

# Optimal Monetary and Fiscal Policy without Fiscal Backing

Masayuki Okada

NYU

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# Introduction

- The Fed is required to transfer all profits to the Treasury.
- The Treasury makes no transfer to offset the Fed's loss.
  - Expense = Interest rate (5p.p.) × Reserves (15% of GDP)
  - Fed's net loss / Treasury's tax revenue = 2%. (2022-2024)
- Asymmetric resource allocation between monetary and fiscal authorities.
- Conventional macroeconomic models assume a consolidated government budget  
(Sargent and Wallace 1981).

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# Research Question

If the government budgets are **unconsolidated**,

(= If Treasury does not provide the **optimal fiscal support** to the central bank)

does the optimal monetary-fiscal policy change?

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# What I do

## Optimal monetary and fiscal policy without commitment

As in the literature,

- Government chooses policies to maximize utility s.t. equilibrium conditions.
- NK model with the budgets of Treasury and central bank.

New

1. Two types of liabilities: Reserves as a novel ingredient. Bonds as in the literature.
2. Constraint on transfers from Treasury to central bank.

# Literature

	<b>Positive</b>	<b>Normative (Optimal Policy)</b>
<b>Consolidated</b>	Sargent and Wallace 1981 among others	Benigno and Woodford 2003 Schmitt-Grohe and Uribe 2004 among others
<b>Unconsolidated</b>	Hall and Reis 2015 Del Negro and Sims 2015 Bassetto and Sargent 2020 Amador and Bianchi 2023	<b>This paper</b>

# Literature

	Positive	Normative (Optimal Policy)
Consolidated (fiscal backing)	Sargent and Wallace 1981 among others	This paper compares the equilibrium between two regimes.
Unconsolidated (No fiscal backing)	Hall and Reis 2015 Del Negro and Sims 2015 Bassetto and Sargent 2020 Amador and Bianchi 2023	

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# What I find

Without fiscal backing,

## Monetary Policy

- The government tolerates **higher inflation** after an inflationary shock.
- **Optimally chooses not to raise** the interest rate as much as the case with fiscal backing.

## Fiscal Policy

- Tax rate is **more volatile** over the business cycle.
- The central bank is limited to helping the Treasury finance government spending.

# Model

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# Environment

- **Time.** Discrete, infinite horizon.
- **Assets.** Reserves and bonds (Differ in duration and liquidity value).
- **Agents**

**Household** consumes and works. Trades reserves and bonds. Get a convenience yield.

**Producers** are NK model, facing cost-push and productivity shock.

**Treasury** finances public expenditure by a sales tax, bonds, and remittance from central bank.

**Central bank** issues reserves for their liquidity value and buys government bonds.

# Household

$$\max_{C_t, N_t(j), B_t, D_t} E_0 \sum_{t=0}^{\infty} \beta^t \left[ \frac{1}{1-\sigma} C_t^{1-\sigma} - \frac{1}{1+\nu} N_t^{1+\nu} + \frac{\chi_1}{1-\gamma_1} \left( Q_t^C \frac{D_t}{P_t} \right)^{1-\gamma_1} + \frac{\chi_2}{1-\gamma_2} \left( Q_t^T \frac{B_t}{P_t} \right)^{1-\gamma_2} \right]$$

s.t.

$$P_t C_t + Q_t^C D_t + Q_t^T B_t = D_{t-1} + (1 + \rho Q_t^T) B_{t-1} + P_t w_t \int_0^1 N_t(j) dj + P_t \Phi_t,$$

- $D_t$  is **reserves** directly held by the household and issued by the central bank.
- $B_t$  is long-duration **bonds** with exponentially declining coupon of  $\rho^{j-1}$  in  $t+j$ .
- $\Phi$  is the firm's profit.

# Firms

- Standard set up of the adjustment cost model.

$$\max_{p_t(i)} E_0 \sum_{t=0}^{\infty} \beta^t \Lambda_t \left( \underbrace{(1 - \tau_t) p_t(i) y_t(i)}_{\text{Sales tax}} - \underbrace{\mu_t^w w_t N_t(i)}_{\text{Exogenous Cost-push shock}} - P_t \frac{\varphi}{2} \left( \frac{p_t(i)}{p_{t-1}(i)} - 1 \right)^2 Y_t \right)$$

Production function  $y_t(i) = \underbrace{A_t}_{\text{Exogenous Productivity}} N_t(i)$

Demand curve for product  $y_t(i) = \left( \frac{p_t(i)}{P_t} \right)^{-\theta} Y_t$

# Government

- Treasury's budget

Remittance from CB

$$Q_t^T B_t^T + P_t \tau_t A_t N_t + \overbrace{P_t H_t}^{\text{Remittance from CB}} = (1 + \rho Q_t^T) B_{t-1}^T + P_t G_t$$

$B^T$  is the total supply of government bonds. The government expenditure,  $G_t$ , is exogenous.

- Central Bank trades reserves and government bonds.

Remittance to Treasury

$$Q_t^C D_t + (1 + \rho Q_t^T) B_{t-1}^C = D_{t-1} + Q_t^T B_t^C + \overbrace{P_t H_t}^{\text{Remittance to Treasury}}$$

$D$  is reserves.  $B^C$  is government bonds held by Central Bank.

- **Inequality constraint on the remittance**

$$H_t \geq H^*$$

# Central Bank's Asset Purchase Policy

- Assume an exogenous asset purchase rule.

$$B_t^C = \alpha B_t^T$$

- $B^T$  is total supply of government bonds.
  - $B^C$  is government bonds held by the central bank.
  - The rest is held by the households.
  - $\alpha$  is a parameter.
- Reduces the size of the state space (4 states → 3 states).
  - The goal of Central Bank's asset purchase policy is to stabilize the financial market.

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# Equilibrium

- Market Clearing Conditions

$$(\text{Goods}) \quad A_t N_t = C_t + G_t + \frac{\varphi}{2} (\pi_t - 1)^2 A_t N_t$$

$$(\text{Government bonds}) \quad B_t + B_t^C = B_t^T$$

# Government's problem under discretion

- The government simultaneously chooses both monetary and fiscal policy.
  - Policies: Two liabilities, their prices, tax on sales, and remittance.
- The government maximizes HH utility taking as given policy functions of HH and firms.
  - State variables: Shock, reserves, and bonds.
- Define **the unconsolidated regime** and **the consolidated regime**.
  - In the unconsolidated regime, the government faces a constraint on transfers.
  - In the consolidated regime, there is no constraint on transfers. Two budgets are fully integrated.

