Overview

Maryclare Griffin

2025-09-05

This material is based on Chapter 1 of Introduction to Statistical Learning (ISL) and Chapter 1 of Elements of Statistical Learning (ESL). We will tend to follow ISL more closely, and look to ESL for occasional additional higher level material.

The phrase statistical learning is a broad term that is not very well defined. The authors of ISL define it as "a set of tools for understanding data." It can be divided into:

- Supervised learning: We observe inputs and (some) outputs, and wish to relate them via a statistical model, e.g. trying to predict a continuous output (linear regression) or trying to predict a categorical or qualitative output (classification).
- Unsupervised learning: We observe inputs and no outputs, and wish to describe the relationships within/structure of the inputs, e.g. clustering.

Throughout, we will use the following notation:

- x_{ij} denotes the value of the j-th variable for observation i, i.e. the i-th observation of input j
- y_i denotes i-th observation of the quantity we want to predict, i.e. the i-th output
- n denotes the number of observations

•
$$X = \begin{pmatrix} x_{11} & \dots & x_{1p} \\ \vdots & \ddots & \vdots \\ x_{n1} & \dots & x_{np} \end{pmatrix}$$
 denotes the matrix of inputs

•
$$x_i = \begin{pmatrix} x_{i1} \\ \vdots \\ x_{ip} \end{pmatrix}$$
 denotes the p dimensional vector of input variables for observation i

•
$$x_j = \begin{pmatrix} x_{1j} \\ \vdots \\ x_{nj} \end{pmatrix}$$
 denotes the n dimensional vector of all observations of input variable j

•
$$n$$
 denotes the number of observations
• p denotes the number of variables
• $X = \begin{pmatrix} x_{11} & \dots & x_{1p} \\ \vdots & \ddots & \vdots \\ x_{n1} & \dots & x_{np} \end{pmatrix}$ denotes the matrix of inputs
• $x_i = \begin{pmatrix} x_{i1} \\ \vdots \\ x_{ip} \end{pmatrix}$ denotes the p dimensional vector of input variables for observation i
• $x_j = \begin{pmatrix} x_{1j} \\ \vdots \\ x_{nj} \end{pmatrix}$ denotes the n dimensional vector of all observations of input variable j
• $y = \begin{pmatrix} y_1 \\ \vdots \\ y_n \end{pmatrix}$ denotes the n dimensional vector observations of the quantity we want to predict or output variable

- When outputs are observed, we denote our observed data as $\{(x_1, y_1), \ldots, (x_n, y_n)\}$.
- We may sometimes drop the subscripts and capitalize to refer to an arbitrary, potentially not yet observed, input or output e.g. $X = (X_1, \ldots, X_p)$ or Y.
- We may denote estimators of unknown quantities by using the same notation but putting a hat on it, e.g. $\hat{\beta}$ refers to an estimator of an unknown parameter β .

Note that the terminology can vary. For instance, what we are referring to as inputs are sometimes also called predictors, independent variables, or features. What we are referring to as outputs are sometimes called responses or dependent variables.