# Unpacking Aggregate Welfare in a Spatial Economy

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#### Motivation

- How do spatially disaggregated shocks affect aggregate welfare?
- Recent developments in quantitative spatial equilibrium models
  - Highly complex and parameterized
  - Obscuring sources of welfare gains/losses
- Alternative: first-order approximation (Hulten, 1978; Fogel, 1964)
  - Frictionless representative agent economy  $\Rightarrow$  revenue is a sufficient stat
- Unclear whether or how this approach extends to spatial economy

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  - (ii) MU dispersion
  - (iii) Fiscal externality
  - (iv) Technological externality
  - (v) Redistribution

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- Conclude with application(s) to the US economy

# Model

#### Environment

- $\blacksquare$  Many locations indexed by i, j
- lacksquare Many households types indexed by heta with mass  $\ell^{ heta}$ 
  - endowed with a unit of labor
  - decides where to live
  - endowed with shares on fixed factors  $\{h_j\}$
- lacksquare Many tradable intermediate goods indexed by k

#### Households

Utility from living in location j:

$$u_j^{\theta}(C_j^{\theta}) + \epsilon_j^{\theta}$$

- Preference shocks are additively separable (come back later)
- The case with  $\epsilon_{i}^{\theta}=0$  corresponds to Rosen-Roback
- Budget constraint:

$$P_j^{\theta} C_j^{\theta} = w_j^{\theta} + T_j^{\theta} + \Pi^{\theta}$$

- Households choose living locations j that maximize utility
- Let  $\mu_j^{\theta}$  be choice probability and  $l_j^{\theta}=\mathscr{E}^{\theta}\mu_j^{\theta}$  be population size of type  $\theta$
- Transfers satisfy government budget,  $\sum_{\theta} \sum_{i} T_{j}^{\theta} l_{j}^{\theta} = 0$

#### Firms

Intermediate goods k produced in i and sold in j:

$$y_{ij,k} = \mathcal{A}_{ij,k} f_{ij,k} \left( \{l_{ij,k}^{\theta}\}_{\theta}, h_{ij,k}, \{x_{ij,k}^{l,m}\}_{l,m} \right)$$

- $\mathcal{A}_{ij,k}$ : TFP (includes trade costs)
- Final goods in location j:  $\mathscr{C}^{\theta}_{j}(\{c_{ij,k}^{\theta}\}_{i,k})$
- TFP is subject to agglomeration externality:  $\mathcal{A}_{ij,k} = A_{ij,k} g_{ij,k} (\{l_i^{\theta}\}_{\theta})$

$$\gamma_{ij,k}^{\theta} \equiv \frac{\partial \ln g_{ij,k}(\{l_i^{\theta}\}_i)}{\partial \ln l_i^{\theta}}$$

Non-labor income is  $\Pi^{\theta} = \alpha^{\theta} \sum_{i} r_{j} \bar{h}_{j}$ 

## Aggregate Welfare

Competitive equilibrium: households and firms optimize and markets clear

Define aggregate welfare as

$$W = \mathcal{W}(\{W^{\theta}\}_{\theta}), \qquad W^{\theta} = \mathbb{E}\left[\max_{j} \{u_{j}(C_{j}^{\theta}) + \epsilon_{j}\}\right]$$

Local welfare weights attached to  $\theta$ :

$$\Lambda^{\theta} \equiv \frac{\partial \mathcal{W}(\{W^{\theta}\}_{\theta})}{\partial W^{\theta}} \frac{1}{l^{\theta}}$$

## Suboptimality of Spatial Equilibria

- First best: max W subject to resource constraints
- Spatial equilibrium does not solve first-best
  - 1. Agglomeration externality (well understood)
  - 2. Spatial dispersion in marginal utility of income (Mirleese, 1972)
    - Incomplete market to insure against uncertainty in location choice
    - Lack of redistribution for households with differing location choices
- Suboptimality arises even without preference shocks or externality
- Implication: Hulten's theorem does not apply

## Experiment

lacksquare Cross-sectional moments across j conditional on heta

$$\mathbb{E}_{j|\theta}[X_j^{\theta}] \equiv \sum_j \mu_j^{\theta} X_j^{\theta}, \qquad \mathbf{Cov}_{j|\theta} \left( X_j^{\theta}, Y_j^{\theta} \right) \equiv \mathbb{E}_{j|\theta}[X_j^{\theta} Y_j^{\theta}] - \mathbb{E}_{j|\theta}[X_j^{\theta}] \mathbb{E}_{j|\theta}[Y_j^{\theta}]$$