# Optimal Policy (Discretion) – Unconsolidated Regime

$$V_t(s_t) = \max_{a_t} \quad \frac{1}{1-\sigma} C_t^{1-\sigma} - \frac{1}{1+\nu} N_t^{1+\nu} + \frac{\chi_1}{1-\gamma_1} \left( Q_t^C \frac{D_t}{P_t} \right)^{1-\gamma_1} + \frac{\chi_2}{1-\gamma_2} \left( (1-\alpha) Q_t^T \frac{B_t}{P_t} \right)^{1-\gamma_2} + \beta E_t V_{t+1}(s_{t+1})$$

States ( $s_t$ ): Shock, reserves, and government bonds.

Euler Equations

Choice

**Allocation:** Consumption, Labor supply.

NKPC

**Prices:** Inflation rate, price of liabilities.

Market Clearing

**Policies:** Sales tax, two liabilities, and remittance.

Treasury

$$Q_t^T B_t^T + P_t \tau_t A_t N_t + P_t H_t = (1 + \rho Q_t^T) B_{t-1}^T + P_t G_t$$

CB

$$Q_t^C D_t + (1 + \rho Q_t^T) B_{t-1}^C = D_{t-1} + Q_t^T B_t^C + P_t H_t$$

Remittance  $H_t \geq H^*$

# Optimal Policy (Discretion) – Consolidated Regime

$$V_t(s_t) = \max_{a_t} \quad \frac{1}{1-\sigma} C_t^{1-\sigma} - \frac{1}{1+\nu} N_t^{1+\nu} + \frac{\chi_1}{1-\gamma_1} \left( Q_t^C \frac{D_t}{P_t} \right)^{1-\gamma_1} + \frac{\chi_2}{1-\gamma_2} \left( (1-\alpha) Q_t^T \frac{B_t}{P_t} \right)^{1-\gamma_2} + \beta E_t V_{t+1}(s_{t+1})$$

States ( $s_t$ ): Shock, reserves, and government bonds.

Euler Equations

Choice

NKPC

Allocation: Consumption, Labor supply.

Market Clearing

Prices: Inflation rate, price of liabilities.

Policies: Sales tax, two liabilities, and remittance.

Consolidated  
Government

$$Q_t^C D_t + Q_t^T (1-\alpha) B_t + \tau_t P_t Y_t = D_{t-1} + (1 + \rho Q_t^T) (1-\alpha) B_{t-1} + P_t G_t.$$

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## Solution

- Markov-perfect equilibrium.
- Shock: Cost-push, productivity, or government expenditure.
  - Include one shock, and exclude the other two.
- **Globally** solve the model.
  - Occasionally binding constraints,  $H_t \geq H^*$ .

# Calibration

Variable	Value	Description	Target	Model	Data
$\beta$	0.995	Discount factor		Standard	
$\sigma$	2	Risk aversion		Standard	
$\nu$	3	Frisch Elasticity		Standard	
$\theta$	10	Elasticity of substitution		Standard	
$\varphi$	100	Price adjustment cost		Standard	
$\rho^T$	0.95	Duration of Treasury	Average maturity	5 years	5 years
$\chi_1(Q^c d)^{1-\gamma_1}$	0.0006	Utility from reserves	Steady-state reserves	15% of GDP	15% of GDP
$\chi_2(Q^T b)^{1-\gamma_2}$	0.0014	Utility from Treasury bond	Steady state Treasury	40% of GDP	80% of GDP
$\gamma_1$	1.7	Curvature of utility from reserves	$\frac{\partial Q^C}{\partial d}$	0.1	0.05~0.2
$\gamma_2$	1.5	Curvature of utility from Treasury	$\frac{\partial Q^T}{\partial b}$	0.05	0~0.1
$\alpha$	0.4	CB's asset holding	CB's Net worth	1	1
$H^*$	-0.0025	Lower bound on remittance	-	-0.25% of GDP	-

# Results

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# First Finding

Without fiscal backing,

## Monetary Policy

- The government tolerates **higher inflation** after an inflationary shock.
- **Optimally chooses not to raise** the interest rate as much as the case with fiscal backing.

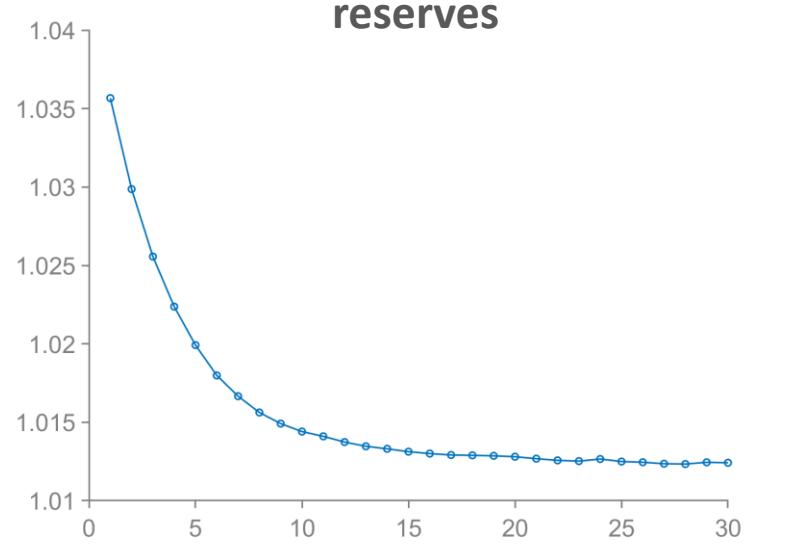
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## Simulation

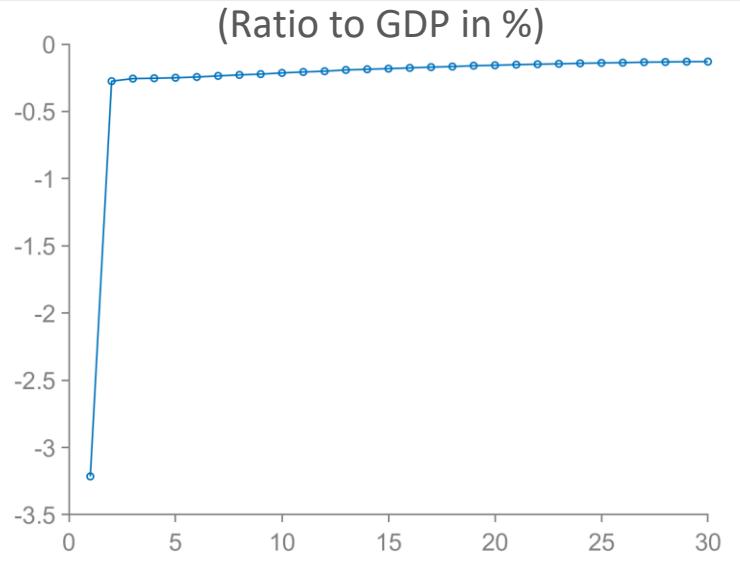
- Transition dynamics following a decline of productivity by 5%.
- The marginal cost increases and consumption drops.
- Optimal to raise nominal interest rate, leading to higher interest expenses.
- The initial state variables are large reserves (90<sup>th</sup> percentile of simulated reserves).
  - The economy moves even when the shock does not hit.

