child only
                                                Node has 2 children
      return node ptr->getLeftChildPtr();
   }//Case 3) Node has two children:
                                                              Will find leftmost leaf in right
   else
                                                                 subtree, save value in
                                                                new node value and
                                                                   delete leaf node
      ItemType new node value;
      node ptr->setRightChildPtr(removeLeftmostNode()
                              node_ptr->getRightChildPtr(), new_node_value));
      node ptr->setItem(new node value);
      return node ptr;
                                                                Safe Programming:
      // end if
                                                            reference parameter is local to
      end removeNode
                                                             the private calling function
                                        65
```

### removeLeftmostNode

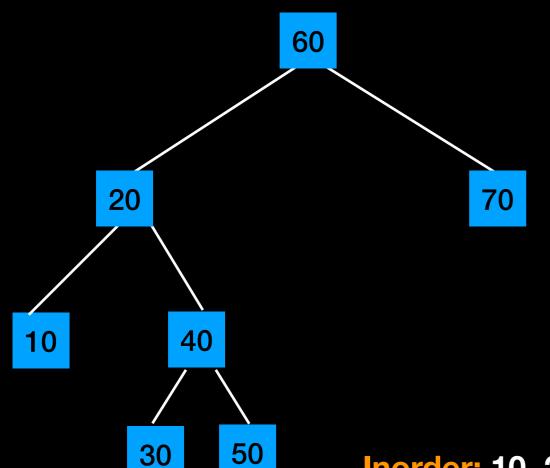
## Traversals

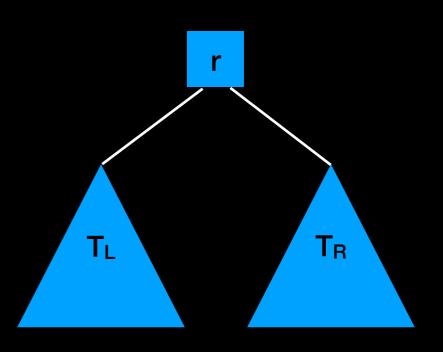
Let's focus on the traversal for now, we will find out what Visitor does next

```
template<typename ItemType>
void BST<ItemType>::preorderTraverse(Visitor<ItemType>& visit) const
   preorder(visit, root_ptr_);
   // end preorderTraverse
template<class ItemType>
void BST<ItemType>::inorderTraverse(Visitor<ItemType& visit) const</pre>
   inorder(visit, root ptr );
   // end inorderTraverse
template<class ItemType>
void BST<ItemType>::postorderTraverse(Visitor<ItemType>& visit) const
   postorder(visit, root ptr );
   // end postorderTraverse
```

```
Visit (retrieve, print, modify ...) every node in the tree Inorder Traversal:
```