 $\blacksquare$  Cross-sectional moments across  $\theta$ 

$$\mathbb{E}_{\theta}[X^{\theta}] \equiv \sum_{\theta} \mathscr{C}^{\theta} X^{\theta}, \qquad \mathsf{Cov}_{\theta} \left( X^{\theta}, Y^{\theta} \right) \equiv \mathbb{E}_{\theta}[X^{\theta} Y^{\theta}] - \mathbb{E}_{\theta}[X^{\theta}] \mathbb{E}_{\theta}[Y^{\theta}]$$

- Consider arbitrary shocks to  $\{d \ln A_{ij,k}\}$  and/or  $\{dT_j^{\theta}\}$
- lacksquare How does aggregate welfare W respond?

$$dW = \sum_{i,j,k} p_{ij,k} y_{ij,k} d \ln A_{ij,k} + \mathbb{E}_{\theta} \left[ \mathsf{Cov}_{j|\theta} \left( -\frac{P_j^{\theta}}{u_j^{\theta'}(C_j^{\theta})}, u_j^{\theta'}(C_j^{\theta}) \right) dC_j^{\theta} \right]$$

(i) Technology  $(\Omega_T)$ 

(ii) MU dispersion  $(\Omega_{MU})$ 

$$+ \quad \mathbb{E}_{\theta} \left[ \mathsf{Cov}_{j|\theta} \left( -T_{j}^{\theta}, d \ln l_{j}^{\theta} \right) \right] \quad + \quad \mathbb{E}_{\theta} \left[ \mathsf{Cov}_{j|\theta} \left( \frac{1}{l_{j}^{\theta}} \sum_{l,k} p_{jl,k} y_{jl,k} \times \gamma_{jl,k}^{\theta}, d \ln l_{j}^{\theta} \right) \right]$$

(iii) Fiscal externality  $(\Omega_{FE})$ 

(iv) Technological externality  $(\Omega_{TE})$ 

$$+ \quad \mathsf{Cov}_{\theta} \left( \Lambda^{\theta} - \mathbb{E}_{j|\theta} \left[ \frac{P_{j}^{\theta}}{u_{j}^{\theta'}(C_{j}^{\theta})} \right], \mathbb{E}_{j|\theta} \left[ u_{j}^{\theta'}(C_{j}^{\theta}) dC_{j}^{\theta} \right] \right)$$

$$dW = \sum_{i,j,k} p_{ij,k} y_{ij,k} d \ln A_{ij,k}$$

(i) Technology (ar)

Direct impact absent reallocation (Hulten)

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$$+ \mathbb{E}_{\theta} \left[ \mathsf{Cov}_{j|\theta} \left( -T_j^{\theta}, d \ln l_j^{\theta} \right) \right]$$

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## Van Result

$$dW = \sum_{i,j,k} p_{ij,k} y_{ij,k} d \ln A_{ij,k}$$

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(i) Technology  $(\Omega_T)$ 

(ii) MU dispersion (Ω)

#### Changes in MU dispersion

- Positive if  $dC_i \uparrow$  in places with high  $u_i^{\theta'}(C_i^{\theta})/P_i^{\theta}$
- Absent if

1. 
$$u_j^{\theta}(C) = C \text{ and } P_j^{\theta} = P^{\theta}$$

2. 
$$u_j^{\theta}(C) = \log C$$
 and  $w_j^{\theta} + T_j^{\theta} = I^{\theta}$ 

3. No preference shocks

 $(\Omega_{TE})$ 

$$dW = \sum_{i,j,k} p_{ij,k} y_{ij,k} d \ln A_{ij,k} + \mathbb{E}_{\theta} \left[ \mathsf{Cov}_{j|\theta} \left( -\frac{P_j^{\theta}}{u_j^{\theta'}(C_j^{\theta})}, u_j^{\theta'}(C_j^{\theta}) \right) dC_j^{\theta} \right]$$

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(i) Technology (2)

(ii) MU dispersion  $(\Omega_{MU})$ 

$$+ \left[\mathbb{E}_{\theta} \left[ \mathsf{Cov}_{j|\theta} \left( -T_{j}^{\theta}, d \ln l_{j}^{\theta} \right) \right] \right] + \mathbb{E}_{\theta} \left[ \mathsf{Cov}_{j|\theta} \left( \frac{1}{l_{j}^{\theta}} \sum_{l,k} p_{jl,k} y_{jl,k} \times \gamma_{jl,k}^{\theta}, d \ln l_{j}^{\theta} \right) \right]$$

