

1. The data set math5305Lab6Data.txt contains 4 columns, Y, X1, X2, and X3 respectively. Perform the following using SAS.;

```
data math5305lab2;  
    infile '/folders/myshortcuts/sas_folder/math5305Lab6Data.txt' dlm=',';  
    input Y X1 X2 X3;  
proc print data=math5305lab2;  
run;
```

- (a) Fit the multiple regression model

$$Y_i = \beta_0 + \beta_1 X_{i1} + \beta_2 X_{i2} + \beta_3 X_{i3} + \epsilon_i;$$

```
proc reg data=math5305lab2;  
    model Y=X1 X2 X3;  
    output out = mult_reg_model  
    r = mult_reg_e  
    predicted=mult_reg_pred;  
run;
```

```
proc print data=math5305lab2;  
run;
```

- (b) What are the estimates  $\hat{\beta}_1, \hat{\beta}_2$ , and  $\hat{\beta}_3$ ?

The estimated values for  $\hat{\beta}_i$  for  $i = 1, 2, 3$  are 17324, -22931, and 35741 respectively.

- (c) Find the  $t$ -statistic and corresponding  $p$ -value for each of  $X_1, X_2$  and  $X_3$ ;

The  $t$ -statistic and  $p$ -value for  $X_1$  are: 13.48, and 0.0001. The  $t$ -statistic and  $p$ -value for  $X_2$  are: -23.61, and 0.0001 The  $t$ -statistic and  $p$ -value for  $X_3$  are: 17.71, and 0.0001

- (d) Find the  $t$ -statistic and corresponding  $p$ -value for testing  $\mathcal{H}_0 : \beta_1 = \beta_2 = \beta_3 = 0$ .

- (e) Find  $R^2$  for this model

The  $R^2$  statistic for this model is 0.9066, and the adjusted  $R^2$  is 0.9037.

- (f) Investigate normality of the residuals for this model using a qq-plot and the Shapiro-Wilk test.

```
proc univariate data=mult_reg_model normal;  
    var mult_reg_e;  
    qqplot mult_reg_e;  
run;
```

The Shapiro-Wilk test gave a  $p$ -value of 0.0003.

- (g) Use the SPEC option to assess homoestadicity of the residuals;

```
proc reg data=math5305lab2;  
    model Y=X1 X2 X3/SPEC;  
run;
```

- (h) Recall that  $e$  is the vector of residuals and  $\hat{Y}$  is the vector of predicted values. Produce the following plots:

- $Y$  vs.  $X_j, j = 1, 2, 3$
- $Y$  vs.  $\hat{Y}$
- $e$  vs.  $X_j, j = 1, 2, 3$
- $e$  vs  $\hat{Y}$

```
proc plot data=mult_reg_model;  
    plot Y * X1  
        Y * X2  
        Y * X3  
        Y * mult_reg_pred  
        mult_reg_e * X1  
        mult_reg_e * X2  
        mult_reg_e * X3  
        mult_reg_e * mult_reg_pred;  
run;
```

- (i) Overall, do the typical linear regression model assumptions appear to hold for this model?;

The residuals do appear to be normally distributed, but the assumption of linearity does not hold.

| Obs | Y          | X1      | X2      | X3      |
|-----|------------|---------|---------|---------|
| 1   | 1259406.18 | 39.0453 | 39.5333 | 20.9620 |
| 2   | 936030.31  | 28.0219 | 30.9788 | 16.4584 |
| 3   | 824255.16  | 32.6895 | 33.5424 | 12.1756 |
| 4   | 791935.54  | 26.0883 | 47.1915 | 20.8821 |
| 5   | 814142.80  | 31.8567 | 30.1321 | 10.3030 |
| 6   | 752152.99  | 14.9992 | 31.7691 | 18.7786 |
| 7   | 176651.36  | 11.6810 | 64.1199 | 20.9198 |
| 8   | 244396.44  | 30.4492 | 68.8134 | 16.1491 |
| 9   | 1004875.12 | 31.3049 | 51.1534 | 26.8269 |
| 10  | 200238.38  | 12.8959 | 51.4379 | 11.9838 |
| 11  | 101651.64  | 13.1630 | 66.5912 | 12.2385 |
| 12  | 635281.47  | 12.1653 | 30.6465 | 18.9123 |
| 13  | 725197.67  | 18.9223 | 46.3227 | 25.7313 |
| 14  | 1600049.16 | 39.2972 | 38.8604 | 29.8250 |
| 15  | 571317.10  | 23.6393 | 51.5862 | 23.2357 |
| 16  | 1005276.89 | 33.5620 | 45.0854 | 25.2475 |
| 17  | 323380.67  | 39.5396 | 61.2474 | 11.7854 |
| 18  | 779123.07  | 25.0209 | 49.6946 | 27.6566 |
| 19  | 490745.33  | 27.8990 | 54.3608 | 21.7202 |
| 20  | 886098.22  | 37.6128 | 39.7350 | 16.8526 |
| 21  | 229456.65  | 35.5826 | 68.9044 | 13.5036 |
| 22  | 337405.68  | 11.0460 | 42.3839 | 17.8423 |
| 23  | 805799.45  | 15.9490 | 40.9920 | 24.9541 |
| 24  | 765921.07  | 28.0789 | 34.7723 | 13.9258 |
| 25  | 350691.07  | 19.1326 | 57.7863 | 22.3733 |
| 26  | 1178033.78 | 19.8324 | 41.4185 | 28.2471 |
| 27  | 1024192.13 | 28.9318 | 30.3775 | 16.6190 |
| 28  | 605820.39  | 27.3136 | 45.0268 | 14.6009 |
| 29  | 1301386.30 | 32.1587 | 44.9900 | 28.2166 |
| 30  | 434518.11  | 38.0469 | 68.5078 | 22.1212 |
| 31  | 1024272.06 | 35.8362 | 48.1053 | 22.1716 |
| 32  | 1256281.77 | 35.3572 | 42.6946 | 22.7589 |
| 33  | 1016415.73 | 38.0535 | 58.8622 | 29.0498 |
| 34  | 576442.20  | 29.5157 | 44.8027 | 12.5180 |
| 35  | 1331182.91 | 18.8233 | 35.8343 | 28.4665 |
| 36  | 717640.89  | 37.1597 | 67.4827 | 29.7086 |
| 37  | 594084.23  | 38.2167 | 57.7957 | 22.6690 |
| 38  | 337520.88  | 36.0285 | 68.3880 | 22.1366 |

| Obs | Y          | X1      | X2      | X3      |
|-----|------------|---------|---------|---------|
| 39  | 760180.80  | 26.1705 | 38.7211 | 17.4500 |
| 40  | 908982.73  | 20.3232 | 31.3945 | 16.2521 |
| 41  | 1236511.35 | 34.4374 | 47.6237 | 27.6603 |
| 42  | 755330.74  | 30.6595 | 55.6435 | 27.4326 |
| 43  | 573772.51  | 18.4482 | 44.9645 | 20.1830 |
| 44  | 643317.00  | 24.9831 | 48.3656 | 19.7600 |
| 45  | 332318.45  | 25.1482 | 52.6470 | 15.1631 |
| 46  | 599135.77  | 33.0721 | 56.4273 | 21.2098 |
| 47  | 1120318.17 | 22.2252 | 36.5392 | 26.9252 |
| 48  | 418112.91  | 28.9907 | 68.2687 | 23.1857 |
| 49  | 531893.54  | 28.5421 | 47.0636 | 14.6195 |
| 50  | 766320.60  | 14.4073 | 34.6296 | 23.1192 |
| 51  | 859140.79  | 19.5943 | 51.2994 | 29.2793 |
| 52  | 1734004.96 | 32.2640 | 31.3606 | 25.8269 |
| 53  | 441216.12  | 14.9251 | 52.4488 | 22.1059 |
| 54  | 502163.83  | 11.6478 | 56.5560 | 27.1347 |
| 55  | 1056067.64 | 36.9109 | 46.6381 | 24.1762 |
| 56  | 783630.08  | 20.6589 | 30.0375 | 15.3360 |
| 57  | 755271.90  | 29.3215 | 45.8394 | 19.8047 |
| 58  | 438922.62  | 32.2792 | 55.4011 | 17.8385 |
| 59  | 779937.25  | 19.2996 | 44.8655 | 28.6092 |
| 60  | 850961.92  | 25.0652 | 52.8184 | 28.4792 |
| 61  | 781417.49  | 37.6999 | 69.2292 | 29.9110 |
| 62  | 1272360.48 | 32.4433 | 39.9670 | 27.4404 |
| 63  | 553085.20  | 20.0492 | 61.5211 | 27.4095 |
| 64  | 718229.09  | 22.3318 | 53.8064 | 27.4870 |
| 65  | 111243.21  | 10.0528 | 62.4303 | 16.9393 |
| 66  | 213516.80  | 37.7933 | 68.3678 | 15.2448 |
| 67  | 549111.01  | 14.6948 | 49.6832 | 27.0536 |
| 68  | 210758.46  | 29.7968 | 61.6762 | 12.7005 |
| 69  | 1043421.10 | 35.1932 | 31.1363 | 13.5069 |
| 70  | 473230.37  | 14.3290 | 58.7712 | 29.3896 |
| 71  | 478283.64  | 31.1134 | 58.0030 | 16.4953 |
| 72  | 571097.77  | 34.9896 | 55.2862 | 19.2766 |
| 73  | 347154.16  | 17.1287 | 61.1559 | 23.3314 |
| 74  | 259174.31  | 15.9392 | 63.6911 | 23.0405 |
| 75  | 1056792.27 | 35.0648 | 42.0847 | 24.4918 |
| 76  | 831176.27  | 29.4815 | 31.3584 | 15.9745 |