## Negative productivity shock in consolidated model

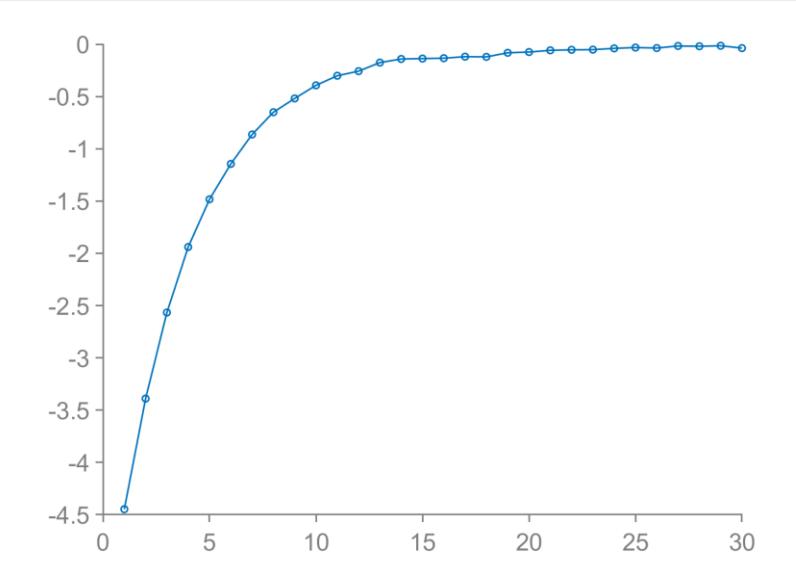
Nominal interest on reserves



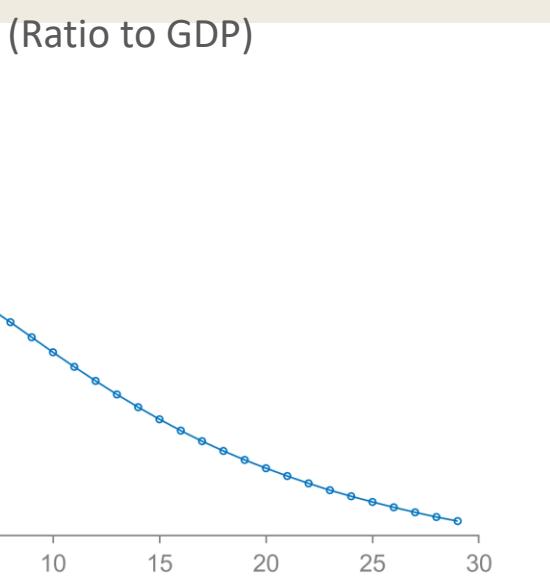
Remittance from CB to Treasury



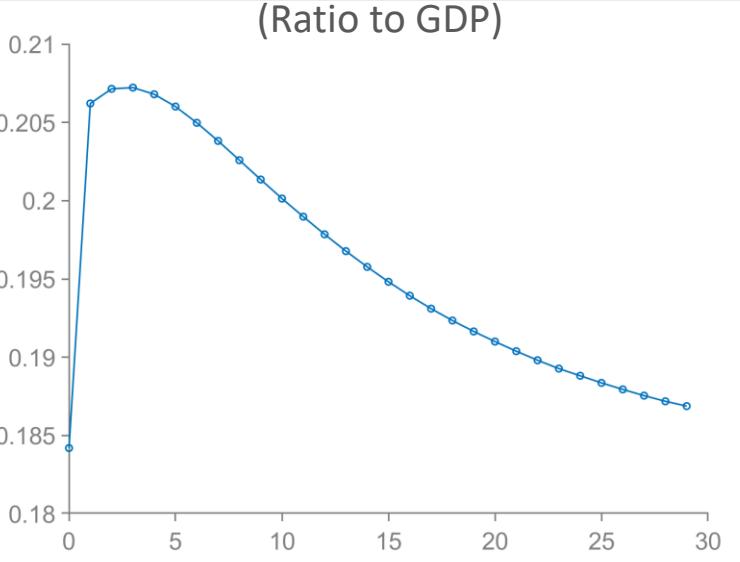
Consumption  
(SS deviation in %)



