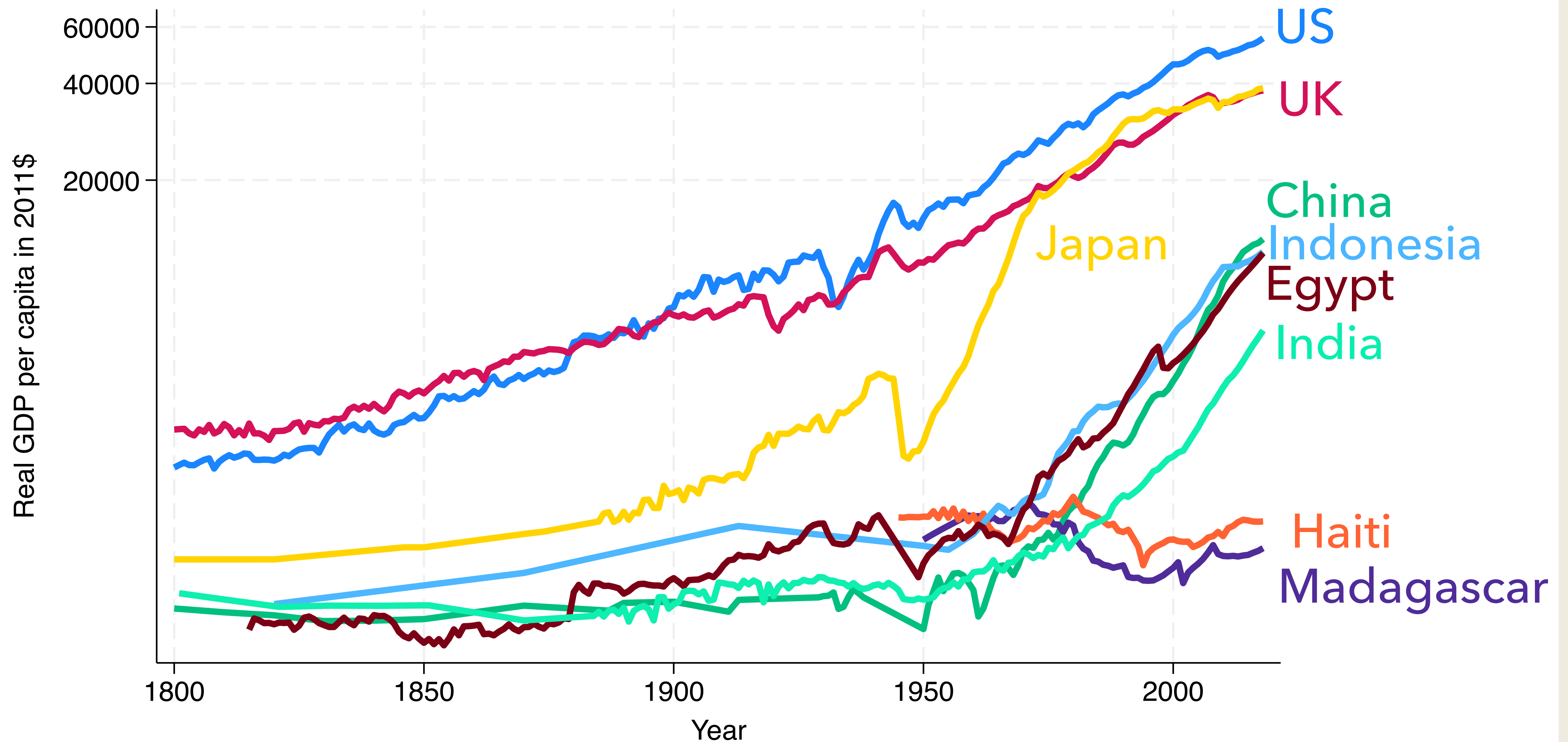

Development and Growth Accounting

EC502 Macroeconomics
Topic 1

Masao Fukui

2024 Spring

Why are Some Countries Richer than Others?



Source: Madison project

Cross-Country Income Differences

- United States today are
 1. 5 times richer than people in China
 2. 10 times richer than people in India
 3. more than 40 times richer than people in Haiti

- What drives these enormous differences in standards of living across countries?

Role of Models

All theory depends on assumptions which are not quite true. That is what makes it theory. The art of successful theorizing is to make the inevitable simplifying assumptions in such a way that the final results are not very sensitive.

—Robert Solow

Production Function

- Suppose the output of a country is produced using
 1. Labor, L
 2. Physical capital (machines, building, etc), K
- A production function tells us how much we can produce output given L and K :

$$Y = F(K, L)$$

- We say $F(K, L)$ features
 - constant returns to scale if $F(\lambda L, \lambda K) = \lambda F(L, K)$
 - decreasing returns to scale if $F(\lambda L, \lambda K) < \lambda F(L, K)$
 - increasing returns to scale if $F(\lambda L, \lambda K) > \lambda F(L, K)$

Cobb-Douglas Production Function

- A popular functional form is Cobb-Douglas production function

$$Y = F(K, L) = AK^{\alpha}L^{\beta}$$

- A : the level of technology
 - $\alpha, \beta \in [0,1]$: importance of each factor
- Using the previous definition,
 - $\alpha + \beta = 1 \Rightarrow$ constant returns to scale
 - $\alpha + \beta < 1 \Rightarrow$ decreasing returns to scale
 - $\alpha + \beta > 1 \Rightarrow$ increasing returns to scale
 - We will assume constant returns to scale. Why?
Replication argument: If all the inputs double, output should double

Important Distinction

$$F(K, L) = AK^\alpha L^{1-\alpha}$$

- Here, $F(K, L)$ is constant returns to scale to all inputs
- But, $F(K, L)$ features diminishing returns to a particular input

- If we only double K , output less than doubles:

$$F(2K, L) = 2^\alpha F(K, L) < 2F(K, L)$$

- Equivalently, $F(K, L)$ is concave in both arguments:

$$F_{KK}(K, L) < 0, \quad F_{LL}(K, L) < 0$$

Development Accounting

Decomposing GDP per Capita

$$Y_i = A_i K_i^\alpha L_i^{1-\alpha}$$

- i : country
- Divide both sides by population size, N_i , and taking log:

$$\log(Y_i/N_i) = \log A_i + \alpha \log(K_i/N_i) + (1 - \alpha) \log(L_i/N_i)$$

Decomposing GDP per Capita

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- How much of differences in GDP per capita due to
 1. capital
 2. labor
 3. technology (which we don't directly observe)

Development Accounting

$$\log(Y_i/N_i) = \log A_i + \alpha \log(K_i/N_i) + (1 - \alpha)\log(L_i/N_i)$$

- This exercise called **development accounting**
 - It is accounting because we do not theorize how each component is determined
- Nevertheless, it helps us to guide what theoretical model we should write down
- In order to implement development accounting, we need to take a stand on α
- What value should we use for α ?

Factor Shares

- Factor shares: what fraction of GDP is paid to each factor?
- Suppose firms need pay w to hire workers and r to rent machines
- Firms take (w, r) as given (competitive market) and choose (L, K) :

$$\max_{K,L} AK^\alpha L^{1-\alpha} - wL - rK$$

Taking the first-order condition with respect to L

$$(1 - \alpha)AK^\alpha L^{-\alpha} = w \tag{1}$$

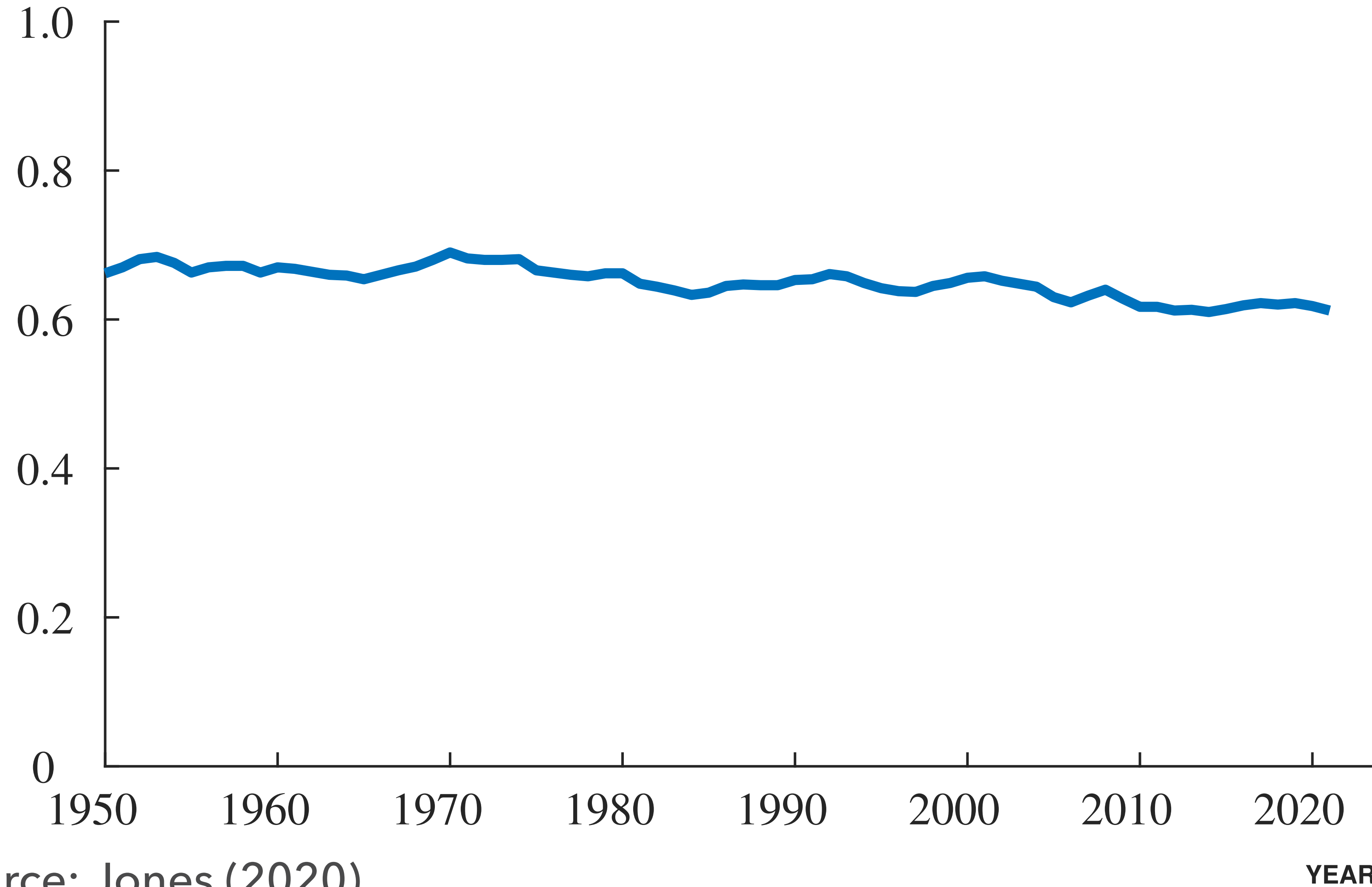
The firm equalizes the marginal product of labor to wages

- Multiplying both sides of (1) by L ,

$$\frac{wL}{Y} = (1 - \alpha) \Rightarrow \text{Labor share of GDP is } 1 - \alpha$$

Stable Labor Share

LABOR SHARE OF GDP



Source: Jones (2020)

Technology as Residual

- Labor share $\approx 2/3$ and stable over time, so we assume $\alpha = 1/3$
- With the assumed value of α , we can construct a measure of “technology”

$$\log A_i = \log(Y_i/N_i) - \alpha \log(K_i/N_i) - (1 - \alpha)\log(L_i/N_i)$$

- Also referred to as “total factor productivity (TFP)” or “Solow residual”
- $\log A_i$ captures differences in GDP not captured by K/N or L/N
- Measure of our ignorance

First Look at the Data 2019

	Y/N	K/N	L/N	A
U.S.	100	100	100	100
China	22	33	116	30
India	10	12	76	26
Haiti	2.5	7	84	7

Data: Penn World Table 2019

- Large differences in K/N and A
- Little difference in L/N (employment per person)

Variance Decomposition

- We can explore more systematically

$$\begin{aligned}\text{Var}(\log Y_i/N_i) &= \text{Cov}(\log(Y_i/N_i), \alpha \log K_i/N_i) && \text{Variance in GDP due to } K/N \\ &+ \text{Cov}(\log Y_i/N_i, (1 - \alpha) \log L_i/N_i) && \text{Variance in GDP due to } L/N \\ &+ \text{Cov}(\log Y_i/N_i, \log A_i) && \text{Variance in GDP due to } A\end{aligned}$$

- Therefore, $\frac{\text{Cov}(\log Y_i/N_i, \log X_i)}{\text{Var}(\log Y_i/N_i)}$ corresponds to the share explained by a factor X