| Obs | Y          | X1      | X2      | X3      |
|-----|------------|---------|---------|---------|
| 77  | 231397.28  | 20.8011 | 56.3855 | 14.4185 |
| 78  | 418711.30  | 13.6223 | 41.0289 | 12.8001 |
| 79  | 527233.05  | 24.5111 | 50.3137 | 17.4720 |
| 80  | 764304.22  | 39.9908 | 46.6062 | 16.0165 |
| 81  | 773714.81  | 29.7744 | 48.1206 | 21.6132 |
| 82  | 461181.59  | 15.0893 | 47.6912 | 19.5957 |
| 83  | 471837.04  | 32.1322 | 49.7682 | 13.9803 |
| 84  | 720949.51  | 27.5739 | 44.1710 | 19.4321 |
| 85  | 537535.97  | 20.7796 | 45.2531 | 20.4768 |
| 86  | 569564.74  | 34.9490 | 61.2257 | 23.6398 |
| 87  | 748416.94  | 22.5883 | 36.8303 | 15.7133 |
| 88  | 502261.03  | 23.7121 | 45.9259 | 12.7609 |
| 89  | 380120.00  | 10.6510 | 62.5630 | 26.5546 |
| 90  | 851262.25  | 12.6378 | 42.1794 | 27.3303 |
| 91  | 217574.53  | 12.9634 | 66.5161 | 22.7152 |
| 92  | 599542.56  | 37.5201 | 57.5624 | 24.6593 |
| 93  | 229270.37  | 29.0588 | 64.5441 | 11.7357 |
| 94  | 1272801.89 | 29.5933 | 31.0164 | 23.5361 |
| 95  | 1395360.80 | 33.2722 | 30.5763 | 22.4219 |
| 96  | 605525.96  | 31.1426 | 57.6391 | 23.4427 |
| 97  | 431882.46  | 21.3066 | 62.4051 | 23.9503 |
| 98  | 664524.15  | 17.2731 | 46.0183 | 23.2666 |
| 99  | 1608001.43 | 29.4377 | 41.8730 | 29.3302 |
| 100 | 1199470.60 | 30.5792 | 40.4430 | 25.5269 |

**The REG Procedure**  
**Model: MODEL1**  
**Dependent Variable: Y**

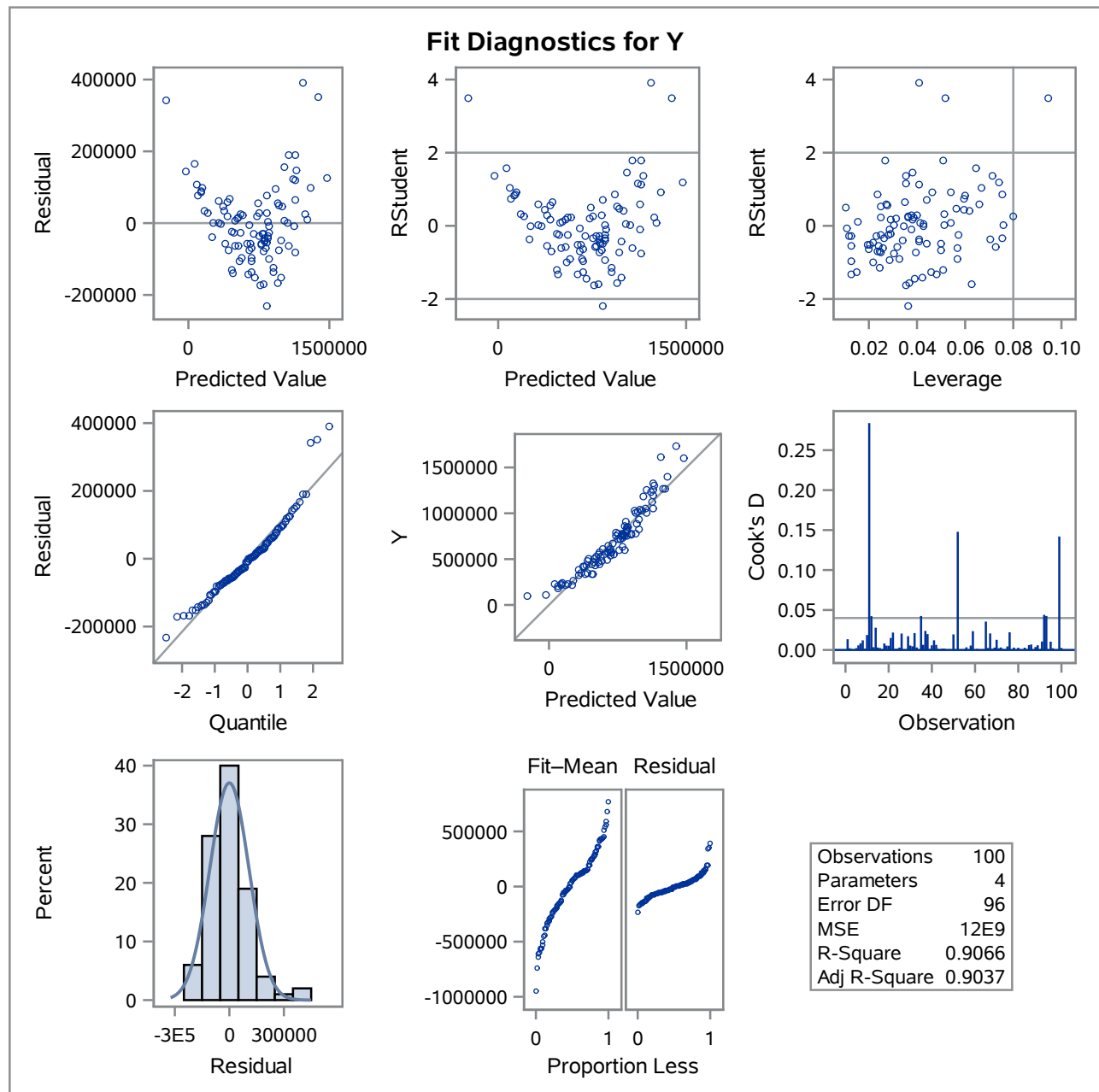
|                             |     |
|-----------------------------|-----|
| Number of Observations Read | 100 |
| Number of Observations Used | 100 |

| Analysis of Variance |    |                |             |         |        |
|----------------------|----|----------------|-------------|---------|--------|
| Source               | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| Model                | 3  | 1.114325E13    | 3.714417E12 | 310.54  | <.0001 |
| Error                | 96 | 1.148277E12    | 11961222055 |         |        |
| Corrected Total      | 99 | 1.229153E13    |             |         |        |

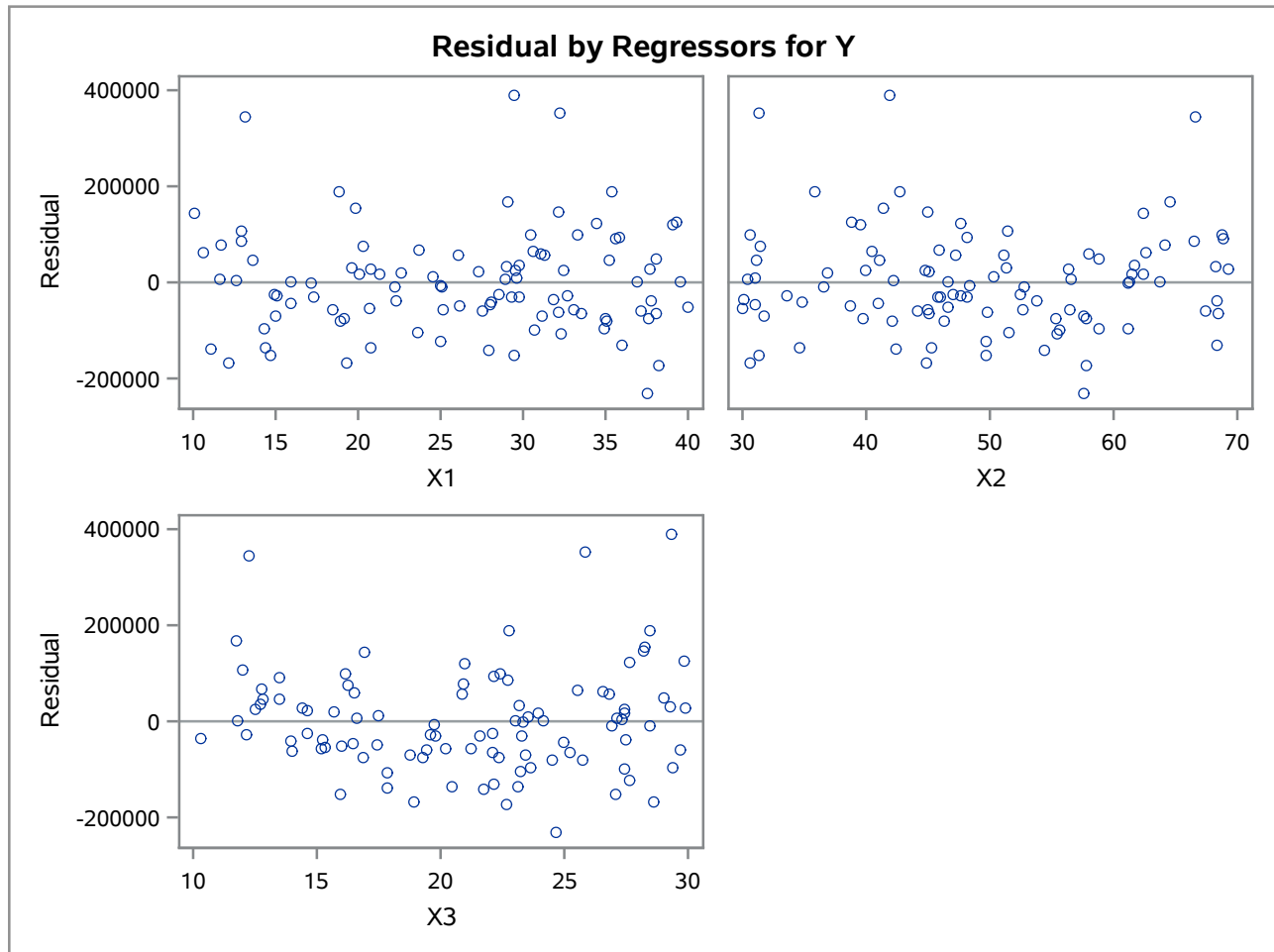
|                |          |          |        |
|----------------|----------|----------|--------|
| Root MSE       | 109367   | R-Square | 0.9066 |
| Dependent Mean | 705093   | Adj R-Sq | 0.9037 |
| Coeff Var      | 15.51106 |          |        |

