

# Optimal Monetary and Fiscal Policy without Fiscal Backing

Masayuki Okada  
NYU

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# Introduction

- The Fed is required to transfer all profits to the Treasury.
- The Treasury makes no transfer to offset the Fed's loss.
  - Expense = Interest rate (5p.p.)  $\times$  Reserves (15% of GDP)
  - Fed's net loss / Treasury's tax revenue = 2%. (2022-2024)
- Asymmetric resource allocation between monetary and fiscal authorities.
- Conventional macroeconomic models assume a consolidated government budget  
(Sargent and Wallace 1981).

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# Research Question

If the government budgets are **unconsolidated**,  
(= If Treasury does not provide the **optimal fiscal support** to the central bank)  
does the optimal monetary-fiscal policy change?

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# What I do

## Optimal monetary and fiscal policy without commitment

As in the literature,

- Government chooses policies to maximize utility s.t. equilibrium conditions.
- NK model with the budgets of Treasury and central bank.

New

1. Two types of liabilities: Reserves as a novel ingredient. Bonds as in the literature.
2. Constraint on transfers from Treasury to central bank.

# Literature

	Positive	Normative (Optimal Policy)
Consolidated	Sargent and Wallace 1981 among others	Benigno and Woodford 2003 Schmitt-Grohe and Uribe 2004 among others
Unconsolidated	Hall and Reis 2015 Del Negro and Sims 2015 Bassetto and Sargent 2020 Amador and Bianchi 2023	This paper

# Literature

	Positive	Normative (Optimal Policy)
<b>Consolidated (fiscal backing)</b>	Sargent and Wallace 1981 among others	<b>This paper compares the equilibrium between two regimes.</b>
<b>Unconsolidated (No fiscal backing)</b>	Hall and Reis 2015 Del Negro and Sims 2015 Bassetto and Sargent 2020 Amador and Bianchi 2023	

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# What I find

Without fiscal backing,

## Monetary Policy

- The government tolerates **higher inflation** after an inflationary shock.
- **Optimally chooses not to raise** the interest rate as much as the case with fiscal backing.

## Fiscal Policy

- Tax rate is **more volatile** over the business cycle.
- The central bank is limited to helping the Treasury finance government spending.

# Model



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# Environment

- **Time.** Discrete, infinite horizon.
- **Assets.** Reserves and bonds (Differ in duration and liquidity value).
- **Agents**

**Household** consumes and works. Trades reserves and bonds. Get a convenience yield.

**Producers** are NK model, facing cost-push and productivity shock.

**Treasury** finances public expenditure by a sales tax, bonds, and remittance from central bank.

**Central bank** issues reserves for their liquidity value and buys government bonds.

# Household

$$\max_{C_t, N_t(j), B_t, D_t} E_0 \sum_{t=0}^{\infty} \beta^t \left[ \frac{1}{1-\sigma} C_t^{1-\sigma} - \frac{1}{1+\nu} N_t^{1+\nu} + \frac{\chi_1}{1-\gamma_1} \left( Q_t^C \frac{D_t}{P_t} \right)^{1-\gamma_1} + \frac{\chi_2}{1-\gamma_2} \left( Q_t^T \frac{B_t}{P_t} \right)^{1-\gamma_2} \right]$$

s.t.

$$P_t C_t + Q_t^C D_t + Q_t^T B_t = D_{t-1} + (1 + \rho Q_t^T) B_{t-1} + P_t w_t \int_0^1 N_t(j) dj + P_t \Phi_t,$$

- $D_t$  is **reserves** directly held by the household and issued by the central bank.
- $B_t$  is long-duration **bonds** with exponentially declining coupon of  $\rho^{j-1}$  in  $t + j$ .
- $\Phi$  is the firm's profit.

