

Particle ID performance of Liquid Argon TPC

J-PARC T32 collaboration

Abstract

This paper describes a study of particle identification performance of liquid Argon TPC (LArTPC) detector using well-defined charged particles (pions, kaons, and protons) with momentum of $800 \text{ MeV}/c$ obtained at J-PARC K1.1Br beamline.

We have build a LArTPC detector with fiducial mass of 150 kg , and injected the beam particle

Keywords:

1. Introduction

Refer [1] for hardware/beam line description

2. Data Quality

2.1. Collected Data

Table 1 shows list of the collected data while Oct/2010 Run. 800 MeV/ c pion is expected to pass-through the detector as MIP, and have uniform energy deposition to all the TPC channels. So this data set is very useful for calibrating the detector response (See section xxx). 800 MeV/ c proton stops after 15 cm of flight distance inside the TPC fiducial volume with relatively large dE/dx . So we use the proton data set for validation of the detector response at high dE/dx region(See section xxx). We have collected three different Kaon data by varying thickness of the degrader. 540, 630, 680 MeV/ c are corresponds to the momentum degraded by 2 lead glass, 1 lead glass + 1 lead block, and 1 lead glass, respectively, and such Kaon stops after 10 cm, 50 cm, and 65 cm of flight distance inside TPC fiducial volume.

Figure 1 shows an 2D display of typical event taken with 800 MeV/ c electron trigger. Horizontal axis corresponds to TPC channel number and zero means most upper stream strip. Since strip pitch is 1 cm, this is equivalent to distance from beam injection point in cm. Vertical axis corresponds to electron drift time in μs and $t=0$ means trigger timing. In this TPC, anode and cathode is located at top and bottom of the detector, respectively, $t=0$ means energy deposition at anode and longer drift time means energy deposition in lower height. With 200 V/cm of electric field, drift velocity is about 0.8 m/ms. So drift of full detector (40 cm) takes 500 μs . Color strength of the plot corresponds to the TPC signal pulse height in ADC counts which is roughly proportional to dE/dx of the track. In this event, triggered electron can be clearly seen center of the detector as an electromagnetic shower while there are two other particles accidentally overlapped with the triggered electron. Track at $t=100 \mu s$ is considered as a proton which stops after 15 cm of flight distance and has large dE/dx around the stopped point. Track at $t=400 \mu s$ is considered as a pion which passes-through the detector and has uniform dE/dx over the TPC channels. This event already gives us some idea for how good the particle identification performance of the LArTPC is.

Figure 2 shows a typical $K \rightarrow \mu\nu$ like event. We can clearly identify a kink of the track at 60 cm which is considered as stopped point of Kaon and it decays to

Energy deposition of the track is about MIP at the injection point and gradually increase towards the stopped point at 60 cm.

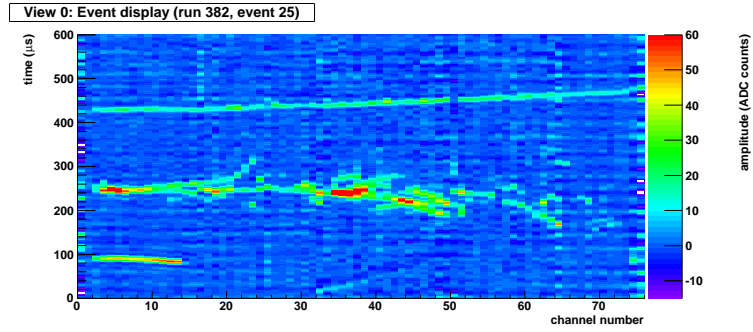


Figure 1: Event display of 800 MeV/c electron triggered event. Accidentally overlapped with a proton and a pion.

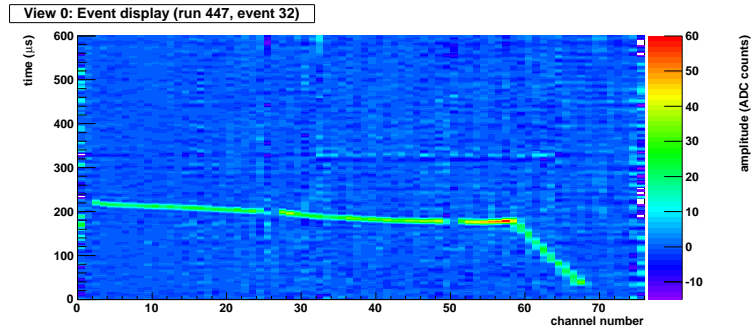


Figure 2: Event display of Kaon 630 MeV/c triggered event

Table 1: List of collected data		
Particle	Momentum (MeV/c)	Number of Events
Pion	800	3,000
Proton	800	1,500
Kaon	540 (2LG)	7,000
Kaon	630 (1LG+1LB)	40,000
Kaon	680 (1LB)	35,000
electron	800	2,500
electron	200	10,000
pion	200	10,000

2.2. Beam Quality(Purity)

We have several beam counters to identify beam particles event by event(see Fig3).Using this when taking data, we can get data of interest selectively.The following describe how to identify beam particles with the typical data including K^+ , π^+ , e^+ , p events, which have the momentum adjusted $\sim 800\text{MeV}/c$.

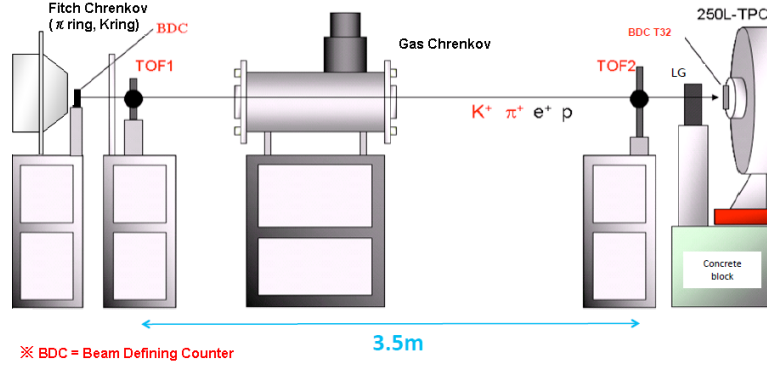


Figure 3: Instruments on K1.1BR Beam Line

Lead particles to K1.1BR beam line pass the Fitch Cherenkov Counter at first. Fitch Cherenkov Counter can select particles with differences of angle of cherenkov light which they radiate. Figure4 shows the response of the Fitch Cherenkov Counter. The horizontal axis shows the total amount of PMT signal where cherenkov light of $800\text{MeV}/c$ π can be detected. The vertical axis shows that of $800\text{MeV}/c$ K . Signals are distinctly separated to

three cluster and can be categorized as following.

1. $\text{FC}(\pi)$ Signal < 1450 & $\text{FC}(K)$ Signal > 2000
2. $\text{FC}(\pi)$ Signal < 1450 & $\text{FC}(K)$ Signal < 2000
3. $\text{FC}(\pi)$ Signal > 1450 & $\text{FC}(K)$ Signal < 2000

Apparently, particles within the region 1 are K^+ candidates. Particles within region 2 are p candidates because $800\text{MeV}/c$ p is impossible to radiate cherenkov light. Particles within region 3 are π^+ or e^+ candidates because their angle of cherenkov light are almost same level.

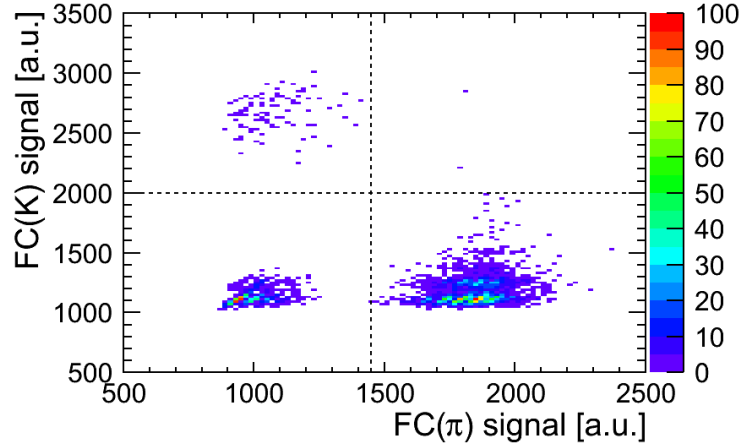


Figure 4: Fitch Cherenkov Counter

Gas Cherenkov Counter can select e^+ from the other particles because only e^+ can radiate cherenkov light at the refractive index of this gas. Figure 5 shows the response of the Gas Cherenkov Counter. The horizontal axis shows the PMT signal of the Gas Cherenkov Counter. The vertical axis shows the number of events. Fitting the pedestal with Gaussian function, the events larger than the value added $\sim 3.5\sigma$ to the mean of the pedestal is e^+ candidates. In this case, GC signal is required more than 104.7 to be e^+

particle	e^+	π^+	K^+	p
Mass(MeV)	0.511	139.57	493.68	938.27
Time of Flight(ns)	11.67	11.84	13.71	17.98

Table 2: Time of flight of each particle

candidates.