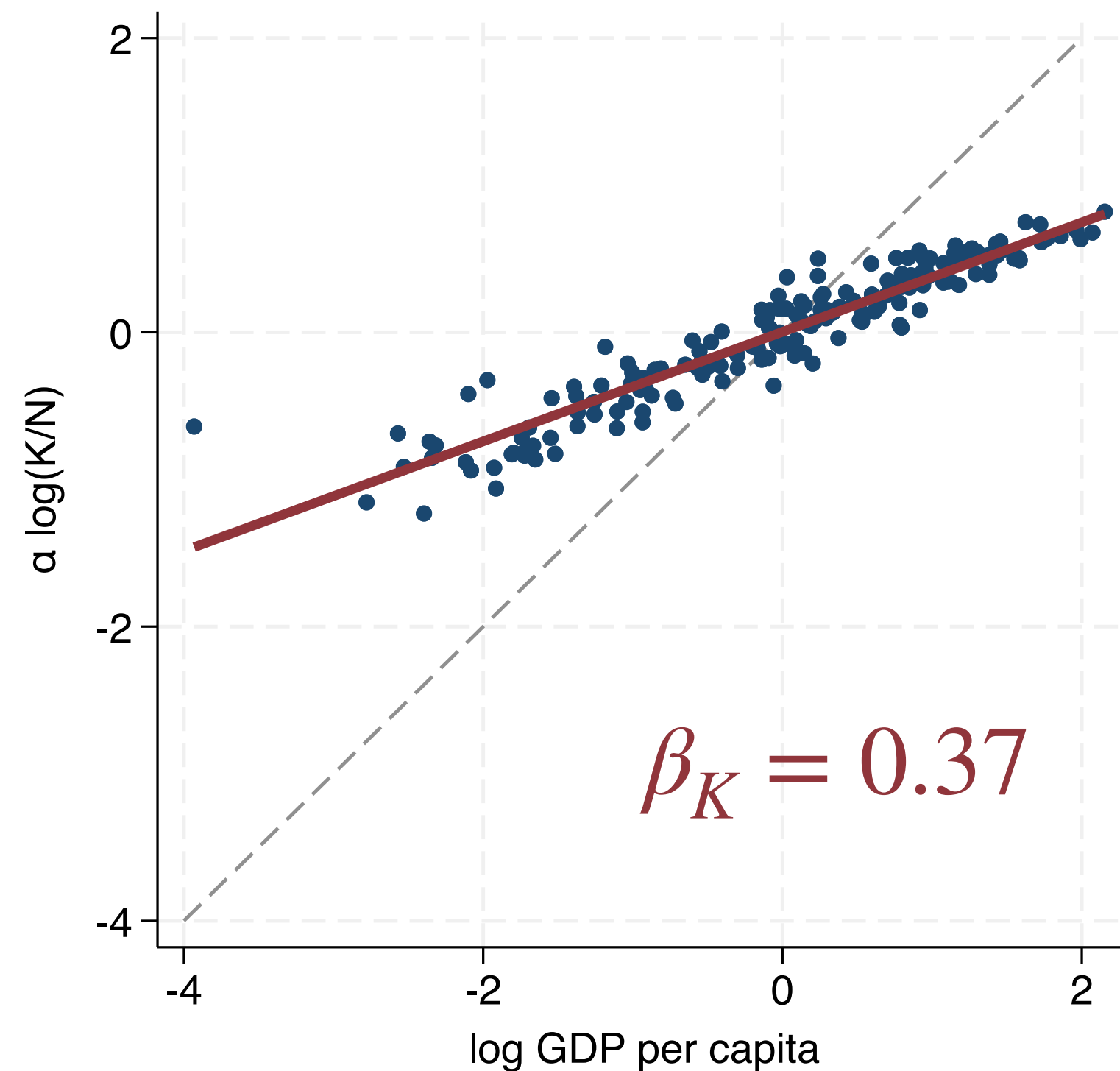
- This can be obtained as a regression coefficient β_X of

$$\log X_i = \beta_X \log(Y_i/N_i) + \gamma + \epsilon_i$$

If $\beta_X = 1$, differences in GDP per capita entirely due to X

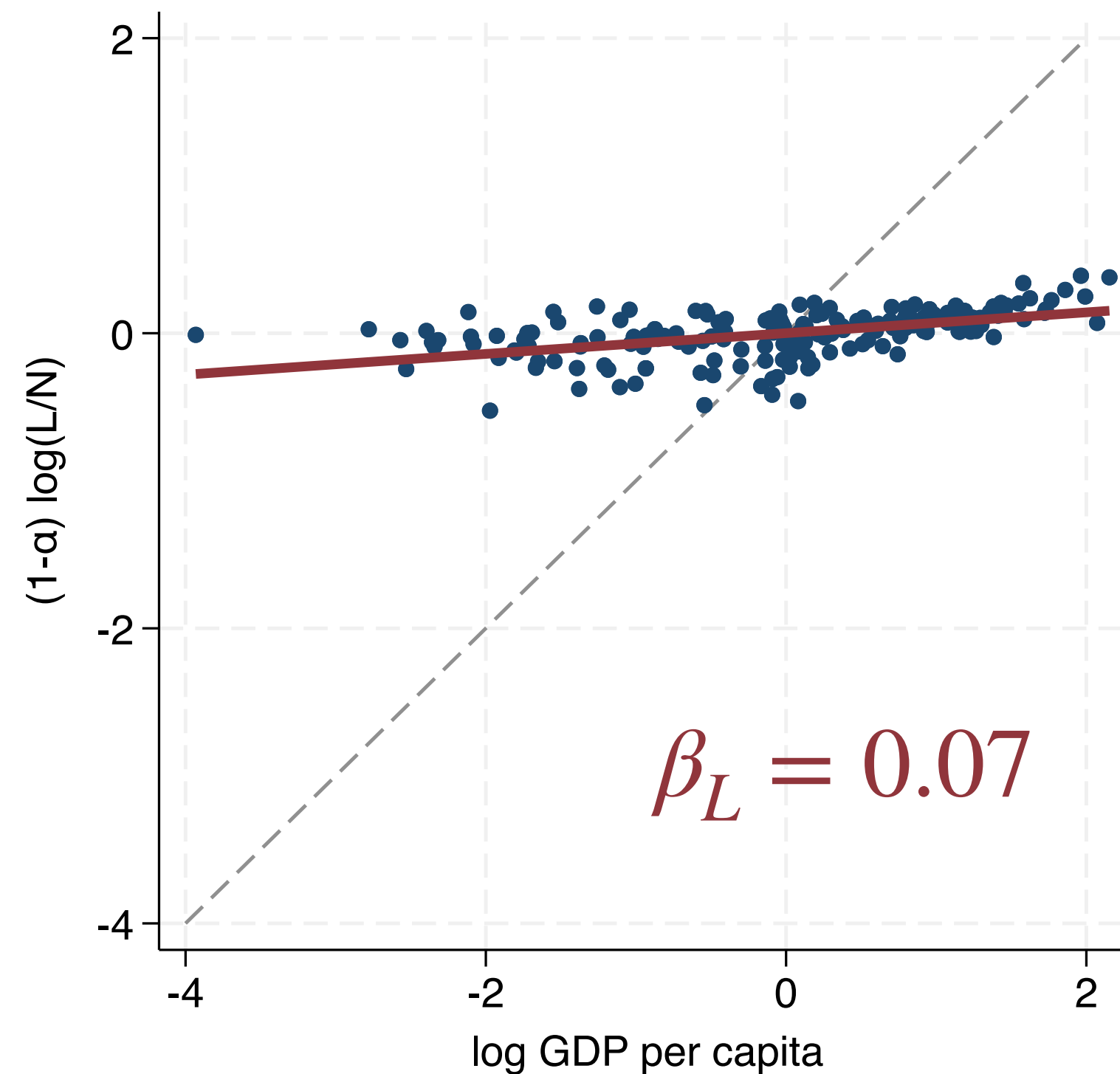
Development Accounting 2019

$\alpha \log(K/N)$



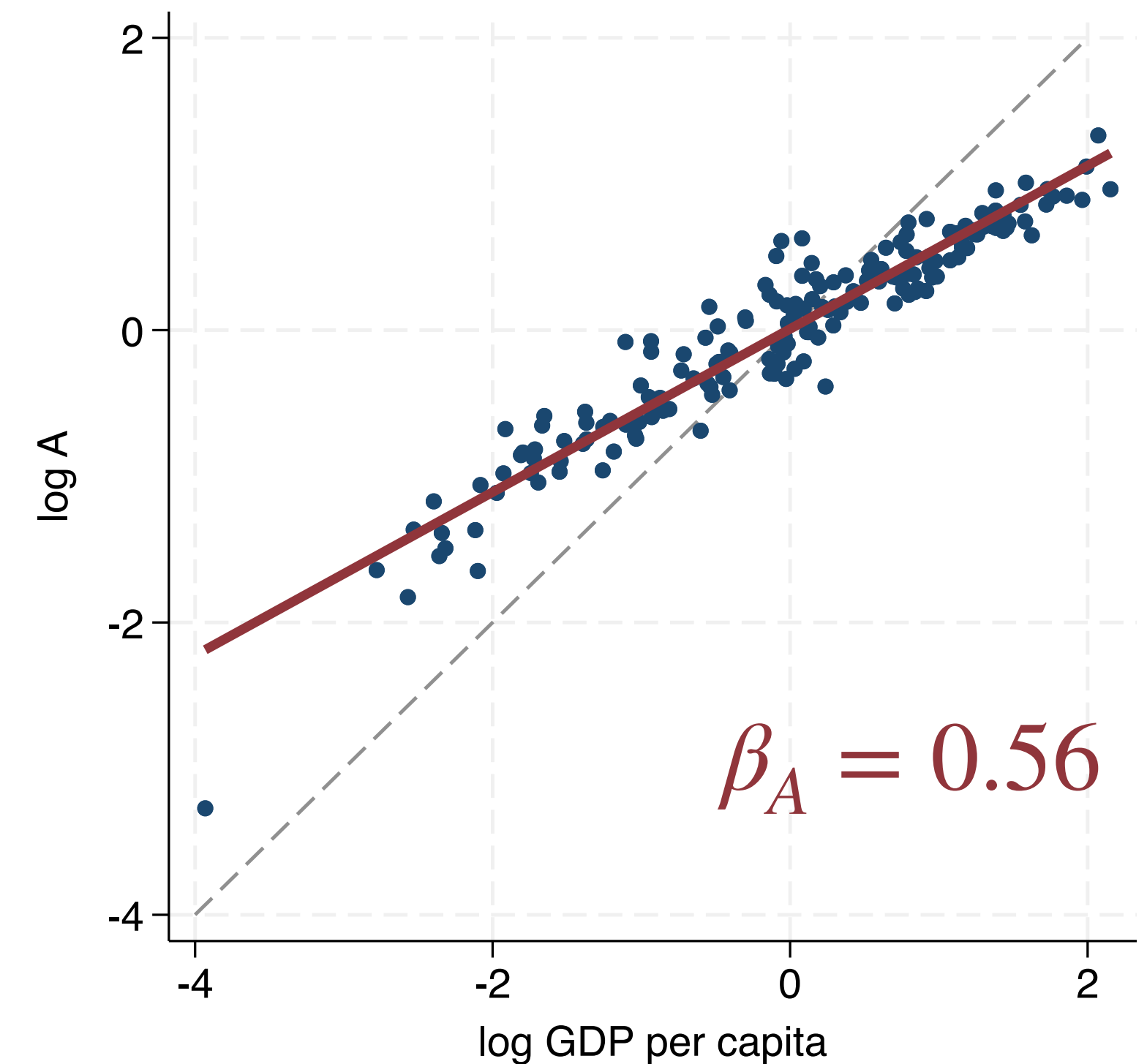
Data source: Penn World Table

$(1 - \alpha) \log(L/N)$



Data source: Penn World Table

$\log A$



Data source: Penn World Table

- Cross-country income differences due to K/N : 37%, L/N : 7%, A : 56%

What Did We Miss?

- Nontirival fraction of income differences due differences in capital
 - This motivates us to build a theory that determines capital
- However, more than half of the differences due to TFP
- Disappointing because more than half attributed to something we don't observe
 - Observable country characteristics explain less than half of income differences
- Are you convinced? What did we potentially miss?