| Parameter Estimates |    |                    |                |         |         |
|---------------------|----|--------------------|----------------|---------|---------|
| Variable            | DF | Parameter Estimate | Standard Error | t Value | Pr >  t |
| Intercept           | 1  | 620077             | 69959          | 8.86    | <.0001  |
| X1                  | 1  | 17324              | 1284.92073     | 13.48   | <.0001  |
| X2                  | 1  | -22931             | 971.27842      | -23.61  | <.0001  |
| X3                  | 1  | 35741              | 2018.01609     | 17.71   | <.0001  |

**The REG Procedure**  
**Model: MODEL1**  
**Dependent Variable: Y**



**The REG Procedure**  
**Model: MODEL1**  
**Dependent Variable: Y**





| Obs | Y          | X1      | X2      | X3      |
|-----|------------|---------|---------|---------|
| 1   | 1259406.18 | 39.0453 | 39.5333 | 20.9620 |
| 2   | 936030.31  | 28.0219 | 30.9788 | 16.4584 |
| 3   | 824255.16  | 32.6895 | 33.5424 | 12.1756 |
| 4   | 791935.54  | 26.0883 | 47.1915 | 20.8821 |
| 5   | 814142.80  | 31.8567 | 30.1321 | 10.3030 |
| 6   | 752152.99  | 14.9992 | 31.7691 | 18.7786 |
| 7   | 176651.36  | 11.6810 | 64.1199 | 20.9198 |
| 8   | 244396.44  | 30.4492 | 68.8134 | 16.1491 |
| 9   | 1004875.12 | 31.3049 | 51.1534 | 26.8269 |
| 10  | 200238.38  | 12.8959 | 51.4379 | 11.9838 |
| 11  | 101651.64  | 13.1630 | 66.5912 | 12.2385 |
| 12  | 635281.47  | 12.1653 | 30.6465 | 18.9123 |
| 13  | 725197.67  | 18.9223 | 46.3227 | 25.7313 |
| 14  | 1600049.16 | 39.2972 | 38.8604 | 29.8250 |
| 15  | 571317.10  | 23.6393 | 51.5862 | 23.2357 |
| 16  | 1005276.89 | 33.5620 | 45.0854 | 25.2475 |
| 17  | 323380.67  | 39.5396 | 61.2474 | 11.7854 |
| 18  | 779123.07  | 25.0209 | 49.6946 | 27.6566 |
| 19  | 490745.33  | 27.8990 | 54.3608 | 21.7202 |
| 20  | 886098.22  | 37.6128 | 39.7350 | 16.8526 |
| 21  | 229456.65  | 35.5826 | 68.9044 | 13.5036 |
| 22  | 337405.68  | 11.0460 | 42.3839 | 17.8423 |
| 23  | 805799.45  | 15.9490 | 40.9920 | 24.9541 |
| 24  | 765921.07  | 28.0789 | 34.7723 | 13.9258 |
| 25  | 350691.07  | 19.1326 | 57.7863 | 22.3733 |
| 26  | 1178033.78 | 19.8324 | 41.4185 | 28.2471 |
| 27  | 1024192.13 | 28.9318 | 30.3775 | 16.6190 |
| 28  | 605820.39  | 27.3136 | 45.0268 | 14.6009 |
| 29  | 1301386.30 | 32.1587 | 44.9900 | 28.2166 |
| 30  | 434518.11  | 38.0469 | 68.5078 | 22.1212 |
| 31  | 1024272.06 | 35.8362 | 48.1053 | 22.1716 |
| 32  | 1256281.77 | 35.3572 | 42.6946 | 22.7589 |
| 33  | 1016415.73 | 38.0535 | 58.8622 | 29.0498 |
| 34  | 576442.20  | 29.5157 | 44.8027 | 12.5180 |
| 35  | 1331182.91 | 18.8233 | 35.8343 | 28.4665 |
| 36  | 717640.89  | 37.1597 | 67.4827 | 29.7086 |
| 37  | 594084.23  | 38.2167 | 57.7957 | 22.6690 |
| 38  | 337520.88  | 36.0285 | 68.3880 | 22.1366 |

| Obs | Y          | X1      | X2      | X3      |
|-----|------------|---------|---------|---------|
| 39  | 760180.80  | 26.1705 | 38.7211 | 17.4500 |
| 40  | 908982.73  | 20.3232 | 31.3945 | 16.2521 |
| 41  | 1236511.35 | 34.4374 | 47.6237 | 27.6603 |
| 42  | 755330.74  | 30.6595 | 55.6435 | 27.4326 |
| 43  | 573772.51  | 18.4482 | 44.9645 | 20.1830 |
| 44  | 643317.00  | 24.9831 | 48.3656 | 19.7600 |
| 45  | 332318.45  | 25.1482 | 52.6470 | 15.1631 |
| 46  | 599135.77  | 33.0721 | 56.4273 | 21.2098 |
| 47  | 1120318.17 | 22.2252 | 36.5392 | 26.9252 |
| 48  | 418112.91  | 28.9907 | 68.2687 | 23.1857 |
| 49  | 531893.54  | 28.5421 | 47.0636 | 14.6195 |
| 50  | 766320.60  | 14.4073 | 34.6296 | 23.1192 |
| 51  | 859140.79  | 19.5943 | 51.2994 | 29.2793 |
| 52  | 1734004.96 | 32.2640 | 31.3606 | 25.8269 |
| 53  | 441216.12  | 14.9251 | 52.4488 | 22.1059 |
| 54  | 502163.83  | 11.6478 | 56.5560 | 27.1347 |
| 55  | 1056067.64 | 36.9109 | 46.6381 | 24.1762 |
| 56  | 783630.08  | 20.6589 | 30.0375 | 15.3360 |
| 57  | 755271.90  | 29.3215 | 45.8394 | 19.8047 |
| 58  | 438922.62  | 32.2792 | 55.4011 | 17.8385 |
| 59  | 779937.25  | 19.2996 | 44.8655 | 28.6092 |
| 60  | 850961.92  | 25.0652 | 52.8184 | 28.4792 |
| 61  | 781417.49  | 37.6999 | 69.2292 | 29.9110 |
| 62  | 1272360.48 | 32.4433 | 39.9670 | 27.4404 |
| 63  | 553085.20  | 20.0492 | 61.5211 | 27.4095 |
| 64  | 718229.09  | 22.3318 | 53.8064 | 27.4870 |
| 65  | 111243.21  | 10.0528 | 62.4303 | 16.9393 |
| 66  | 213516.80  | 37.7933 | 68.3678 | 15.2448 |
| 67  | 549111.01  | 14.6948 | 49.6832 | 27.0536 |
| 68  | 210758.46  | 29.7968 | 61.6762 | 12.7005 |
| 69  | 1043421.10 | 35.1932 | 31.1363 | 13.5069 |
| 70  | 473230.37  | 14.3290 | 58.7712 | 29.3896 |
| 71  | 478283.64  | 31.1134 | 58.0030 | 16.4953 |
| 72  | 571097.77  | 34.9896 | 55.2862 | 19.2766 |
| 73  | 347154.16  | 17.1287 | 61.1559 | 23.3314 |
| 74  | 259174.31  | 15.9392 | 63.6911 | 23.0405 |
| 75  | 1056792.27 | 35.0648 | 42.0847 | 24.4918 |
| 76  | 831176.27  | 29.4815 | 31.3584 | 15.9745 |