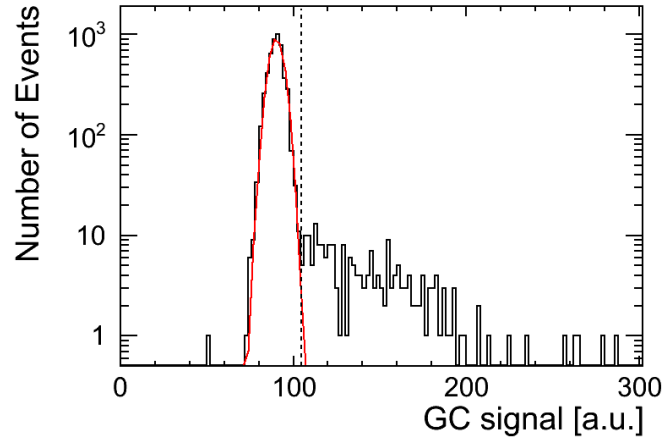


Figure 5: Gas Cherenkov Counter

There are two TOF Counters which has ~ 200 ps resolution 3.5m apart, and each particle can be selected with the difference of time of flight between them. Following table2 is calculated time of flight when each 800MeV/c particle passes two counters. As this table shows, e^+ and π^+ cannot be selected because the difference of time of flight is too short for the TOF resolution.

Figure6 shows the response of the TOF Counters. The horizontal axis shows the time of flight between TOF1 and TOF2 Counter. The vertical axis shows the number of events. The signals clearly show three distinct structures. From table2, in ascending order of time of flight, the first structure includes e^+ or π^+ candidates, the second structure includes K^+ candidates, and the third structure includes p candidates. The cut value to separate the first structure and the second structure is $\sim 4.5\sigma$ (in this case, the value is set to 13.15ns), and because the second structure and the third structure are clearly separated, the

cut value to select them is set 16.47ns fully apart from the second structure.

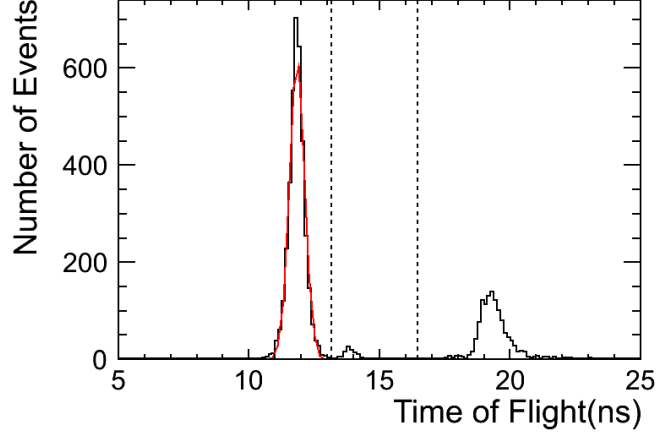


Figure 6: TOF Counter

K^+ can be selected very efficiently with Fitch Cherenkov Counter, so we require the condition $\text{FC Signal}(K)$ is more than 2000 to get K^+ events in taking data. Figure 7 shows the response of the TOF Counters before and after the above cut. The histogram which is filled with black is what is after cut. This figure shows we can get high-purity K^+ samples with this condition.

Particles which satisfy all conditions for the same candidate are identified themselves, and the others are defined ‘uncertain’ particles. Herewith, we can identify beam particles with high purity before injection to 250L detector. Table 2.2 shows the beam components of the data used for analysis.

Run 52, 55, 59 and 60 are the data required the condition $\text{FC Signal}(K)$ is more than 2000 in taking data to get K^+ events. Therefore the selection of K^+ on the analysis required by only TOF, that is, time of flight is 12.72~17.72ns, and the others are defined *uncertain*. As Table 2.2 shows, these data are almost occupied K^+ events and the ratio is ~99.2% on average.

2.3. Beam Energy

2.3.1. Kaon energy

Time resolution of TOF counters is not enough to determine Kaon beam energy. Kaon beam energy is estimated by comparing decay point distribu-

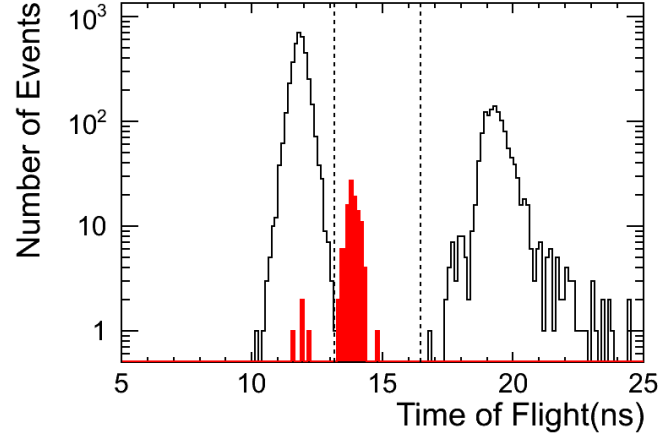


Figure 7: TOF Counter after K^+ selection

Run Number	e^+	π^+	K^+	p	<i>uncertain</i>	Number of Events
42	68	1617	27	232	5	1949
48	128	1594	78	126	11	1937
49	0	341	0	1146	12	1499
52	0	0	3169	0	34	3203
55	0	0	8534	0	66	8600
59	0	0	5900	0	50	5950
60	0	0	1899	0	13	1912

Table 3: Beam components of data used for analysis

tion of data and MC simulation as described in section 6.8.1.

2.3.2. Proton energy

Since proton mass is relatively heavy, proton energy is determined by TOF counters information. Figure 8 shows ΔTOF distribution of TOF counters. Figure 9 shows proton momentum estimated by TOF counters information.

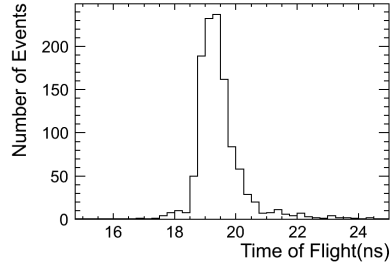


Figure 8: ΔTOF distribution of TOF counters with proton data

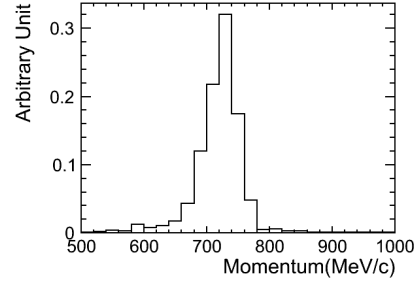


Figure 9: proton momentum estimated by ΔTOF of TOF counters information

2.4. Beam Position

We measured beam profile in front of 250LAr TPC beam window by using plastic scintillation counters. Figure 10 shows beam profile result.

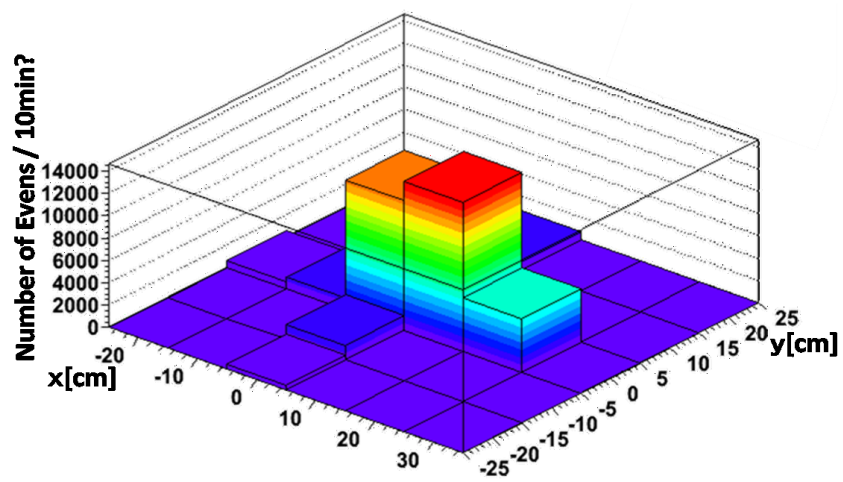


Figure 10: Beam profile on the front of 250LAr TPC

3. Software Framework

Qscan is a general purpose software package for LArTPC analysis(reference) which provides,

- event reconstruction: noise reduction, hit finding, clustering, and tracking...
- event simulation: GEANT VMC with ROOT geometry, ionization electron recombination, drift, digitization...
- event visualization: display raw data waveform and reconstructed quantities

4. Event Reconstruction

4.1. Noise Reduction

Figure 12 shows raw waveform of the TPC signal before applying any noise reduction. Two waveforms shown in this plot are channel 13 and 37 in Figure 1 which are roughly proton stopped point and electron shower maximum point, respectively. Signal-to-noise ratio for this particular case is poor and pion signal which is supposed to be $t=400 \mu s$ is almost hidden by the noise. While time width of TPC signal is few μs which is determined by drift time between anode and anode-grid, dominant noise component looks higher frequency. To reduce such noises, we have applied FFT (Fast Fourier Transformation) filter to cut the high frequency component. Figure ?? shows amplitude as a function of frequency for the same event. This clearly shows dominant noise component with > 200 kHz has good separation with signal component (< 100 kHz). Figure 13 shows the waveform after removing high frequency (> 80 kHz) component by the FFT filter. Signal-to-noise ratio is dramatically improved. On the other hand, we expect certain bias to the signal charge measurement by this filter, and it will be discussed in Section X.