(iii) Fiscal externality  $(\Omega_{FE})$ 

(iv) Technological externality  $(\Omega_{TE})$ 

Changes in government budget Positive if  $d \ln l_i^{\theta} \uparrow$  in places with low  $T_i^{\theta}$ 

$$dW = \sum_{i,j,k} p_{ij,k} y_{ij,k} d \ln A_{ij,k} + \mathbb{E}_{\theta} \left[ \mathsf{Cov}_{j|\theta} \left( -\frac{P_j^{\theta}}{u_j^{\theta'}(C_j^{\theta})}, u_j^{\theta'}(C_j^{\theta}) \right) dC_j^{\theta} \right]$$

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Positive if  $d \ln l_j^{\theta} \uparrow$  in places with high  $\gamma_{jl,k}^{\theta}$   $\gamma_{jl,k}^{\theta}$  Constant elasticity  $\gamma$  does not imply  $\Omega_{TE} = 0$ 

$$dC_j^{\theta}$$

$$+ \quad \mathbb{E}_{\theta} \left[ \mathsf{Cov}_{j|\theta} \left( -T_{j}^{\theta}, d \ln l_{j}^{\theta} \right) \right] \quad + \quad \mathbb{E}_{\theta} \left[ \mathsf{Cov}_{j|\theta} \left( \frac{1}{l_{j}^{\theta}} \sum_{l,k} p_{jl,k} y_{jl,k} \times \gamma_{jl,k}^{\theta}, d \ln l_{j}^{\theta} \right) \right]$$
(iii) Fiscal externality  $(\Omega_{FE})$ 

(iv) Technological externality (a)

$$+ \quad \mathsf{Cov}_{\theta} \left( \Lambda^{\theta} - \mathbb{E}_{j|\theta} \left[ \frac{P_{j}^{\theta}}{u_{j}^{\theta'}(C_{j}^{\theta})} \right], \mathbb{E}_{j|\theta} \left[ u_{j}^{\theta'}(C_{j}^{\theta}) dC_{j}^{\theta} \right] \right)$$

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Redistribution

Positive if  $dC_j^{\theta} \uparrow$  for types with high  $\Lambda^{\theta}$ 

(iii) Fiscal externality  $(\Omega_{FE})$ 

$$\sum_{l\theta} p_{jl,k} y_{jl,k} \times \gamma_{jl,k}^{\theta}, d \ln l_j^{\theta}$$

(iv) Technological externality  $(\Omega_{TE})$ 

$$+ \left(\operatorname{Cov}_{\theta}\left(\Lambda^{\theta} - \mathbb{E}_{j|\theta}\left[\frac{P_{j}^{\theta}}{u_{j}^{\theta'}(C_{j}^{\theta})}\right], \mathbb{E}_{j|\theta}\left[u_{j}^{\theta'}(C_{j}^{\theta})dC_{j}^{\theta}\right]\right)$$

## Second-Best Spatial Transfer Formula

- Optimal  $T_j \Rightarrow dW = 0$  with respect to perturbations  $\{dT_j\}$
- Rearranging, we obtain non-parametric second-best spatial transfer formula:

$$\mu_{j}^{\theta} \left[ \Lambda^{\theta} u_{j}^{\theta'}(C_{j}^{\theta}) - P_{j}^{\theta} \right] = \sum_{i} \frac{\partial \mu_{i}^{\theta}}{\partial C_{j}^{\theta}} \left[ T_{i}^{\theta} - \frac{1}{l_{i}^{\theta}} \sum_{l,k} p_{il,k} y_{il,k} \gamma_{il,k}^{\theta} \right]$$

- LHS: marginal benefit of transferring to location j
  - equalize MU
- **RHS**: marginal cost of transferring to location *j* 
  - fiscal and technological externalities
- Strict generalization of Fajgelbaum-Gaubert (2020)
- Tight link to Bailey-Chetty optimal UI formula

## Hulten in a Spatial Economy

Suppose optimal spatial transfers are implemented, then

$$dW = \sum_{i,j,k} p_{ij,k} y_{ij,k} d \ln A_{ij,k}$$

$$i,j,k$$
(i) Technology  $(\Omega_T)$ 

- Hulten's characterization holds despite the economy being second-best
- $\blacksquare$  This is precisely because transfers are set so that  $\Omega_{MU}+\Omega_{FE}+\Omega_{TE}+\Omega_{R}=0$

