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# **Large Firms, Monopsony, and Concentration in the Labor Market**

741 Macroeconomics  
Topic 8

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# Motivation

- We have been talking about firm size...  
... but no firm is really “large” in Hopenhayn-Rogerson – each firm is measure zero

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  - The wage HHI of a local labor market is 0.11-0.35 on average.
    - “Effective” number of firms: 3-9
  - Local labor market: 3-digit NAICS × commuting zone

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    - “Effective” number of firms: 3-9
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- Natural to expect that these firms exploit ***labor market power***
- Today: a model of oligopsony in the labor market

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# **General Equilibrium Oligopsony Model**

- Based on Berger-Mongey-Herkenhoff (2022)**

# Environment

- Static model
- Representative family
  - Continuum of labor markets  $j \in [0,1]$
  - Labor market  $j$  has a fixed number of firms  $i \in \{1,2,\dots,M_j\}$
  - Continuum of workers within a family, choosing where to work  $(i,j)$
- Firms
  - Each firm produces final goods using  $y_{ij} = z_{ij}^{1-\alpha} n_{ij}^\alpha$
- Markets
  - Local labor market: Cournot competition for labor

# Representative Family

- Mass  $L$  of workers within the family
- Each worker  $l \in [0, L]$  has efficiency unit of labor  $\epsilon_{ij}(l)$  when working at  $(i, j)$
- The family solves

$$\max_{C, \{\mathbb{I}_{ij}(l)\}} C$$

$$\text{s.t. } C = \int_0^1 \sum_{i=1}^{M_j} \int_0^L w_{ij} \epsilon_{ij}(l) \mathbb{I}_{ij}(l) dl dj + \Pi$$

- Assume the distribution of  $\epsilon_{ij}(l)$  follow nested Fréchet (GEV)

$$\Pr \left( \{\epsilon_{ij}(l) \leq a_{ij}\}_{ij} \right) = \exp \left[ -G \left( \{a_{ij}\}_{ij} \right) \right], \quad G(\{a_{ij}\}) = \int_0^1 \left( \sum_{i=1}^{M_j} a_{ij}^{-(\eta+1)} \right)^{\frac{\eta+1}{\theta+1}} dj$$

with  $\eta > \theta$

# Representation Result

- The family's problem can be equivalently represented as

$$\begin{aligned} & \max_{C, \{\ell_{ij}\}: \sum_{ij} \ell_{ij} = 1} C \\ \text{s.t. } & C = \int_0^1 \sum_{i=1}^{M_j} w_{ij} \ell_{ij} S_{ij}(\{\ell_{ij}\}) dj \times L + \Pi \\ & \int_0^1 \sum_j \ell_{ij} di = 1 \end{aligned}$$

where

$$S_{ij}(\{\ell_{ij}\}) = \left( \frac{\ell_{ij}}{\sum_i \ell_{ij}} \right)^{-1/(\eta+1)} \left( \sum_i \ell_{ij} \right)^{-1/(\theta+1)}$$

- $\ell_{ij}$ : share of workers working for firm  $i$  in market  $j$
- $S_{ij}$ : average efficiency of workers in  $(i, j)$ , and it captures selection:  
more workers work in  $(i, j) \Rightarrow$  average efficiency of workers worsens
- See Donald-Fukui-Miyauchi (2024) Appendix C for a proof

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FOC:  $w_{ij} [S_{ij} + \ell_{ij} \partial_{\ell_{ij}} S_{ij}] = \lambda$

# Nested CES Labor Supply System

**Solutions:** Given a vector of wages,  $\{w_{ij}\}_{ij}$ ,

- The share of workers who choose to work in  $(i, j)$  is

$$\ell_{ij}(\{w_{ij}\}_{ij}) = \left( \frac{w_{ij}}{\mathbf{w}_j} \right)^{\eta+1} \left( \frac{\mathbf{w}_j}{\mathbf{W}} \right)^{\theta+1}$$

where  $\mathbf{w}_j \equiv \left[ \sum_i w_{ij}^{\eta+1} \right]^{1/(\eta+1)}$ ,  $\mathbf{W} \equiv \left[ \int_0^1 \mathbf{w}_j^{\theta+1} dj \right]^{1/(\theta+1)}$

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- The efficiency units of labor supply for  $(i, j)$  is

$$n_{ij}(\{w_{ij}\}_{ij}) \equiv \ell_{ij} S_{ij}(\{\ell_{ij}\}) L = \left( \frac{w_{ij}}{\mathbf{w}_j} \right)^\eta \left( \frac{\mathbf{w}_j}{\mathbf{W}} \right)^\theta L$$

# Oligopsonistic Labor Market

- The inverse labor supply function is

$$w_{ij}(\{n_{ij}\}) = \left( \frac{n_{ij}}{\mathbf{n}_j} \right)^{\frac{1}{\eta}} \left( \frac{\mathbf{n}_j}{\mathbf{N}} \right)^{\frac{1}{\theta}} \quad (1)$$

$$\mathbf{n}_j \equiv \left[ \sum_i n_{ij}^{\frac{\eta+1}{\eta}} \right]^{\frac{\eta}{\eta+1}}, \quad \mathbf{N} \equiv \left[ \int_0^1 \mathbf{n}_j^{\frac{\theta+1}{\theta}} dj \right]^{\frac{\theta}{\theta+1}}$$

(2)

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- Firms engage in Cournot competition, taking competitor's hiring as given,  $n_{-ij} = n_{-ij}^*$

$$\max_{n_{ij}} z_{ij}^{1-\alpha} n_{ij}^\alpha - w_{ij}(n_{ij}, n_{-ij}^*) n_{ij} \quad (2)$$

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- General solution:

$$w_{ij} = \mu_{ij} \times \alpha z_{ij}^{1-\alpha} n_{ij}^{\alpha-1}, \quad \mu_{ij} \equiv \frac{\varepsilon_{ij}}{\varepsilon_{ij} + 1}, \quad \varepsilon_{ij} \equiv \frac{d \ln n_{ij}}{d \ln w_{ij}}$$

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wage markdown

MPL

# Equilibrium Definition

A (Cournot) equilibrium consists of  $\{w_{ij}(\{n_{ij}\}), n_{ij}\}$  such that

- $w_{ij}(\{n_{ij}\})$  is consistent with household's optimality (1)
- Taking  $\{n_{-ij}\}$  as given, firm  $i$  solves (2)

# Wage Markdown

- With our functional form assumption, the labor supply elasticity takes the form of

$$\varepsilon_{ij}(s_{ij}) = \left[ \frac{1}{\eta} (1 - s_{ij}) + \frac{1}{\theta} s_{ij} \right]^{-1}, \quad \mu_{ij}(s_{ij}) = \frac{\varepsilon_{ij}(s_{ij})}{\varepsilon_{ij}(s_{ij}) + 1}$$