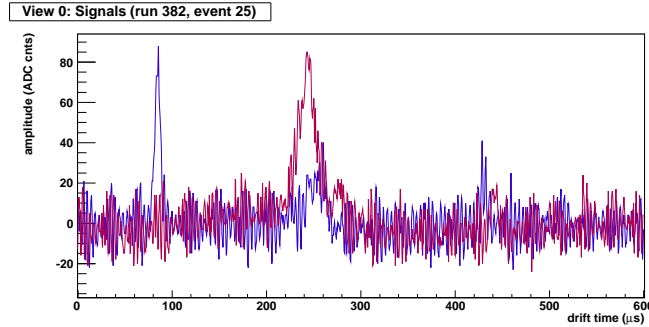


Figure 11: TPC raw signal waveform for "Textbook" event channel 13 and 37.

4.2. Hit Finding/Clustering

After noise reduction we find signal hits and create clusters associated to single tracks. Hit is defined as bump over given threshold in a channel. After finding all hits in an event, we construct cluster by merging adjacent hits. The example of hit finding and clustering is shown in Fig 14, which

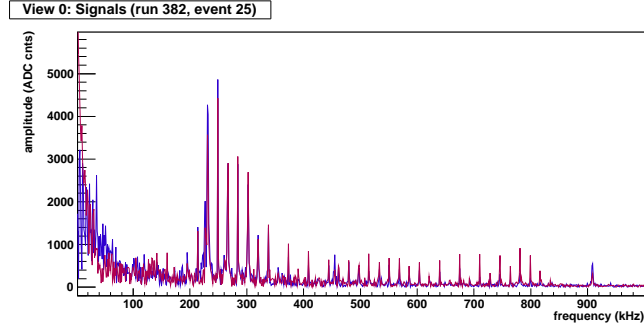


Figure 12: FFT frequency amplitude distribution

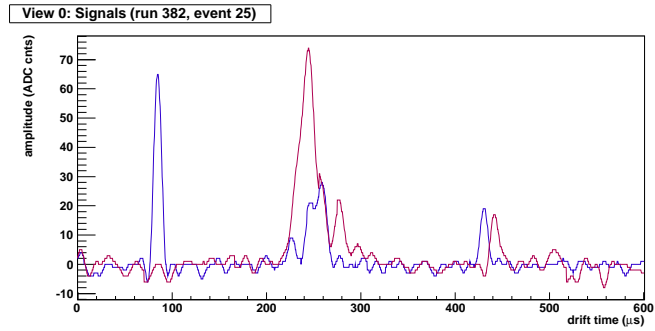


Figure 13: TPC signal waveform after cutting the frequency > 80 kHz.

indicates reasonable hit and cluster findings. Threshold of hit finding is 6 ADC counts, which is about 2.5σ from typical data noise level (as shown in Fig 12) and keeping more than 99% of Kaon hit finding efficiency from simulation. ADC count distribution is fitted by step function plus Gaussian to estimate the charge of hit in $\text{ADC} \times \mu\text{s}$ unit. Fitting $\chi^2 < 3$ and $2.5 < (\text{time width of hit}) < 8 \mu\text{s}$ are required to remove noise hits further.

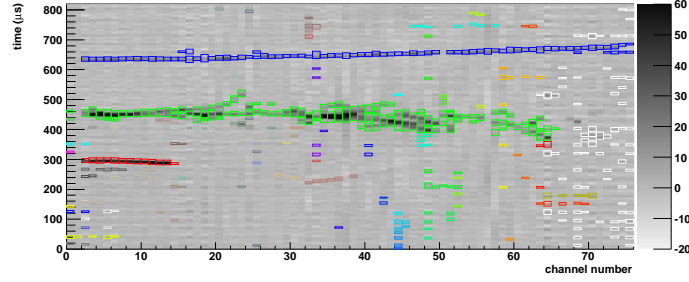


Figure 14: Example of hit finding and clustering. A colored box corresponds to a hit and colors represent different clusters.

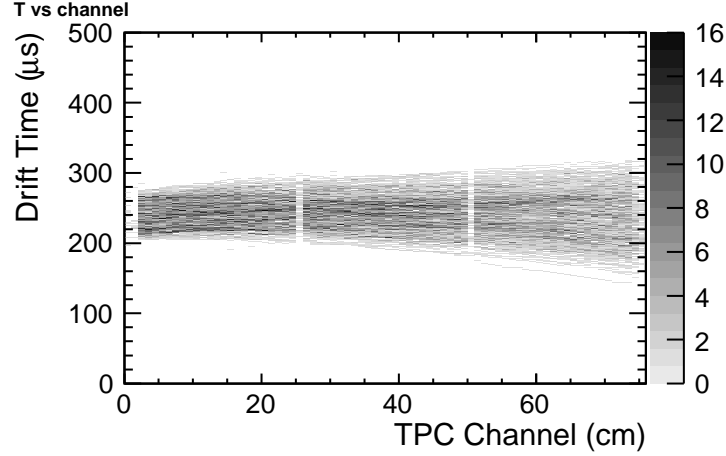


Figure 15: 800 MeV/c pion sample

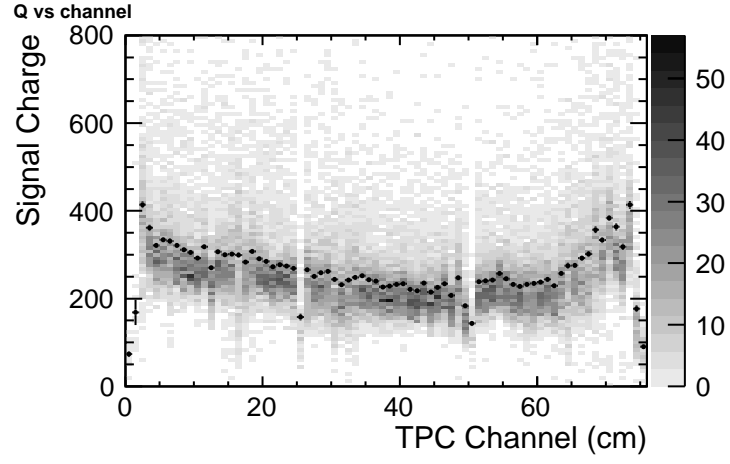


Figure 16: 800 MeV/c pion average hit charge

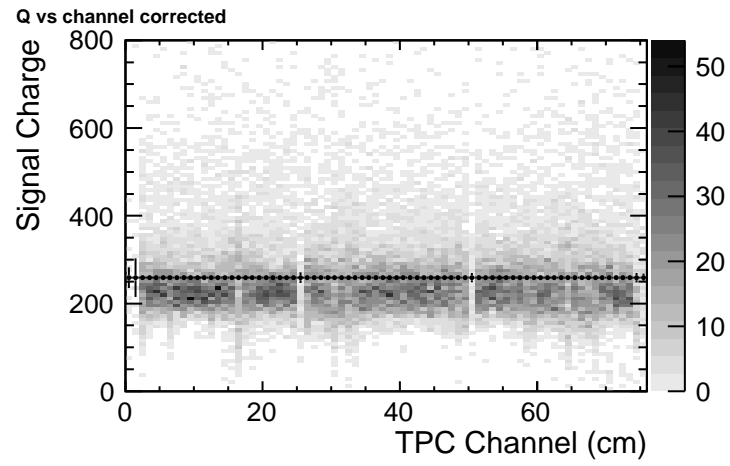


Figure 17: 800 MeV/c pion average hit charge after calibration

4.3. Stopped Point Finding

4.3.1. Proton

Figure 18 shows typical event of proton. Proton has simple structure of events because proton doesn't decay any particles. Therefore, it is easy to define stopped point. We define the hit which has the maximum channel number as stopped point. However, it should be noted that stopped point include fake hit in a proportion because of the influence of cross talk as described in section 6.6.

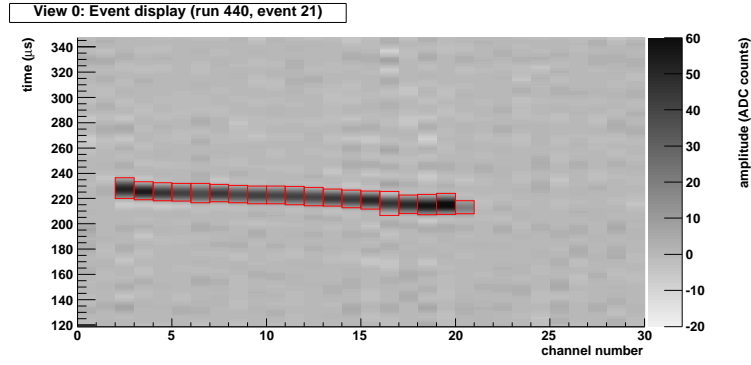


Figure 18: Typical Event Display of Proton

4.4. Stopped Kaon

Hough transform was invented for machine analysis of bubble chamber photographs by Paul.V.C.Hough.[6] We find straight lines using hough method, and find Kaon stopped point from the intersection of straight lines. Figure 19 shows hit map like a Kaon track. One point in the X-Y space can be transformed into sinusoidal curve in the ρ - θ space. Figure 20 shows sinusoidal curves in all points. And, we find the straight line associated with the largest number of points by choosing the most dense point in ρ - θ space. Next, the sinusoidal curves of the hits associated with first straight line are removed from figure 20. Figure 21 shows sinusoidal curves after the hits associated with first straight line removed. We find second straight line using the same procedure. This procedure is repeated until there are less than three points. Figure 22 shows the two straight lines found by hough transform method.

Kaon stopped point in the liquid argon detector defined as charge maximum point around the intersection of some lines.