| Obs | Y          | X1      | X2      | X3      |
|-----|------------|---------|---------|---------|
| 77  | 231397.28  | 20.8011 | 56.3855 | 14.4185 |
| 78  | 418711.30  | 13.6223 | 41.0289 | 12.8001 |
| 79  | 527233.05  | 24.5111 | 50.3137 | 17.4720 |
| 80  | 764304.22  | 39.9908 | 46.6062 | 16.0165 |
| 81  | 773714.81  | 29.7744 | 48.1206 | 21.6132 |
| 82  | 461181.59  | 15.0893 | 47.6912 | 19.5957 |
| 83  | 471837.04  | 32.1322 | 49.7682 | 13.9803 |
| 84  | 720949.51  | 27.5739 | 44.1710 | 19.4321 |
| 85  | 537535.97  | 20.7796 | 45.2531 | 20.4768 |
| 86  | 569564.74  | 34.9490 | 61.2257 | 23.6398 |
| 87  | 748416.94  | 22.5883 | 36.8303 | 15.7133 |
| 88  | 502261.03  | 23.7121 | 45.9259 | 12.7609 |
| 89  | 380120.00  | 10.6510 | 62.5630 | 26.5546 |
| 90  | 851262.25  | 12.6378 | 42.1794 | 27.3303 |
| 91  | 217574.53  | 12.9634 | 66.5161 | 22.7152 |
| 92  | 599542.56  | 37.5201 | 57.5624 | 24.6593 |
| 93  | 229270.37  | 29.0588 | 64.5441 | 11.7357 |
| 94  | 1272801.89 | 29.5933 | 31.0164 | 23.5361 |
| 95  | 1395360.80 | 33.2722 | 30.5763 | 22.4219 |
| 96  | 605525.96  | 31.1426 | 57.6391 | 23.4427 |
| 97  | 431882.46  | 21.3066 | 62.4051 | 23.9503 |
| 98  | 664524.15  | 17.2731 | 46.0183 | 23.2666 |
| 99  | 1608001.43 | 29.4377 | 41.8730 | 29.3302 |
| 100 | 1199470.60 | 30.5792 | 40.4430 | 25.5269 |

**The UNIVARIATE Procedure**  
**Variable: mult\_reg\_e (Residual)**

| Moments                |            |                         |            |
|------------------------|------------|-------------------------|------------|
| <b>N</b>               | 100        | <b>Sum Weights</b>      | 100        |
| <b>Mean</b>            | 0          | <b>Sum Observations</b> | 0          |
| <b>Std Deviation</b>   | 107697.543 | <b>Variance</b>         | 1.15988E10 |
| <b>Skewness</b>        | 1.02729692 | <b>Kurtosis</b>         | 2.30908572 |
| <b>Uncorrected SS</b>  | 1.14828E12 | <b>Corrected SS</b>     | 1.14828E12 |
| <b>Coeff Variation</b> | .          | <b>Std Error Mean</b>   | 10769.7543 |

| Basic Statistical Measures |          |                            |            |
|----------------------------|----------|----------------------------|------------|
| Location                   |          | Variability                |            |
| <b>Mean</b>                | 0.00     | <b>Std Deviation</b>       | 107698     |
| <b>Median</b>              | -7978.69 | <b>Variance</b>            | 1.15988E10 |
| <b>Mode</b>                | .        | <b>Range</b>               | 621756     |
|                            |          | <b>Interquartile Range</b> | 120730     |

| Tests for Location: Mu0=0 |           |      |                     |        |
|---------------------------|-----------|------|---------------------|--------|
| Test                      | Statistic |      | p Value             |        |
| <b>Student's t</b>        | <b>t</b>  | 0    | <b>Pr &gt;  t </b>  | 1.0000 |
| <b>Sign</b>               | <b>M</b>  | -3   | <b>Pr &gt;=  M </b> | 0.6173 |
| <b>Signed Rank</b>        | <b>S</b>  | -221 | <b>Pr &gt;=  S </b> | 0.4501 |

| Tests for Normality       |             |          |                     |        |
|---------------------------|-------------|----------|---------------------|--------|
| Test                      | Statistic   |          | p Value             |        |
| <b>Shapiro-Wilk</b>       | <b>W</b>    | 0.942319 | <b>Pr &lt; W</b>    | 0.0003 |
| <b>Kolmogorov-Smirnov</b> | <b>D</b>    | 0.083089 | <b>Pr &gt; D</b>    | 0.0881 |
| <b>Cramer-von Mises</b>   | <b>W-Sq</b> | 0.150516 | <b>Pr &gt; W-Sq</b> | 0.0234 |
| <b>Anderson-Darling</b>   | <b>A-Sq</b> | 1.067692 | <b>Pr &gt; A-Sq</b> | 0.0083 |

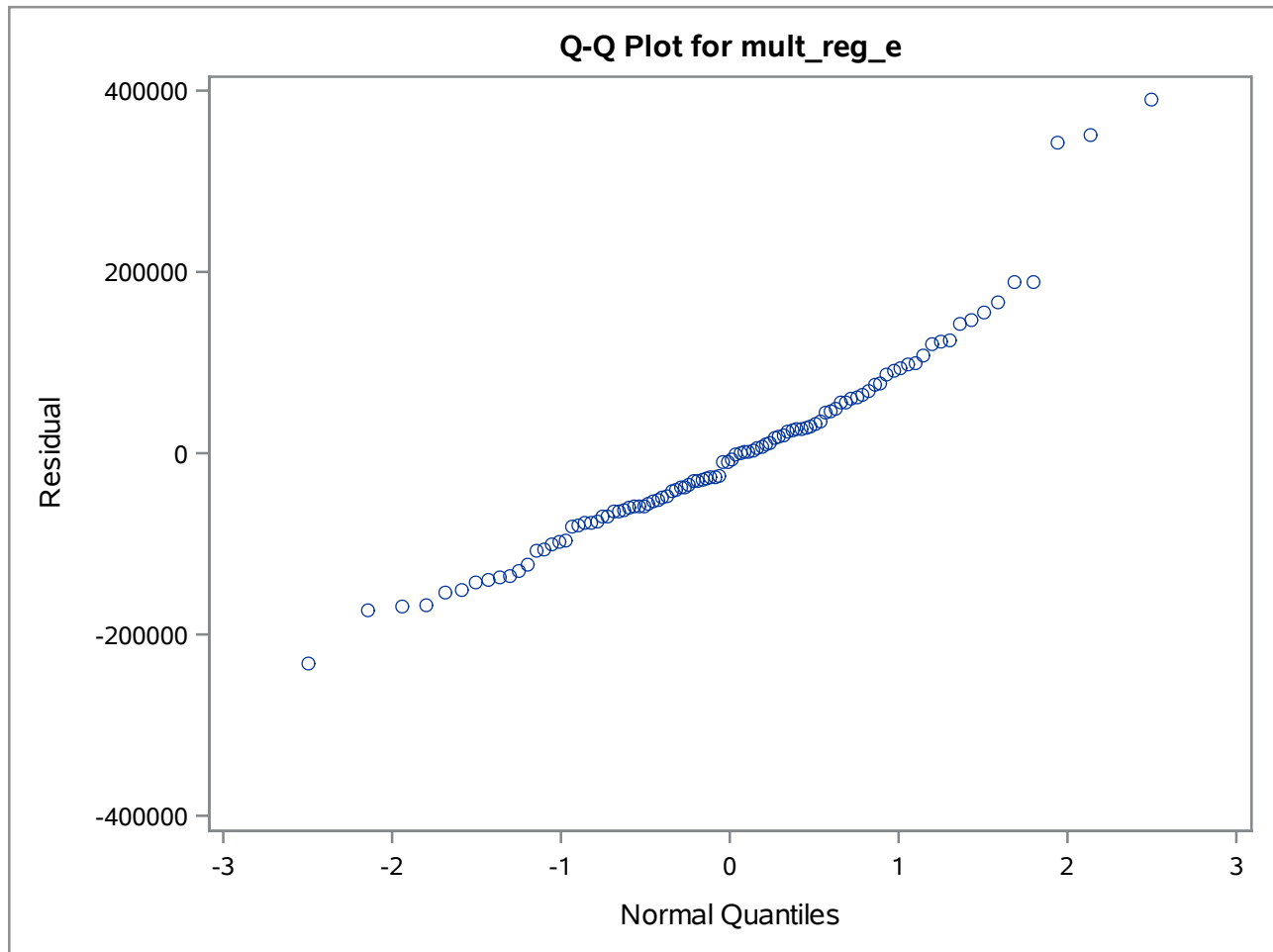
| Quantiles (Definition 5) |           |
|--------------------------|-----------|
| Level                    | Quantile  |
| <b>100% Max</b>          | 389854.74 |
| <b>99%</b>               | 370451.53 |
| <b>95%</b>               | 177850.94 |
| <b>90%</b>               | 123821.01 |
| <b>75% Q3</b>            | 56189.93  |
| <b>50% Median</b>        | -7978.69  |
| <b>25% Q1</b>            | -64539.84 |