```
\label{eq:traverse} \begin{tabular}{ll} \textbf{($T$ is not empty) //implicit base case} \\ \textbf{(} \\ \textbf{traverse $T_L$} \\ \textbf{visit the root r} \\ \textbf{traverse $T_R$} \\ \end{tabular}
```



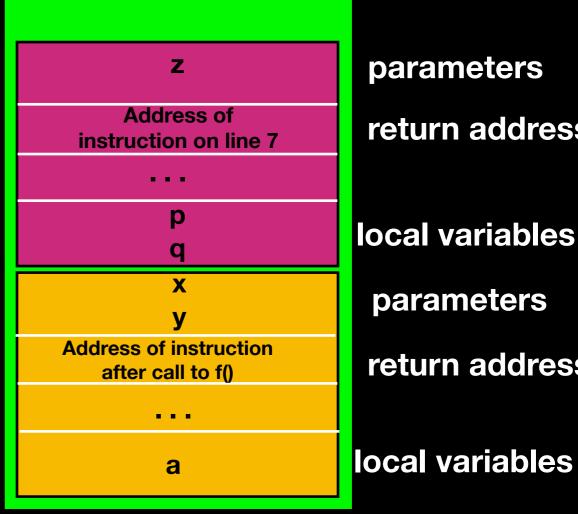


**Inorder:** 10, 20, 30, 40, 50, 60, 70

## inorderTraverse Helper Function

# Recall: Program Stack

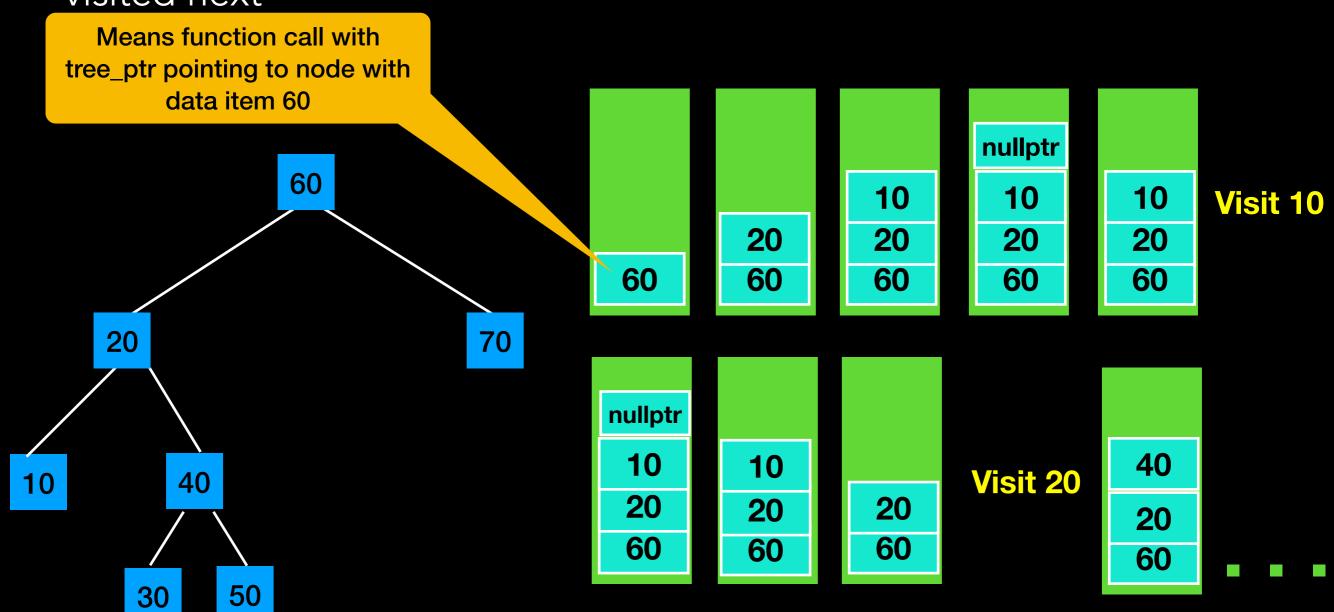
```
1
   void f(int x, int y)
2
3
     int a;
4
    // stuff here
5
   if(a<13)
6
        a = g(a);
7
   // stuff here
                      Stack Frame
8
                        for g()
9
   int g(int z)
10
11
     int p ,q;
                     Stack Frame
12 // stuff here
                        for f()
13 return q;
14 }
```



return address local variables parameters return address

## Recursive Traversal

In recursive solution program stack keeps track of what node must be visited next



## Recursive Traversal

#### With recursion:

- program stack implicitly finds node traversal must visit next
- If traversal backs up to node *d* from right subtree it backs up further to *d*'s parent as a consequence of the recursive program execution

### Non-recursive Traversal

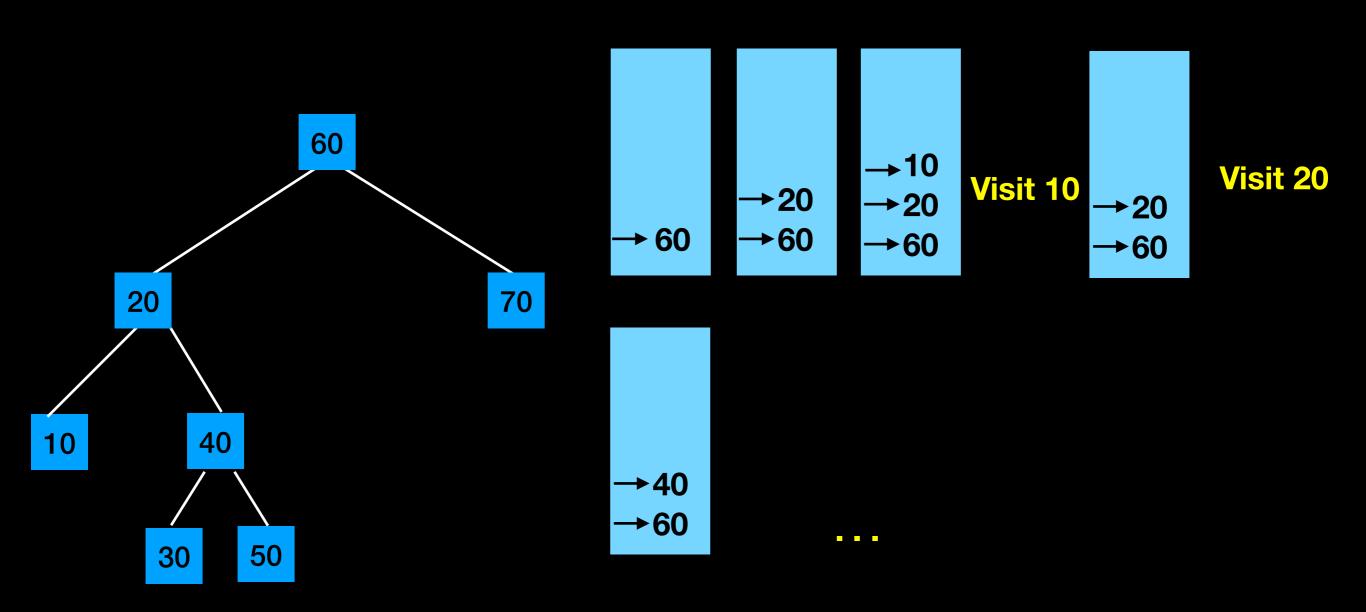
Optimize: Implement iterative approach that maintains an explicit stack to keep track of nodes that must be visited

Place pointer to node on stack **only** before traversing it's left subtree but **NOT** before traversing right subtree

This will also save some "steps" that were unnecessary but implicit in recursive implementation

# Non-recursive Traversal

Iterative solution explicitly maintains a stack of pointers to nodes to keep track of what node must be visited next



#### Non-recursive Traversal