# Identification of Marginal Utility

- lacksquare Marginal utility across space,  $u_j^{\theta'}(C_j^{\theta})$ , is a key statistic in welfare evaluation
- Can it be non-parametrically identified from the location choice data?
  - $\Rightarrow$  Yes, as long as  $\epsilon_j^{\theta}$  is additive separable (Allen-Rehbeck, 2019)
- What if  $\epsilon_j^{\theta}$  is not additive?
- **Result:** If utility is  $\tilde{e}_j^{\theta} \tilde{u}_j^{\theta}(C_j^{\theta})$  and  $\{\tilde{e}_j^{\theta}\}$  follows Frechet with arbitrary correlation (GEV)  $\Rightarrow$  positive and normative predictions isomorphic to  $\log \tilde{u}_j^{\theta}(C_j^{\theta}) + \log \tilde{e}_j^{\theta}$
- Without multiplicative Frechet, identification is not possible...
   ... but GEV approximates arbitrary discrete choice system
- Welfare changes can be non-parametrically identified in a broad class of models

# Application: "Ex-post" Welfare Evaluation

#### "Ex-Post" Welfare Evaluation

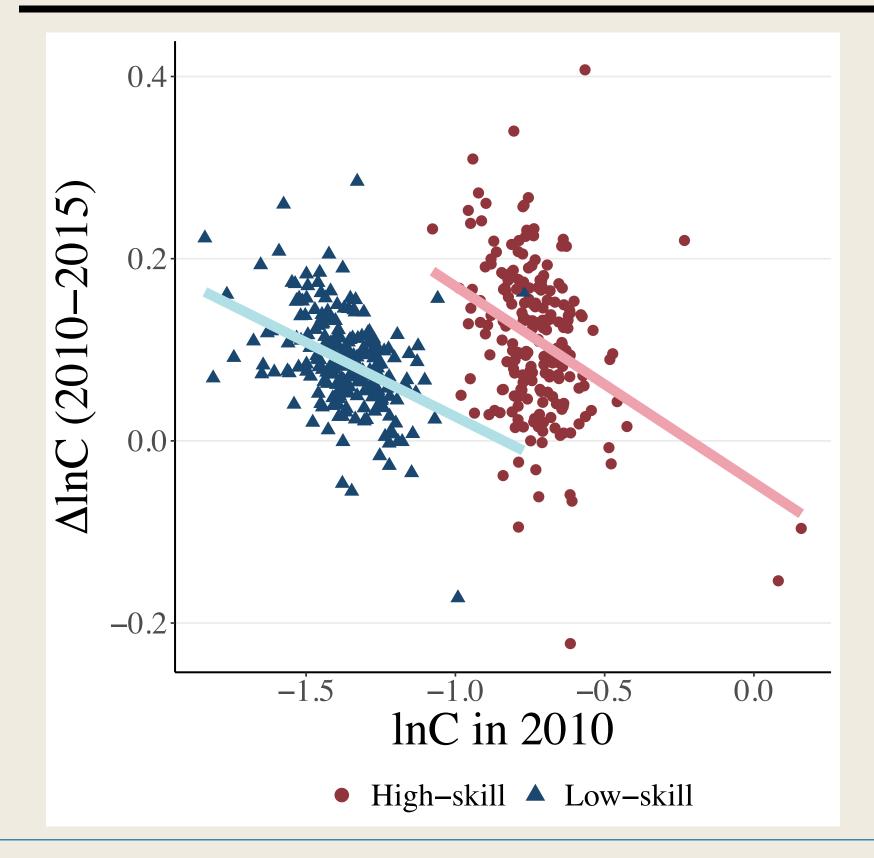
- Study welfare changes in the US 2010-2019
  - 214 MSAs
  - Two skill types (college, non-college)
- Obtain  $l_j^{\theta}$  and  $C_j^{\theta} \equiv (w_j^{\theta} + T_j^{\theta})/P_j^{\theta}$  from the data
- Take values of  $\{\gamma_{ij,k}^{\theta}\}$  from Fajgelbaum-Gaubert (2020)
- Estimate utility function,  $u(C) = \frac{C^{1-\rho_{\theta}}}{1-\rho_{\theta}}$  using shift-share IV and GMM
  - Our estimates:  $\rho_{\theta} = 1.52$  for low-skill and  $\rho_{\theta} = 1.29$  for high-skill
- Obtain  $\Omega_T = \sum_{i,j,k} p_{ij,k} y_{ij,k} d \ln A_{ij,k}$  as Solow residual (adjusted for agglomeration)
- Assume utilitarian  $\Lambda^{\theta} = 1$