where

$$s_{ij} = \frac{w_{ij} n_{ij}}{\sum_k w_{kj} n_{kj}} \tag{3}$$

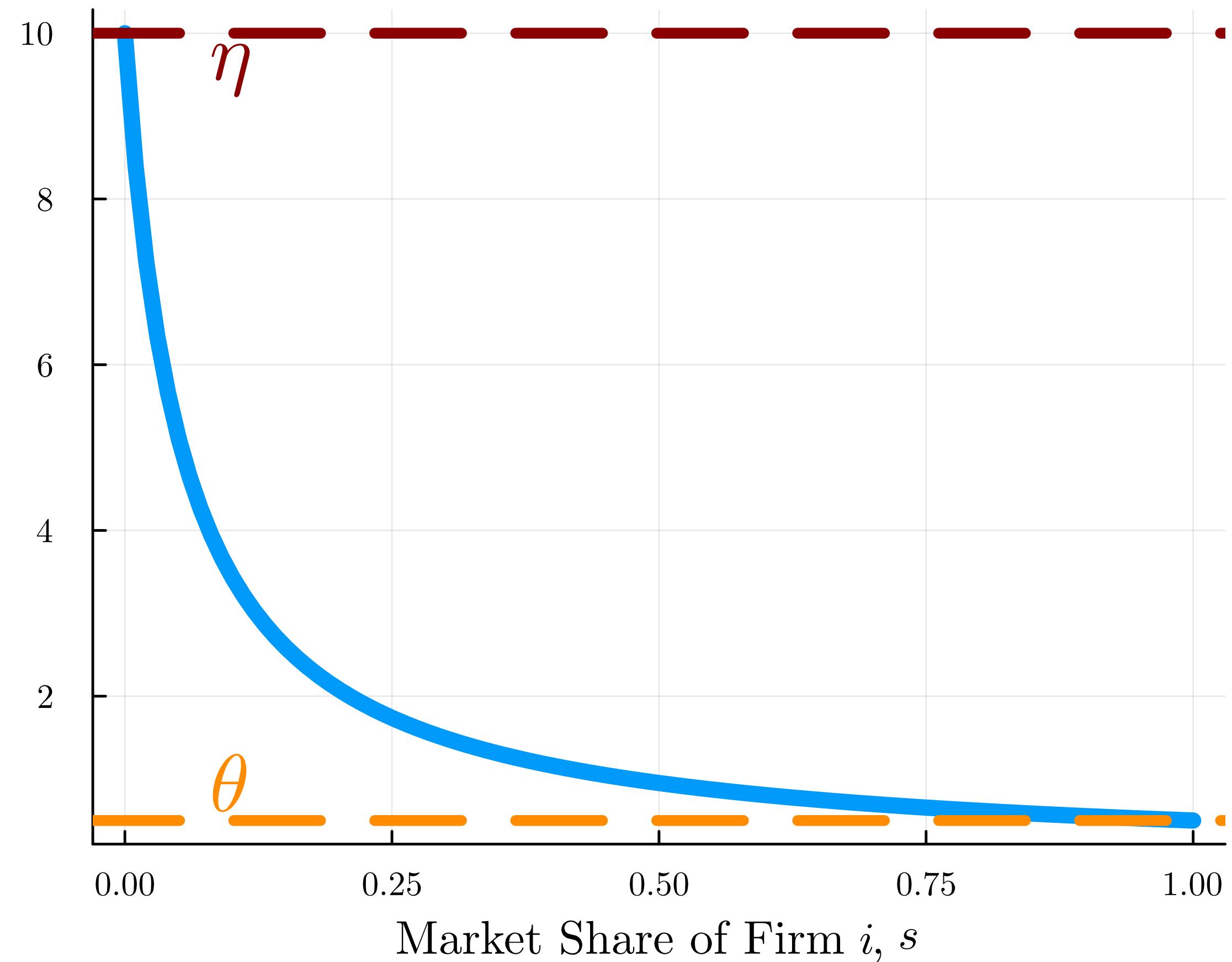
is the labor market share of firm  $i$  in market  $j$

- Competitive labor market:  $\theta, \eta \rightarrow \infty \Rightarrow \varepsilon_{ij} \rightarrow \infty$
- Monopsonistic competition within a market  $j$ :  $M_j \rightarrow \infty \Rightarrow s_{ij} \rightarrow 0 \Rightarrow \varepsilon_{ij} \rightarrow \eta$
- Monopsony within a market  $j$ :  $s_{ij} \rightarrow 1 \Rightarrow \varepsilon_{ij} \rightarrow \theta$

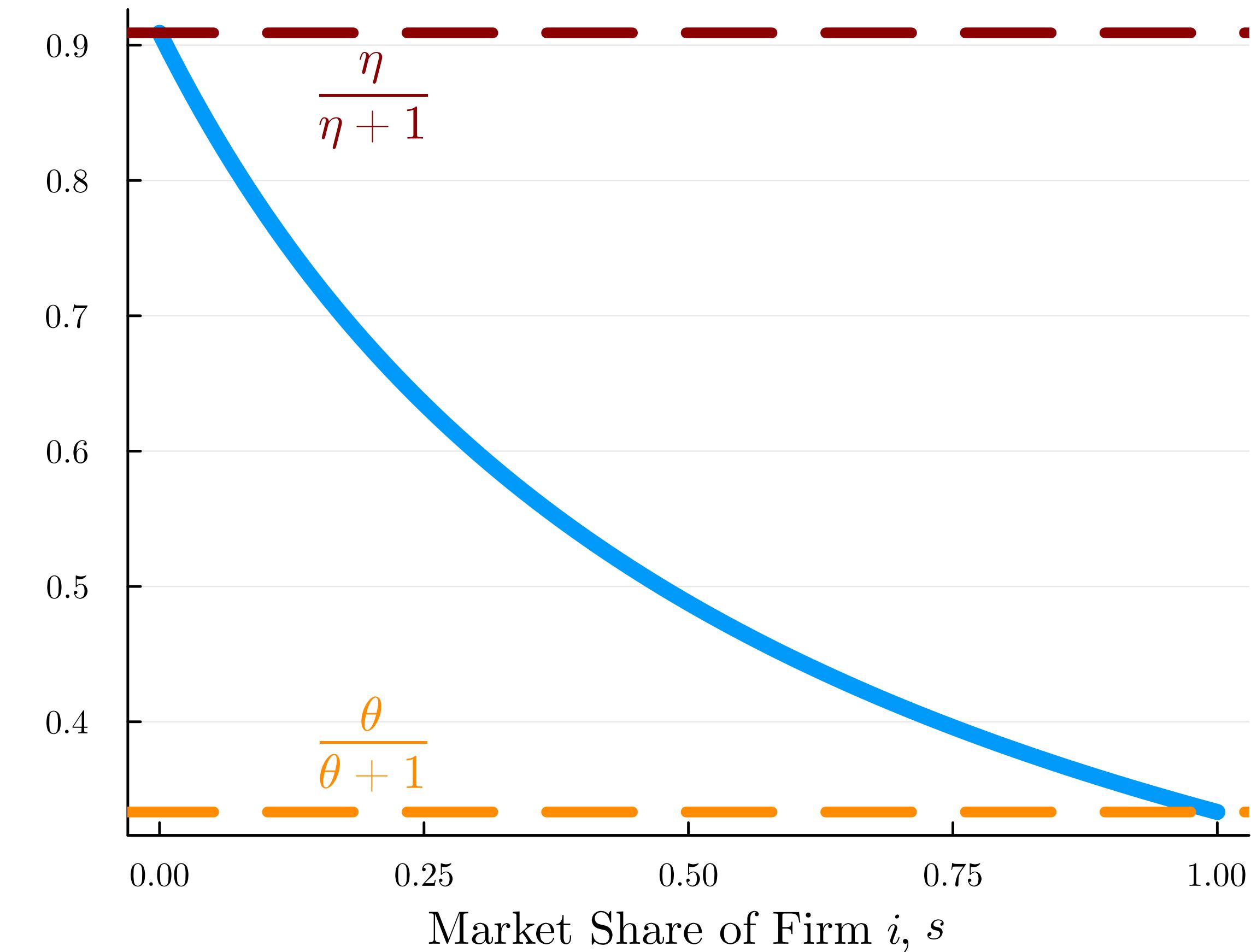
- See also Atkeson-Burstein (2008)

# Numerical Illustration

Labor Supply Elasticity of Firm  $i$ ,  $\varepsilon$



Wage Markdown of Firm  $i$ ,  $\mu$



# Equilibrium System

The equilibrium  $\{s_{ij}\}$  solve

$$s_{ij} = \frac{\left(\mu_{ij}(s_{ij})z_{ij}^{1-\alpha}\right)^{\frac{1+\eta}{1+\eta(1-\alpha)}}}{\sum_k \left(\mu_{kj}(s_{kj})z_{kj}^{1-\alpha}\right)^{\frac{1+\eta}{1+\eta(1-\alpha)}}}$$