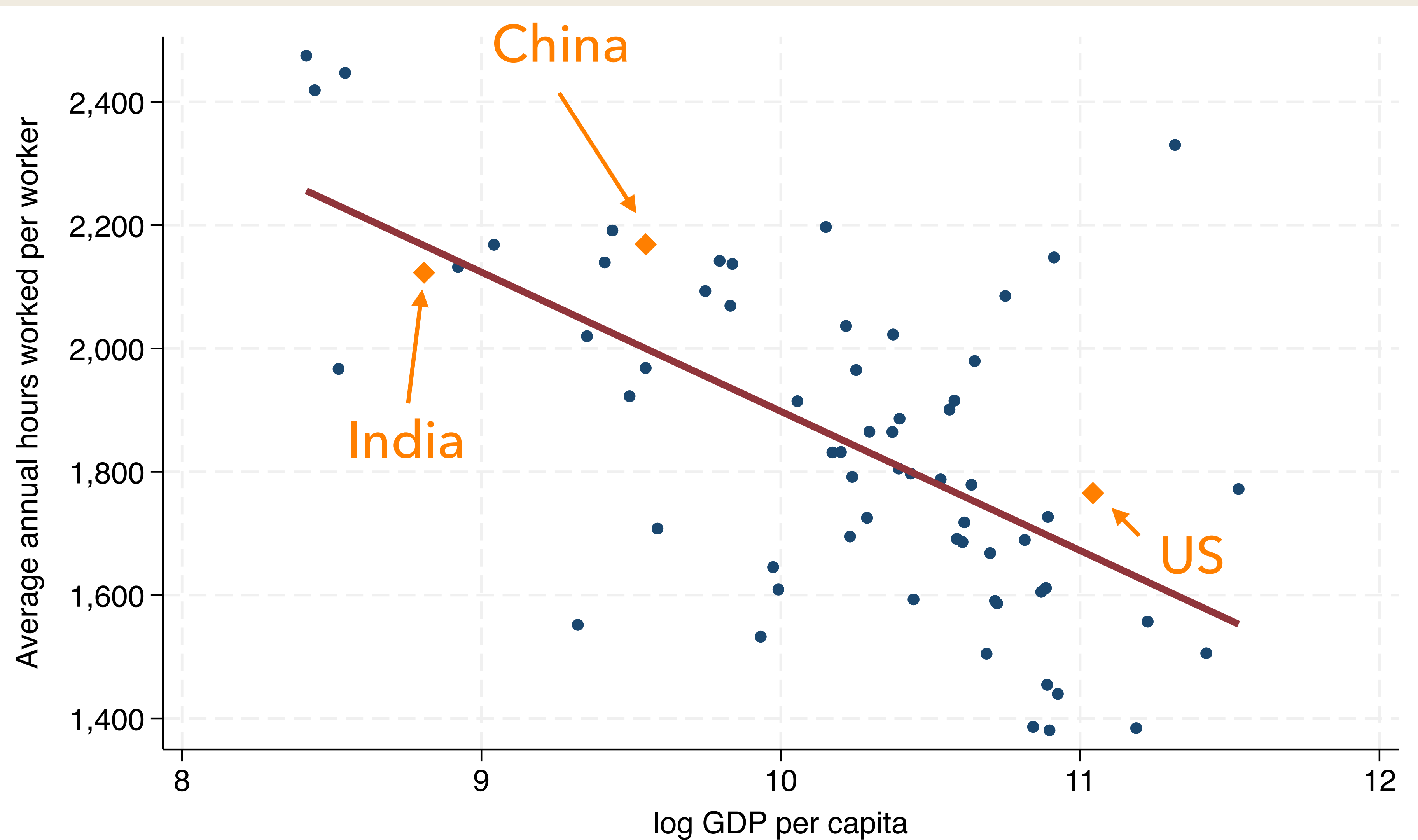
1. Hours Worked

$$Y_i = A_i K_i^\alpha (\textcolor{red}{h}_i L_i)^{1-\alpha}$$

$\textcolor{red}{h}_i$: hours worked per worker

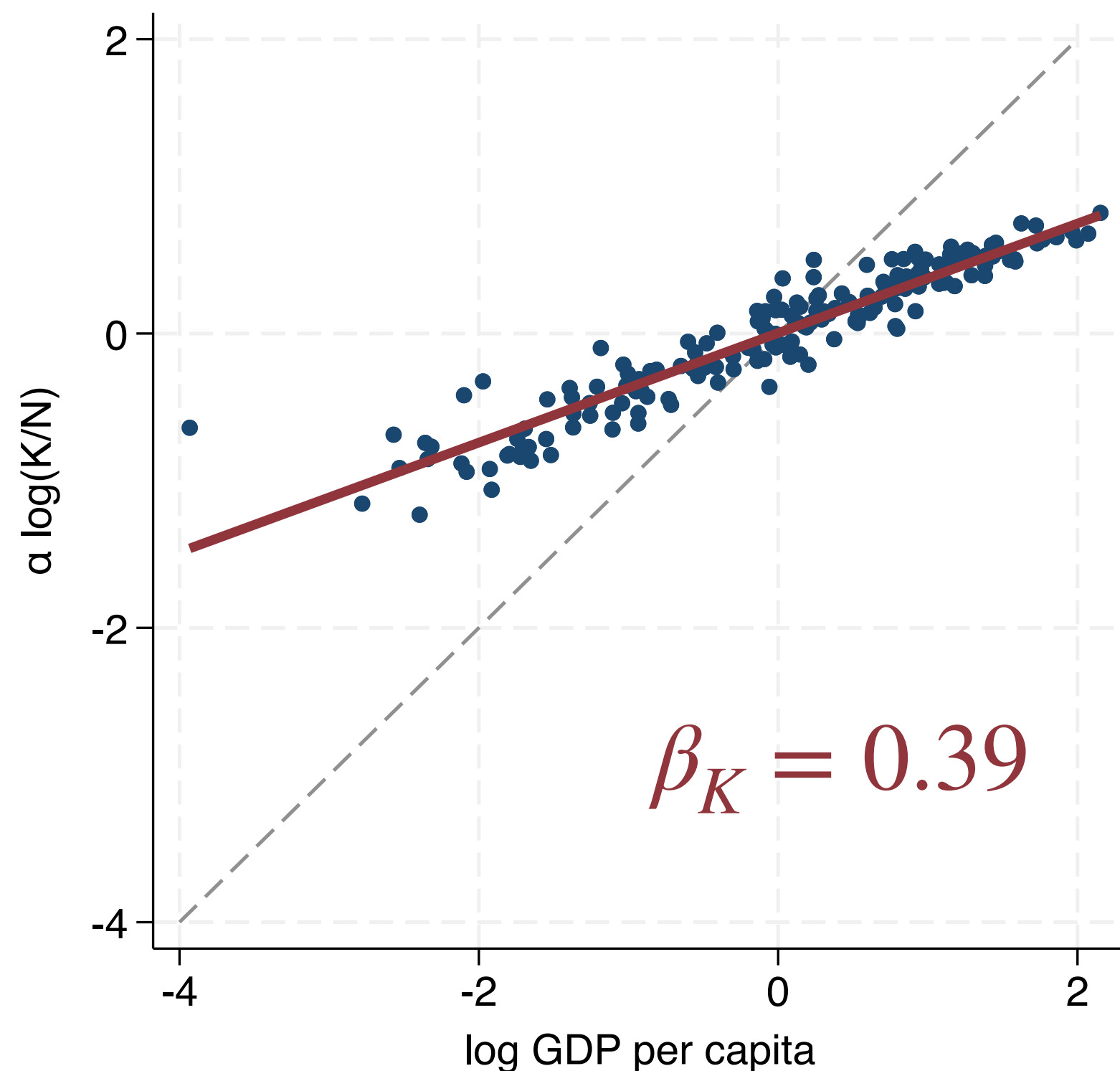
- Before, we assumed all workers worked for the same hours in all countries
- If h_i is higher for richer countries, this may help explain income differences

Hours Worked Declines with GDP



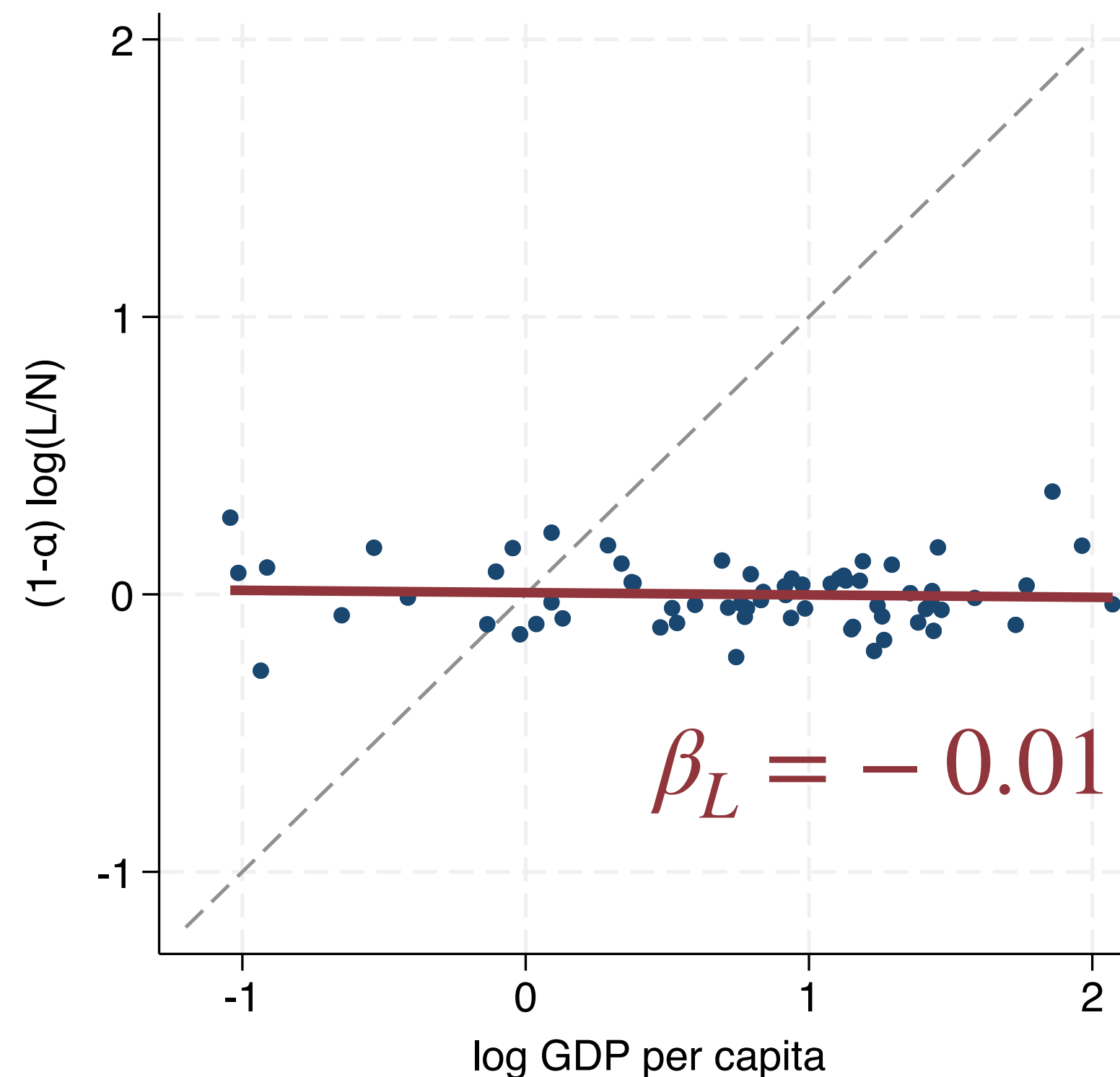
Development Accounting with Hours Worked

$$\alpha \log(K/N)$$



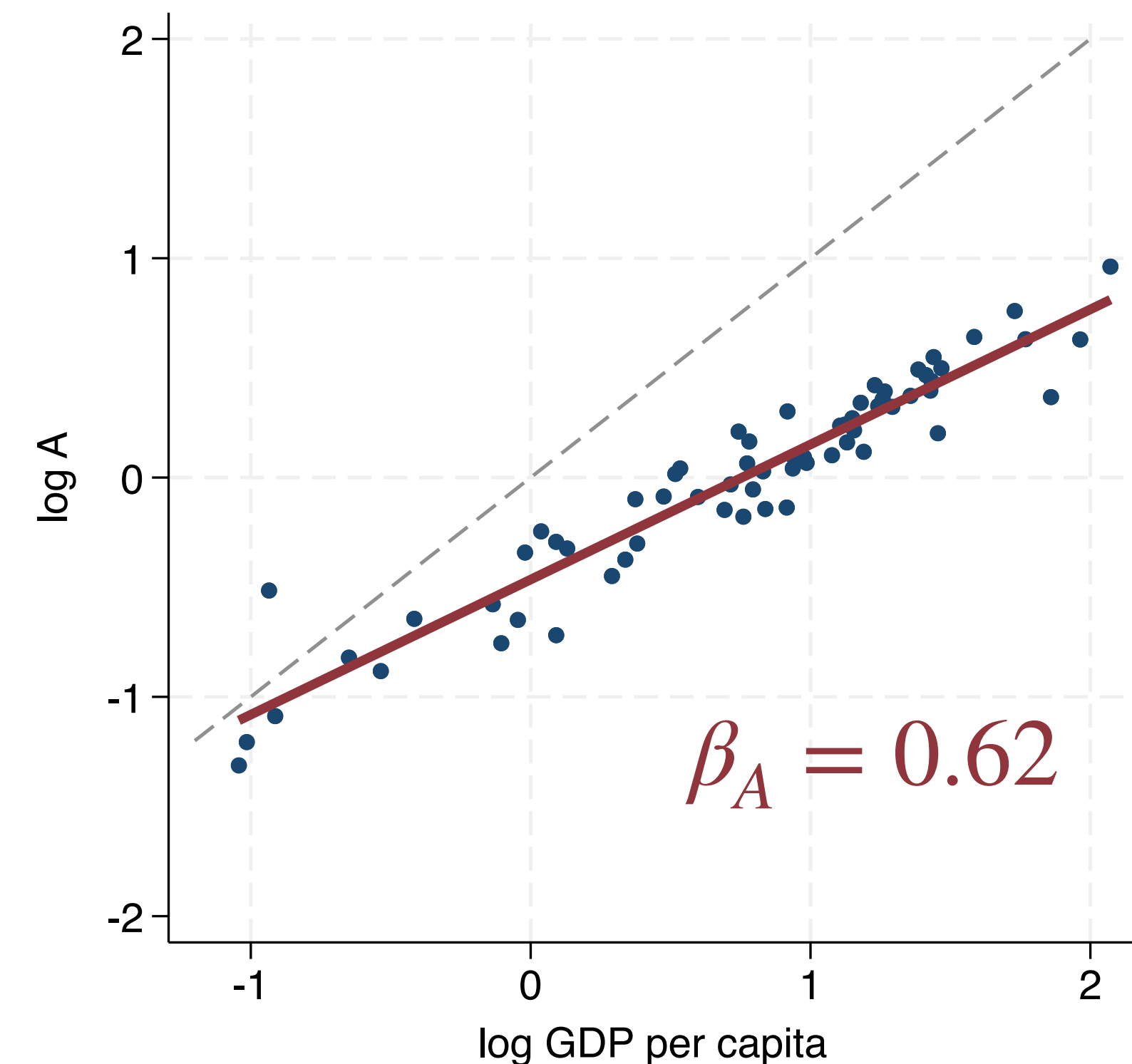
Data source: Penn World Table

$$(1 - \alpha) \log(hL/N)$$



Data source: Penn World Table

$$\log A$$

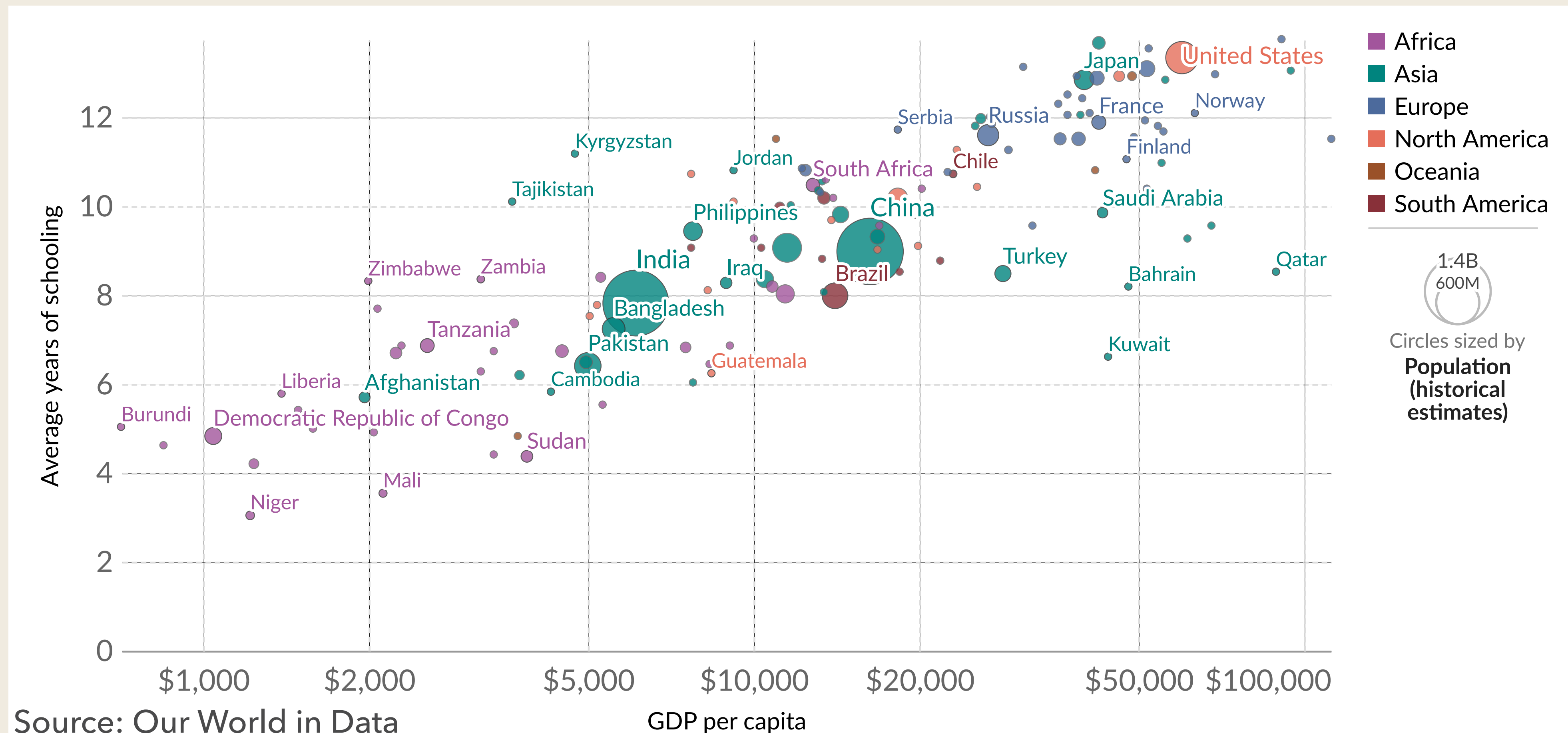


Data source: Penn World Table

- Even more important role of A once we allow hours worked to vary

2. Human Capital

- We have assumed that workers in rich countries and poor countries are the same
- Is this plausible? – Perhaps not



How Do We Measure Human Capital?