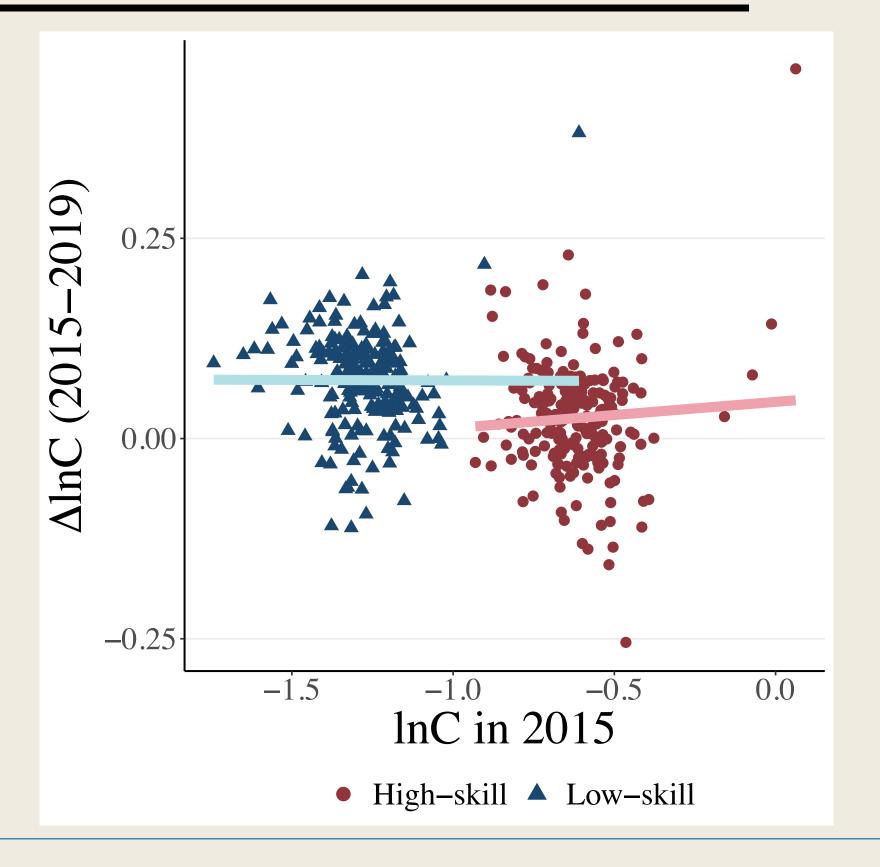
### **Ex-Post Evaluation in the US**

	dW	$\Omega_T$	$\Omega_{MU}$	$\Omega_{FE}$	$\Omega_{TE}$	$\Omega_R$
2010-2015	2.247%	2.043%	0.136%	0.022%	0.014%	0.033%
2015-2019	1.843%	1.354%	-0.003%	0.009%	-0.073%	0.556%

## **Ex-Post Evaluation in the US**

	dW	$\Omega_T$	$\Omega_{MU}$	$\Omega_{FE}$	$\Omega_{TE}$	$\Omega_R$
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## Summary

Theory to unpack source of welfare gains/losses in a spatial economy

- Exact decomposition of welfare changes into five terms
- Non-parametric optimal spatial transfer formula
- Hulten is recovered when optimal spatial transfer policy is in place
- Non-parametric identification of welfare changes

# Application: "Ex-ante" Welfare Evaluation

#### "Ex-Ante" Welfare Evaluation

- Study welfare changes in response to shocks using Allen-Arkoakis (2022) model
  - One-type
  - log-utility and Armington
  - Route choice and congestion in shipments
  - No spatial transfers
- 228 MSAs and 704 links in the U.S.
- Two experiments:
  - 1. reduce exogenous component of trade cost by 1%
  - 2. reduce productivity by 1%

### **Ex-Ante Welfare Evaluation**

	Dependent Variable:							
	$\Omega_T$	$\Omega_{MU}$	$\Omega_{TE,S}$	$\Omega_{TE,A}$	$\Omega_{Resid}$			
Panel A. Transportation Infrastructure Improvements								
$\Delta W$	2.04	-0.03	-1.03	0.01	0.02			
R-squared	0.767	0.004	0.479	0.004	0.657			
Panel B. Productivity Shocks								
$\Delta W$	1.08	-0.30	0.10	0.10	0.02			
R-squared	0.990	0.653	0.773	0.653	0.998			