# Firms

- Standard set up of the adjustment cost model.

$$\max_{p_t(i)} E_0 \sum_{t=0}^{\infty} \beta^t \Lambda_t \left( \underbrace{(1 - \tau_t)p_t(i)y_t(i)}_{\text{Sales tax}} - \underbrace{\mu_t^w w_t N_t(i)}_{\substack{\text{Exogenous} \\ \text{Cost-push shock}}} - P_t \frac{\varphi}{2} \left( \frac{p_t(i)}{p_{t-1}(i)} - 1 \right)^2 Y_t \right)$$

Production function  $y_t(i) = \underbrace{A_t}_{\substack{\text{Exogenous} \\ \text{Productivity}}} N_t(i)$

Demand curve for product  $y_t(i) = \left( \frac{p_t(i)}{P_t} \right)^{-\theta} Y_t$

# Government

- Treasury's budget

Remittance from CB

$$Q_t^T B_t^T + P_t \tau_t A_t N_t + \overbrace{P_t H_t}^{\text{Remittance from CB}} = (1 + \rho Q_t^T) B_{t-1}^T + P_t G_t$$

$B^T$  is the total supply of government bonds. The government expenditure,  $G_t$ , is exogenous.

- Central Bank trades reserves and government bonds.

Remittance to Treasury

$$Q_t^C D_t + (1 + \rho Q_t^T) B_{t-1}^C = D_{t-1} + Q_t^T B_t^C + \overbrace{P_t H_t}^{\text{Remittance to Treasury}}$$

$D$  is reserves.  $B^C$  is government bonds held by Central Bank.

- **Inequality constraint on the remittance**

$$H_t \geq H^*$$

# Central Bank's Asset Purchase Policy

- Assume an exogenous asset purchase rule.

$$B_t^C = \alpha B_t^T$$

- $B^T$  is total supply of government bonds.
  - $B^C$  is government bonds held by the central bank.
  - The rest is held by the households.
  - $\alpha$  is a parameter.
- Reduces the size of the state space (4 states  $\rightarrow$  3 states).
  - The goal of Central Bank's asset purchase policy is to stabilize the financial market.

# Equilibrium

- Market Clearing Conditions

$$\text{(Goods)} \quad A_t N_t = C_t + G_t + \frac{\varphi}{2} (\pi_t - 1)^2 A_t N_t$$

$$\text{(Government bonds)} \quad B_t + B_t^C = B_t^T$$

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# Government's problem under discretion

- The government simultaneously chooses both monetary and fiscal policy.
  - Policies: Two liabilities, their prices, tax on sales, and remittance.
- The government maximizes HH utility taking as given policy functions of HH and firms.
  - State variables: Shock, reserves, and bonds.
- Define **the unconsolidated regime** and **the consolidated regime**.
  - In the unconsolidated regime, the government faces a constraint on transfers.
  - In the consolidated regime, there is no constraint on transfers. Two budgets are fully integrated.

# Optimal Policy (Discretion) – Unconsolidated Regime

$$V_t(s_t) = \max_{a_t} \frac{1}{1-\sigma} C_t^{1-\sigma} - \frac{1}{1+\nu} N_t^{1+\nu} + \frac{\chi_1}{1-\gamma_1} \left( Q_t^C \frac{D_t}{P_t} \right)^{1-\gamma_1} + \frac{\chi_2}{1-\gamma_2} \left( (1-\alpha) Q_t^T \frac{B_t}{P_t} \right)^{1-\gamma_2} + \beta E_t V_{t+1}(s_{t+1})$$

States ( $s_t$ ): Shock, reserves, and government bonds.

Choice

**Allocation:** Consumption, Labor supply.

**Prices:** Inflation rate, price of liabilities.

**Policies:** Sales tax, two liabilities, and remittance.

Euler Equations

NKPC

Market Clearing

Treasury

$$Q_t^T B_t^T + P_t \tau_t A_t N_t + P_t H_t = (1 + \rho Q_t^T) B_{t-1}^T + P_t G_t$$