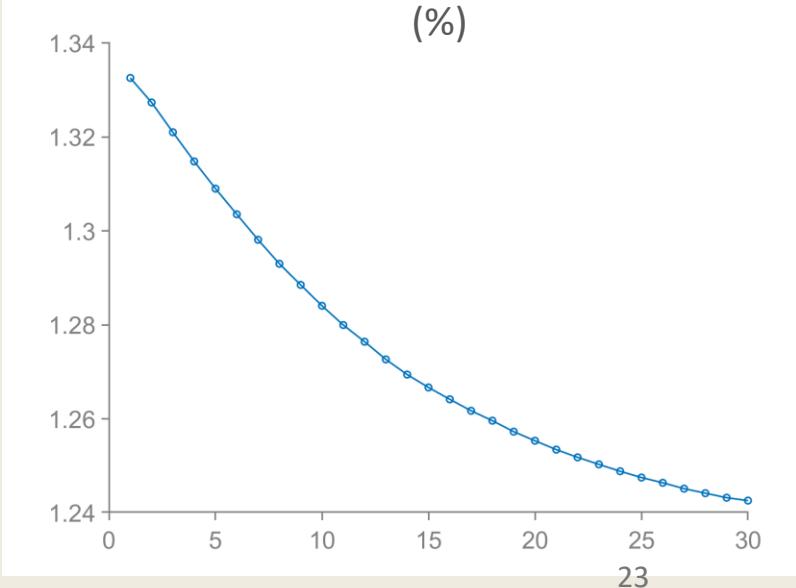
Reserves



Government bonds

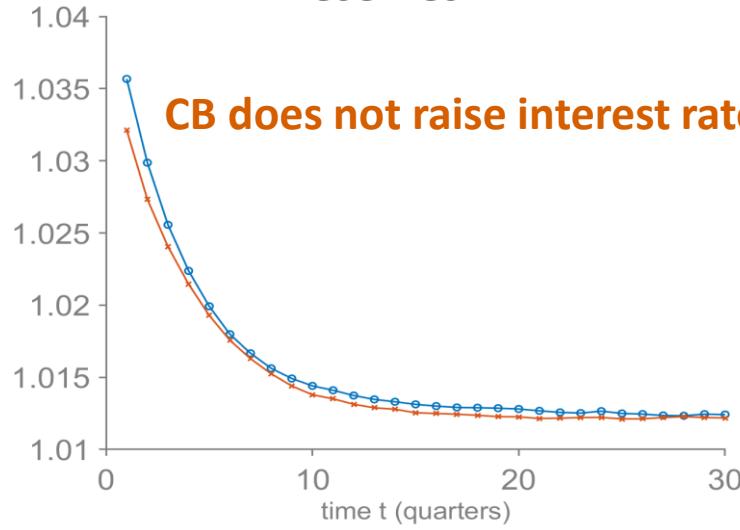


Inflation

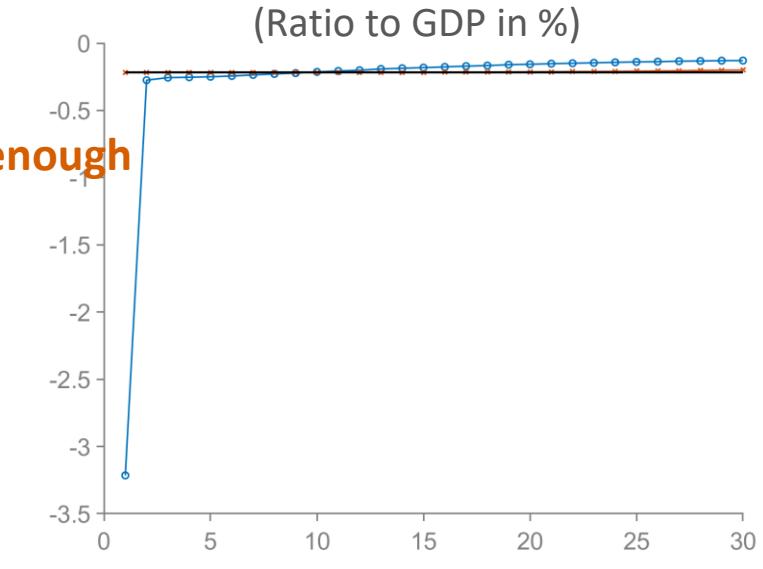


## Consolidated (blue) and unconsolidated (red)

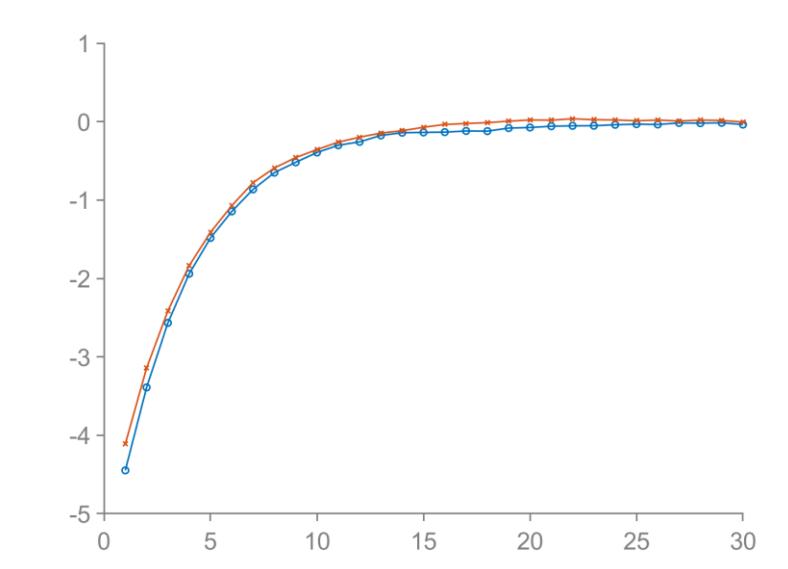
Nominal interest on reserves



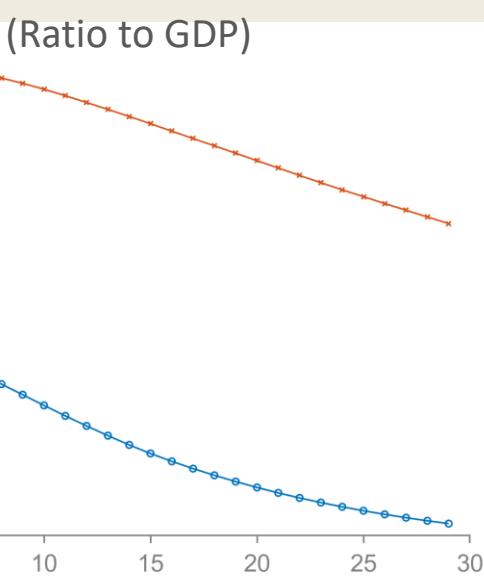
Remittance from CB to Treasury



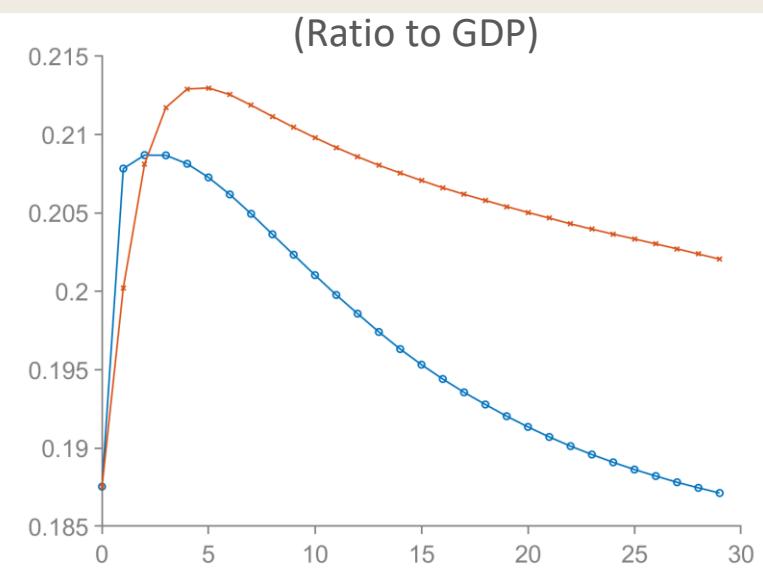
Consumption  
(SS deviation in %)



