

1. Task 1:

Assumptions:

- 1- Unlimited number of taxis
- 2- Disregarding rides without passengers
- 3- Ignoring temporal aspects
- 4- Capacity limitation=1

d_{rk} = distance from node r to node k

p_i = pick up point passenger i

d_i = drop off point passenger i

Minimum total travel distance= $\sum_{i=1}^n d_{p(i)d(i)} = 110319.18$ km

2. Task 2:

Assumptions:

- 1- Unlimited number of taxis
- 2- Disregarding rides without passengers
- 3- Ignoring temporal aspects
- 4- Capacity limitation=2

Parameters:

r = set of all nodes

n = set of all passengers

i = index of passenger

d_{rk} = distance from node r to node k

p_i = pick up point passenger i

d_i = drop off point passenger i

Decision Variables:

$$x_{ij} = \begin{cases} 1 & \text{if taxi goes from pickup point of passenger i to pickup point of passenger j} \\ 0 & \text{otherwise} \end{cases}$$

$$m_{ij} = \begin{cases} 1 & \text{if taxi drops off passenger i before passenger j} \\ 0 & \text{otherwise} \end{cases}$$

$$n_{ij} = \begin{cases} 1 & \text{if taxi drops off passenger i after passenger j} \\ 0 & \text{otherwise} \end{cases}$$

$$f_i = \begin{cases} 1 & \text{if taxi goes direct from pickup i to drop off i with just one passenger} \\ 0 & \text{otherwise} \end{cases}$$

Objective:

$$\min z = \sum_{j=1}^n \sum_{i=1}^n d_{p(i)p(j)} x_{ij} + \sum_{j=1}^n \sum_{i=1}^n (d_{p(j)d(i)} + d_{d(i)d(j)}) m_{ij} + \sum_{j=1}^n \sum_{i=1}^n (d_{p(j)d(j)} + d_{d(j)d(i)}) n_{ij} + \sum_{i=1}^n d_{p(i)d(i)} f_i$$

Subject to:

$$(\forall i, j) m_i + n_j = x_{ij}$$

$$(\forall i) \sum_{j \neq i} x_{ij} + \sum_{j \neq i} x_{ji} + f_i = 1$$