- Proof: Relative employment between  $i$  and  $k$ :

$$\frac{n_{ij}}{n_{kj}} = \left(\frac{w_{ij}}{w_{kj}}\right)^\eta = \left(\frac{\mu_{ij}(s_{ij})z_{ij}^{1-\alpha}n_{ij}^{\alpha-1}}{\mu_{kj}(s_{kj})z_{kj}^{1-\alpha}n_{kj}^{\alpha-1}}\right)^\eta \quad \Leftrightarrow \quad \frac{n_{ij}}{n_{kj}} = \left(\frac{\mu_{ij}(s_{ij})z_{ij}^{1-\alpha}}{\mu_{kj}(s_{kj})z_{kj}^{1-\alpha}}\right)^{\frac{\eta}{1+\eta(1-\alpha)}}$$

- Substituting into (3) gives the expression
- Given  $\{s_{ij}\}$ , we can immediately compute  $\{\mu_{ij}, n_{ij}, w_{ij}\}$

# Sufficient Statistics for Labor Share

- Define the aggregate labor share as

$$LS = \frac{\int_0^1 \sum_{i \in j} w_{ij} n_{ij} dj}{\int_0^1 \sum_{i \in j} y_{ij} dj}$$

- Define the payroll weighted HHI as

$$HHI = \int_0^1 s_j HHI_j dj, \quad s_j = \frac{\sum_{i \in j} w_{ij} n_{ij}}{\int_0^1 \sum_{i \in j} w_{ij} n_{ij} dj}, \quad HHI_j = \sum_{i \in j} s_{ij}^2$$

- Result:

$$LS = \alpha \left[ (1 - HHI) \left( \frac{\eta}{\eta + 1} \right)^{-1} + HHI \left( \frac{\theta}{\theta + 1} \right)^{-1} \right]^{-1}$$

⇒ Conditional on the knowledge of  $(\alpha, \theta, \eta)$ , payroll shares are sufficient to infer  $LS$

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# Planning Problem

# Planning Problem

- The planner maximizes total consumption subject to the resource constraints:

$$\max_{\{n_{ij}, \ell_{ij}\}} \int_0^1 \sum_i z_{ij}^{1-\alpha} n_{ij}^\alpha dj$$

$$\text{s.t. } n_{ij} = \ell_{ij} S_{ij}(\{\ell_{ij}\}) L$$

$$\int_0^1 \sum_j \ell_{ij} di = 1$$

- The FOC is

$$\alpha z_{ij}^{1-\alpha} n_{ij}^{\alpha-1} \left[ S_{ij} + \ell_{ij} \partial_{\ell_{ij}} S_{ij} \right] = \lambda$$

# Equilibrium vs. Planner

Planner:

$$\alpha z_{ij}^{1-\alpha} n_{ij}^{\alpha-1} \left[ S_{ij} + \ell_{ij} \partial_{\ell_{ij}} S_{ij} \right] = \lambda$$

Equilibrium:

$$\mu_{ij} \alpha z_{ij}^{1-\alpha} n_{ij}^{\alpha-1} \left[ S_{ij} + \ell_{ij} \partial_{\ell_{ij}} S_{ij} \right] = \lambda$$

- Is the equilibrium efficient? – No, as long as  $\{\mu_{ij}\}$  vary in equilibrium
  - If  $\mu_{ij} = \mu$  for all  $i, j$ , then  $\mu$  is indistinguishable from  $\lambda$
- In what way?
  - Firms with low  $\mu_{ij}$  (high labor market power) are too small in eqm!
  - Firms with high  $\mu_{ij}$  (low labor market power) are too large in eqm!
- Minimum wage reallocates workers from high  $\mu_{ij}$  to low  $\mu_{ij}$   
⇒ can improve efficiency (but Berger-Herkenhoff-Mongey (2025) say it's small)

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# Bringing the Model to the Data

# Identification

- Key parameters:  $(\theta, \eta)$
- Labor supply equation with potential labor supply shifter  $\xi_{ij}$

$$n_{ij}(\{w_{ij}\}_{ij}) = \xi_{ij} \left( \frac{w_{ij}}{\mathbf{w}_j} \right)^\eta \left( \frac{\mathbf{w}_j}{\mathbf{W}} \right)^\theta L$$

- Taking log,

$$\log n_{ij} = \eta \log(w_{ij}) + (\theta - \eta) \log \mathbf{w}_j - \theta \log \mathbf{W} + \log L + \log \xi_{ij}$$

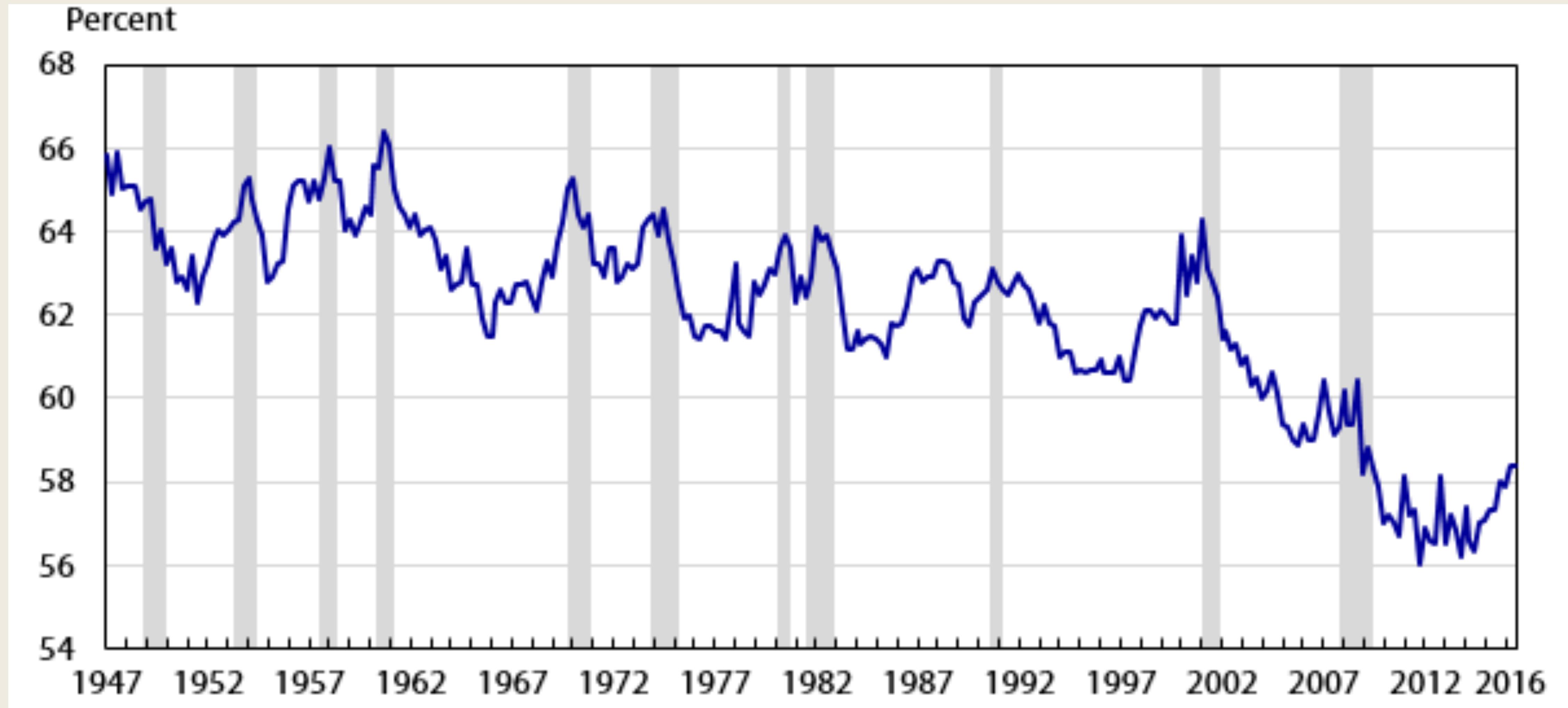
- With suitable instruments (labor demand shifter), one can identify  $(\theta, \eta)$ 
  1. Berger-Mongey-Herkenhoff (2021): changes in state corporate taxes
  2. Felix (2023): changes in tariffs