```
template<typename ItemType>
void BST<ItemType>::inorder(Visitor<ItemType>& visit) const
    std::stack<ItemType> node stack;
    std::shared ptr<BinaryNode<ItemType>> current_ptr = root ptr ;
    bool done = false;
   while(!done)
        if(current_ptr != nullptr)
            node stack.push(current_ptr);
            //traverse left subtree
            current_ptr = current_ptr->getLeftChildPtr();
```

# Non-recursive Traversal cont.

```
//backtrack from empt subtree and visit the node at top of
  //stack, but if stack is empty traversal is completed
  else{
      done = node stack.isEmpty();
      if(!done)
          current ptr = node stack.top();
          visit(current_ptr->getItem());
          node stack.pop();
           //traverse right subtree of node just visited
          current_ptr = current_ptr->getRightChildPtr();
end inorder
```

#### Traversals

The last cool trick for you this semester

```
emType>& visit)
```

```
template<typename ItemType>
void BST<ItemType>::preorderTraverse(Visitor<ItemType>& visit)
   preorder(visit, root ptr );
   // end preorderTraverse
template<class ItemType>
void BST<ItemType>::inorderTraverse(Visitor<ItemType>& visit) const
   inorder(visit, root ptr );
   // end inorderTraverse
template<class ItemType>
void BST<ItemType>::postorderTraverse(Visitor<ItemType>& visit) const
   postorder(visit, root ptr_);
   // end postorderTraverse
```

## Functors

Objects that by overloading operator() can be "called" like a function

#### POLYMORPHISM! ABSTRACT CLASS!!!

```
#ifndef Visitor hpp
#define Visitor hpp
#include <string>
template<typename ItemType>
class Visitor
public:
    virtual void operator()(ItemType&) = 0;
    virtual void operator()(ItemType&, ItemType&) = 0;
};
#endif /* Visitor hpp */
```

```
#ifndef StringPrinter hpp
#define StringPrinter hpp
#include "Visitor.hpp"
#include <iostream>
#include <string>
class StringPrinter: public Visitor<std::string>
public:
    void operator()(std::string&) override;
    void operator()(std::string&, std::string&) override;
};
#endif /* StringPrinter hpp */
```

```
#include "StringPrinter.hpp"

void StringPrinter::operator()(std::string& x)
{
    std::cout << x << std::endl;
}

void StringPrinter::operator()(std::string& a, std::string& b)
{
    std::cout << a << b << std::endl;
}</pre>
```

```
#ifndef Inverter hpp
#define Inverter hpp
#include "Visitor.hpp"
#include <iostream>
#include <string>
#include <algorithm>
class Inverter: public Visitor<std::string>
public:
    void operator()(std::string&) override;
    void operator()(std::string&, std::string&) override;
};
#endif /* Inverter hpp */
```

```
#include "Inverter.hpp"
void Inverter::operator()(std::string& x)
    std::reverse(x.begin(), x.end());
    std::cout << x << std::endl;</pre>
void Inverter::operator()(std::string& a, std::string& b)
{
    a.swap(b);
    std::cout << a << b << std::endl;</pre>
```

# Traversal with Functor parameter

```
int main() {
    std::string a string = "a string";
    std::string anoter string = "o string";
    BST<std::string> a_tree(a_string);
    a tree.add(anoter string);
    StringPrinter p;
    Inverter i;
    a tree.inorderTraverse(p);
    std::cout << std::endl;</pre>
    a tree.inorderTraverse(i);
    return 0;
```

```
"a string"

"o string"
```

```
a string
o string
gnirts a
gnirts o
Program ended with exit code: 0
```

```
int main() {
    std::string a string = "a string";
    std::string anoter string = "o string";
    BST<std::string> a_tree(a_string);
    a tree.add(anoter string);
    StringPrinter p;
    Inverter i;
    a tree.inorderTraverse(p);
    std::cout << std::endl;</pre>
    a tree.inorderTraverse(i);
    return 0;
```

```
root ptr
      "a string"
                 "o string"
TA-DAH!
```

```
a string
o string
gnirts a
gnirts o
Program ended with exit code: 0
```