

Notes-splitleaf

In the algorithm, we pop out a tree from the queue and then iterate through all the leaves:

```
# enumerate through all the leaves
for i in range(len(leaves)):
```

For each leaf i , if it is not dead and if `tree.splitleaf[0, i] == 1`, then we split it, otherwise we continue:

```
# enumerate through all the leaves
for i in range(len(leaves)):
    # print("d!!!",d)
    # if the leaf is dead, then continue
    if tree.leaves[i].is_dead == 1:
        continue

    # 0 for not split; 1 for split

    if spl[i] == 0:
        continue
```

We split leaf i , and the lower bound is calculated using all leaves except leaf i . We iterate through all features, and for each feature j , if it is not in the path from root to leaf i , then we split leaf i using feature j , and then push the new tree into the queue.

```
lb = tree.lbound[i] # the lower bound
b0 = tree.leaves[i].B0 # the b0 defined in (28) of the paper

d0 = removed_leaf.rules

# split the leaf d0 with feature j
for j in range(1, nrule + 1):
    if j not in d0 and -j not in d0:
        # split leaf d0 with feature j, and get 2 leaves l1 and l2
        l1 = d0 + (-j,)
        l2 = d0 + (j,)
```

Notes - the generate_new_splitleaf function

```
def generate_new_splitleaf(splitleaf_list, cap_l, incorr_l, ndata, nleaves, lb, b0, lamb, R_c):
```

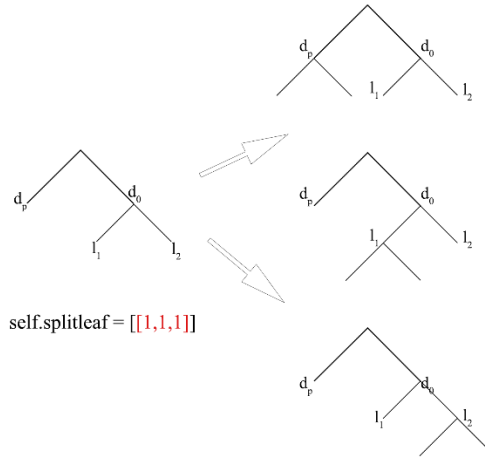
Equivalent Support Bound combined with lookahead: $\text{bound} + b_0 + \text{lamb} < R^c$,

Accurate Support Bound: $a < \text{lamb}$,

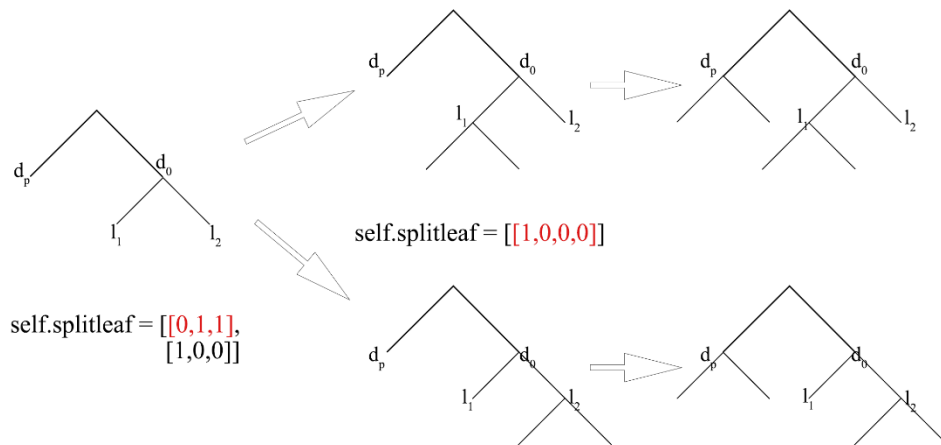
- (1) If Equivalent Support Bound does NOT hold, we can prune all trees that contain d_p , which means we need to split at least one leaf in d_p .
- (2) If Accurate Support Bound does NOT hold, we can prune all trees that contain (l_1, l_2) , which means we need to split at least one of (l_1, l_2) .

There are 4 cases, here is how it goes:

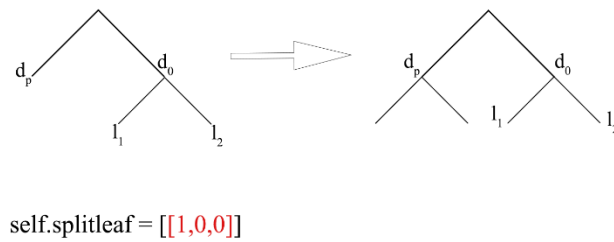
- A. If not(1) and not(2), we don't prune any tree, and we push one row $[1,1,1,1 \dots, 1,1]$ into *self.splitleaf*, which marks every leaf to be split.



- B. If (1) and (2), we push two rows into *self.splitleaf*, after the two rows are popped out and those leaves are split, we will only get trees which split one leaf in d_p and one leaf in (l_1, l_2) .



- C.** If (1) and not(2), we push one row into *self.splitleaf*, which marks all leafs in d_p to be split, but l_1 and l_2 to be not split.



- D.** If not(1) and (2), we push one row into *self.splitleaf*, which marks all leafs in (l_1, l_2) to be split, but d_p to be not split.