- Now we construct the human capita index:

$$L_i = \sum_{s=0}^S \phi^s L_i^s$$

- L_i^s : number of workers with schooling year s
 - ϕ^s : relative efficiency of workers with schooling year s
- We normalize $\phi^0 = 1$
 - How do we obtain ϕ^s ?

Inferring Human Capital from Wages

- Suppose workers with different schooling years are paid different wages
- The profit maximization is now

$$\max_{K, L_i^s} AK^\alpha \left(\sum_s \phi^s L_i^s \right)^{1-\alpha} - \sum_s w_i^s L_i^s - rK$$

- Taking the first-order condition with respect to L_i^s ,

$$(1 - \alpha) \phi^s AK^\alpha \left(\sum_s \phi^s L_i^s \right)^{-\alpha} = w_i^s$$

- Taking ratio,

$$\frac{\phi^s}{\phi^0} = \frac{w_i^s}{w_i^0} \Rightarrow \text{relative wages informative about } \phi^s$$

Human Capital Index

- Many estimates of $\{w_i^s\}$ in the labor economics literature
 - How wages vary depending on education
- Now we plug estimates of ϕ^s and construct our human capital index:

$$L_i = \sum_{s=0}^S \phi^s L_i^s$$

- With new L_i , let us re-do development accounting

Differences in Human Capital

	Y/N	K/N	L/N <i>employment</i>	L/N <i>human capital</i>	A <i>human capital</i>
U.S.	100	100	100	100	100
China	22	33	116	83	37
India	10	12	76	44	38
Haiti	2.5	7	84	38	12

Data: Penn World Table 2019

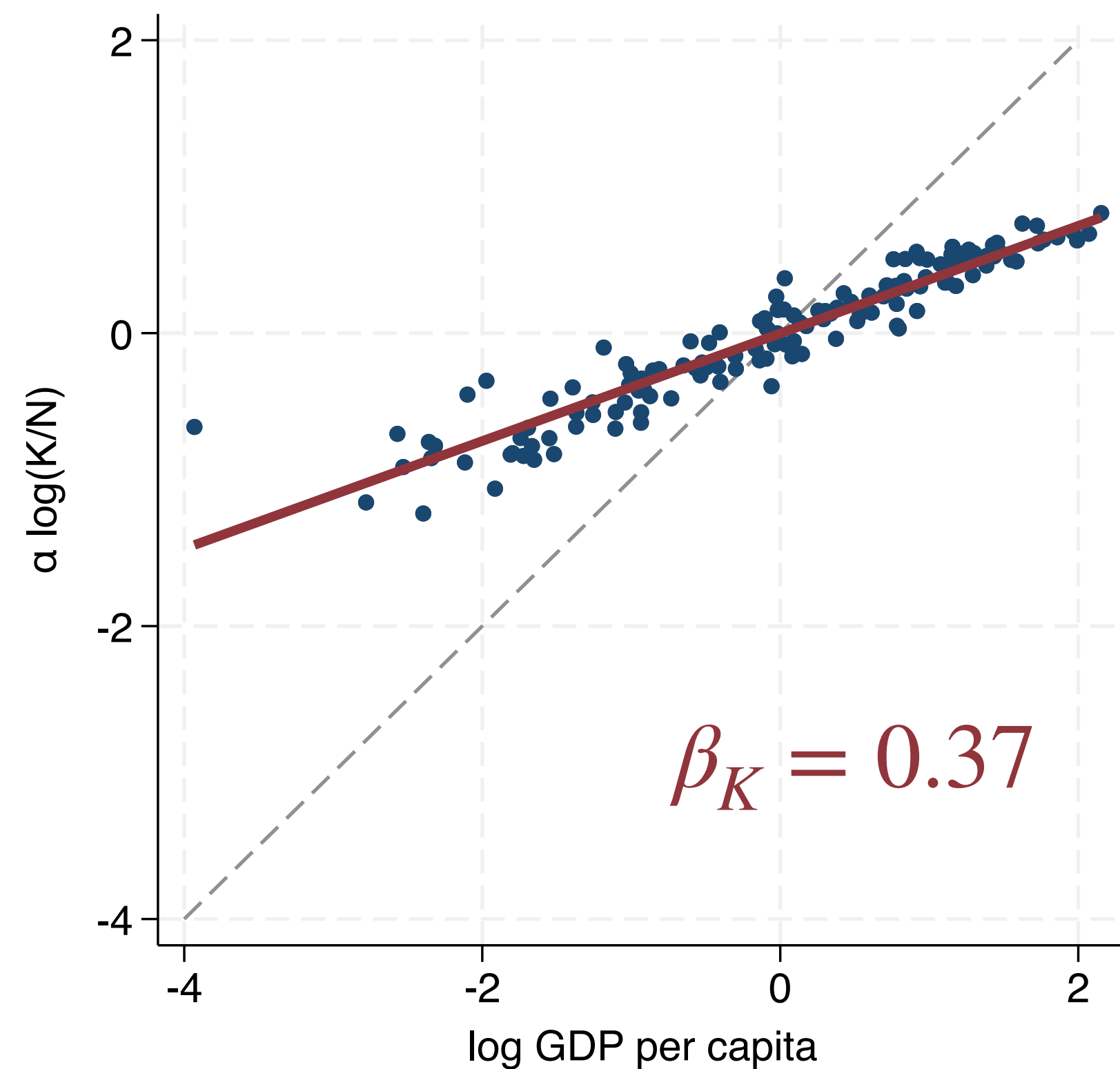
- More differences in L/N , but not quite as much as A or K/N