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# Estimation Results

- BHM's implementation: US Census LBD data
- Market: 3-digit NAICS  $\times$  commuting zone
- Estimates:  $\eta = 10.85, \theta = 0.42$
- With  $HHI = 0.11$  in 2014, the model implies **30%** aggregate wage markdown

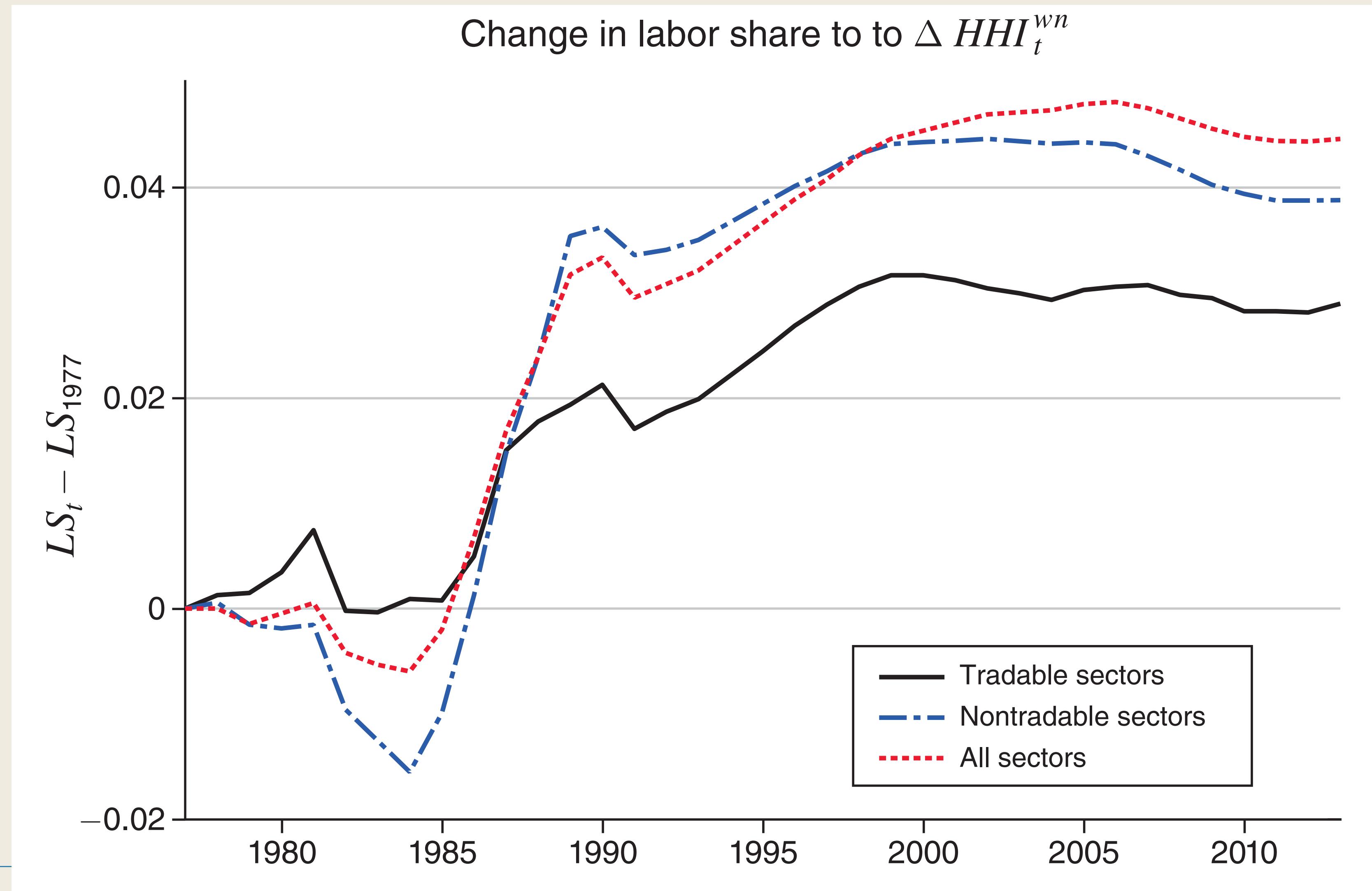
# Labor Share



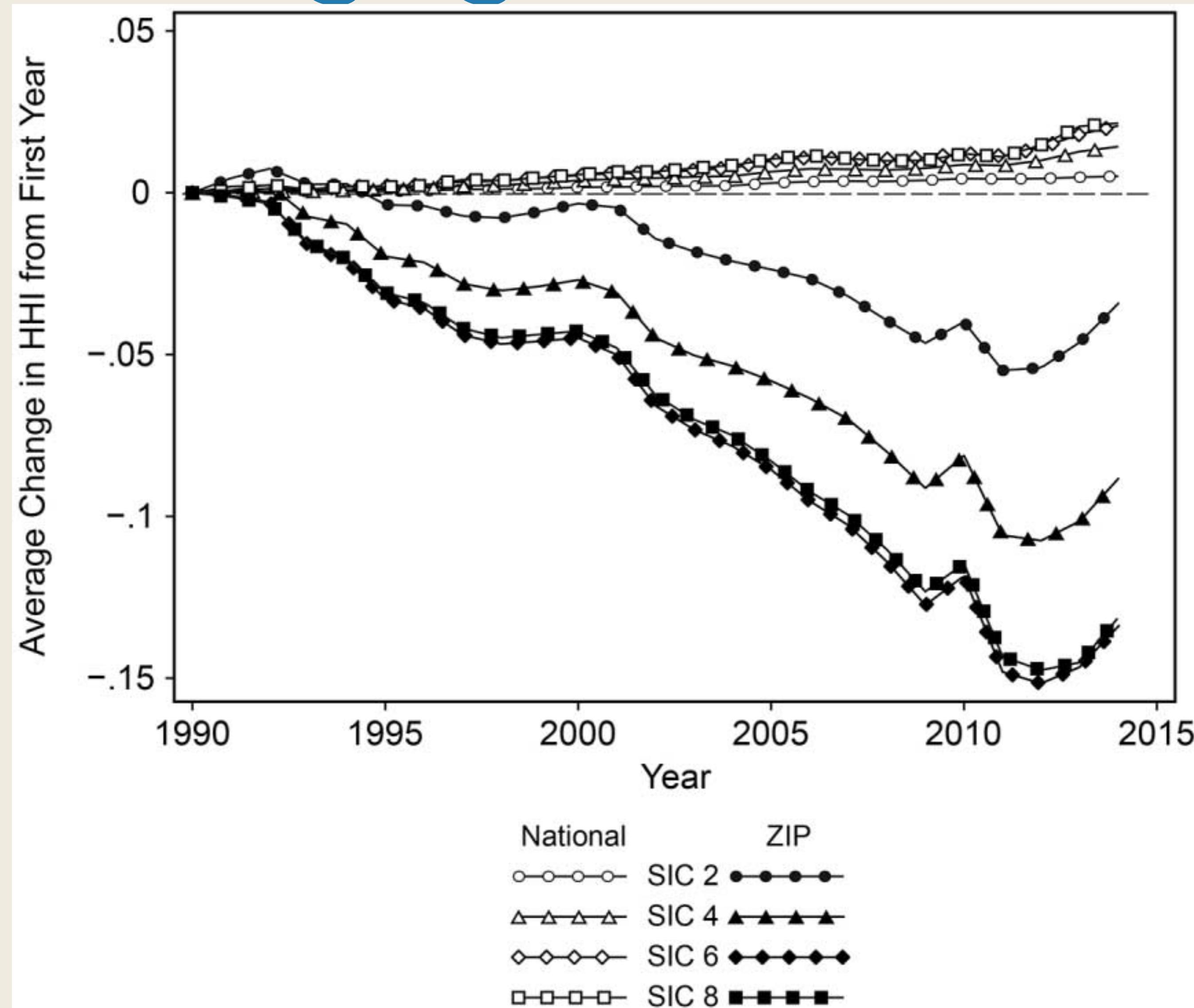
- Can the changes in concentration explain the changes in labor share?