**The UNIVARIATE Procedure**  
**Variable: mult\_reg\_e (Residual)**

| Quantiles (Definition 5) |            |
|--------------------------|------------|
| Level                    | Quantile   |
| 10%                      | -132615.92 |
| 5%                       | -152329.55 |
| 1%                       | -202423.03 |
| 0% Min                   | -231901.08 |

| Extreme Observations |     |         |     |
|----------------------|-----|---------|-----|
| Lowest               |     | Highest |     |
| Value                | Obs | Value   | Obs |
| -231901              | 92  | 189295  | 32  |
| -172945              | 37  | 189315  | 35  |
| -168733              | 12  | 343135  | 11  |
| -168189              | 59  | 351048  | 52  |
| -153166              | 67  | 389855  | 99  |

## The UNIVARIATE Procedure



**The REG Procedure**  
**Model: MODEL1**  
**Dependent Variable: Y**

|                             |     |
|-----------------------------|-----|
| Number of Observations Read | 100 |
| Number of Observations Used | 100 |

| Analysis of Variance |    |                |             |         |        |
|----------------------|----|----------------|-------------|---------|--------|
| Source               | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| Model                | 3  | 1.114325E13    | 3.714417E12 | 310.54  | <.0001 |
| Error                | 96 | 1.148277E12    | 11961222055 |         |        |
| Corrected Total      | 99 | 1.229153E13    |             |         |        |

|                |          |          |        |
|----------------|----------|----------|--------|
| Root MSE       | 109367   | R-Square | 0.9066 |
| Dependent Mean | 705093   | Adj R-Sq | 0.9037 |
| Coeff Var      | 15.51106 |          |        |

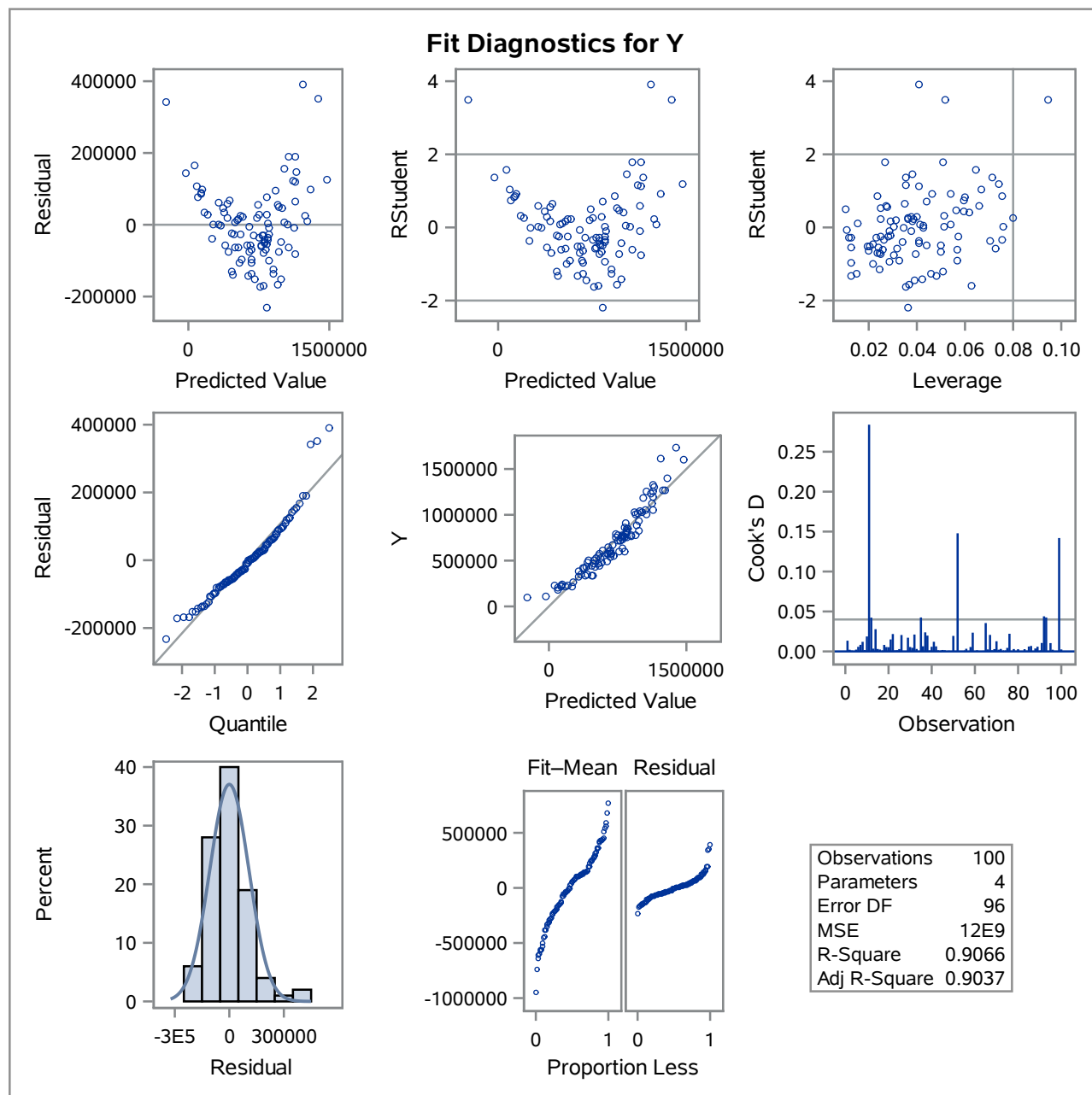
| Parameter Estimates |    |                    |                |         |         |
|---------------------|----|--------------------|----------------|---------|---------|
| Variable            | DF | Parameter Estimate | Standard Error | t Value | Pr >  t |
| Intercept           | 1  | 620077             | 69959          | 8.86    | <.0001  |
| X1                  | 1  | 17324              | 1284.92073     | 13.48   | <.0001  |
| X2                  | 1  | -22931             | 971.27842      | -23.61  | <.0001  |
| X3                  | 1  | 35741              | 2018.01609     | 17.71   | <.0001  |

**The REG Procedure**  
**Model: MODEL1**  
**Dependent Variable: Y**

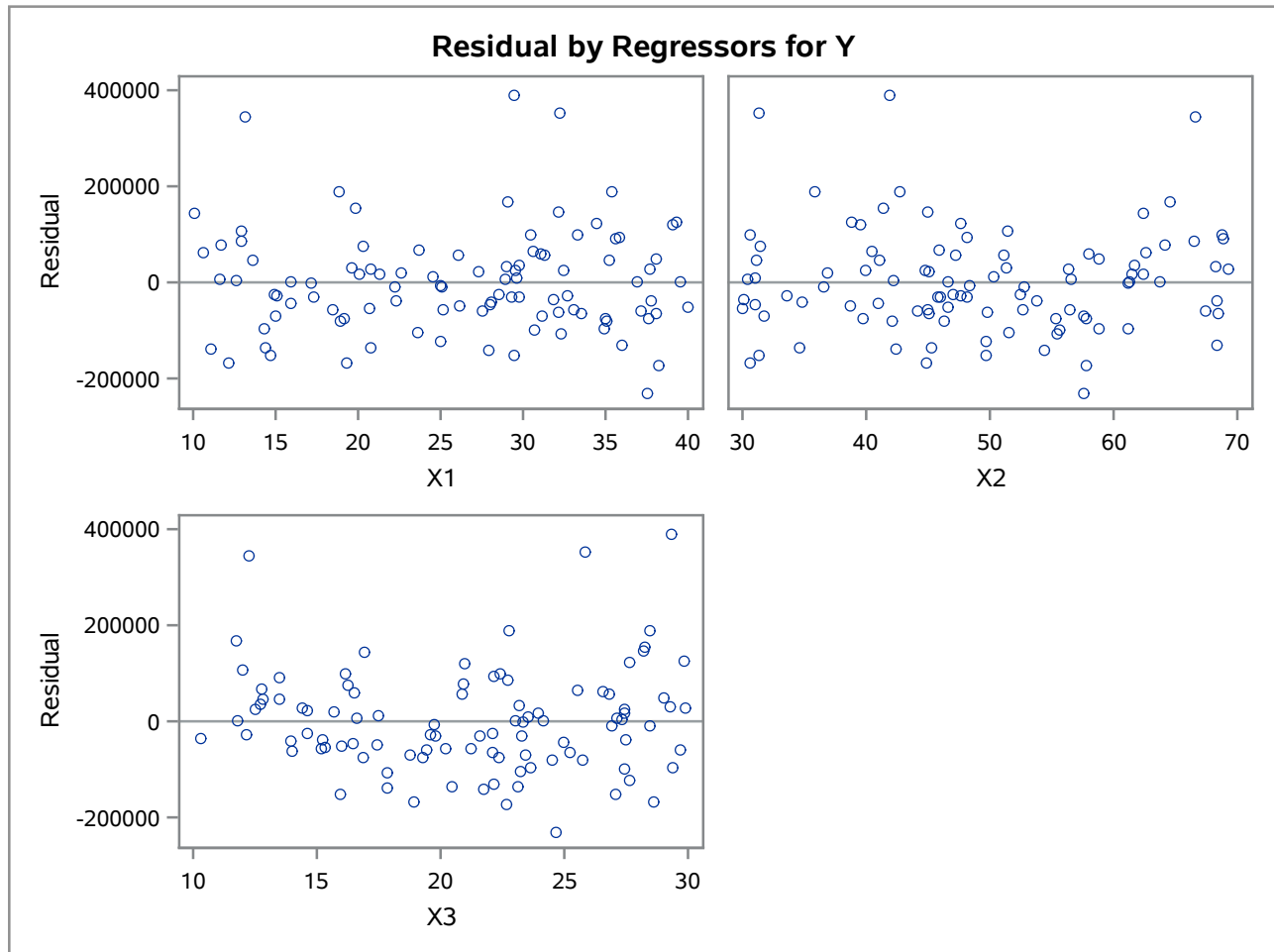
| Test of First and Second<br>Moment Specification |            |            |
|--|------------|------------|
| DF   | Chi-Square | Pr > ChiSq |
| 9  | 13.12      | 0.1571     |