Development Accounting with Human Capital

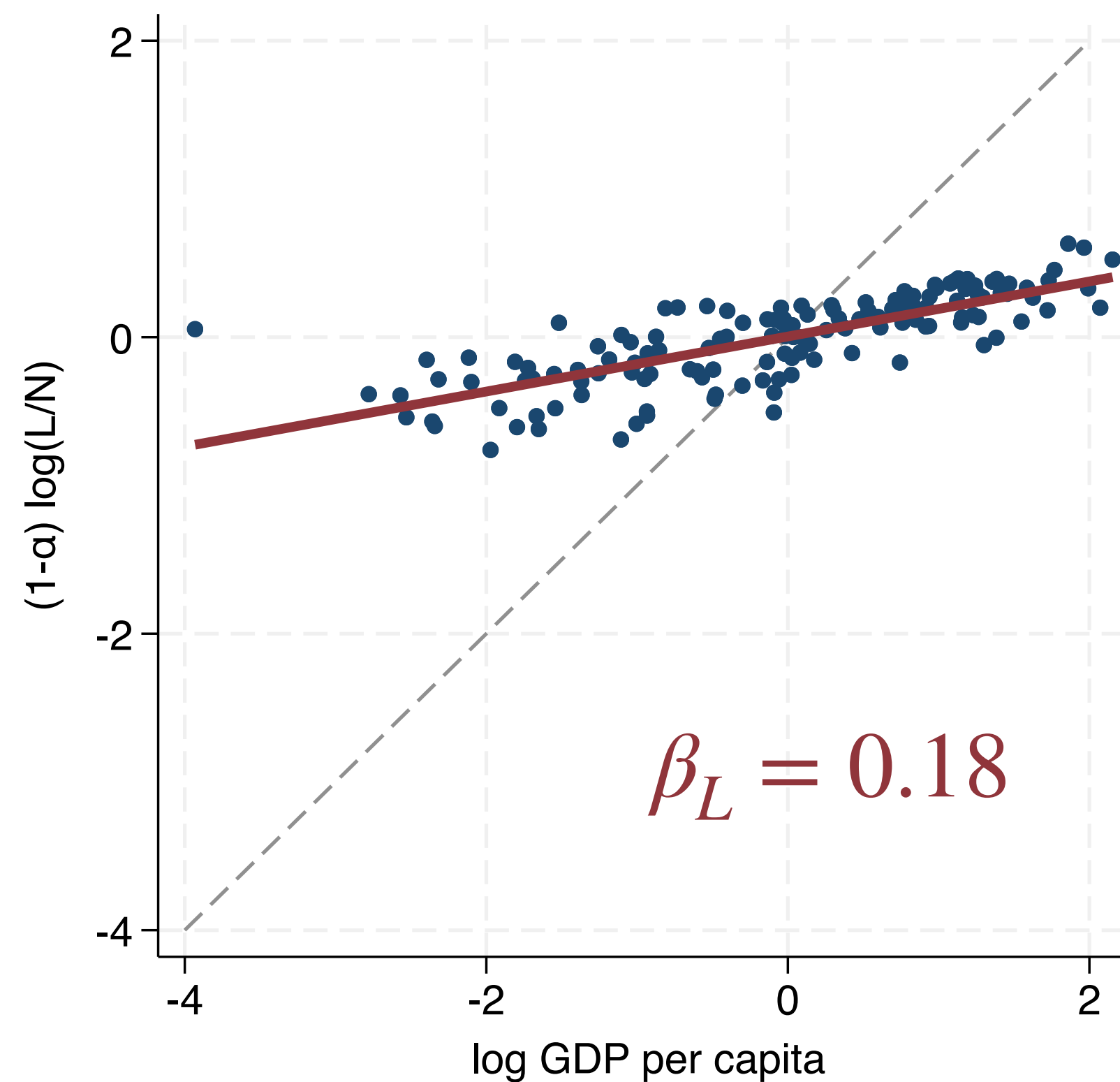
$$\alpha \log(K/N)$$

$$(1 - \alpha) \log(L/N)$$

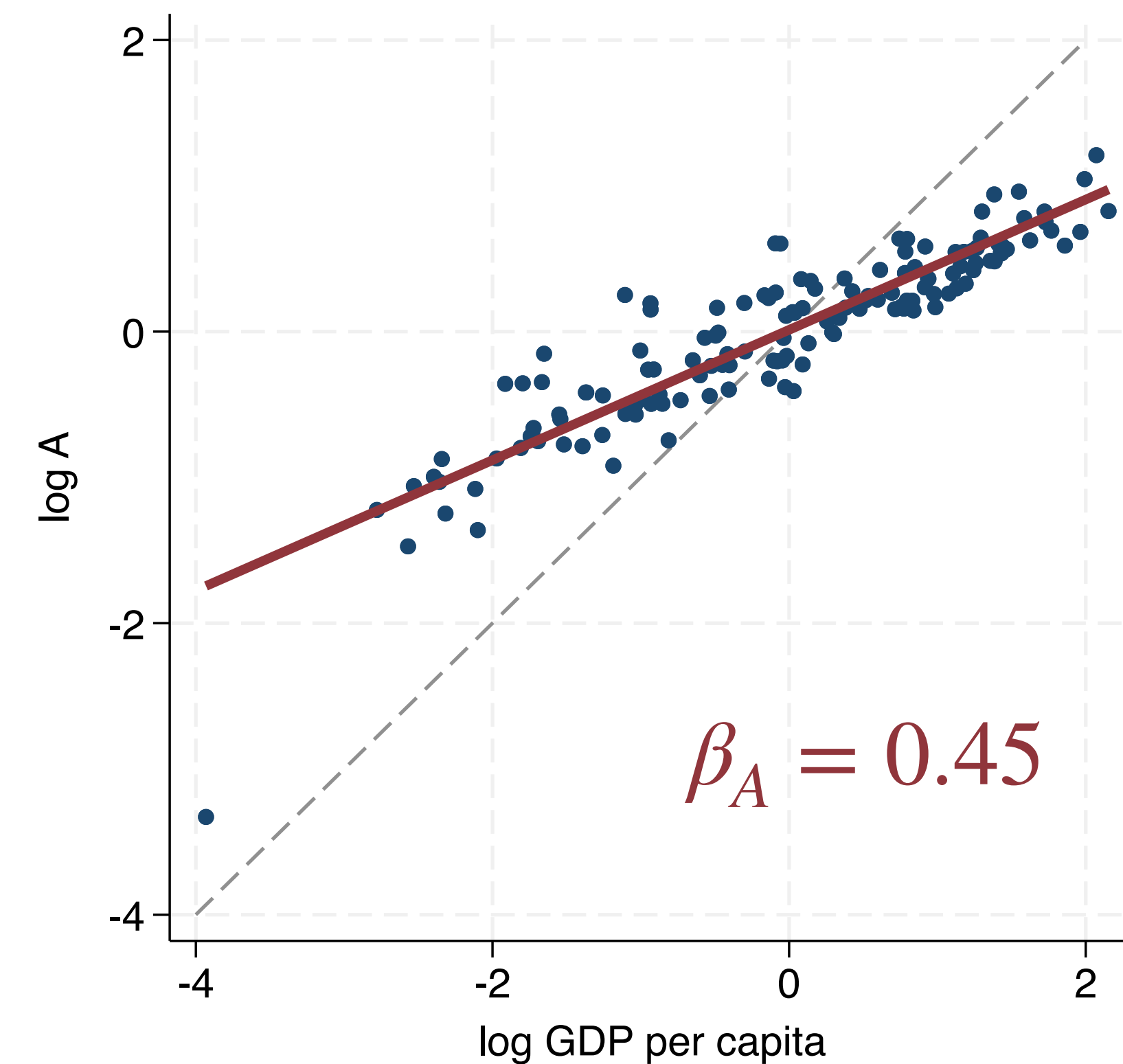
$$\log A$$



Data source: Penn World Table



Data source: Penn World Table



Data source: Penn World Table

■ Cross-country income differences due to K/N : 37%, L/N : 18%, A : 45%

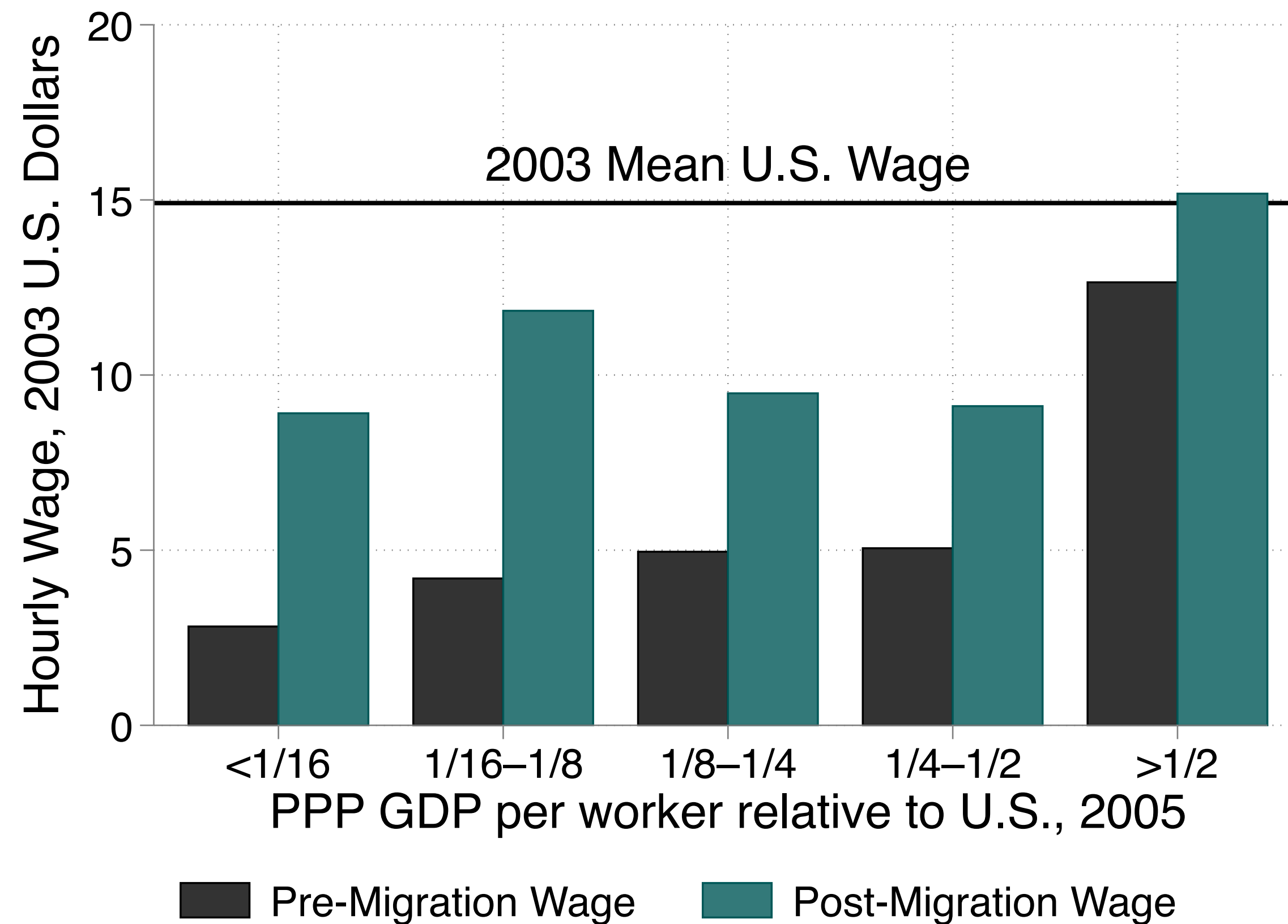
Ongoing Debate

- Human capital explains 18% of cross-country income differences
- This reduces the contribution of our measure of ignorance to less than half
- Lots of debate on the role of human capital:
 1. Functional form: $L_i = G(\{L_i^s\}_{s=0}^S)$ rather than $L_i = \sum_{s=0}^S \phi^s L_i^s$
 2. ϕ^s could be different across countries
 3. Schooling is not the only source of human capital (e.g., experience)
- Some argue human capital can explain almost all cross-country differences

What Do Immigrants Tell Us?

- Let us tackle the problem from a different angle (Hendricks and Schoellman, 2018)
- Focus on immigrants to the US
- How much wage gains do immigrants experience upon arrival to the US?
- Immigrants bring their human capital (L) but do not bring A or K of home country
 - Instead, they can now use technology or physical capital in the US
- If A or K very important, their wages rise one-for-one with GDP gap
- If A or K not important, their wages should not change

Wage Gains from Immigration



Pre- and Post-Migration Wages



Wage Gains at Migration

How Do Wage Gains Compare to GDP Gap?

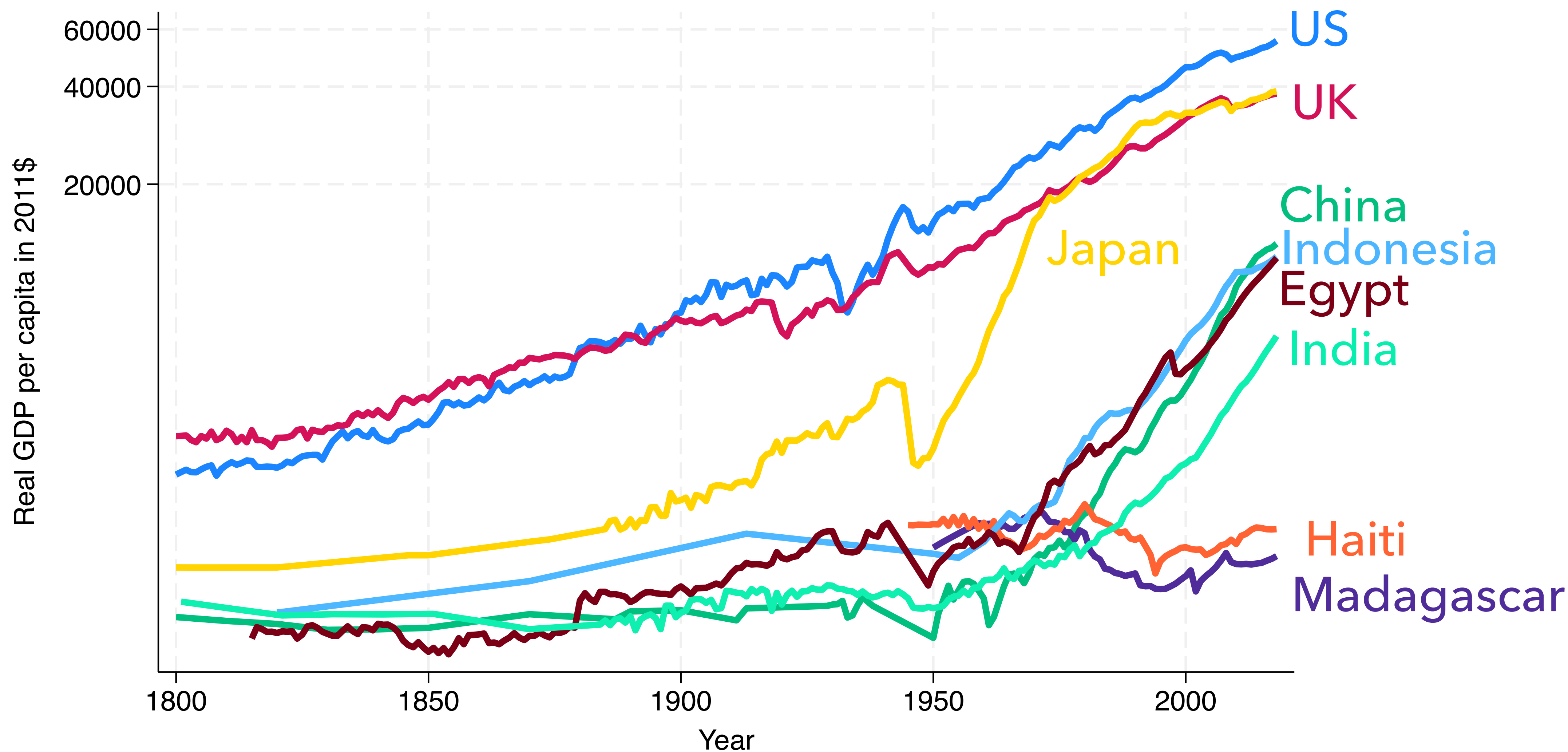
Group	Hourly Wage		Development Accounting			
	Pre-Mig.	Post-Mig.	Wage Gain	GDP Gap	<i>h</i> share	95% C.I.
Panel A: NIS Sample by GDP per worker category						
< 1/16	\$2.82	\$8.91	3.2	31.8	0.66	(0.60, 0.73)
1/16 – 1/8	\$4.19	\$11.83	2.8	11.9	0.58	(0.54, 0.62)
1/8 – 1/4	\$4.95	\$9.48	1.9	5.6	0.63	(0.55, 0.71)
1/4 – 1/2	\$5.05	\$9.11	1.8	3.0	0.48	(0.34, 0.62)
1/2 – 1	\$12.64	\$15.18	1.2	1.3	0.48	(-0.23, 1.19)

Source: Hendricks and Schoellman (2018)

- Wage gains are typically much smaller than GDP gap
- This implies that human capital is an important component of income differences
- Differences in TFP or physical cannot be the whole story

Growth Accounting

Why Do Countries Grow?



Source: Madison project

Growth Accounting

- Why do countries grow?
- The growth rate of the economy between t and $t + T$:

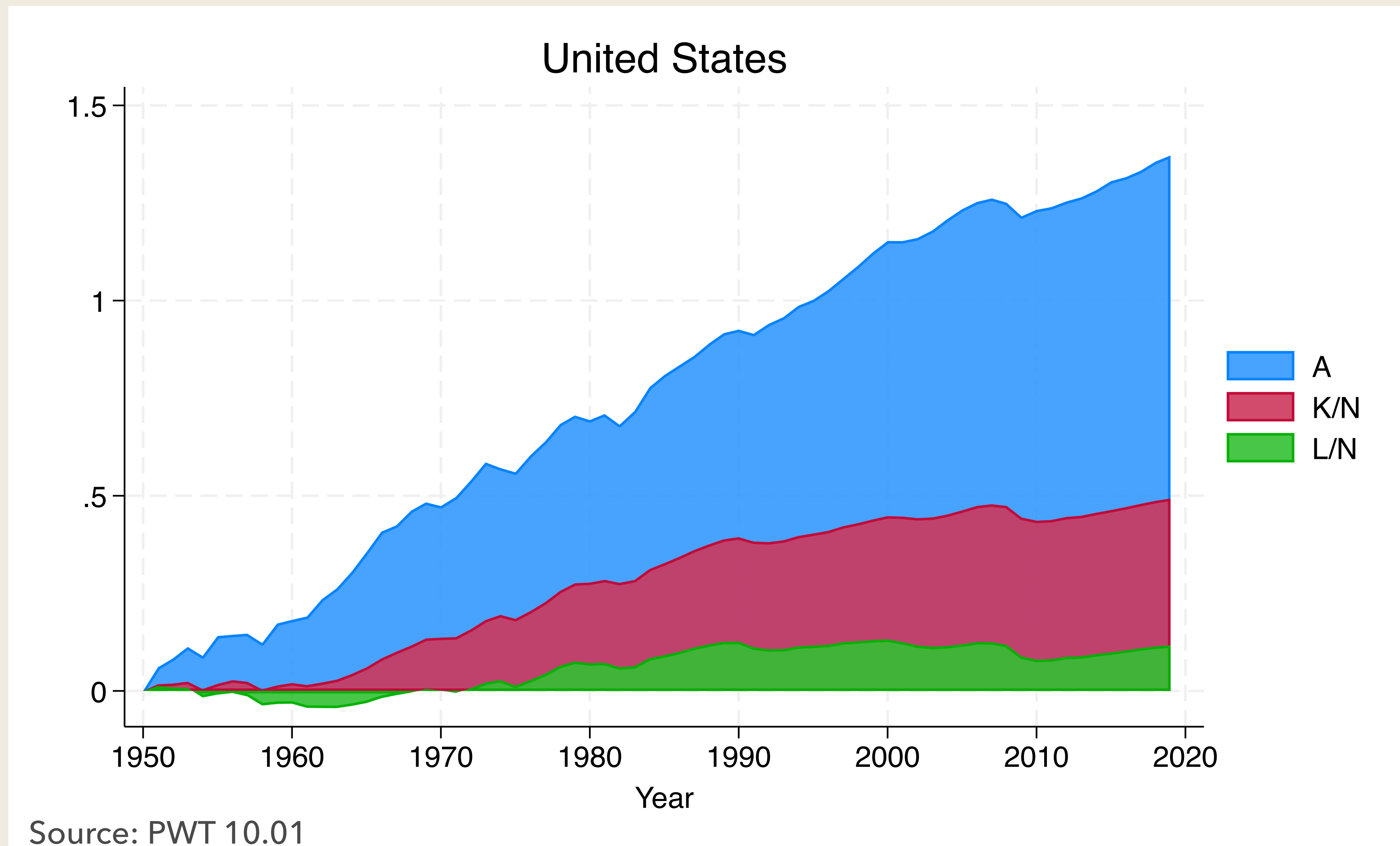
$$\Delta_T \log(Y_t/N_t) \equiv \log(Y_{t+T}/N_{t+T}) - \log(Y_t/N_t)$$

- With $Y_t = A_t K_t^\alpha L_t^{1-\alpha}$, we can decompose growth into:

