

## **Understanding Cryptography**

Due Date: 1400.02.05

**Homework No.3** 

## Chapter 5

1.

1.1. Compare five modes of operation designed to be used with modern Block Ciphers.

Operation Mode	Description	Data Unit Size
ECB		
CBC		
CFB		
OFB		
CTR		

1.2. What are the advantages and disadvantages of Mode ECB?

2. Besides simple bit errors, the deletion or insertion of a bit yields even more severe effects since the synchronization of blocks is disrupted. In most cases, the decryption of subsequent blocks will be incorrect. A special case is the CFB mode with a feedback width of 1 bit. Show that the synchronization is automatically re-stored after K+1 steps, where K is the block size of the block cipher.

3.

## Programming

Complete the file "operationModes.ipynb" related to the implementations of operational modes including ECB, CBC, OFB, CFB, and CTR. In this file, we use AES as our block cipher. For the sake of your convenience, the input string and outputs of functions are processed to make them suitable and compatible for use with the block cipher. This way, all you have to do is to complete the parts in which you're asked to write your codes. However, feel free to change any parts you deem inconsistent with your needs. At the same time, note that the purpose of this exercise is to have you understand and implement the algorithms yourself. Therefore, using built-in implementations of encryption modes does not merit any score. (To open the file you might need to use ipython or jupyter notebooks)

# Chapter 6

#### **Euler's Phi Function**

**4.** If p is a prime and a is a positive integer, prove

$$\emptyset (p^a) = p^a - p^{a-1}$$

#### Wilson theorem

5. If p is a prime, prove that

$$\binom{p-1}{k} \equiv (-1)^k \ (mod \ p).$$

**6.** If *p* is a prime, prove that

$$(p-1)! + 1 = 0 \mod p$$

## **Number Theory**

7. Prove that any prime of the form 3k + 1 is of the form 6k + 1.

**8.** Prove for *n* a natural number, If  $n \ge 2$  then  $n^3 - n$  is always divisible by 3.

## • Deliverables:

Put the answer to each of the questions in your answer sheet. For the programming assignment, save your desired changes to the "operationModes.ipynb" file, and put this file along with the "AES.py" file in your answer folder.