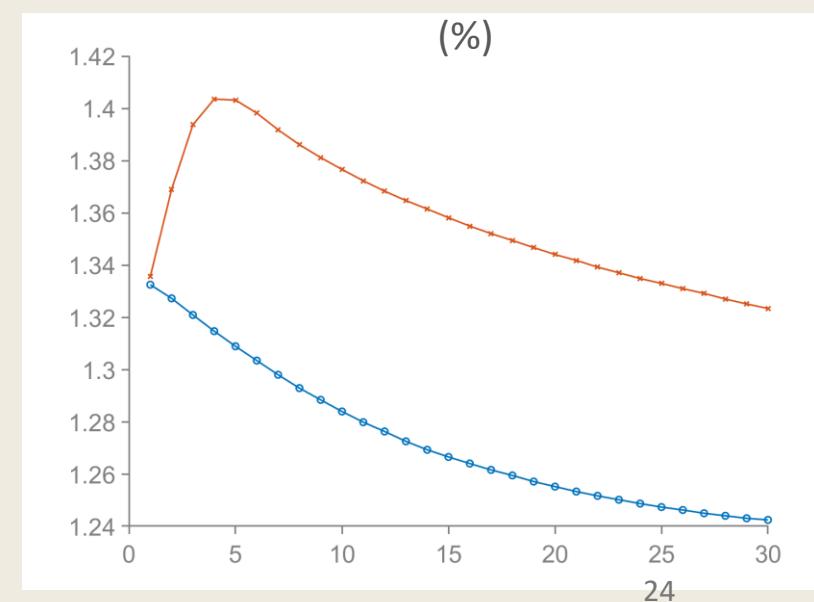
Reserves



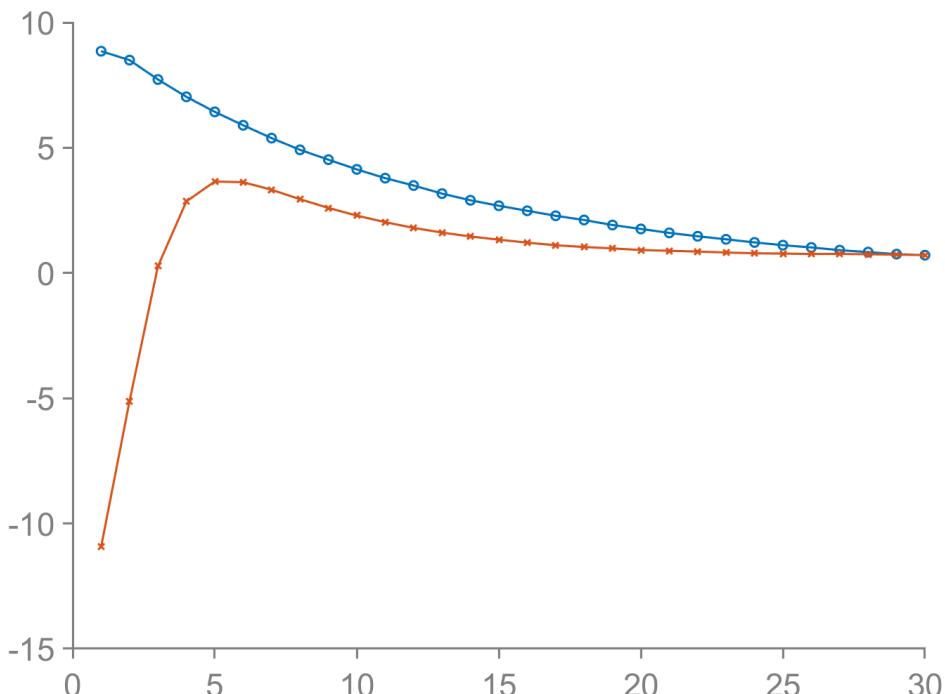
Government bonds



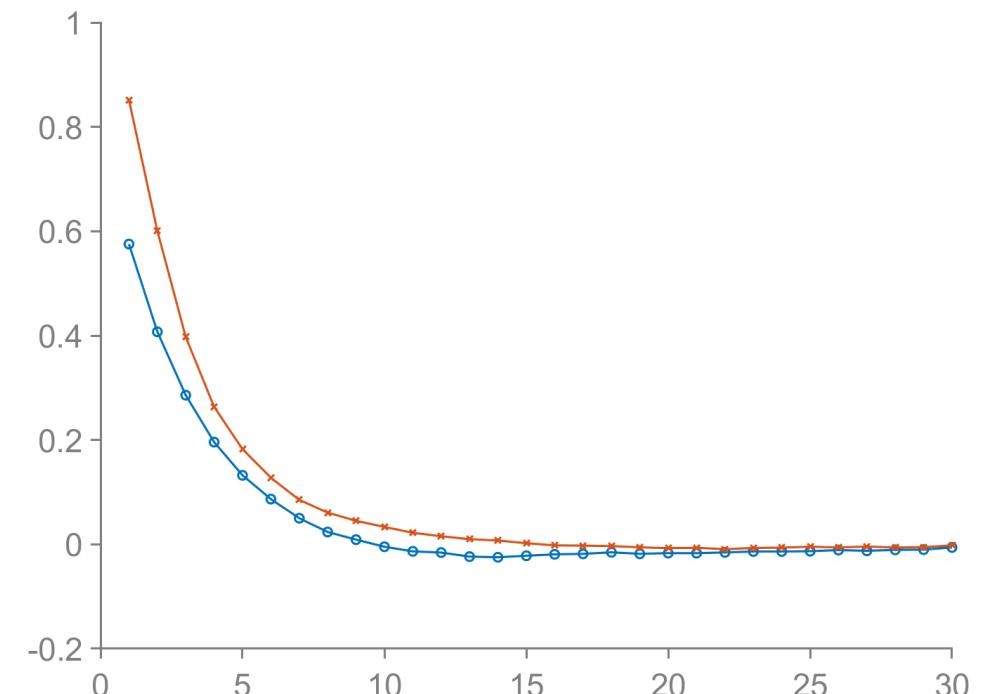
Inflation



**Tax rate on sales  
SS deviation**



**Labor supply  
SS deviation**



# Intuition & Takeaway

## Finding

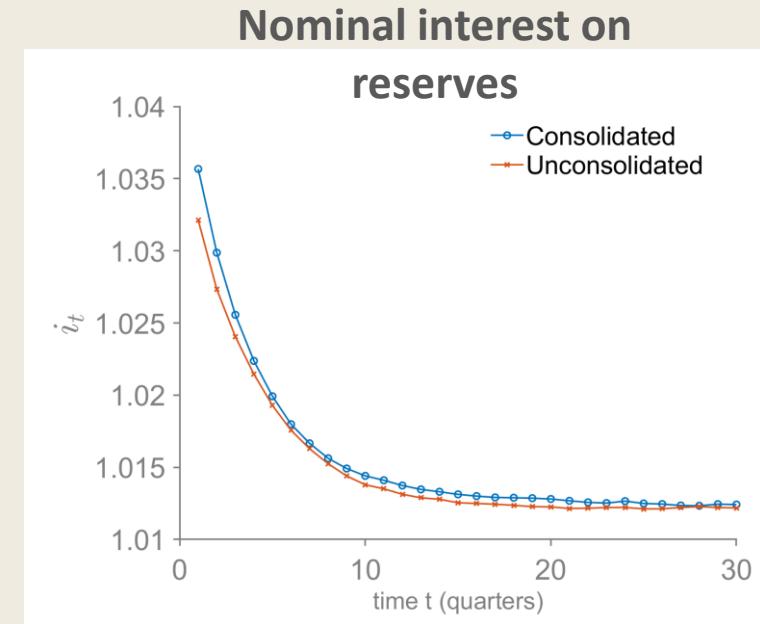
- Optimally not to raise the interest rate as much as with fiscal backing.

## Intuition

- Suppose the nominal interest rate is high in the unconsolidated regime.
- No fiscal backing to reduce reserves. → Larger reserves.
- Higher nominal interest rates are required because of the downward-slope demand curve.

## Takeaway

- Lower nominal interest rate and tolerate higher inflation rate is optimal.



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## Second Finding

Without fiscal backing,

### Fiscal Policy

- Tax rate is more volatile over the business cycle.
- The central bank is limited to helping the Treasury finance government spending.

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## Procedure

- I feed the exogenous path of **public expenditure ( $G_t$ )** that follows AR(1) with a shock.