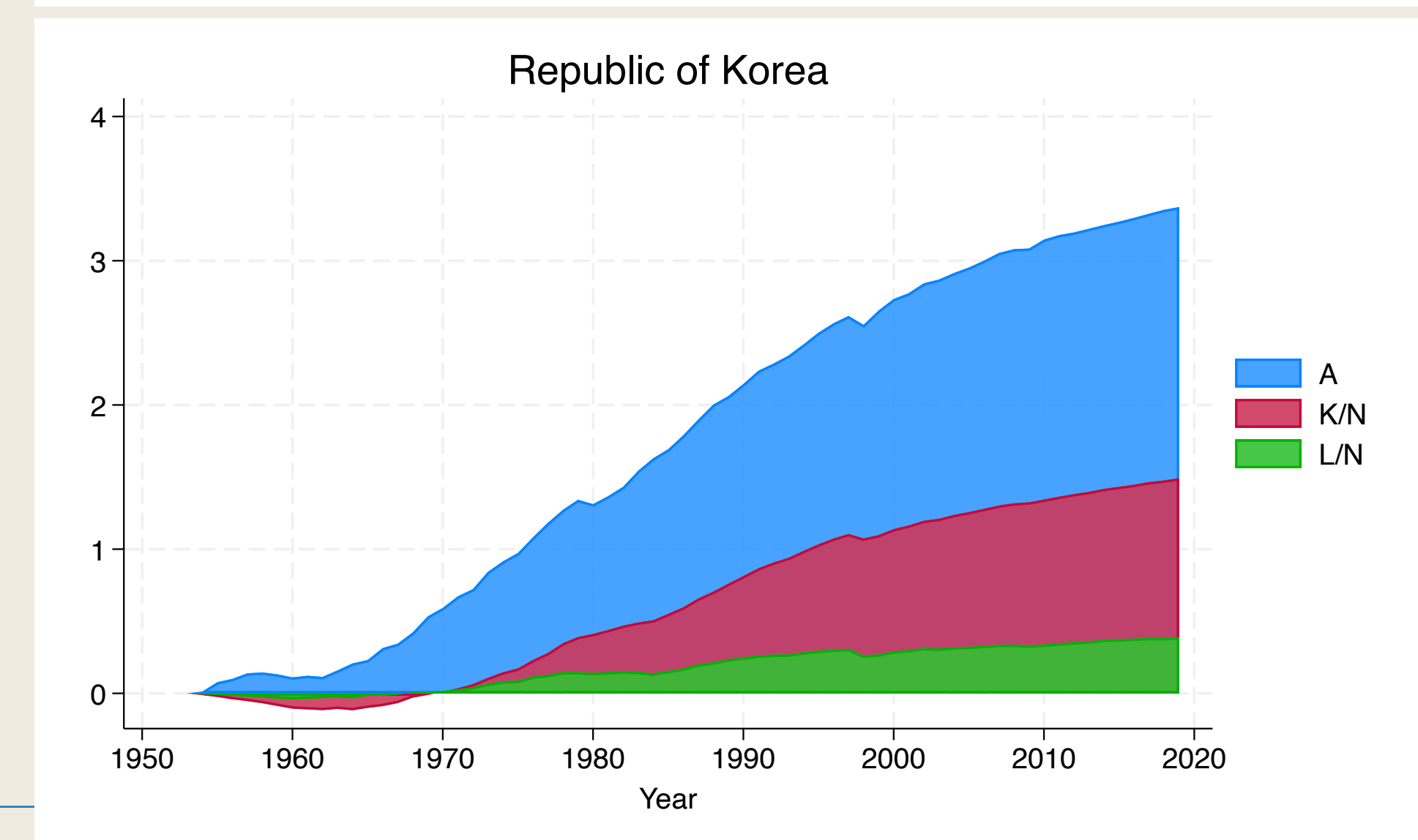
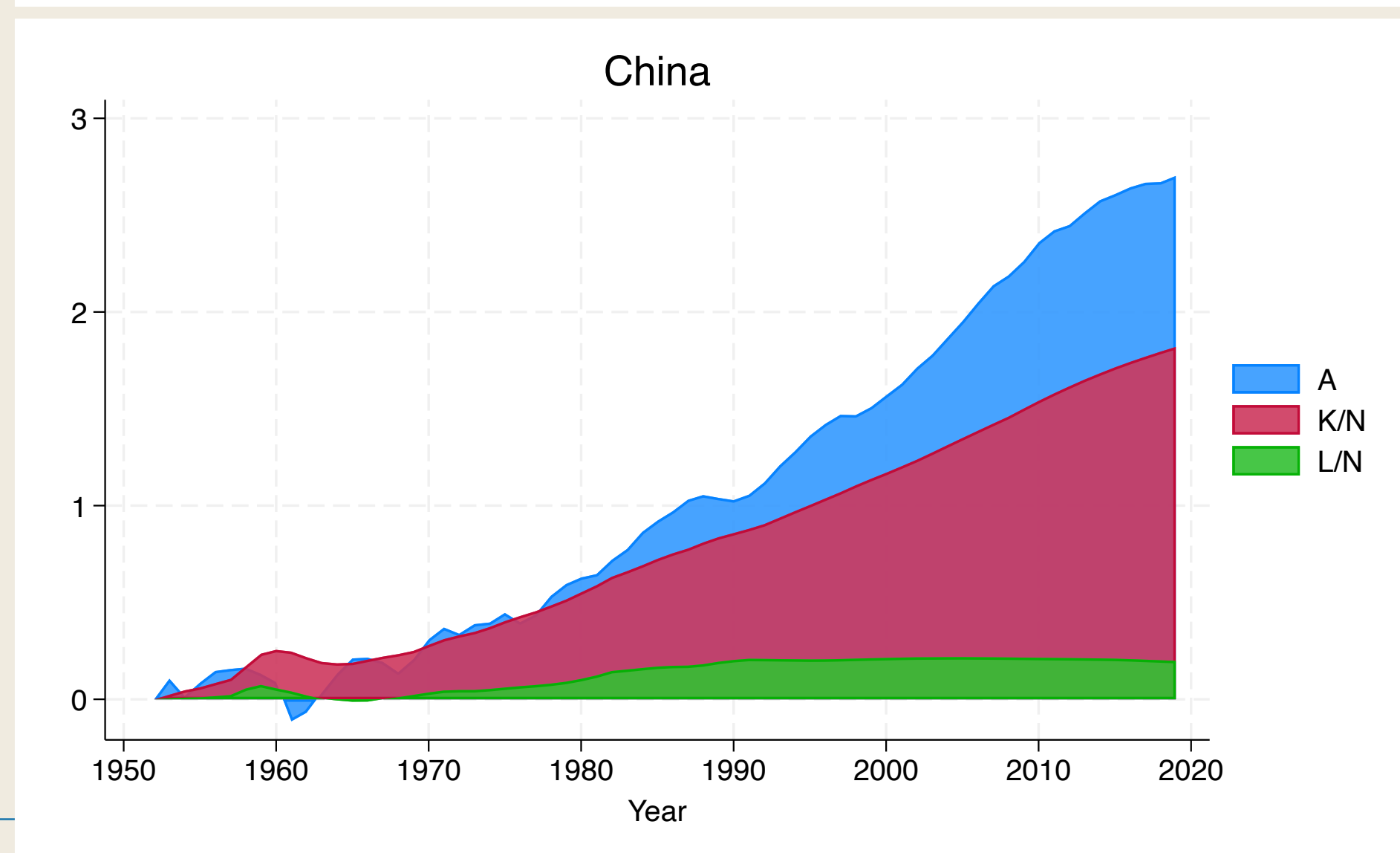
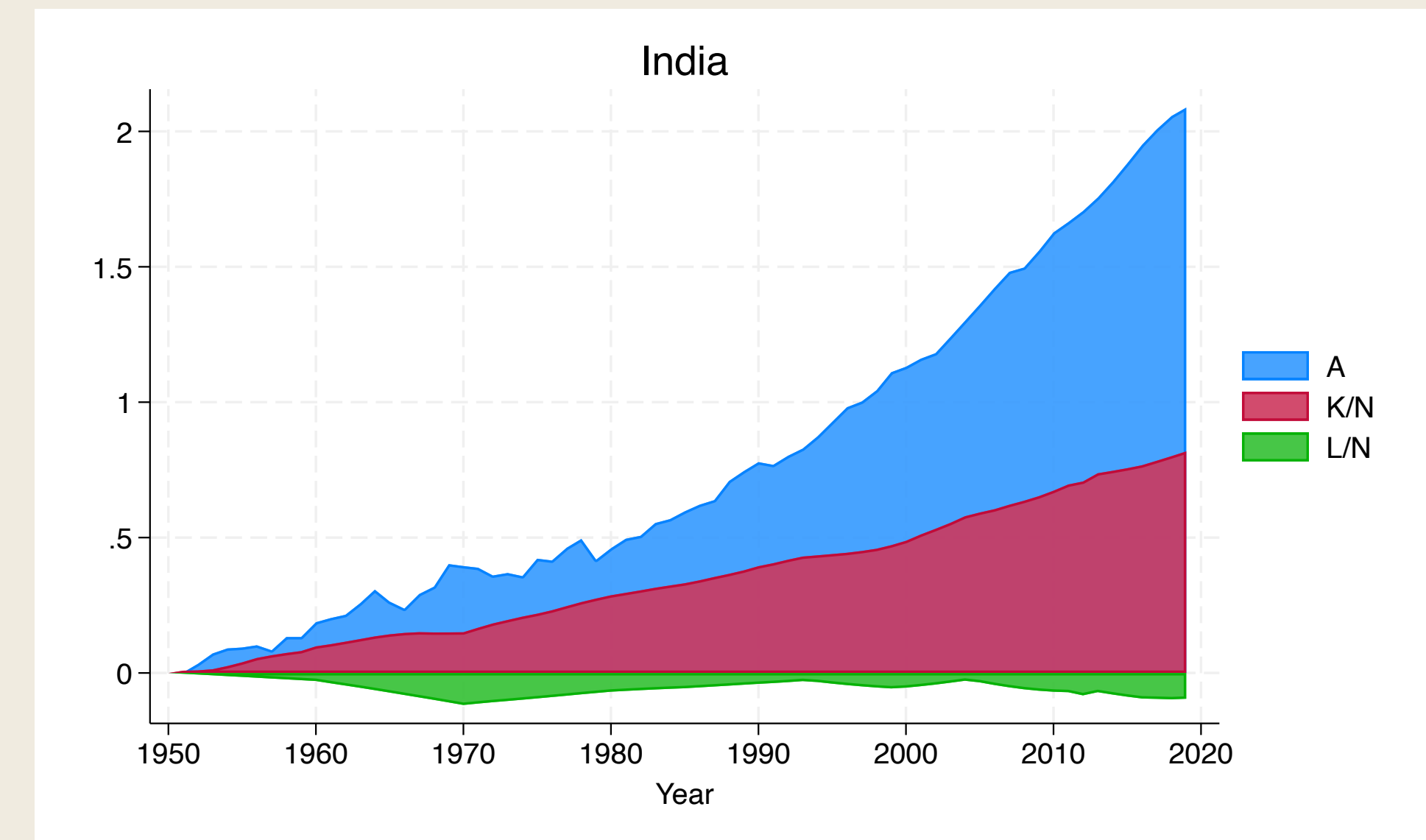
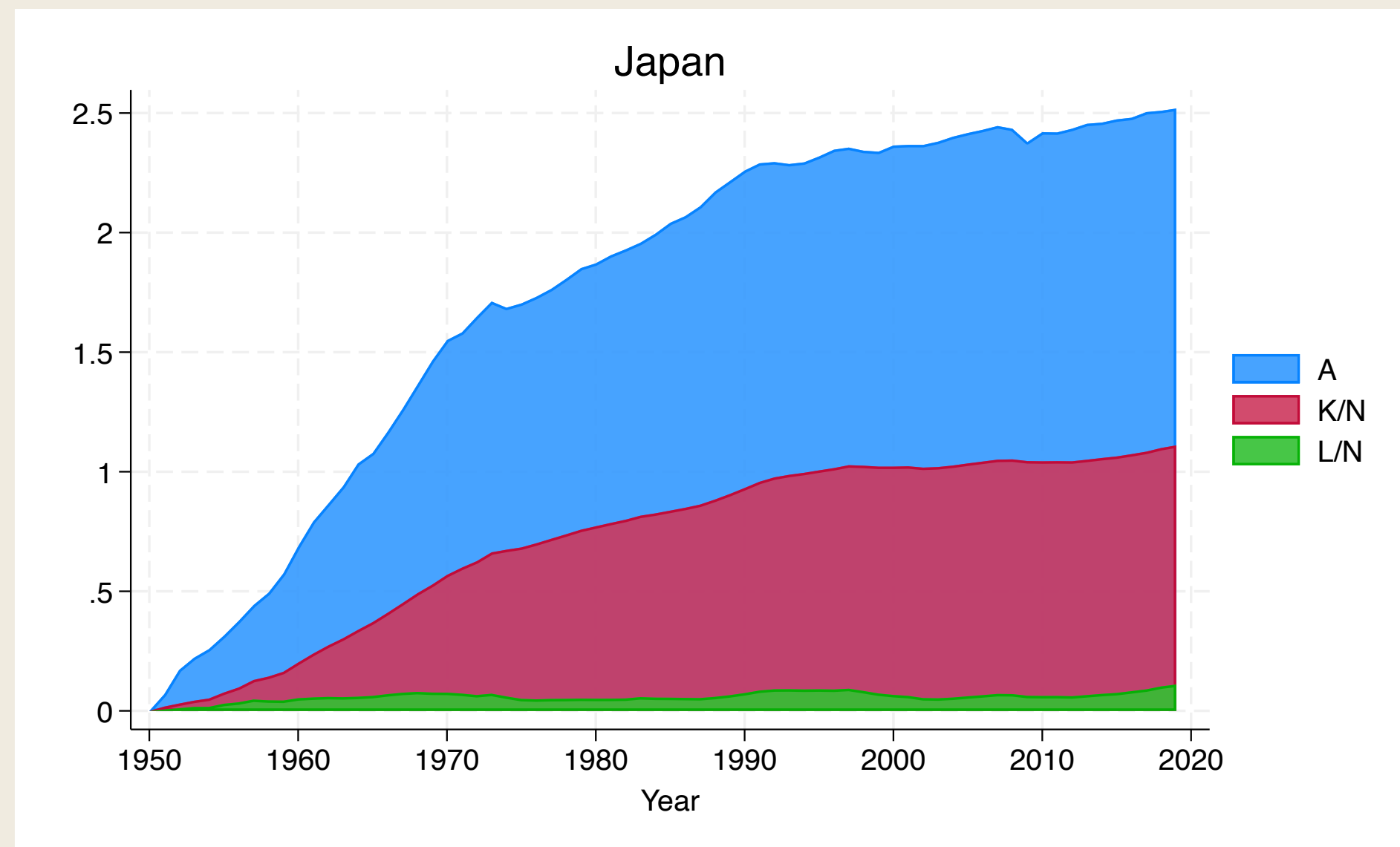
$$\begin{aligned} \Delta_T \log(Y_t/N_t) &= \alpha \Delta_T \log(K_t/N_t) && \text{Growth due to } K \\ &+ (1 - \alpha) \Delta_T \log(L_t/N_t) && \text{Growth due to } L \\ &+ \Delta_T \log(A_t) && \text{Growth due to } A \end{aligned}$$

- **Growth accounting:** decomposition over time-series
- **Development accounting:** decomposition over cross-section