# Labor Share Increases due to $\Delta HHI$

- Fix  $(\eta, \theta, \alpha)$  and feed the changes in HHI over time



# Diverging Trends in HHI

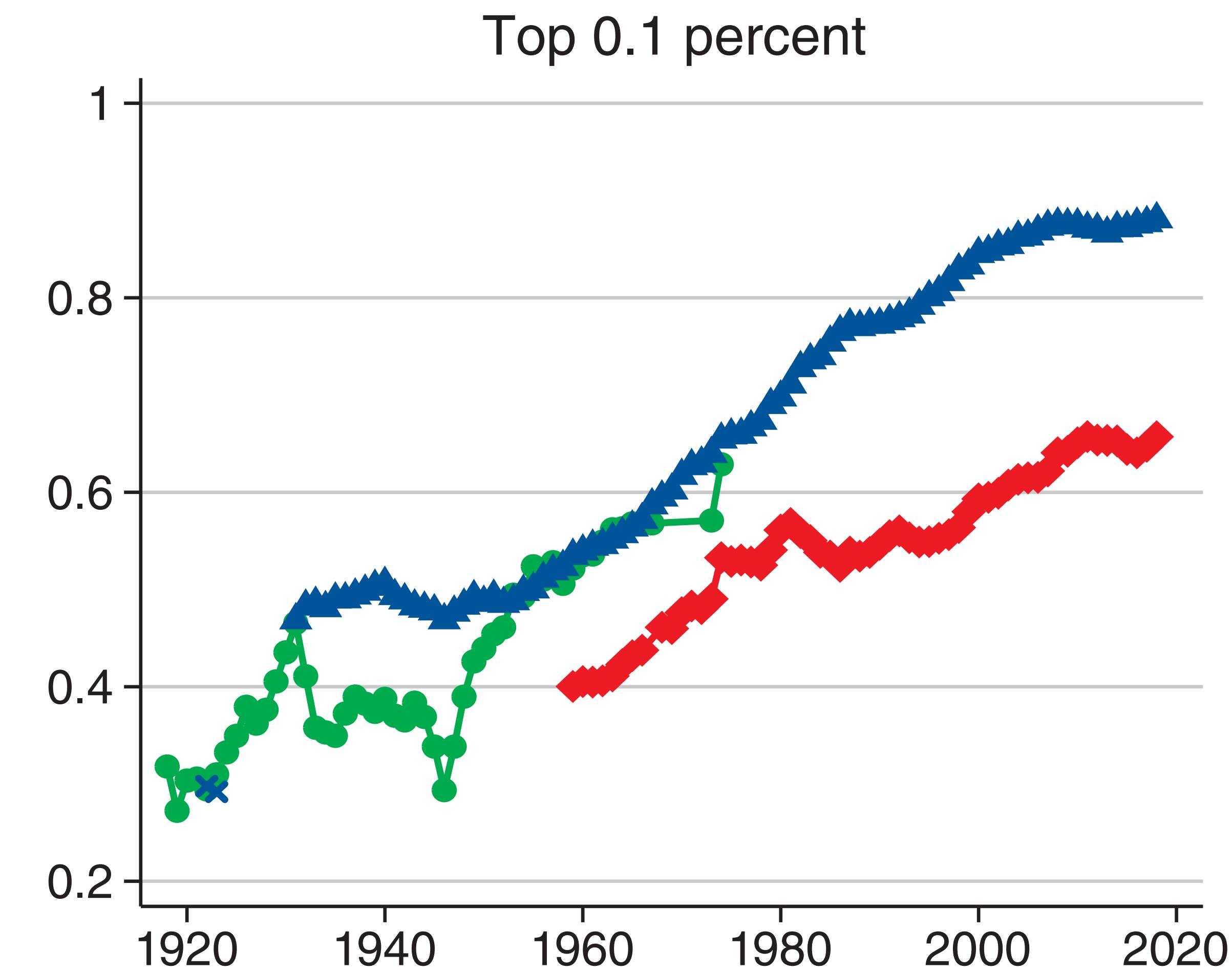
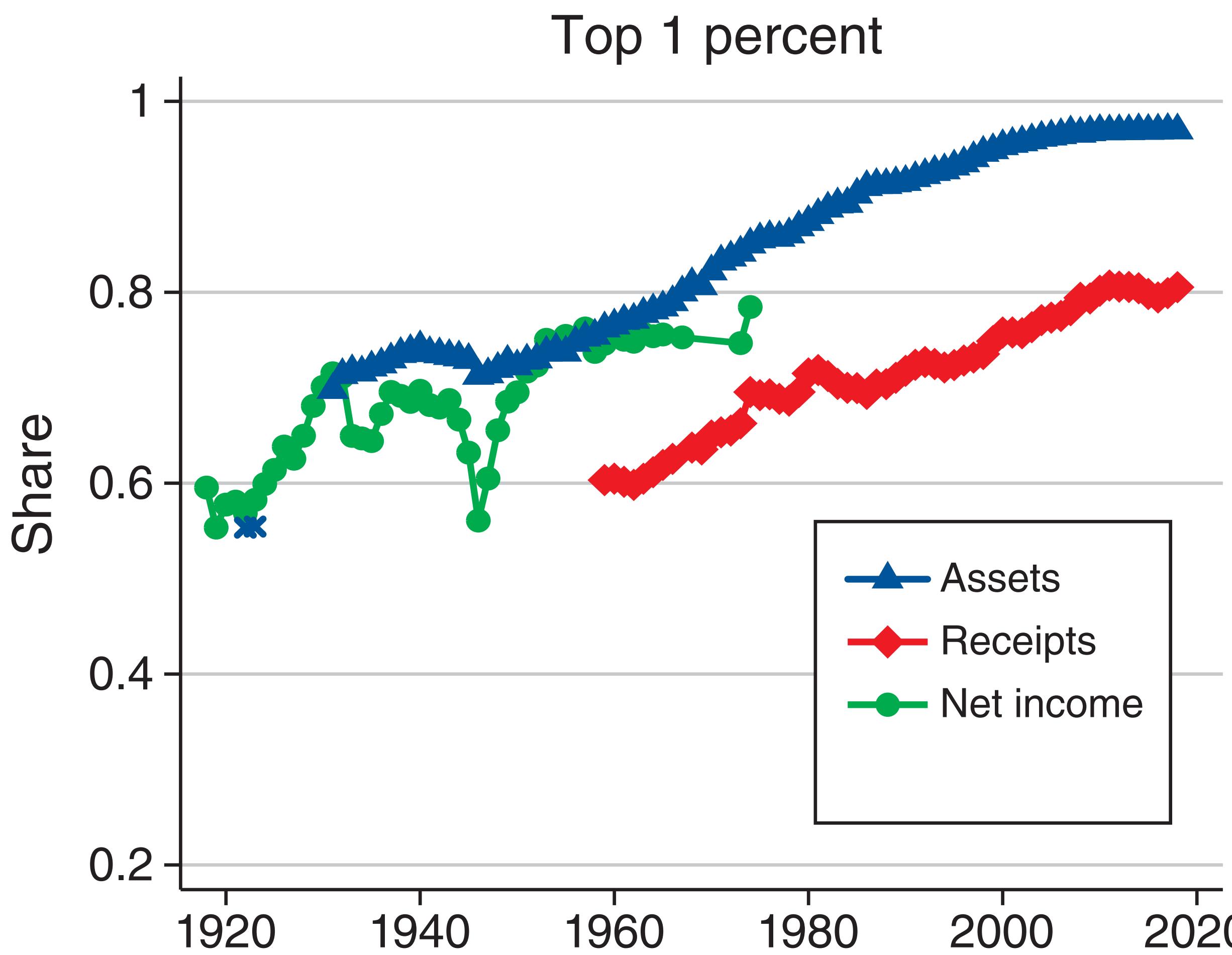