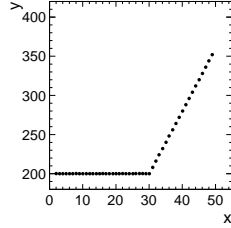


Figure 19: Hit map like a Kaon track

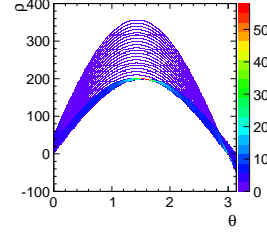


Figure 20: sinusoidal curves getting form all hough transformed points of Figure 19

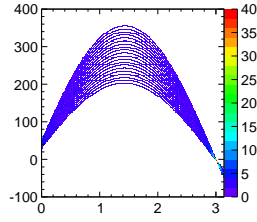


Figure 21: sinusoidal curves removed the points associated with first straight line from figure 20

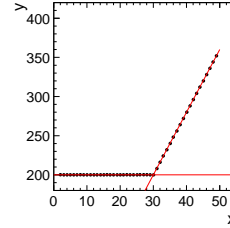


Figure 22: Two lines found with hough transform method

4.4.1. Chi2 method

χ^2 method is the algorithm that search the point of rapidly increasing fit χ^2 and the point defined as the stopped point. Because the charged particle coming from upstream of beam line, track reconstruction is started from minimum channel to the maximum channel of the cluster.

Figure 23 shows hit map like a Kaon track. We start fitting with straight line from minimum channel to maximum channel. Figure 24 shows range vs fit χ^2 distribution. As it can be noticed for figure 24, χ^2 is increased rapidly if the straight line is strayed out. Then, we search the strayed point from the straight line by setting reasonable threshold and draw from minimum channel to the strayed point. This procedure is done from maximum channel to minimum channel in the same way. And we draw from maximum channel to

the strayed point. Kaon stopped point in the liquid argon detector defined as charge maximum point around the intersection of two lines.

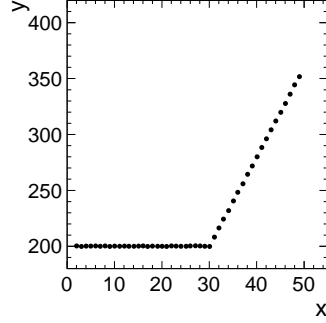


Figure 23: hit map like a Kaon track

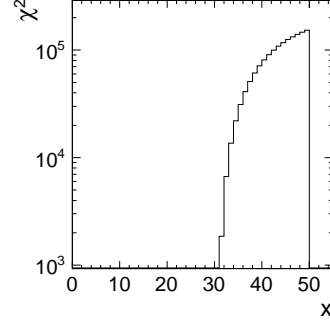


Figure 24: range vs χ^2 distribution

4.4.2. BS method

In the χ^2 method, we can't find Kaon stopped point in the case of backward decay. Then, we find Kaon stopped point using BS method. BS method is concept that the Kaon stopped point defined as lightmost channel in the case of backward decay. we describe below how the track defined as backward decay. N_1 is defined as Number of cluster hits found by the clustering. Stopped point finding is started from minimum channel. We search for the closet timing hit in next channel from current channel hit. Then, we repeat this procedure until maximum channel and count the number of selected hit information(N_2). In the case of backward decay, N_1 is larger than N_2 . So, we set reasonable threshold of the difference between N_1 and N_2 , and if the $N_1 > N_2$ is over the threshold, the track is defined as backward decay. In the case of backward decay, we defined charge maximum point around the maximum channel as the stopped point.

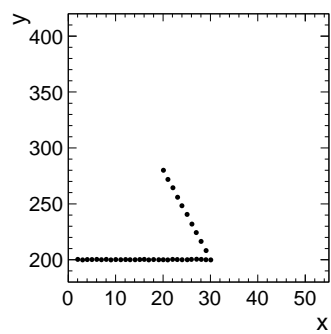


Figure 25: hit map like a Kaon track

5. Liquid Argon Purity

Attenuation of the drift electron depends on purity of LAr since electronegative impurities capture it [5]. Thus we need to apply correction to TPC signal charge depends on the drift time. We use cosmic ray sample triggered by inner PMT at off-beam timing for measuring the LAr purity, and use this to correct the beam data. Figure 26 shows an event display of typical cosmic muon event across TPC channels. The attenuation of readout charge depending on drift time is clearly seen in the right plot. Readout charge in an event cannot be fitted by exponential because energy deposition follows Landau distribution and charge readout is affected by electric field distortion which is described latter in section ??.

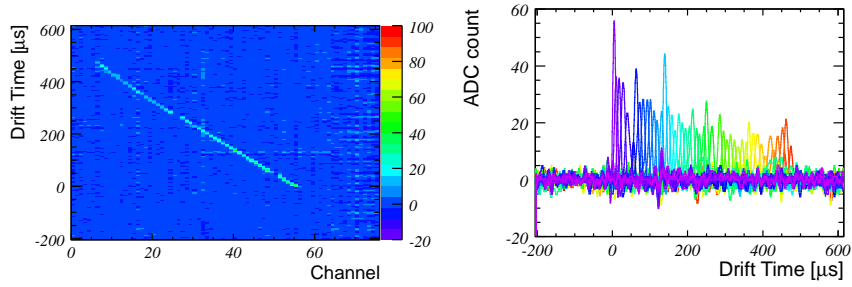


Figure 26: Left: Typical cosmic muon event across TPC channels. Right: Charge deposit as a function of drift time. Colors correspond to different TPC channels.

We select cosmic ray event with more than 20 TPC channels which corresponds to zenith angle of more than 27° and consistent with straight line by χ^2 fit. Readout charge is corrected for field distortion and projected to beam direction to correct injection angle. We fit readout charge by Landau function in each drift time bin to estimate average charge deposit. Figure 27 shows example of the average readout charge as a function of drift time which is fitted by exponential to obtain drift electron lifetime. Realistic Monte Carlo simulation shows about 13% (TBU) smaller lifetime estimation due to noise, field distortion, and FFT effects. We correct output lifetime from these effects. Figure 28 shows an drift electron lifetime as a function of duration after initial LAr filling. Drift electron lifetime was $600 \mu\text{s}$ at 60 hours, and $400 \mu\text{s}$ after 150 hours. The degradation is possibly due to impurity from micro

leak or out-gassing penetrating faster than purification by gas recirculation. But we kept enough drift electron lifetime during data taking period.

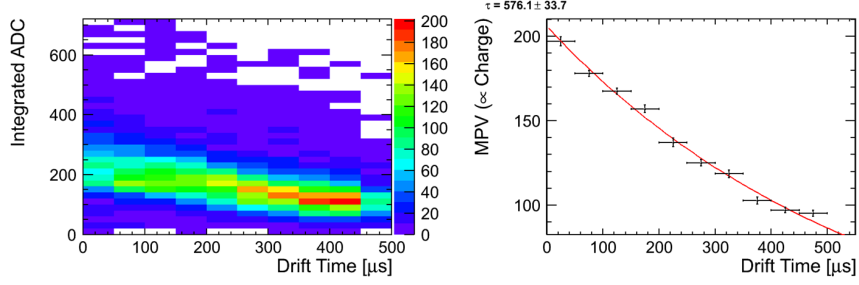


Figure 27: TBU. Left: Readout charge as a function of drift time. Readout charge in each drift time bin is fitted by landau function. Right: Average charge readout as a function of drift time which is fitted by exponential to estimate drift electron lifetime.

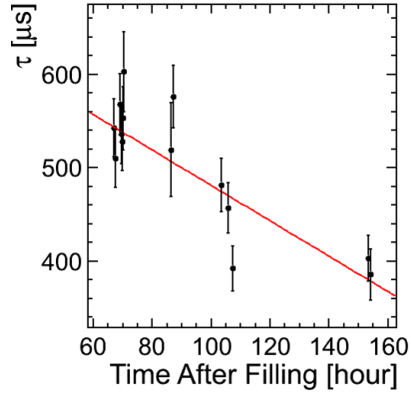


Figure 28: TBU. Drift electron lifetime as a function of duration after initial LAr filling. The lifetime is used to correct the beam data.

6. Event Simulation

6.1. *Geant3, recombination, drift velocity*

We use GEANT3 for simulating energy deposition of initial beam particles and secondary particles to LArTPC detector and beamline counters.

we set the maximum step of Geant to 0.5 mm which is enough smaller than the readout pitch of 1 cm. It means charge deposition in one strip is typically simulated with 20 GEANT steps.

We set energy cut-off for soft electron/photon emission to 10 keV which is minimum possible energy can be set in GEANT3. This cut-off is very important for ionization electron recombination.

Recombination of electron and Argon ion depends on the electric field and dE/dx . We use a measurement in Ref.[3].

$$Q = A \frac{Q_0}{1 + k dE/dx}, A = 0.800, k = 0.486 \quad (1)$$

Velocity of the drift electron depends on the liquid Argon temperature and the electric field. We use a measurement in Ref [4].

- Plot: Geant Geometry, typical track (Tanaka)
- Plot: recombination factor, drift velocity (Tanaka)

6.2. *Electric Field*

Electric field of the TPC field cage We have calculated the electric field using a 2D FEM (Finite Element Method) package [?].

This field map is used for simulating electron drift.