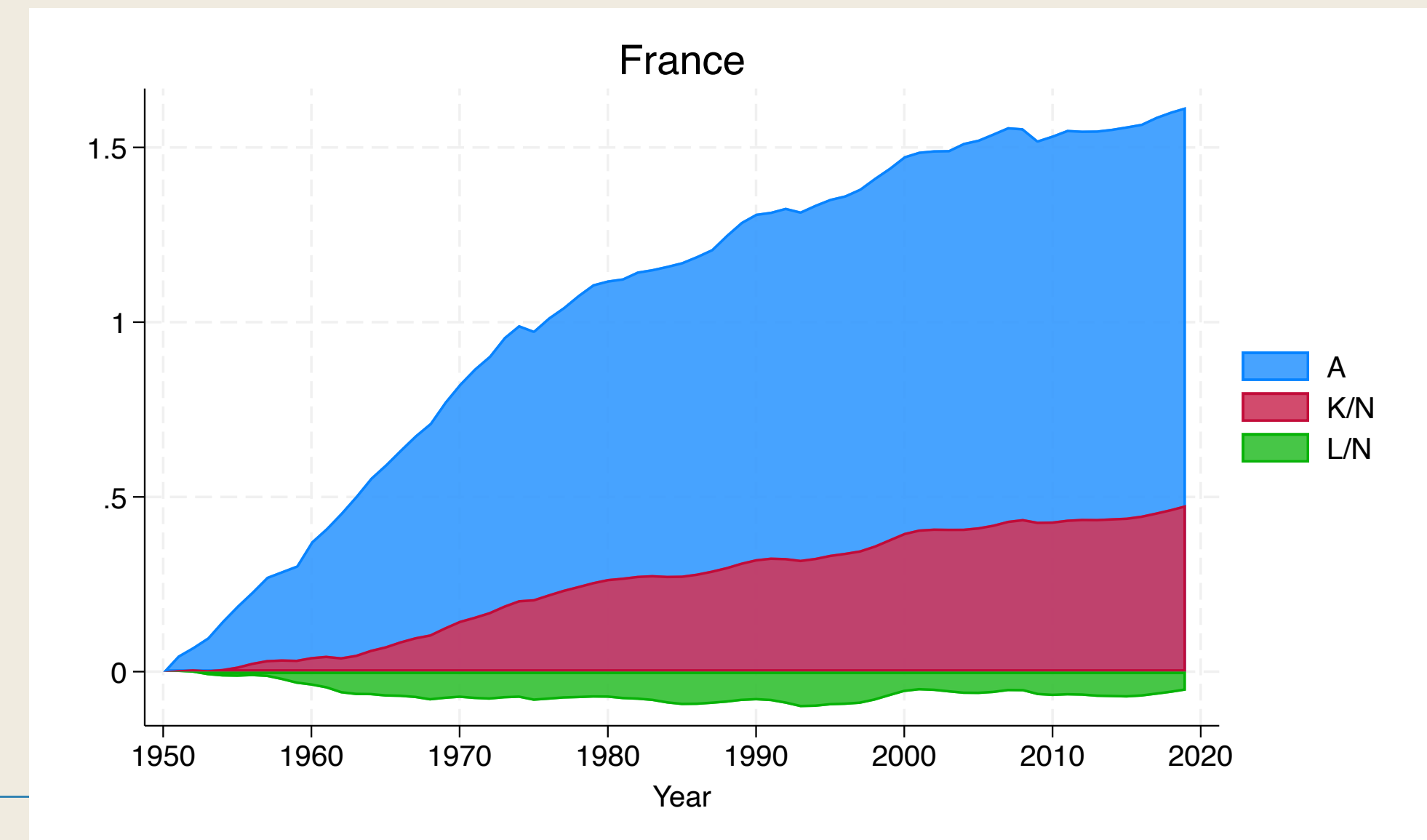
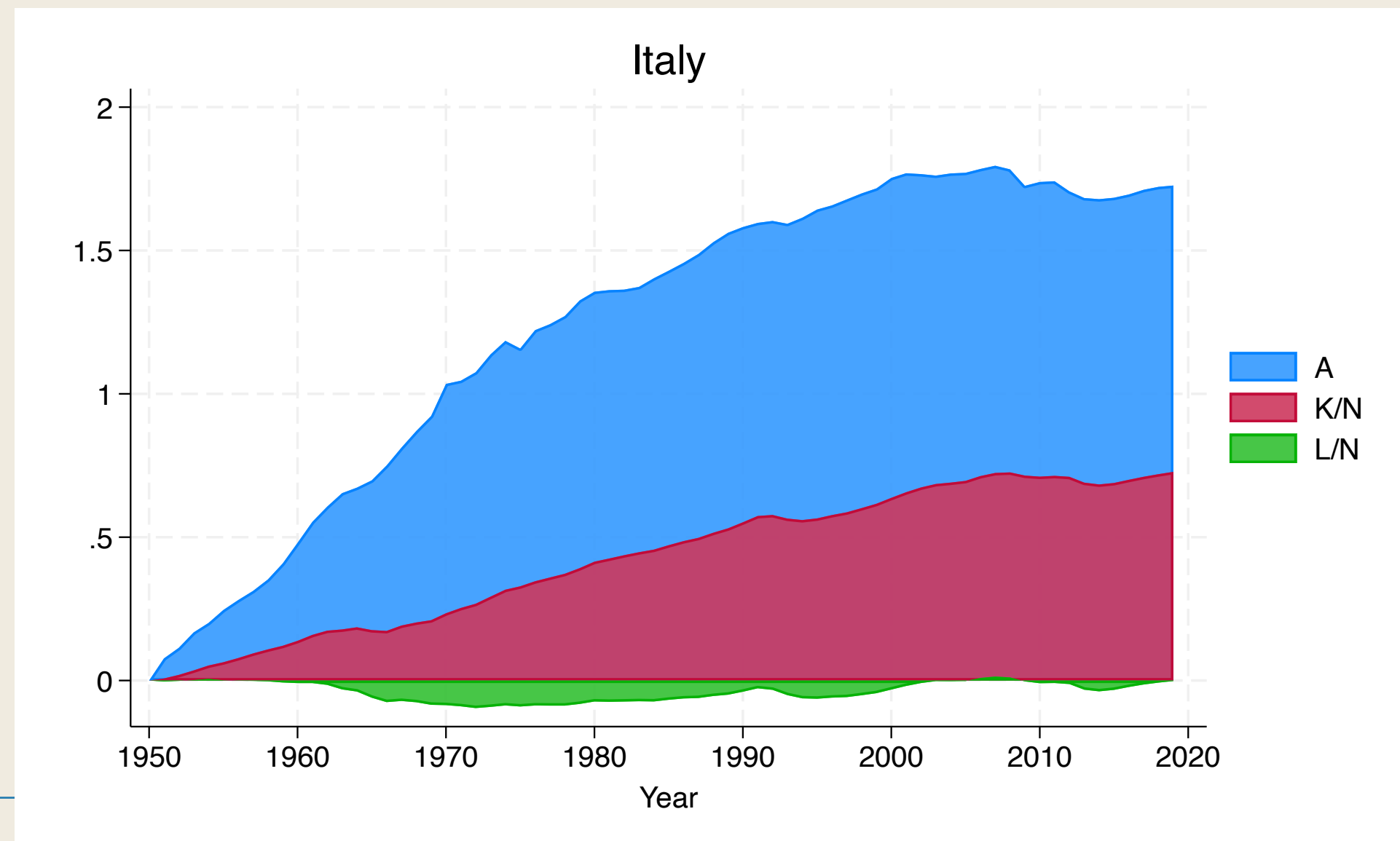
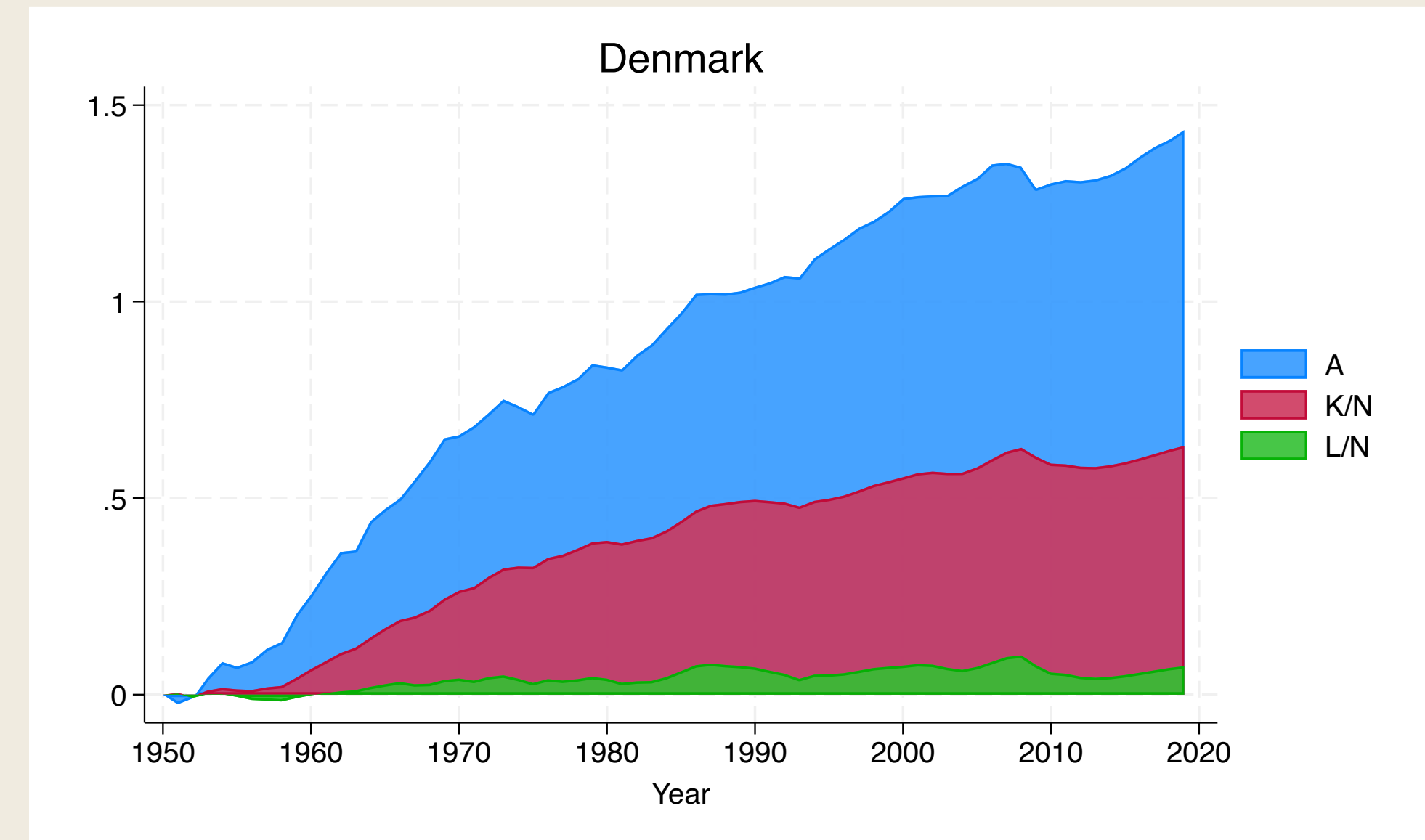
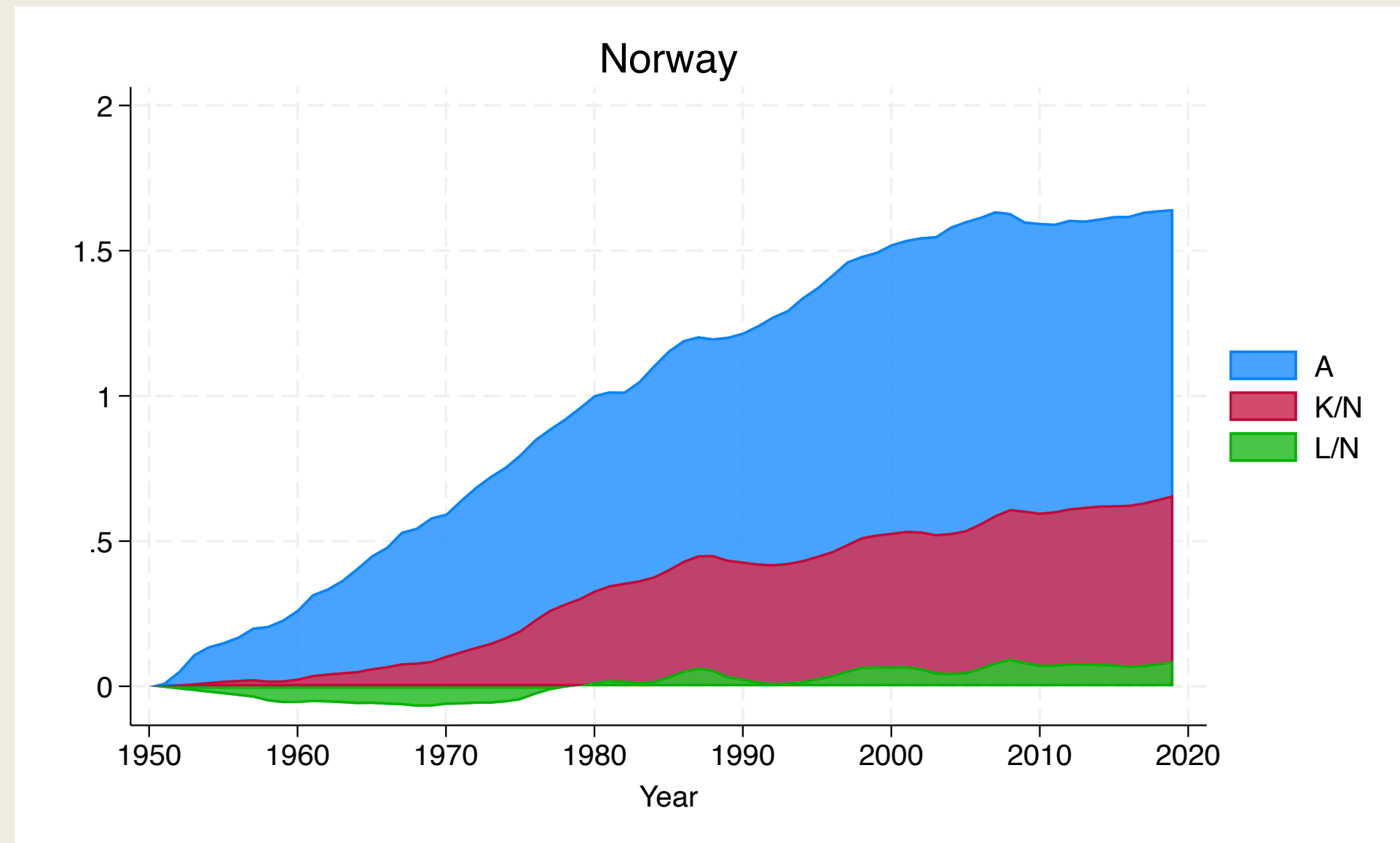
Growth Accounting: US