- I simulate the economy in the consolidated and unconsolidated regimes for 1000 periods.
- Compute the variance of tax rate on sales.

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## Intuition in the consolidated regime.

- Positive shock to public expenditure ( $G_t$ ).
- The government wants to smooth tax distortion ( $\tau_t$ ) over time by issuing liabilities.
- The Treasury can issue bonds ( $B_t$ ). The central bank can issue reserves ( $D_t$ ).
- The Treasury receives funds from the central bank ( $H_t$ ) and finance  $G_t$ .

Treasury

$$Q_t^T B_t^T + P_t \tau_t A_t N_t + P_t H_t = (1 + \rho Q_t^T) B_{t-1}^T + P_t G_t$$

CB

$$Q_t^C D_t = D_{t-1} + P_t H_t$$

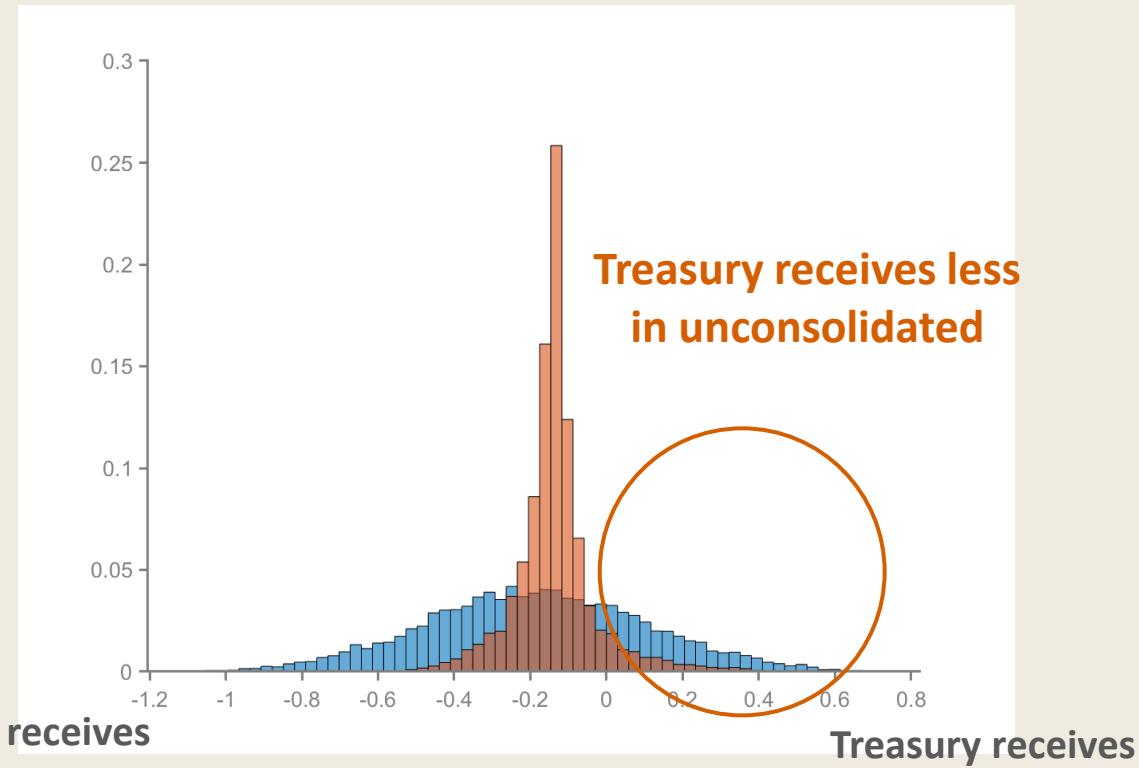
- Show standard deviation in the consolidated and unconsolidated regimes.

	Consolidated	Unconsolidated
Tax rate on sales (percent)	<b>0.57</b>	<b>0.60</b>
Reserve (ratio to GDP in %)	<b>4.1</b>	<b>1.1</b>
Bonds (ratio to GDP in %)	<b>4.1</b>	<b>6.3</b>

## Intuition - Forward looking decision-making

- A lower bound on remittance motivates the central bank to reduce remittance.
- Large reserves cannot be reduced through remittance later.