6.3. *Drift Electron Diffusion*

- Plot: drift simulation (Tanaka)

6.4. *Preamplifier Gain Calibration*

- Preamp gain vs channel number (Naito)

6.5. *FFT Noise*

Adding realistic noise to MC simulation is very important. In this section, we will introduce how to make realistic noise and implement to MC.

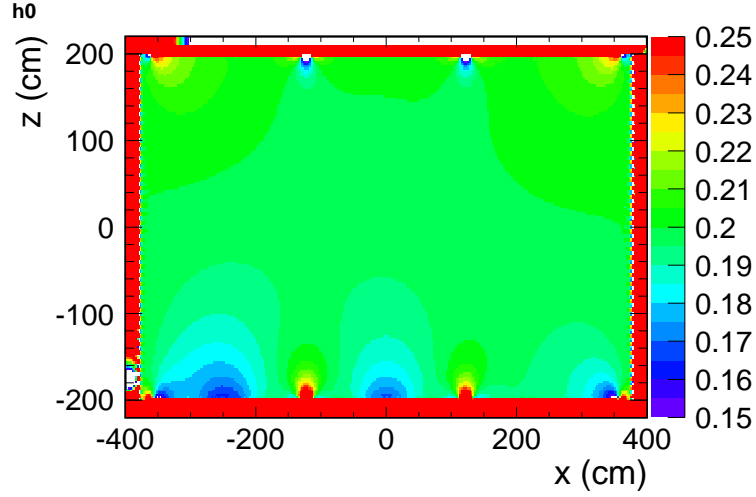


Figure 29: Electric field map obtained from 2D FEM calculation

6.5.1. Noise information of Real DATA

As a first step, we checked distribution of frequency from real data using FFT(Fast Fourier Transform)(see Fig30). Next, We got distribution of amplitude value channel by channel and frequency by frequency. Fig30 shows an example. In this event, amplitude is 200 about 400 [kHz] in 10 channel. After repeating this procedure, we could obtain histograms of amplitude value channel by channel, frequency by frequency(31). We used these histograms to reproduce realistic noise. Details are described in the next section

6.5.2. Making FFT noise

The procedure of making FFT noise is below:

1. Get amplitude from the histograms of amplitude at random.
2. Perform Inverse FFT

After performing inverse FFT, there is random noise (Fig32)which have the same distribution of frequency as real data. Real DATA have coherent noise but random noise don't have coherent components, therefore adding coherent components is necessary to reproduce realistic noise.

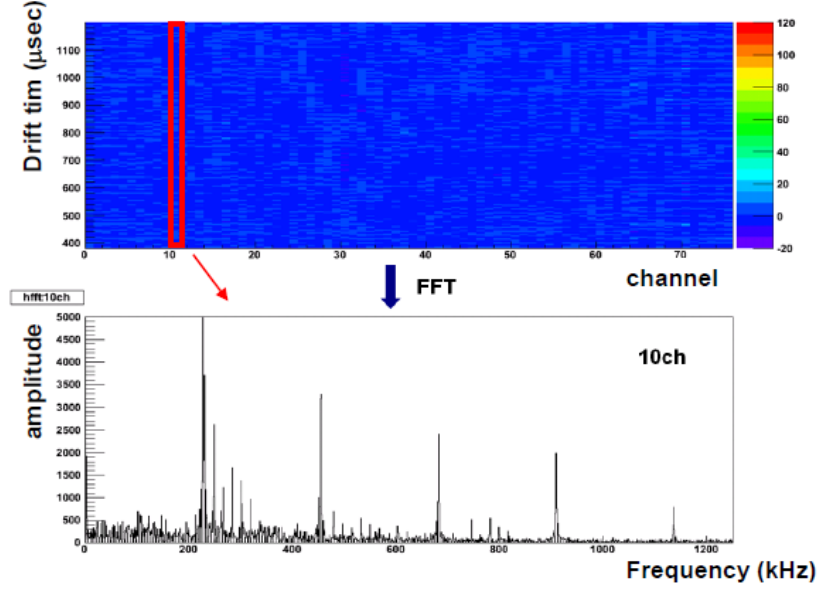


Figure 30: example distribution of frequency:10ch

3. Select random noise 0 and 32 and 64ch
4. Insert random noise 0 ch to 1-31ch, 32ch to 33-63ch, 64ch to 65-75ch
5. Scaling each channel

Real DATA look having coherent noise board by board(We used 3 readout board in T32 experiment). We chosen 3 random noise(0ch,31ch,63ch) in this reason. After that, each channel needs to be corrected as each noise scale. Fig33 shows coherent noise after scaling as Fig34. Vertical axis of Fig34 is RMS of FADC, it stands for noise level.

6.Mixing Random noise and Coherent noise.

Finally, We mixed Random noise and coherent noise as

$$Realistic\ Noise = \frac{Random\ Noise + Coherent\ Noise}{2} \quad (2)$$

- Plot: simulated event (Nagasaka)

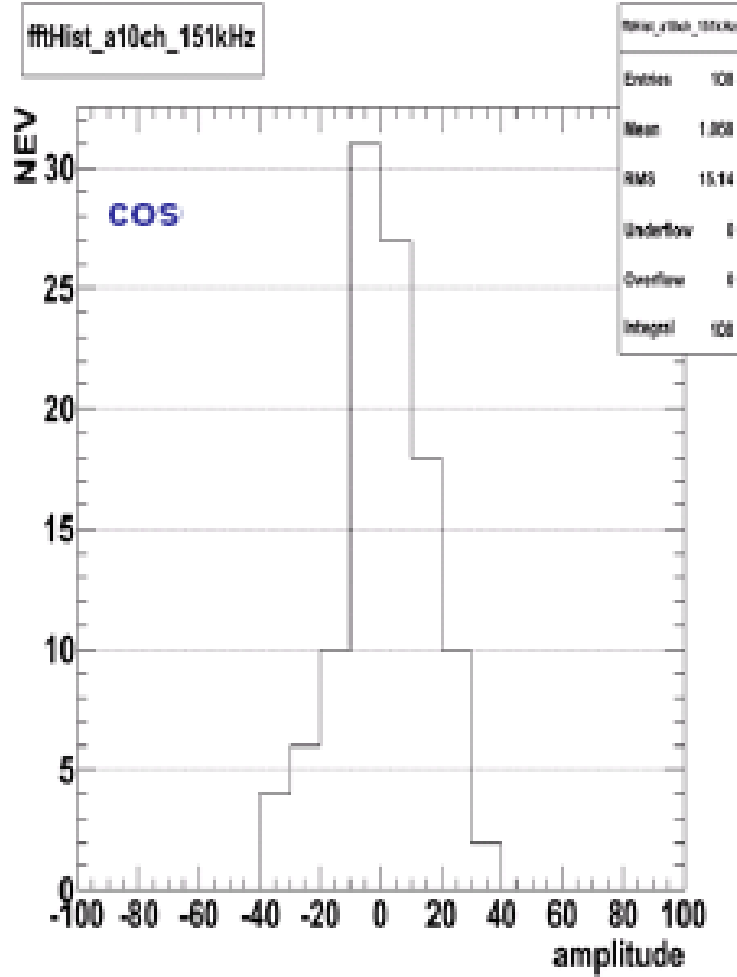


Figure 31: An example of distribution of amplitude

6.6. Cross Talk

The distance between anode channels is very short, so the influence of mutual capacitance become large and this capacitive coupling induce cross talk noise. This effect notably appears the channel where the difference of the charge between adjacents channels is large, such as the channel around stopped point of proton. Figure35 shows the signal wave form of stopped channel and the front channel of typical proton event. The signal wave form of stopped channel is differential form of the one of the front channel. This

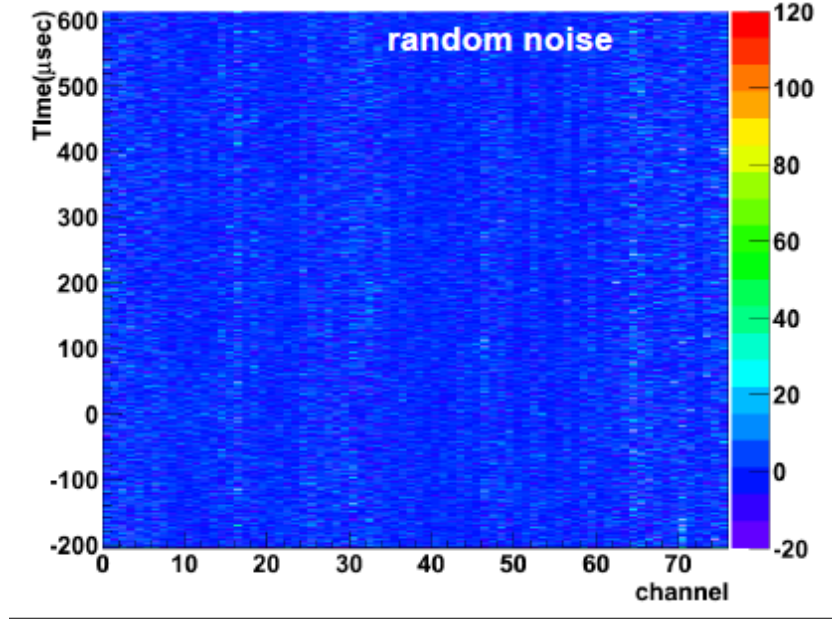


Figure 32: Random noise

shape is appeared at channel number 1 which cannot enter drifted ionization electron in electric power lines. These facts show the existence of cross talk. Then, we implement this crosstalk phenomenon in Monte Carlo Simulation by adding bipolar shape of the signal gaussian shape at adjacent channels. The area of the mountain of cross talk bipolar shape is 10.5% of the area of signal gaussian at each adjacent channel. The value of 10.5% is determined by comparing the distribution of integrated ADC at stopped channel between DATA and MC. Figure36 shows integrated ADC distribution of stopped channel. Black is DATA and blue is simulation with cross talk red is simulation without cross talk. As this figure shows, DATA and MC with cross talk is good agreement, and the value of 10.5% is reasonable.