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# The Rise of Large Firms

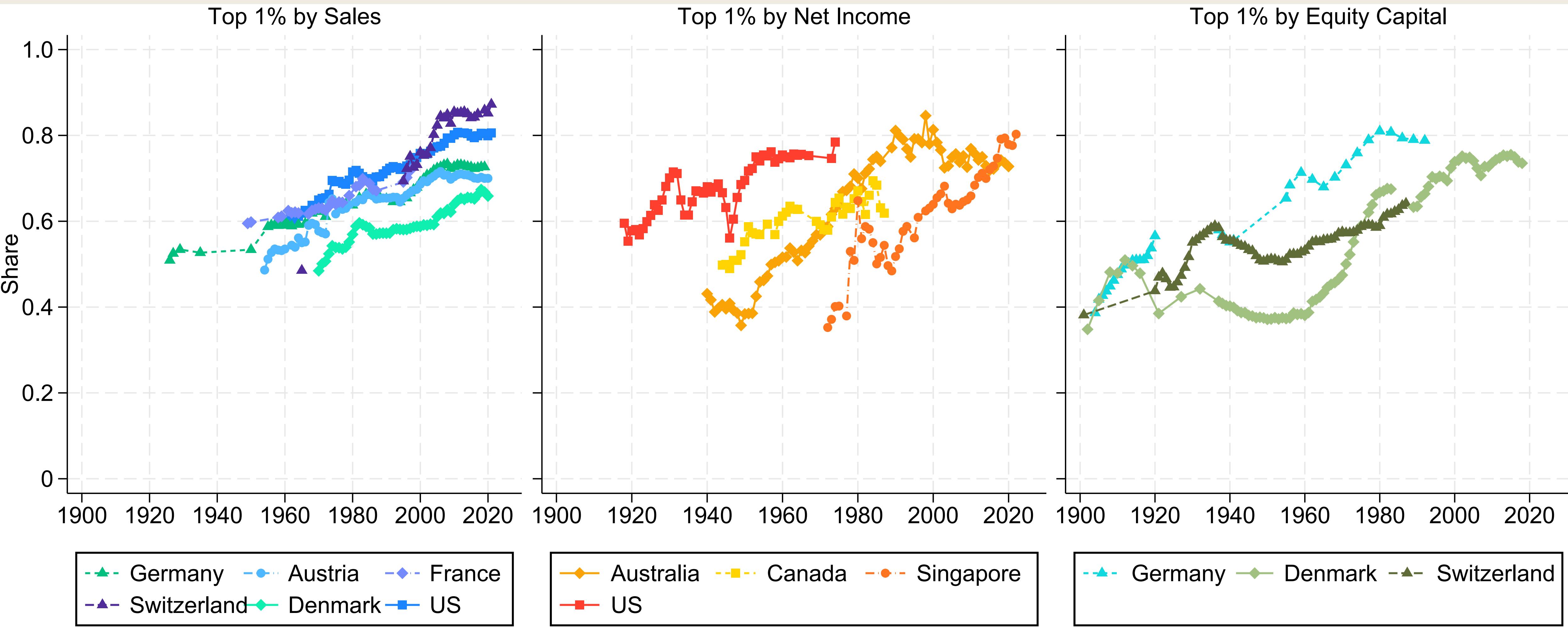
– Ma, Zhang, and Zimmermann (2025)

# 100 Years of Rising Concentration in the US



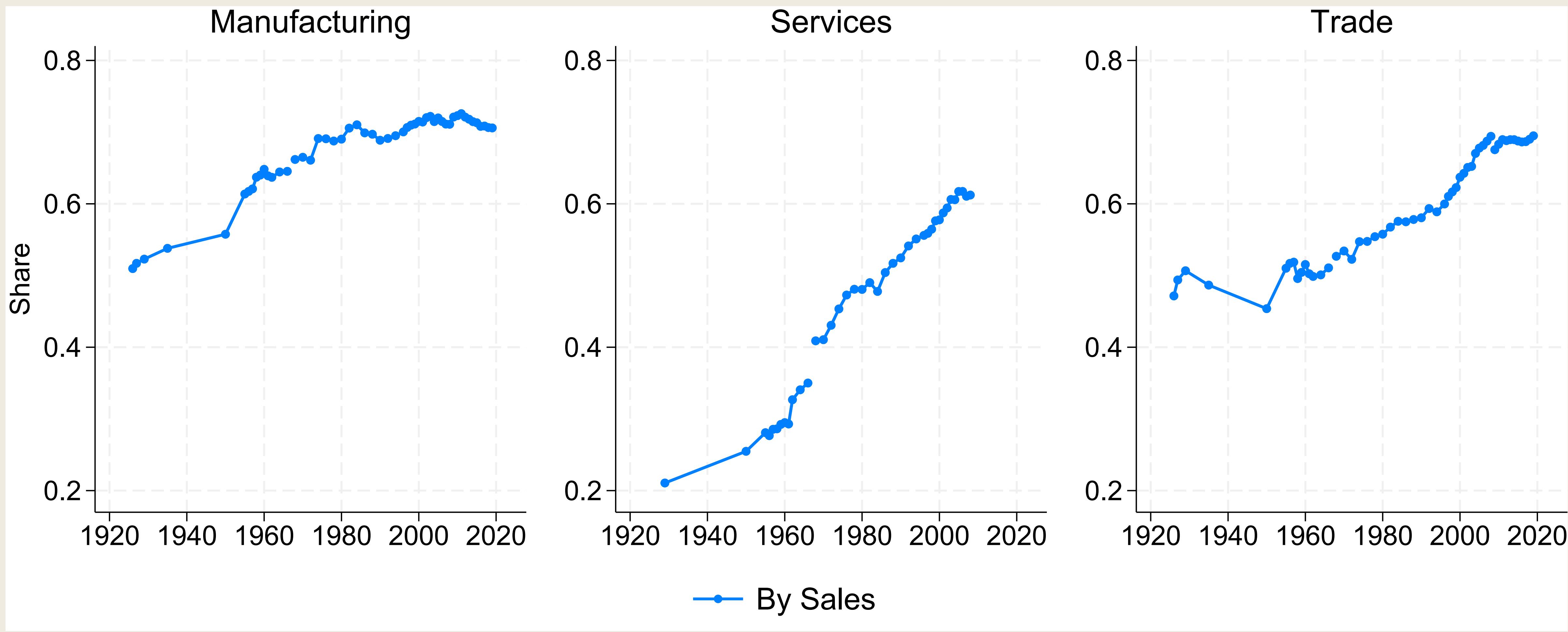
Source: Kwon, Ma, & Zimmermann (2024)

