## Homework 3

Due: Thursday 2/20/20 by 8:30am

This homework assignment focuses on material covered in Chapter 1 of the textbook.

1. Suppose Instagram magically knew that every time the number of times user i purchases a product, denoted by  $Y_i$ , is related to the number of times the product has been advertised to user i, denoted by  $X_i$ , as follows:

$$Y_i = 1 + 2X_i + \epsilon_i$$

where  $\epsilon_i$  is a normal random error term with mean  $E\{\epsilon_i\}=0$  and variance  $\sigma^2\{\epsilon_i\}=0.1$ ;  $\epsilon_i$  and  $\epsilon_j$  are uncorrelated so that their covariance is zero (i.e.,  $\sigma\{\epsilon_i,\epsilon_j\}=0$  for all  $i\neq j$ ) for  $i=1,\ldots n$ .

- (a) Using R, make a plot with three panels. You can make a single plot with three panels by typing par(mfrow = c(1, 3)) before running any lines of code that create plots. Plot the density of the errors  $\epsilon_i$  for  $X_i = 0$ ,  $X_i = 1$ , and  $X_i = 10$ , using a separate panel for each value of  $X_i$ . Ensure that the axes are the same across all three plots.
- (b) Based on the assumed model and the information provided, can we conclude that the number of times user i purchases a product  $Y_i$  is independent of the number of times user j purchases a product  $Y_j$ ?
- (c) Based on the assumed model and the information provided, can we state the exact probability that a single value  $Y_i$  will be greater than 4 given that  $X_i = 1$ ?
- (d) Simulate n = 100 observations from the model, with  $X_i = i$ . Using R, make a scatter plot of the data and overlay the regression function on the scatterplot.
- (e) Repeat (d), but instead of assuming that  $\sigma^2 \{ \epsilon_i \} = 0.1$ , assume that  $\sigma^2 \{ \epsilon_i \} = 10$ . In at most one sentence, describe how increasing  $\sigma^2 \{ \epsilon_i \}$  changes how the regression function relates to the scatter plot.
- 2. Problem 1.27 from the .pdf version of the textbook. Requires use of the muscle data that has been posted on the Homework page.
- 3. Problem 1.34 from the .pdf version of the textbook.
- 4. Problem 1.42 from the .pdf version of the textbook.
- 5. Integrative Experience Step 2, as described in ieproject.pdf on the Project page.