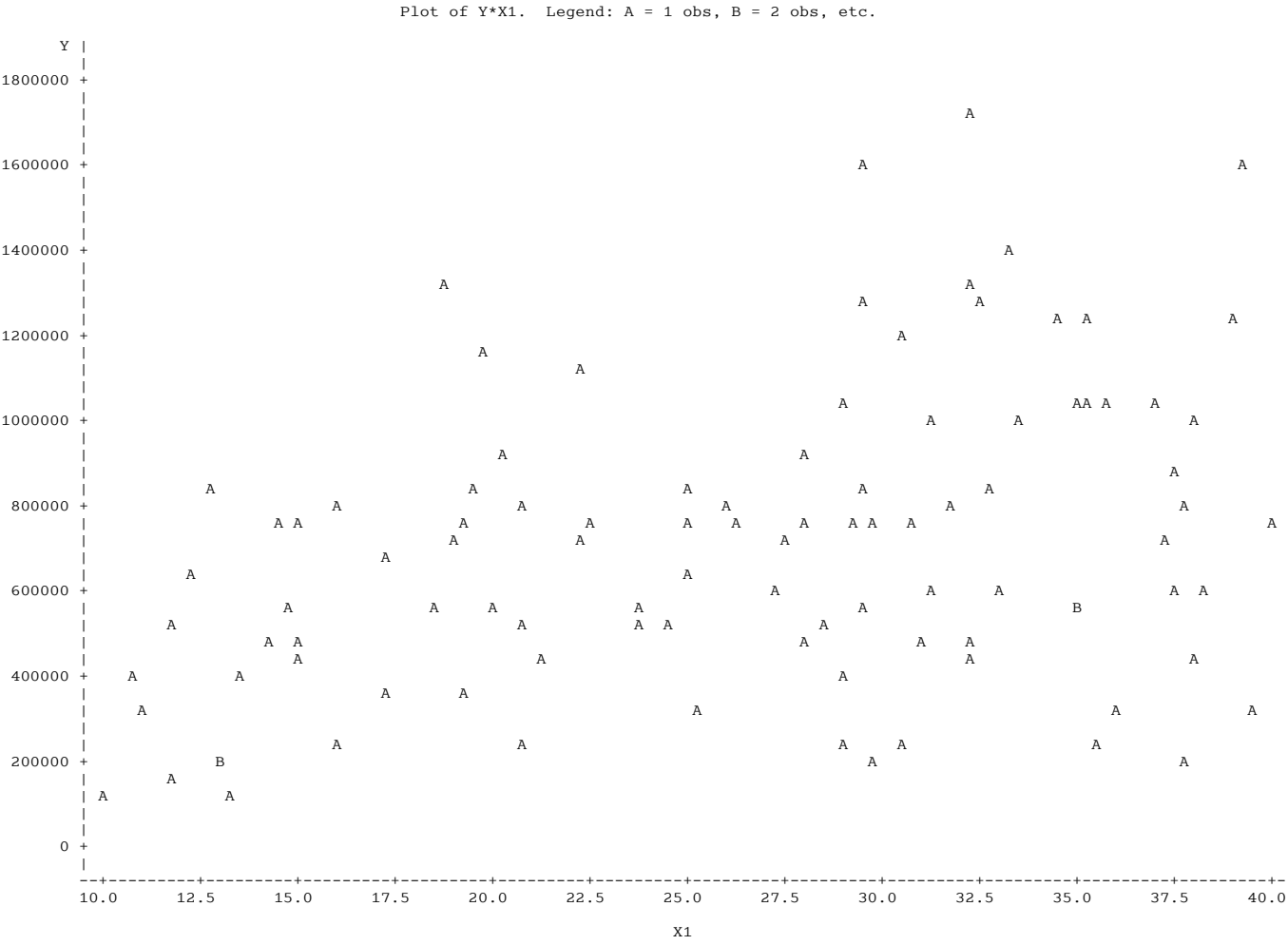


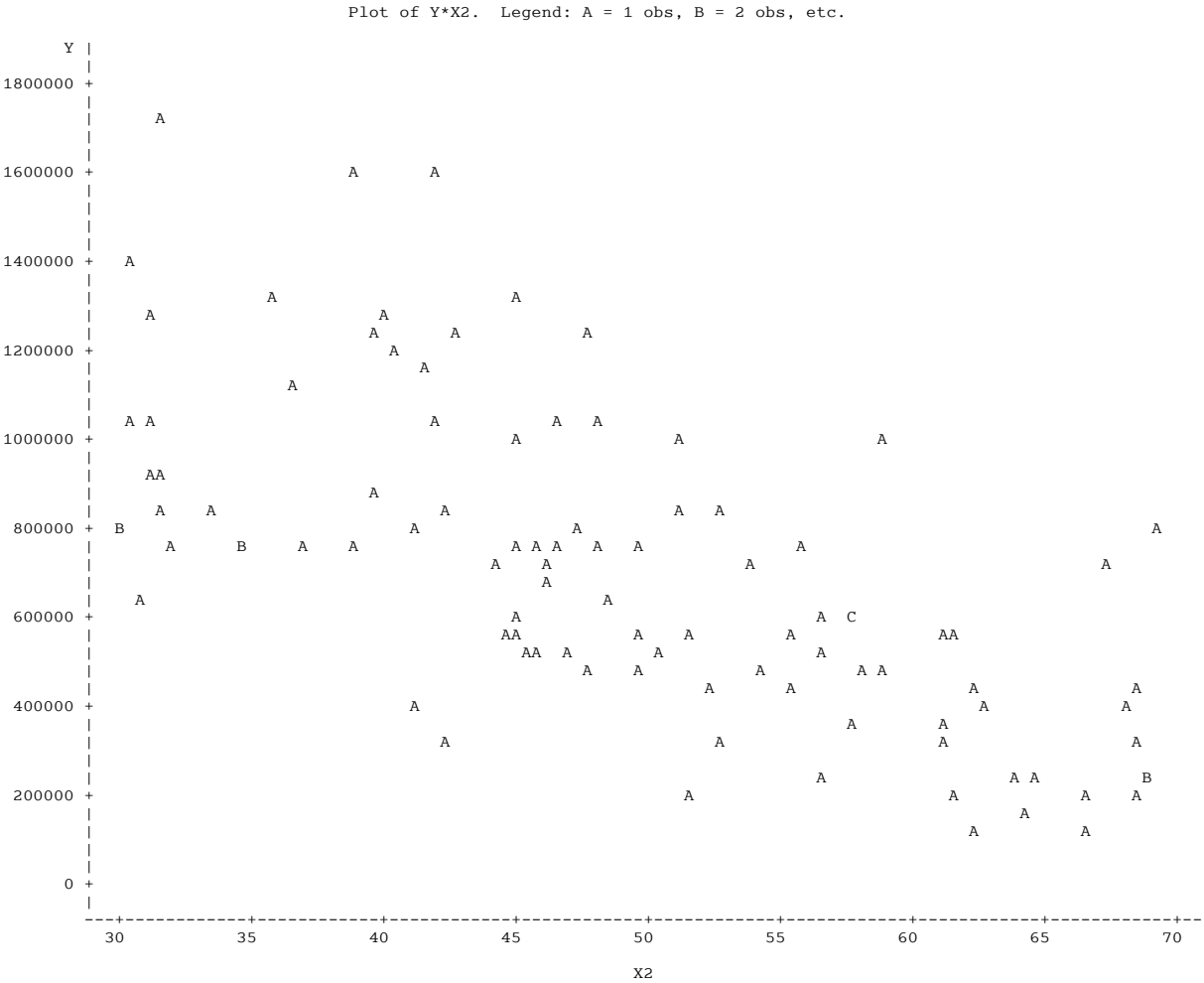
**The REG Procedure**  
**Model: MODEL1**  
**Dependent Variable: Y**