- Plot: signal waveform (proton stopped point + 1) (A. Okamoto)
- Plot: simulated event with and without cross talk (A. Okamoto)

6.7. Signal and Noise Scale Tuning

- Plot: Landau distribution after the tuning (Tanaka)

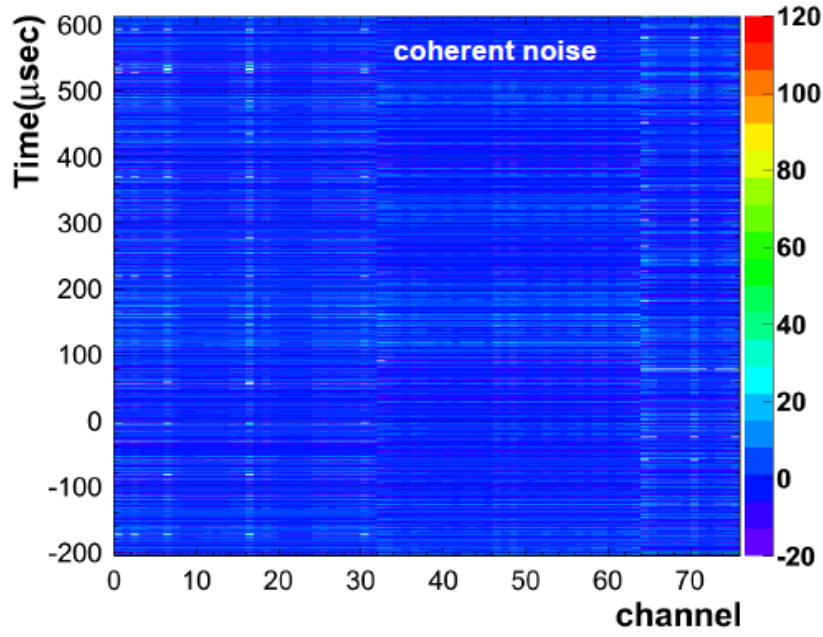


Figure 33: Coherent noise

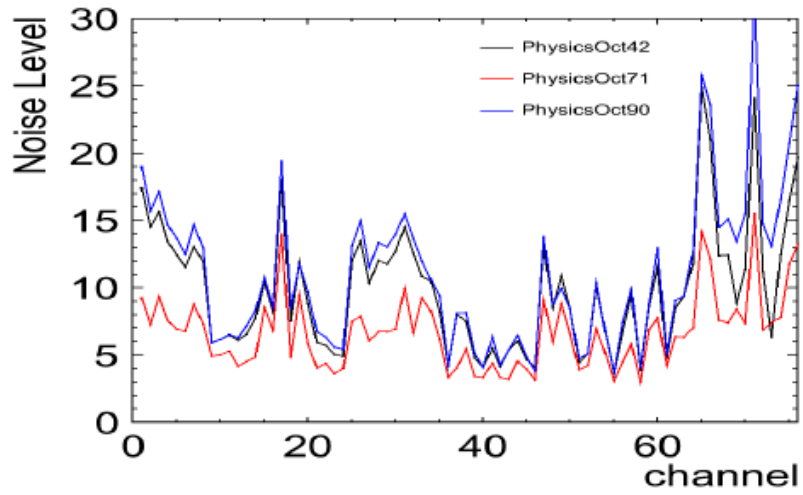


Figure 34: Noise level

6.8. Beam energy

We estimated a beam momentum using simple MC simulation. Figure 37 shows MC simulation's geometry. We generate 800MeV/ c pencil beam and

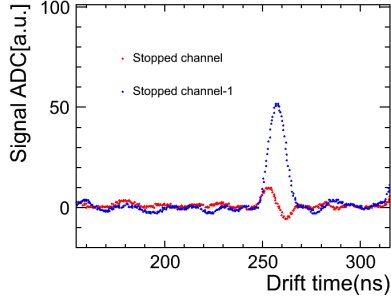


Figure 35: Signal wave form of stopped channel and the front channel

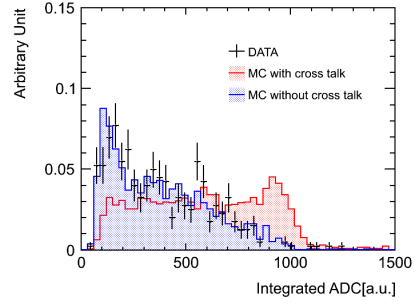


Figure 36: Integrated ADC distribution of stopped channel

shoot the beam downstream. Figure 38 shows Kaon and Pion momentum distribution using this MC simulation at BDC. Kaon beam momentum is estimated by the momentum distribution of MC simulation.

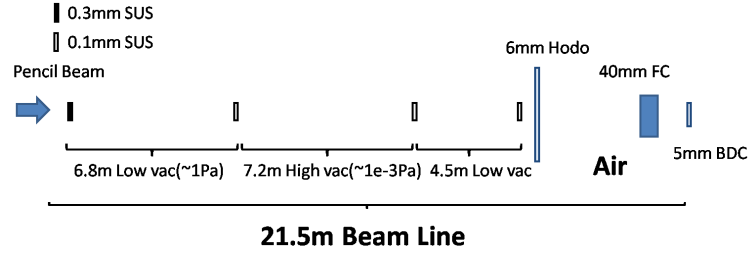


Figure 37: K1.1 Br beam line

6.8.1. Kaon energy

Kaon beam momentum is estimated by the momentum distribution of MC simulation. We change Kaon beam momentum in a range of 700 - 800 MeV/ c and search the momentum that decay point distribution of MC simulation is consistent with data one.

6.8.2. Proton energy

Proton momentum shown in Figure 9 is used as proton beam momentum of MC simulation.

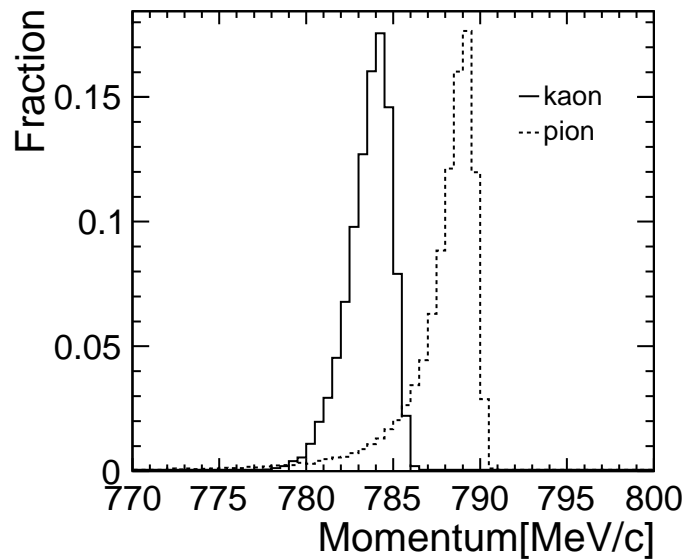


Figure 38: Kaon and Pion momentum distribution at BDC

6.8.3. Energy deposition in degrader

It is too high energy that Kaon beam stops in the fiducial volume of 250LAr TPC. In order to degrade the beam momentum, some lead glass blocks and a lead brick were inserted in front of 250LAr TPC as degrader. Figure 39 shows energy deposition distribution in degrader.

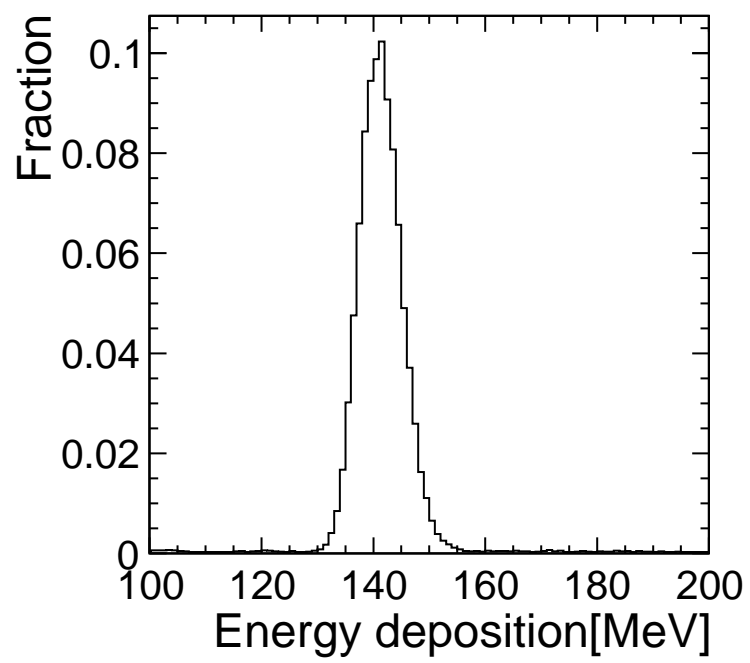


Figure 39: Energy deposition in degrader

7. Data- MC Comparison

7.1. Through-going Pion

- Plot: Data-MC comparison (Tanaka)

7.2. Stopped Proton

When we indicate the validity of charge response in high dE/dx region, proton is good sample due to its simple event structure. At the same time, we verificate the recombination factor by proton in this analysis because proton has wide dE/dx range, and this is meaningless if the charge response of MC doesn't agree with that of DATA. Therefore proton is very impotant in terms of comprehension of charge response.