Histogram for remittance in **consolidated** and **unconsolidated**.



$$Q_t^T B_t^T + P_t \tau_t A_t N_t + \underbrace{P_t H_t}_{\text{Less help from CB}} = (1 + \rho Q_t^T) B_{t-1}^T + P_t G_t$$



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# Policy Implications and Takeaway

## Policy in practice

- The central bank's profit finances public expenditure.
  - Fed's profits / Federal expenditure = 2% (2010-2022).
- The central banks have motive to retain earnings.
  - Bank of Japan **retains 5% of profits** and transfers the rest to the Treasury.
  - Bank of England retains profits if its net worth is below a threshold.

## Takeaway

- The lack of *fiscal* backing constraints optimal *fiscal* policy.

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# Additional Findings

## 1. Non-linearity of the model

- The higher inflation due to lack of fiscal backing is exacerbated by (i) larger shocks and (ii) higher initial reserves.

## 2. The conditional welfare gain after a large shock is substantial.

- Following a shock that increases the wage mark-up by 10%, the welfare loss from the shock is 20% lower in the unconsolidated model compared to the consolidated model

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# Additional Findings

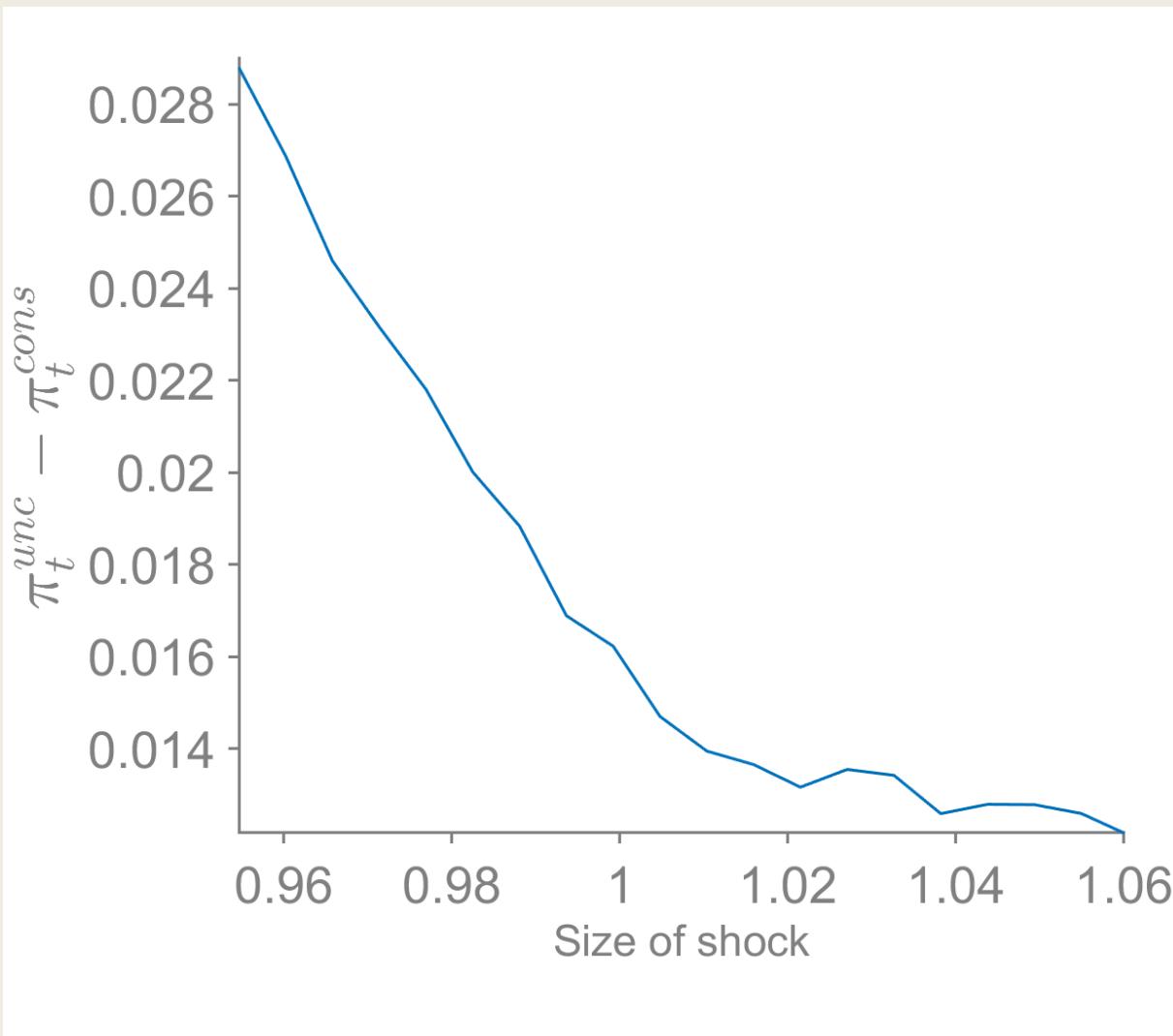
## 1. Non-linearity of the model

- The higher inflation due to lack of fiscal backing is exacerbated by (i) larger shocks and (ii) higher initial reserves.
- If the inflationary shock is small or the central bank holds small reserves, the inequality constraint on transfers is not binding;  $H_t \geq H^*$ .