Growth Accounting: Asia

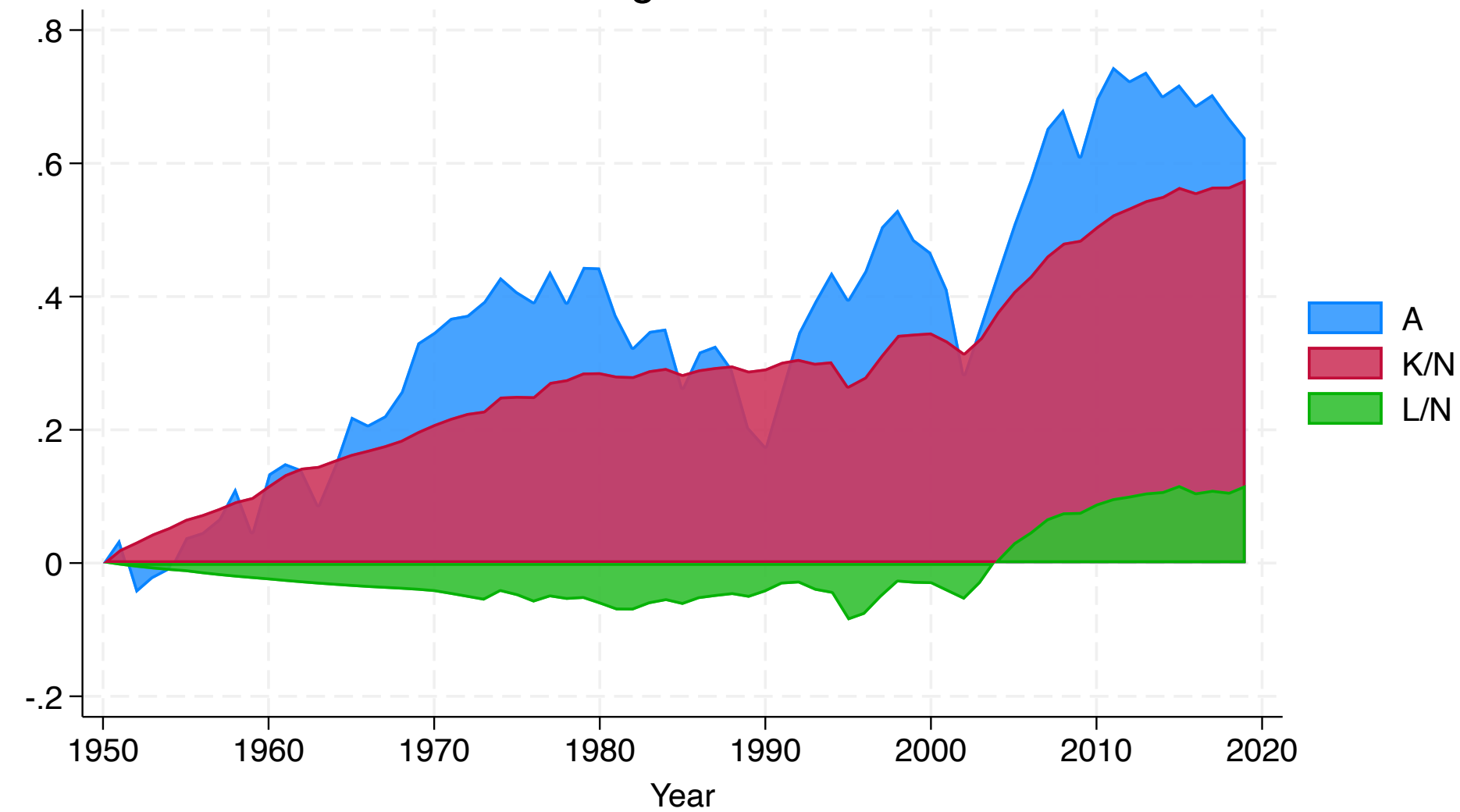


Growth Accounting: Europe

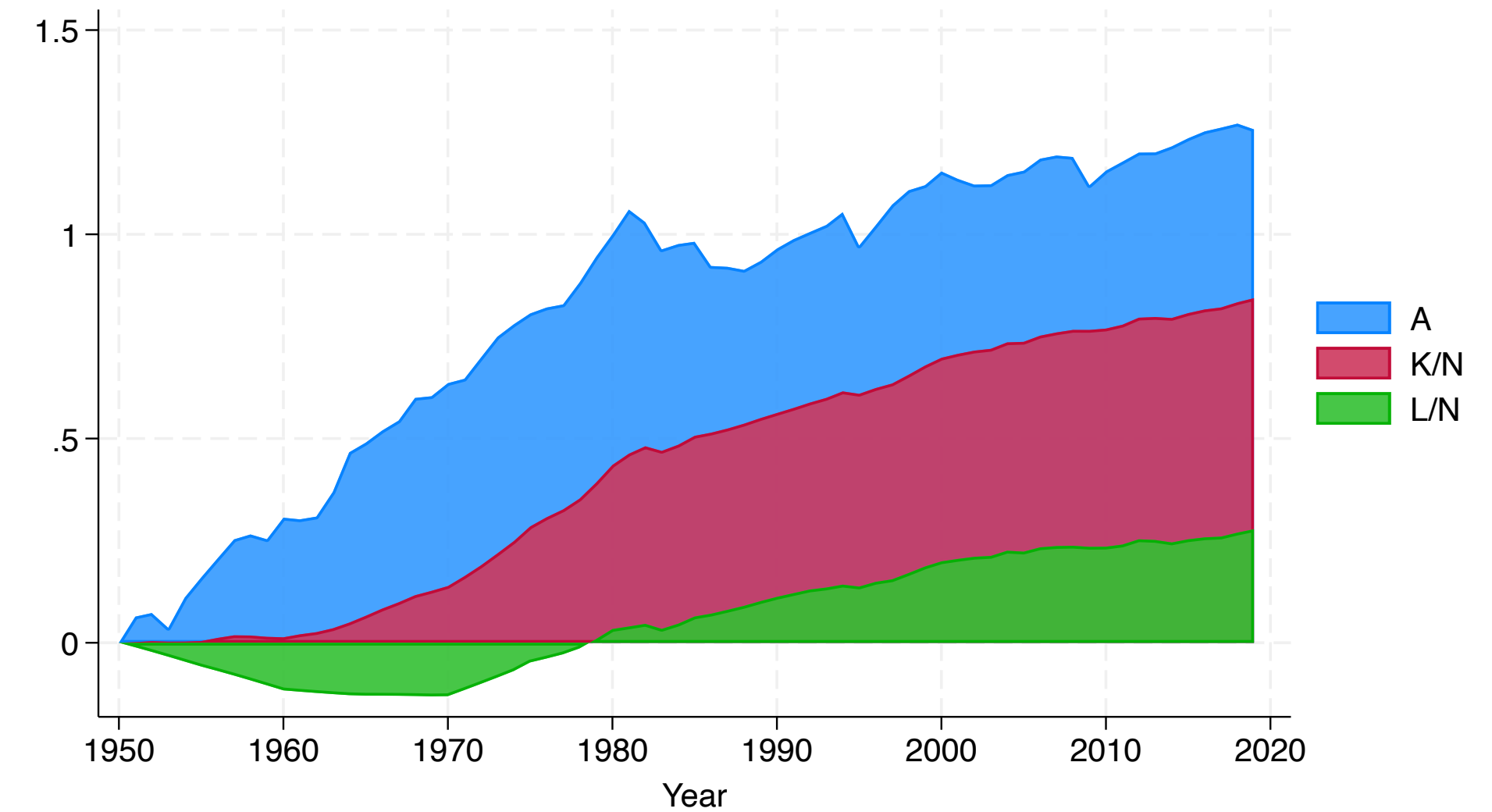


Growth Accounting: Latin America

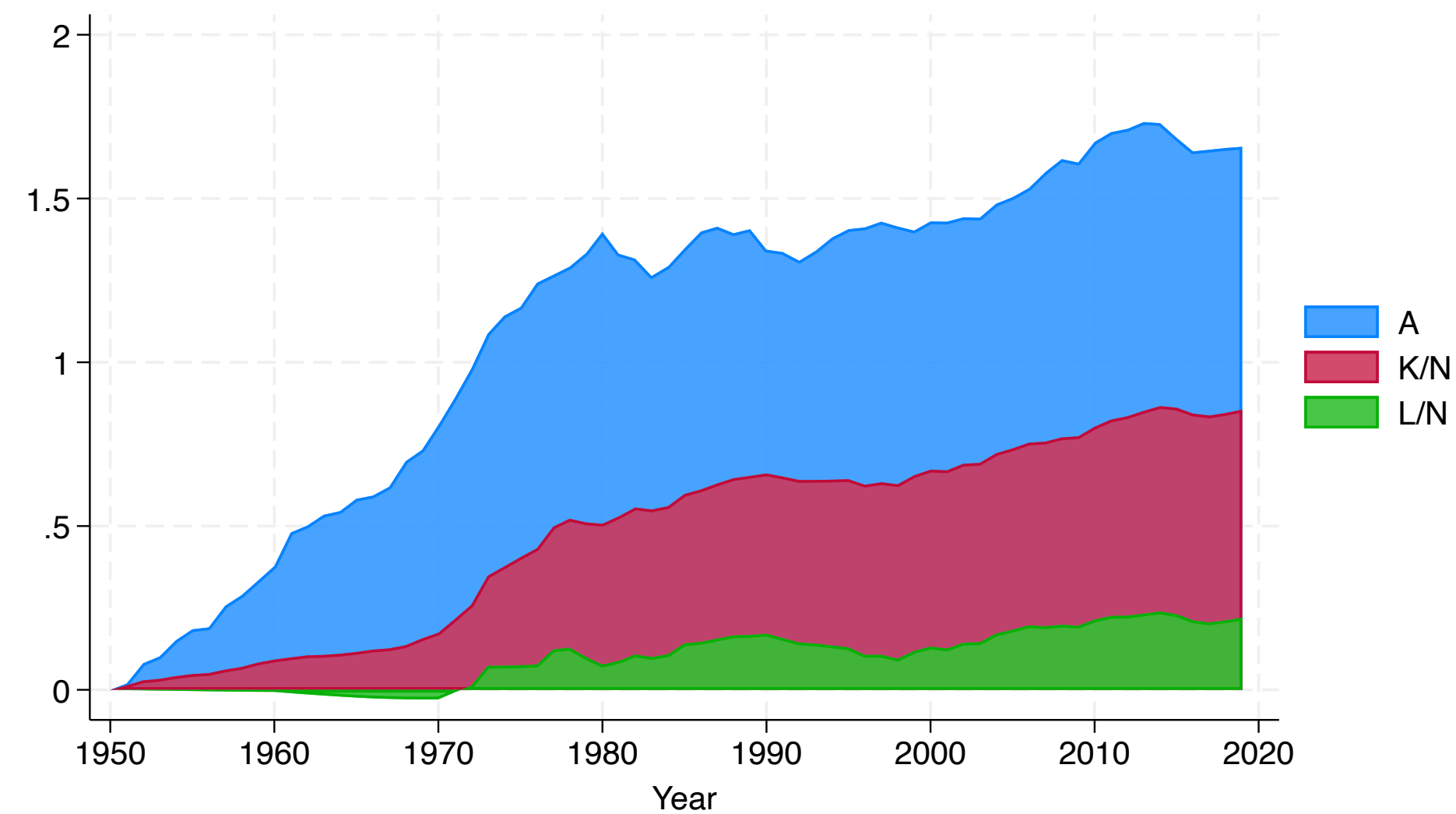
Argentina



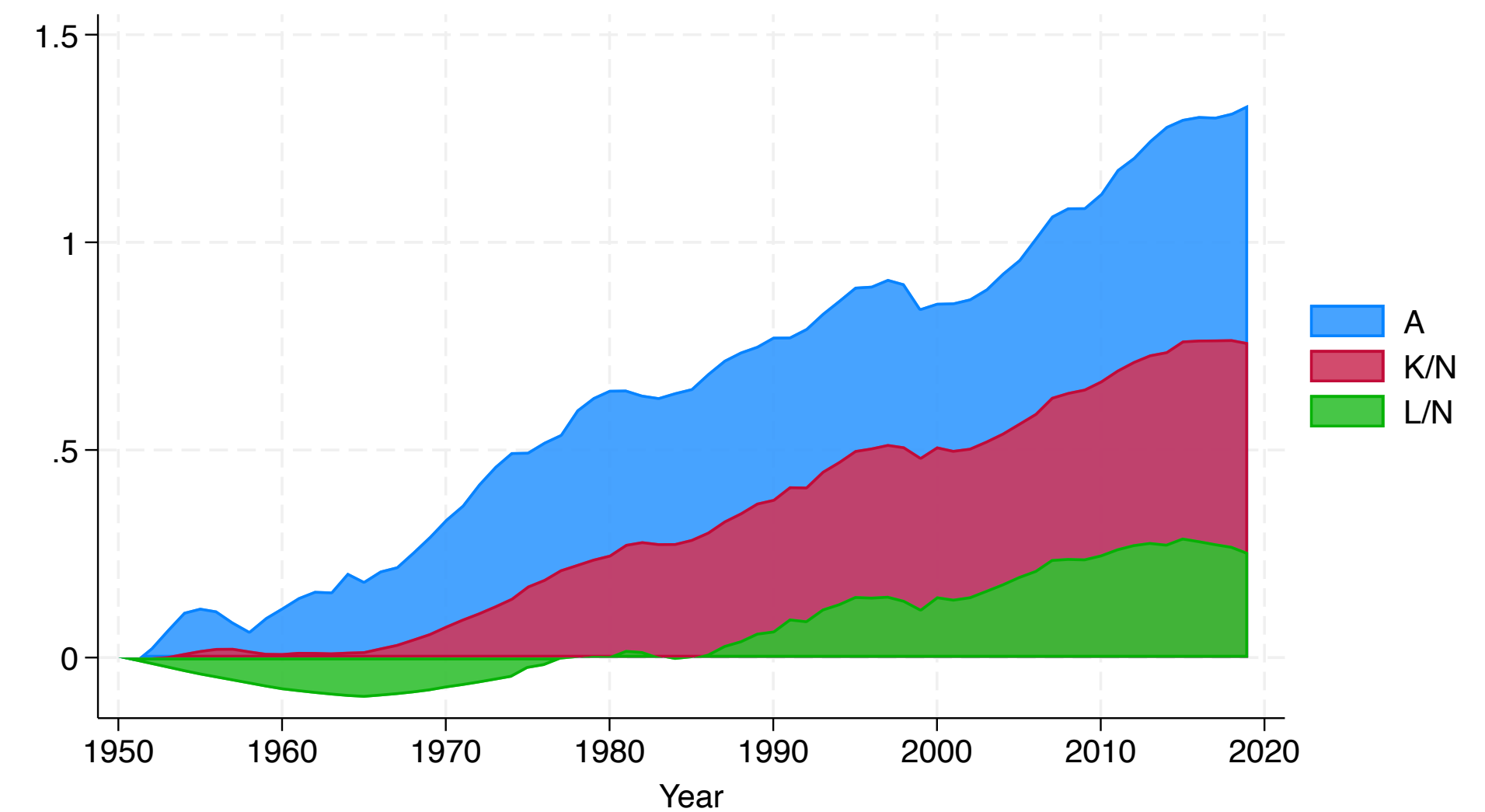
Mexico



Brazil



Colombia



Takeaway from Growth Accounting

- In almost all countries, the predominant driver of growth is TFP
- Capital is also important
- Labor seems to matter less

Looking Ahead

- We have learned two accounting tools
- **Development accounting:**
Cross-sectional decomposition of difference in GDP per capita
- **Growth accounting:**
Time-series decomposition of growth in GDP per capita
- Both exercises suggest that
 1. important role of K
 2. even more important role of A
- Next lectures develop theories that determine K and A