First, protons are selected by the information of beam counters. Then, proton events are applied following simple selections.

1. The drift time of the hit of the minimum channel number in the cluster is between $150\mu s \sim 300\mu s$ (this time window is signal region).
2. The minimum channel number of hits in the cluster is below 2.
3. The maximum channel number of hits in the cluster is below 60.
4. The total hit number in the cluster is 5 or more.
5. The number of hits which are in the same channel is only one.

We define the events which the number of clusters in the event which passed above selections is only one as good proton events. For good proton events, we compare each paremeters of DATA and MC. Figure?? shows the comparison of the distribution of Hit Charge, Hit Sigma, Stopped Channel and Cluster Charge between DATA and MC. Table7.2 shows the comparison of the mean of these distribution.

All four distribution of MC reproduce DATA well. Especially, the agreement of stopped channel distribution indicates the success of the momentum estimation by TOF infomation because where proton stopped depends on

	DATA	MC	DATA/MC ratio
Hit Charge	607.5 ± 19.6	622.3 ± 0.8	0.9762 ± 0.0316
Hit Sigma(μ s)	3.838 ± 0.003	3.881 ± 0.002	0.9889 ± 0.0009
Stopped Channel	18.16 ± 0.20	17.72 ± 0.11	1.0247 ± 0.0132
Cluster Charge	9940 ± 407	9735 ± 59	1.0210 ± 0.0422

Table 4: Comparison of the mean of four distributions between DATA and MC

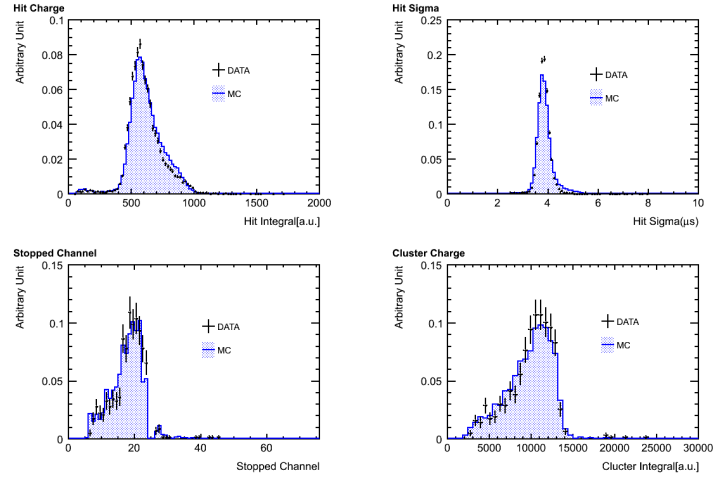


Figure 40: DATA-MC comparison of Hit Charge, Hit Sigma, Stopped Channel, Cluster Charge

the initial momentum.

Figure41 shows the integrated ADC distribution of each channel from stopped channel. The MC distribution of the channels after stopped channel are good agreements with DATA.

The left of figure42 shows the mean of the above distribution of each channel. The right of figure42 shows the ratios of DATA/MC. The ratios are suppressed within 94%~105%. From this result, we succeed in reproducing the charge response of DATA in high and wide dE/dx region.

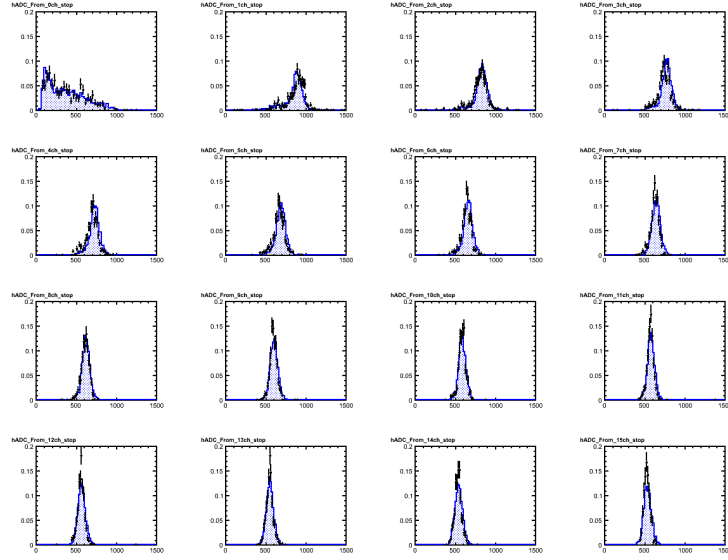


Figure 41: Integrated ADC distribution of each channel from stopped channel

7.3. Recombination Factor

Electron-ion recombination depends on the electric field and stopping power dE/dx . We study this factor using tagged proton beam. Recombination factor measurement using proton beam is relatively easy because of stability of proton. This is why we used proton beam for this study as a first step.

Expression for recombination can be derived

$$Q = A \frac{Q_0}{1 + (k/E) \times (dE/dx) \times (1/\rho)} \quad (3)$$

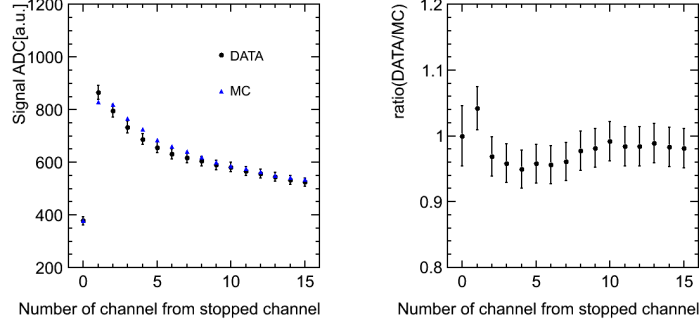


Figure 42: DATA-MC comparison of the mean of Integrated ADC distribution

where Q_0 is initial ionization charge, E is electric field, dE/dx is energy deposit per distance, ρ is density of liquid Argon, A and k are fit parameters. This formula can be rearranged like below:

$$\frac{Q_0}{Q} = \frac{1}{A} + \frac{(k/E)(dE/dx)(1/\rho)}{A} \quad (4)$$

The ratio of Q_0/Q depends on stopping power dE/dx , so we determined fit parameter A and k using proton data and Monte Carlo simulation. In this analysis, we need Q , Q_0 and dE/dx channel by channel. First, electric field E was 200 V/cm in our test. Second, Q is integrated charge in an anode readout channel. Third, Q_0 is integrated charge without recombination factor in an anode readout channel. And then, dE/dx per an anode channel is determined with truth information of Monte Carlo simulation. Figure 43, 44, 45 show Q , Q_0 , dE/dx as a function of distance from stopped channel between 1 to 14 channel. Q is obtained from data, Q_0 and dE/dx are obtained from Monte Carlo simulation. In many case, integrated charge in stopped channel are more affected by noise from next channel. This is the reason why we don't use information from stopped channel in this analysis.

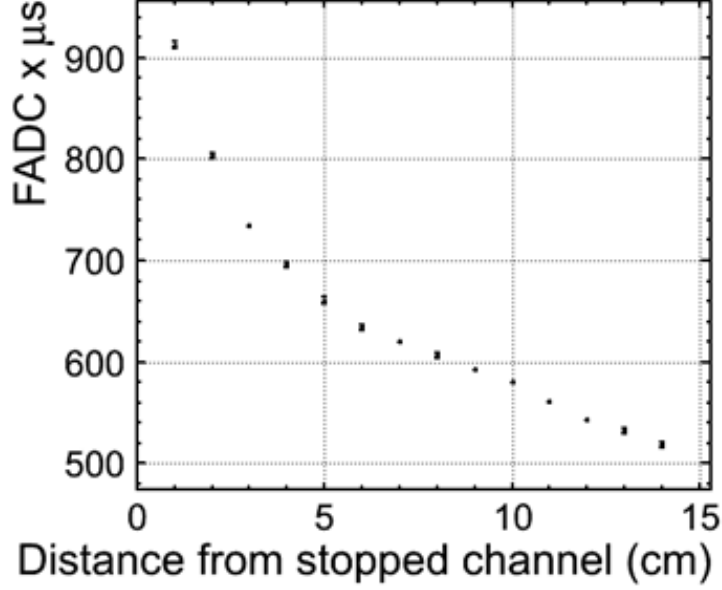


Figure 43: DATA: Integrated Flash ADC counts from stopped channel -1

The result of this study is shown in Fig46. Vertical axis is Q_0/Q , and horizontal axis is dE/dx in this figure, this plot is fitted by Birks law. As a result, we got fitting parameter

$$\begin{aligned}
 A &= 0.782 \pm 0.009 \\
 k &= 0.0467 \pm 0.0009 [kV(g/cm^2)/cm/MeV]
 \end{aligned} \tag{5}$$

We checked Birks law in the range $4 \text{ MeV}/(g/cm^2) \leq dE/dx \leq 12 \text{ MeV}/cm^2$ and the result is consistent with ICARUS experiment's one[3] in \sim sigma.