## Simulation

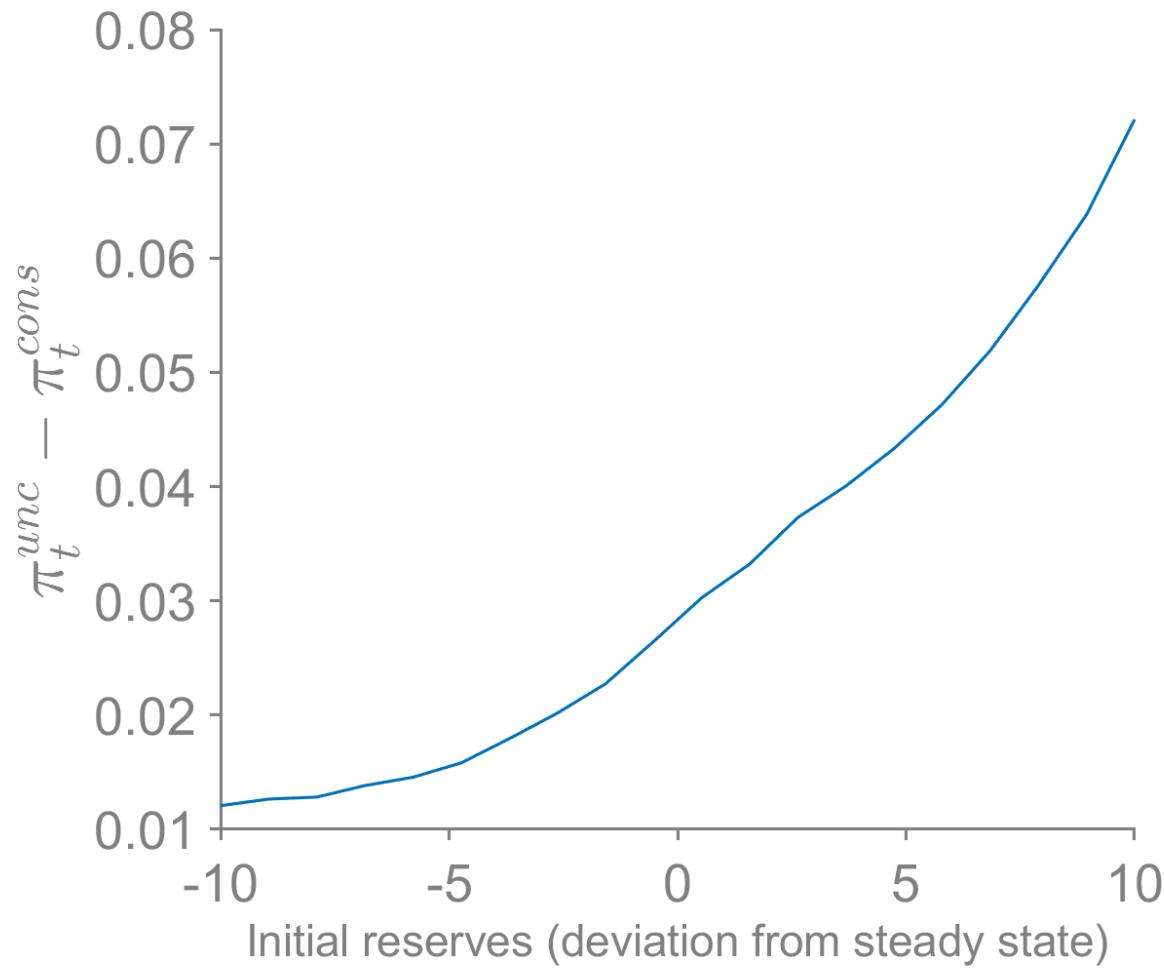
- Compute the response of inflation rate for both regimes (i) following the different size of shock (ii) different size of initial condition for reserves.

# The size of a shock.



- The horizontal is  $A_t$  at t=1.
- The vertical is the difference in inflation between two regimes.
- When productivity drops by 4%, the inflation rate is higher by 0.028%.

# The initial condition for reserves

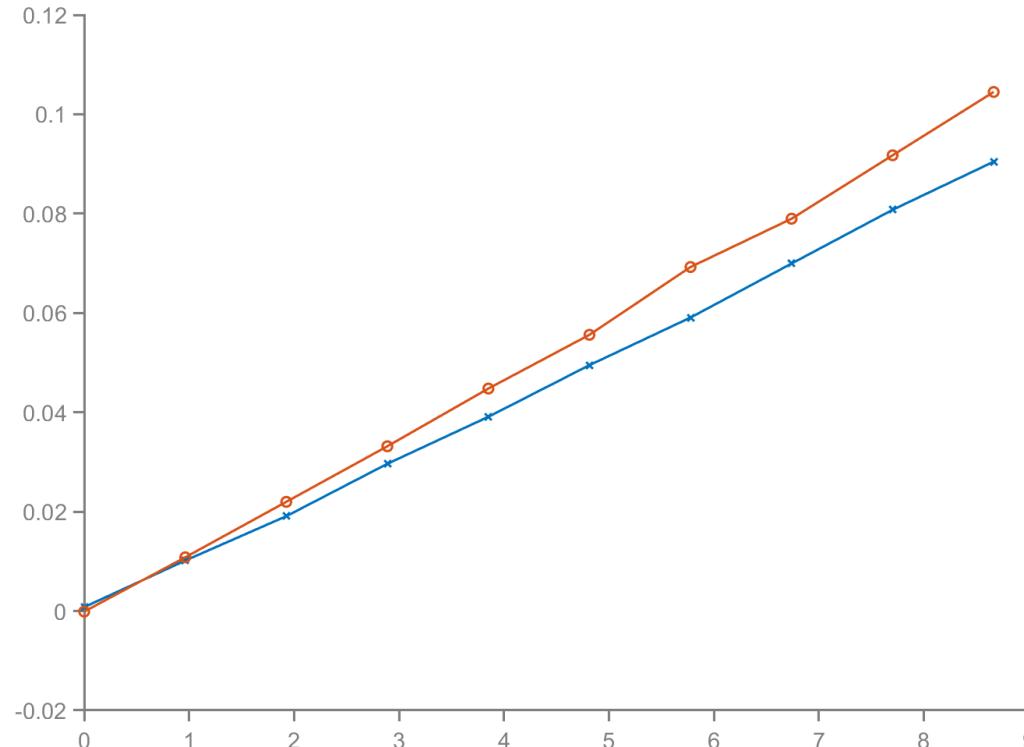


- The horizontal is the initial condition for reserves.
- The vertical is the difference in inflation between two regimes following the decline of productivity by 5%.
- When the central bank holds 10% higher reserves, the difference in inflation is 0.07%.

# The welfare gain of fiscal backing

# The welfare gain of fiscal backing increases with the size of shock.

Welfare cost of  
cost-push shock in  
consumption  
equivalence (%).



Increase in wage mark-up in %.

- Compute the welfare loss of cost-push shock compared to the steady-state.
- Show the welfare loss (horizontal) on the size of shock (vertical) for **consolidated** and **unconsolidated**.
- Fiscal backing can reduce the welfare loss by 20%.

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## The welfare gain of fiscal backing < 0.01% in consumption equivalence.

- I compute the welfare gain of increasing the lower bound on remittance,  $H^*$ .
- Simulate the economy for 1000 periods. Consumption equivalence compared to the case of  $H^* = -\infty$ .

(Intuition)

- Fiscal backing affects the variance but less the mean.