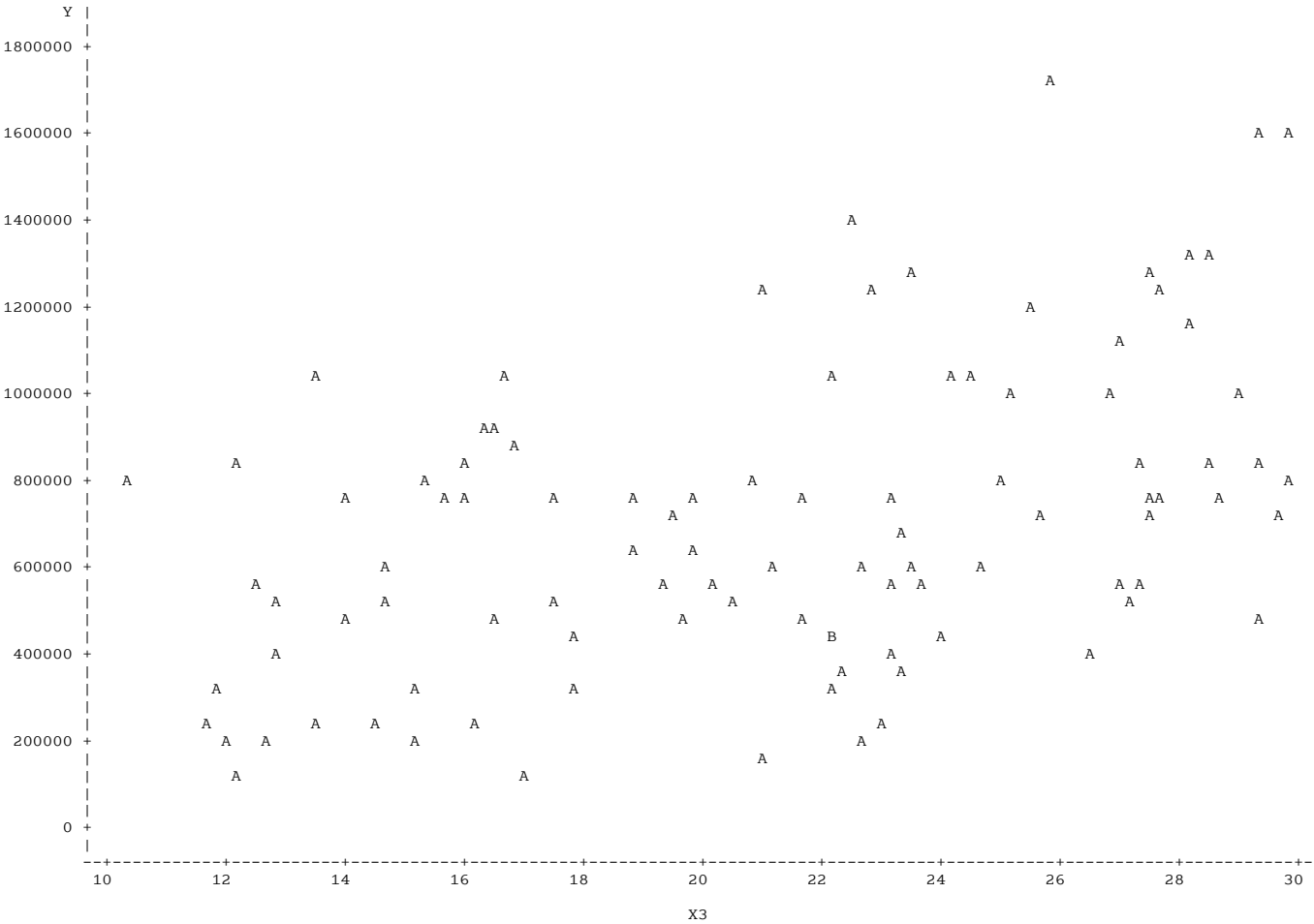
**The REG Procedure**  
**Model: MODEL1**  
**Dependent Variable: Y**