7.4. Stopped Kaon

In this section, we compare some quantities of data and MC simulation that K stops in the liquid argon detector and we can find stopped point. Figure 47 shows Data and MC comparison for signal hit charge, signal width, decay point and total particle charge distribution. Data of signal charge and signal width are consistent with MC one in error by less than two % and data

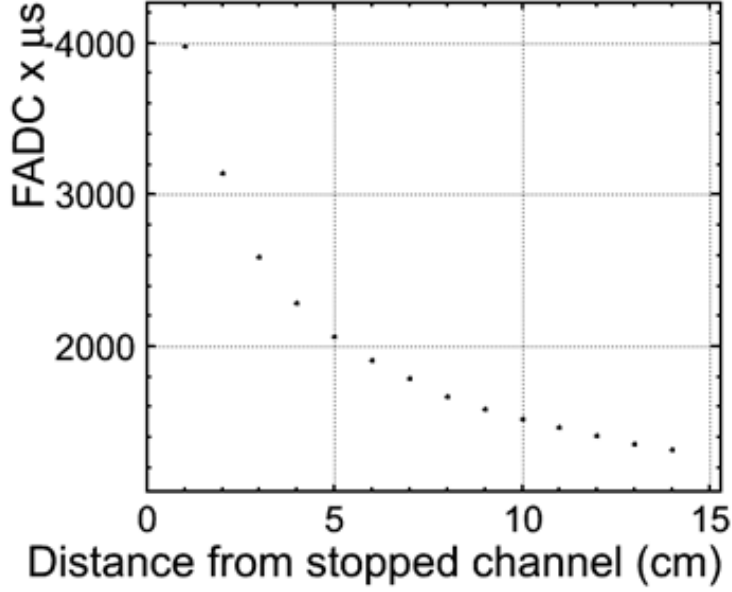


Figure 44: MC without recombination: Integrated Flash ADC counts from stopped channel -1

of cluster charge and primary charge are consistent with MC one in error by less than five %.

Figure 7.4 shows signal hit charge distribution of restricted channel 27. As shown in figure 7.4, signal charge have two peaks at 300 and 500 ADCus. Because two peaks has correlation of Δ TOF, possible assumption of the cause is that beam line were bipolarized and the beam didn't pass in the center of the detector. So, we use only the event that signal charge of restricted channel 27 is less than 350. Figure 49 shows signal hit charge distribution in different distance from the stopped point.

As shown in figure 49, data is consistent with MC one. Figure 51 shows data/MC ratio of signal hit charge distribution in different distance from the stopped point. Data of signal charge in different distance from stopped point are consistent with MC one with in 5%.

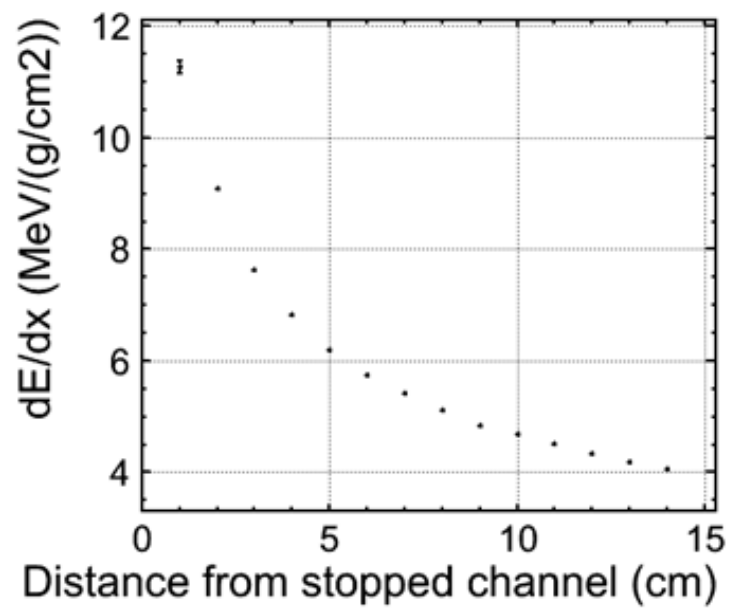


Figure 45: dE/dx from stopped channel -1

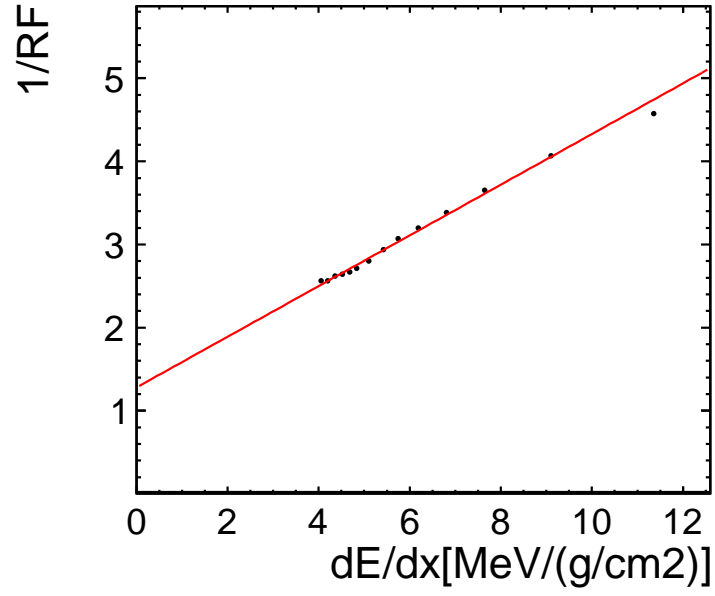


Figure 46: $1/RF$ VS dE/dx : fitted by Birks law

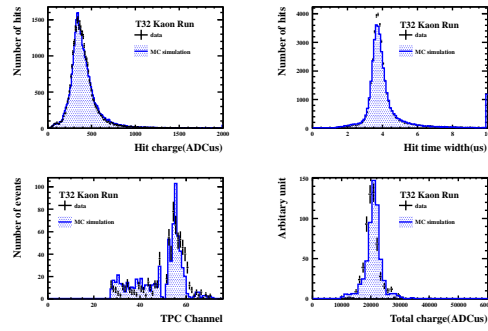


Figure 47: Data-MC comparison for hit charge, hit sigma, cluster charge, primary particle charge

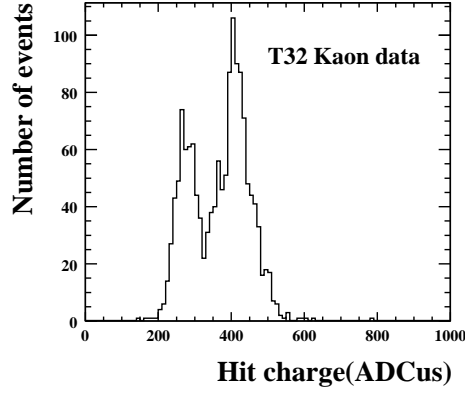


Figure 48: Hit charge in channel 27

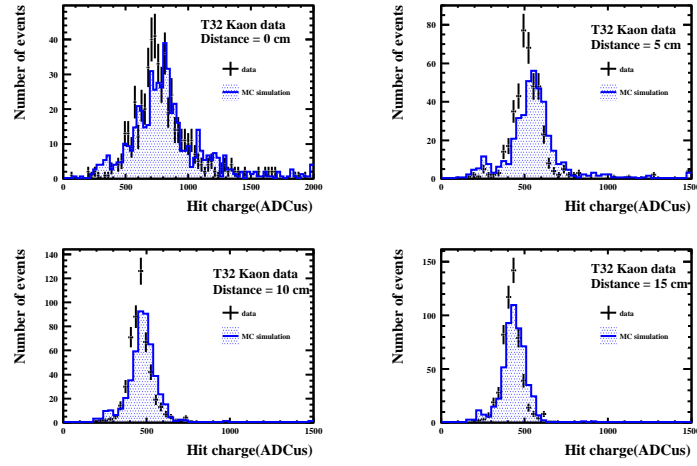


Figure 49: Data-MC comparison for hit charge distribution in different distance from the stopped point(top left:decay point,top light:decay point-5cm,bottom left:decay point-10cm,decay point-15cm)

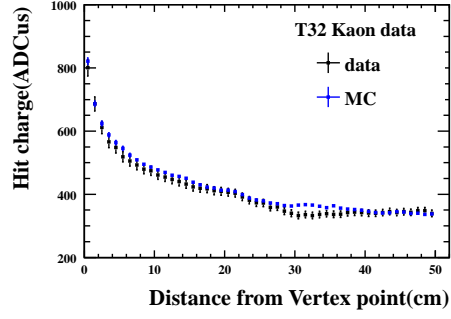


Figure 50: Data-MC comparison for hit charge distribution in different distance from the stopped point

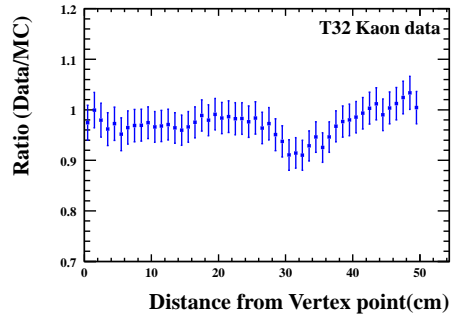


Figure 51: Data/MC ratio for hit charge distribution in different distance from the stopped point

8. Summary

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