# Top 1% Share in the World

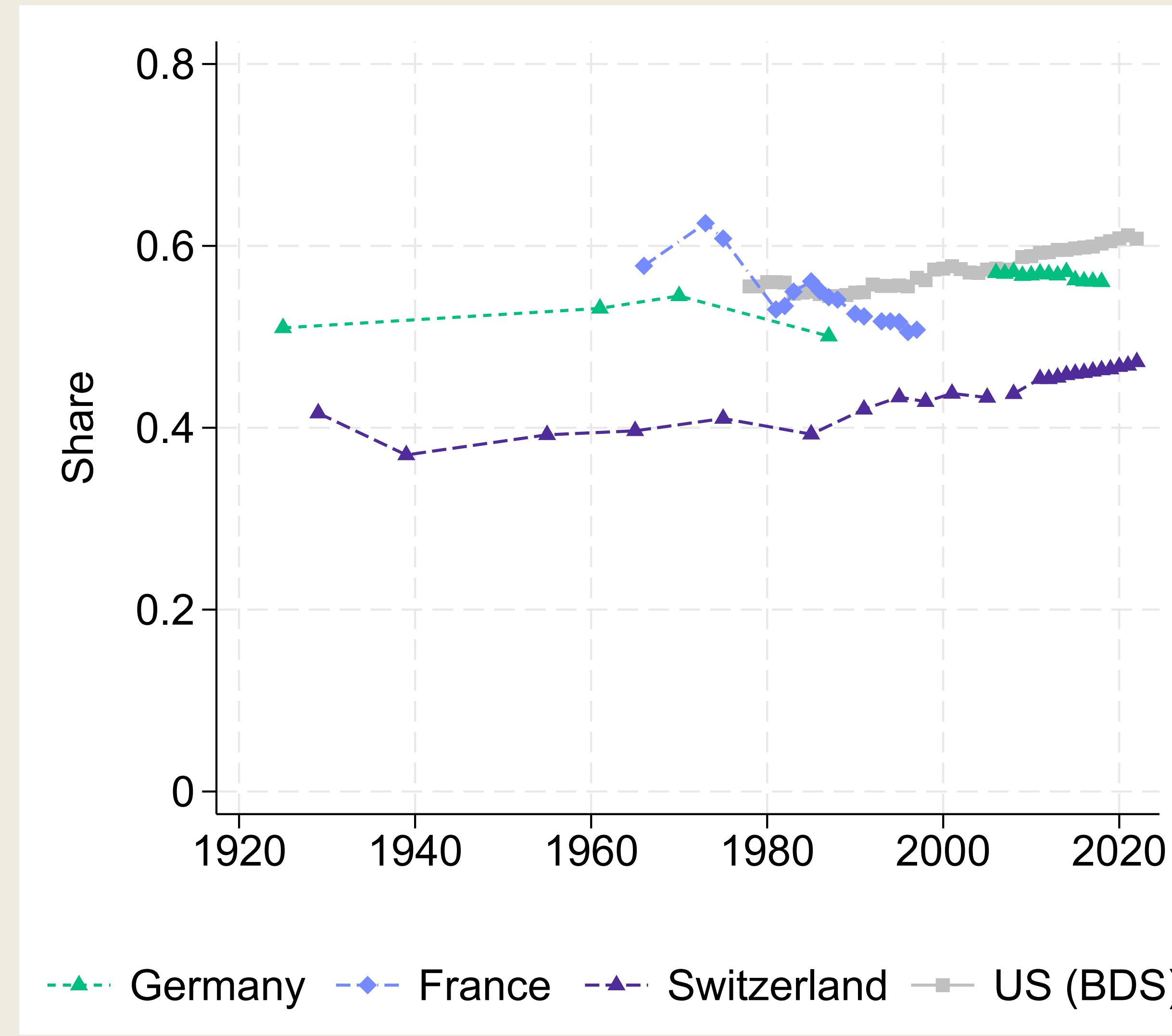


# Top 1% Sales Share by Sectors

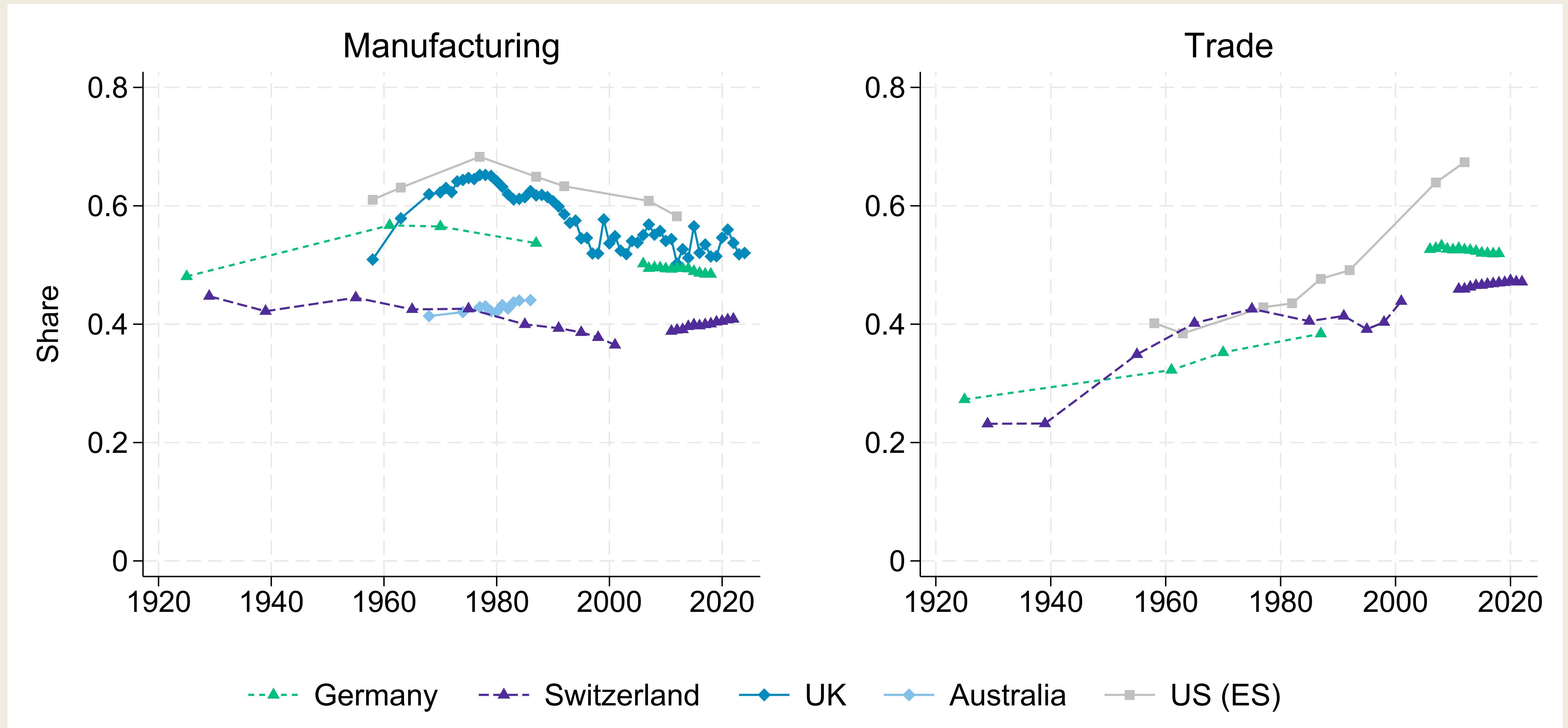
Panel A. Top 1% Share



# Top 1% Employment Share Has Been Stable

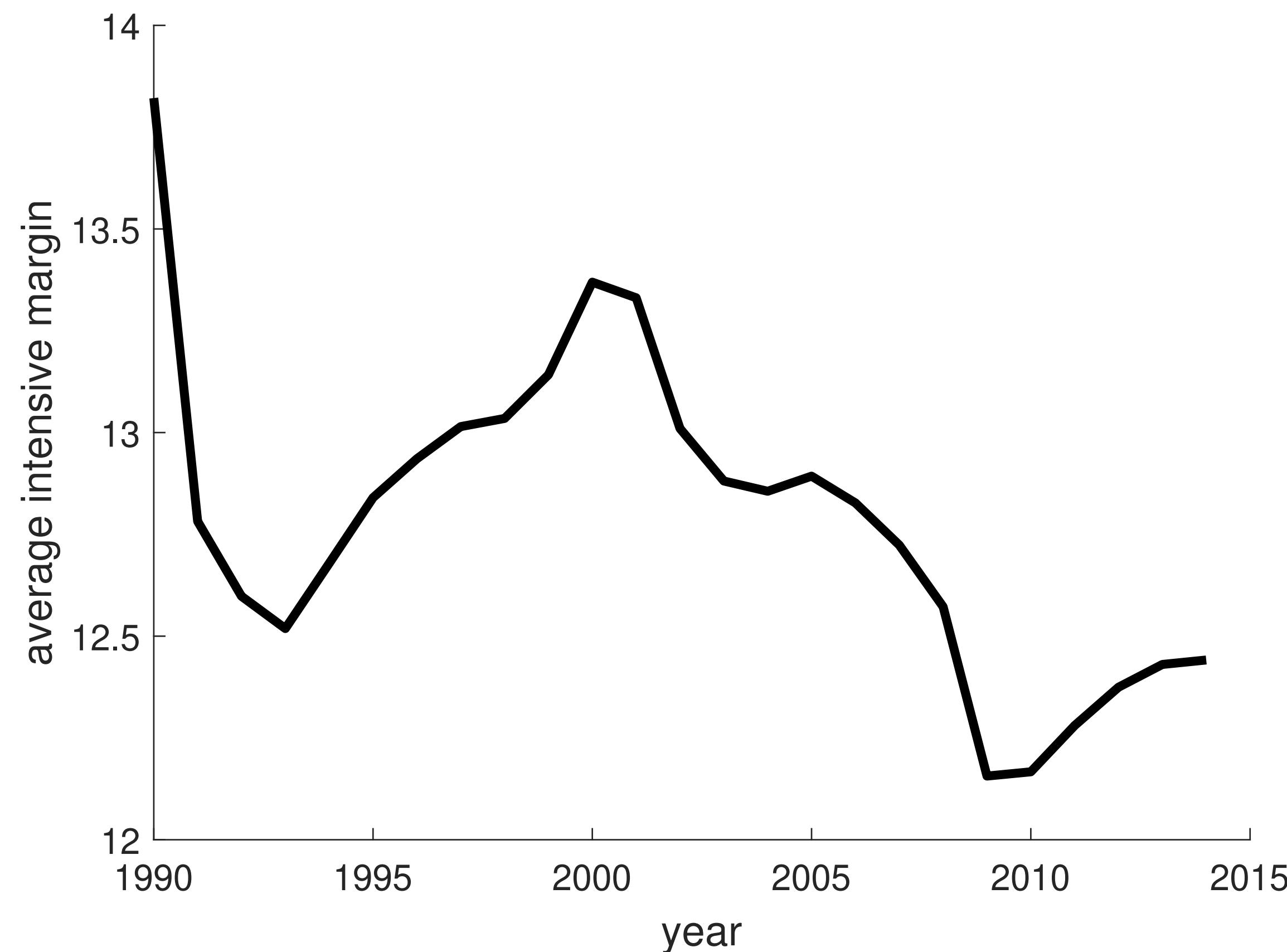


# Top 1% Emp. Share in Manufacturing & Trade

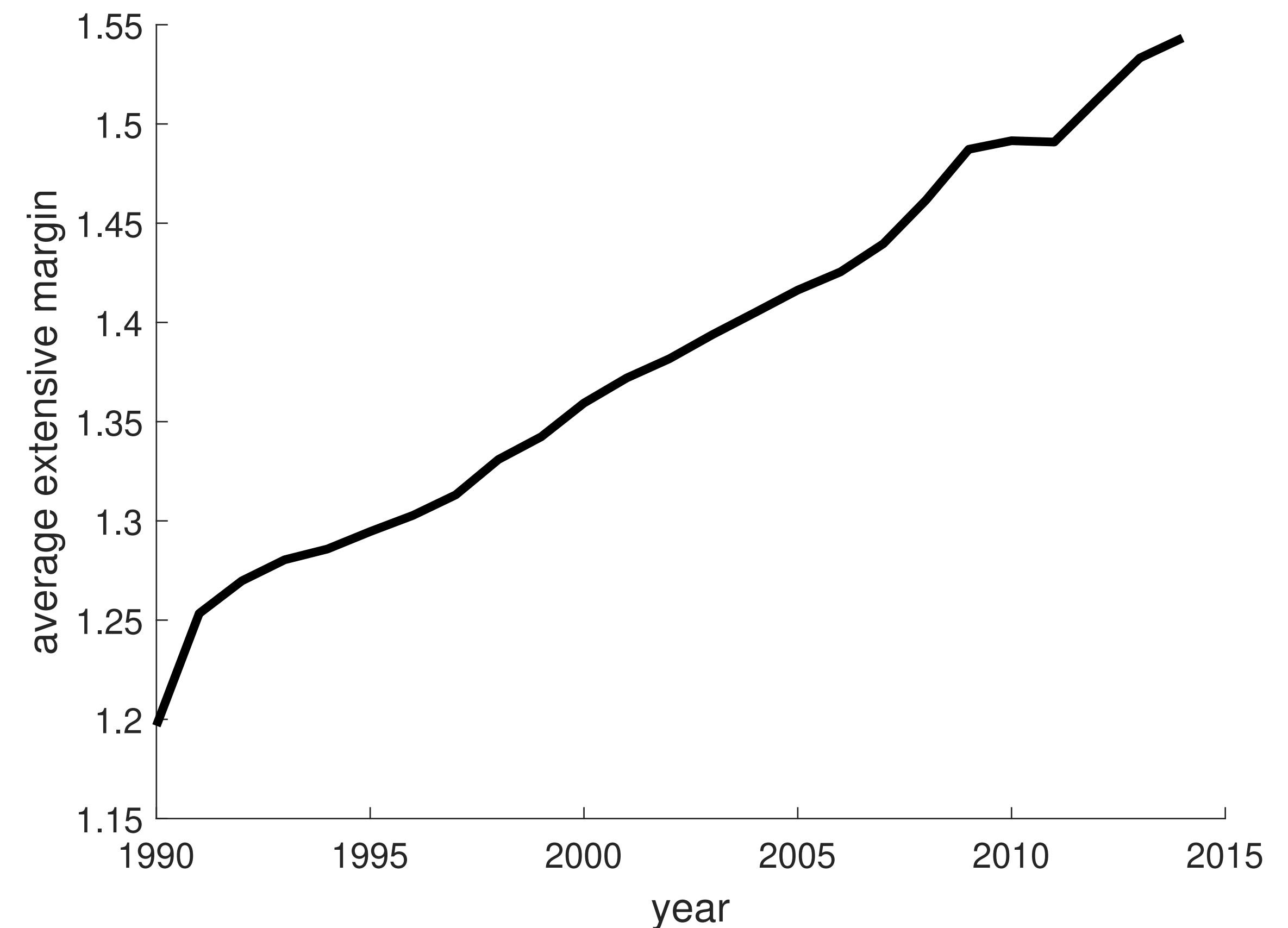


# Firm Growth Through Establishments

Average size of establishment



Number of establishments



Source: Cao, Hayyatt, Mukoyama, Sager (2022)

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# Wrapping Up

1. Problem set 2 is due Dec 21
2. I also look forward to reading your research proposal!