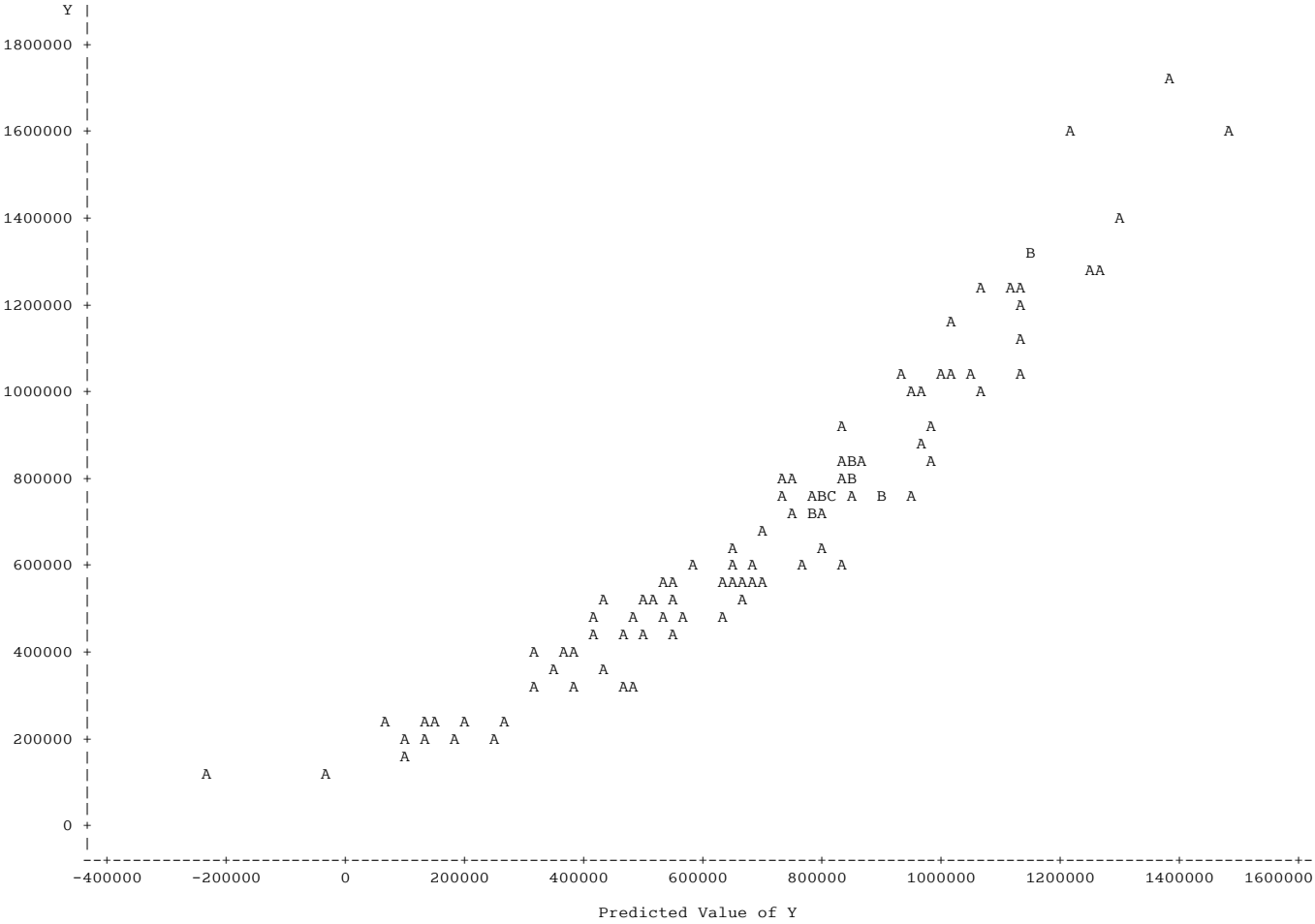


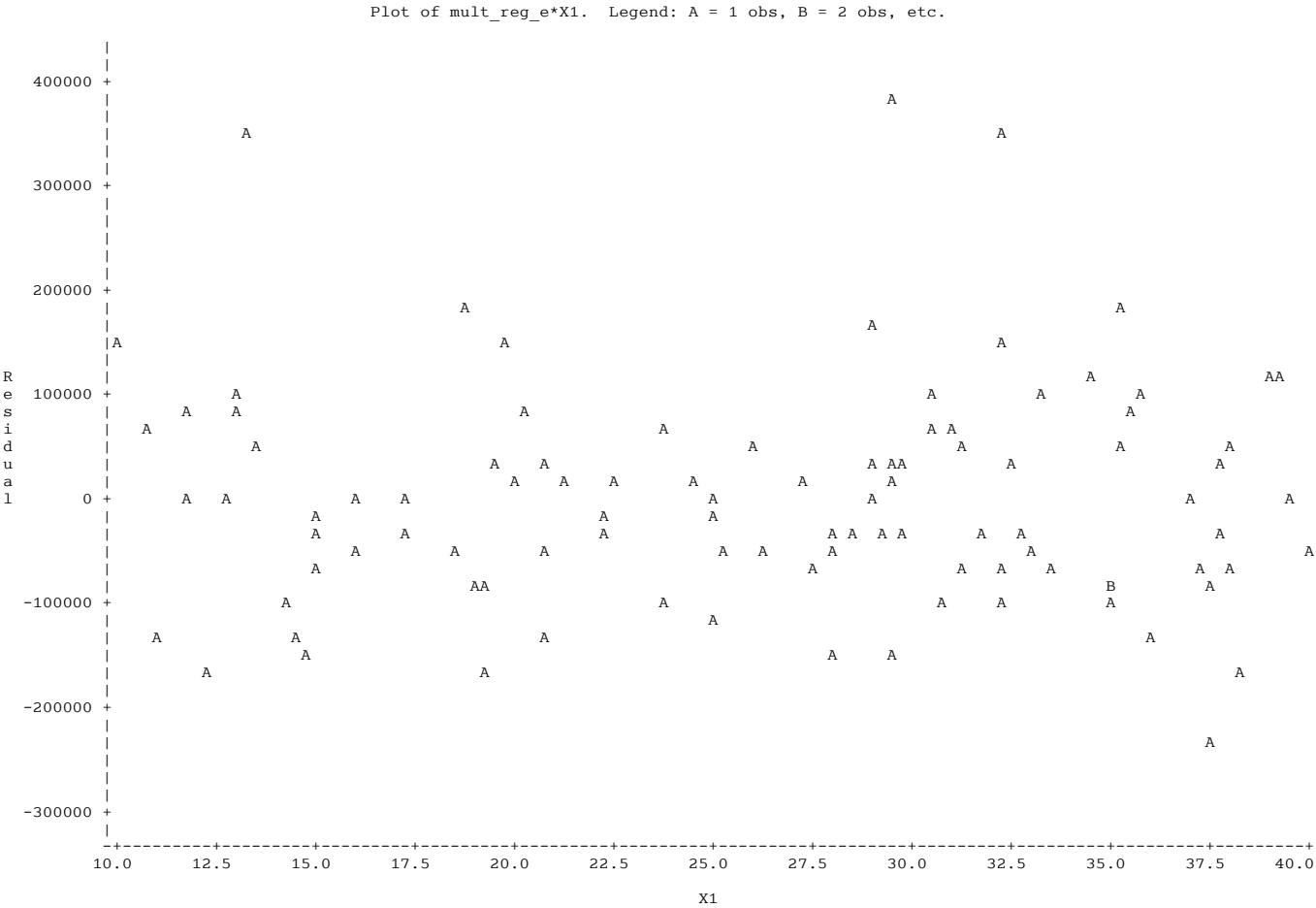


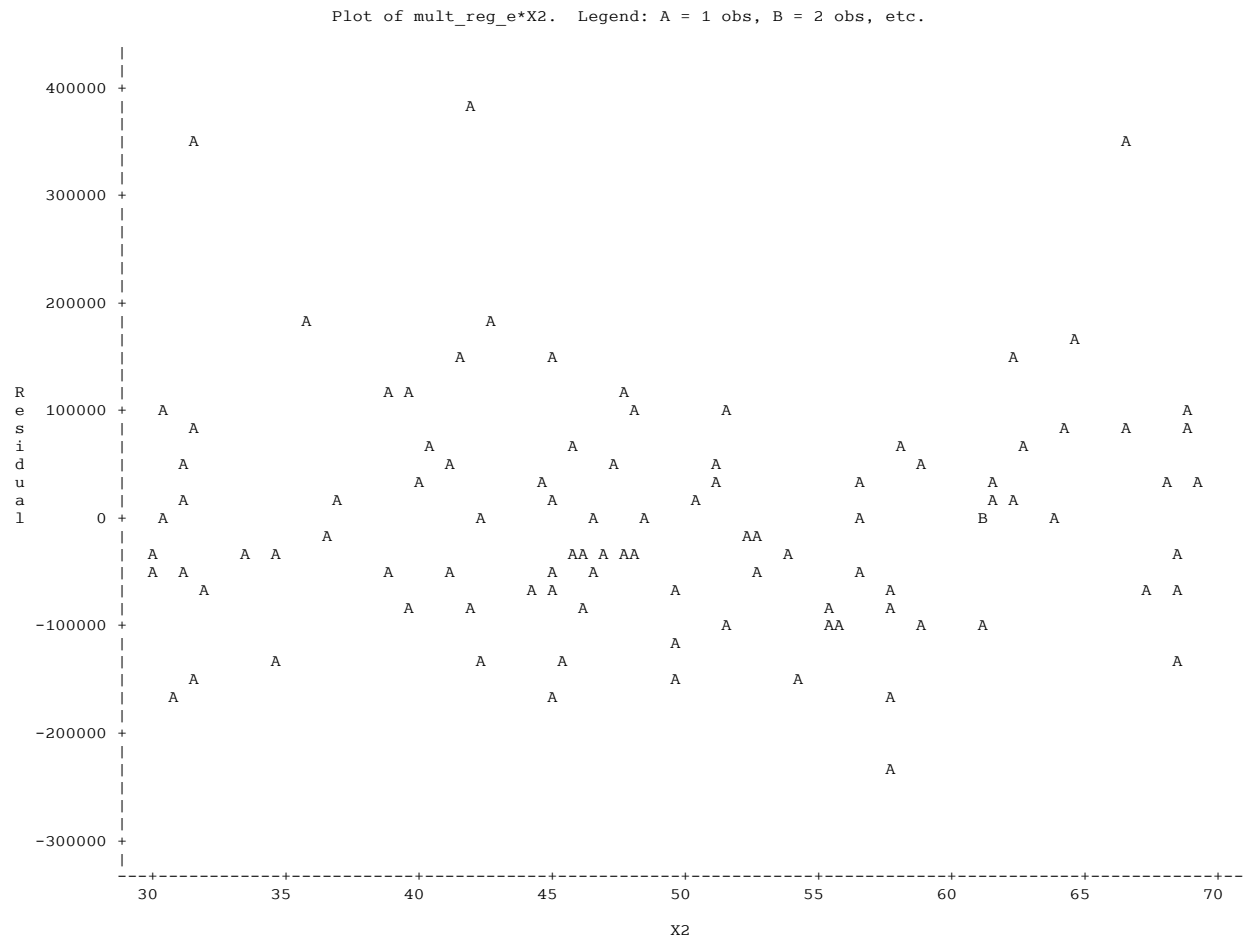
Plot of Y\*X3. Legend: A = 1 obs, B = 2 obs, etc.



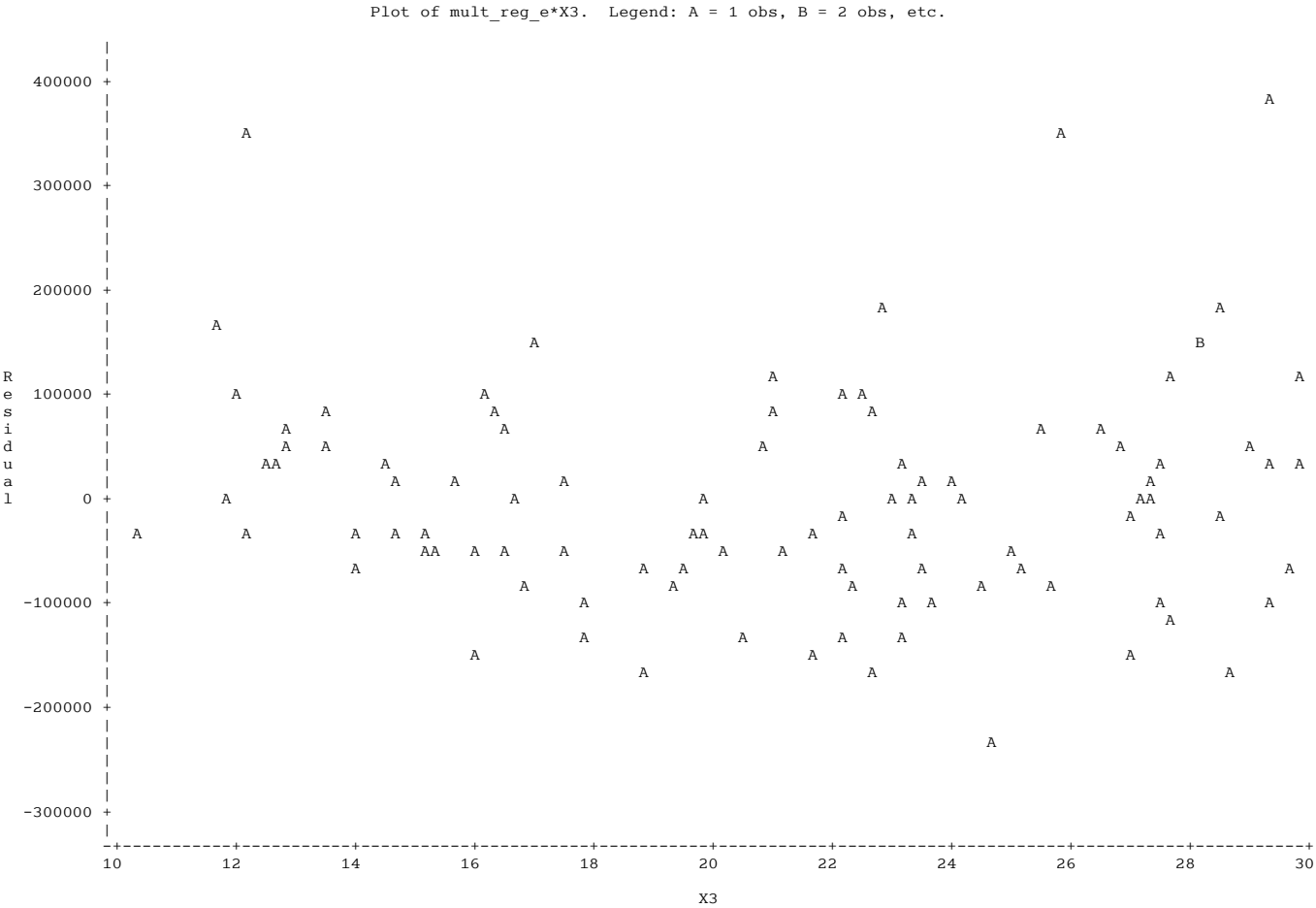
Plot of Y\*mult\_reg\_pred. Legend: A = 1 obs, B = 2 obs, etc.











Plot of mult\_reg\_e\*mult\_reg\_pred. Legend: A = 1 obs, B = 2 obs, etc.