CB

$$Q_t^C D_t + (1 + \rho Q_t^T) B_{t-1}^C = D_{t-1} + Q_t^T B_t^C + P_t H_t$$

Remittance  $H_t \geq H^*$



# Optimal Policy (Discretion) – Consolidated Regime

$$V_t(s_t) = \max_{a_t} \frac{1}{1-\sigma} C_t^{1-\sigma} - \frac{1}{1+\nu} N_t^{1+\nu} + \frac{\chi_1}{1-\gamma_1} \left( Q_t^C \frac{D_t}{P_t} \right)^{1-\gamma_1} + \frac{\chi_2}{1-\gamma_2} \left( (1-\alpha) Q_t^T \frac{B_t}{P_t} \right)^{1-\gamma_2} + \beta E_t V_{t+1}(s_{t+1})$$

States ( $s_t$ ): Shock, reserves, and government bonds.

Choice

**Allocation:** Consumption, Labor supply.

**Prices:** Inflation rate, price of liabilities.

**Policies:** Sales tax, two liabilities, and remittance.

Euler Equations

NKPC

Market Clearing

Consolidated  
Government

$$Q_t^C D_t + Q_t^T (1-\alpha) B_t + \tau_t P_t Y_t = D_{t-1} + (1 + \rho Q_t^T) (1-\alpha) B_{t-1} + P_t G_t.$$

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## Solution

- Markov-perfect equilibrium.
- Shock: Cost-push, productivity, or government expenditure.
  - Include one shock, and exclude the other two.
- **Globally** solve the model.
  - Occasionally binding constraints,  $H_t \geq H^*$ .

# Calibration

Variable	Value	Description	Target	Model	Data
$\beta$	0.995	Discount factor		Standard	
$\sigma$	2	Risk aversion		Standard	
$\nu$	3	Frisch Elasticity		Standard	
$\theta$	10	Elasticity of substitution		Standard	
$\varphi$	100	Price adjustment cost		Standard	
$\rho^T$	0.95	Duration of Treasury	Average maturity	5 years	5 years
$\chi_1$	0.0006	Utility from reserves	Steady-state reserves	15% of GDP	15% of GDP
$\chi_2$	0.0014	Utility from Treasury bond	Steady state Treasury	40% of GDP	80% of GDP
$\gamma_1$	1.7	Curvature of utility from reserves	$\frac{\partial Q^c}{\partial d}$	0.1	0.05~0.2
$\gamma_2$	1.5	Curvature of utility from Treasury	$\frac{\partial Q^T}{\partial b}$	0.05	0~0.1
$\alpha$	0.4	CB's asset holding	CB's Net worth	1	1
$H^*$	-0.0025	Lower bound on remittance	-	-0.25% of GDP	-

# Results

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# First Finding

Without fiscal backing,

## Monetary Policy

- The government tolerates **higher inflation** after an inflationary shock.
- **Optimally chooses not to raise** the interest rate as much as the case with fiscal backing.

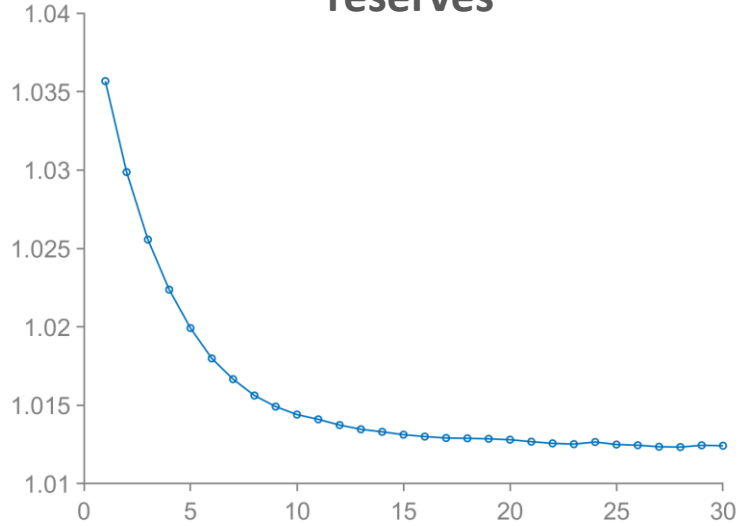
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## Simulation

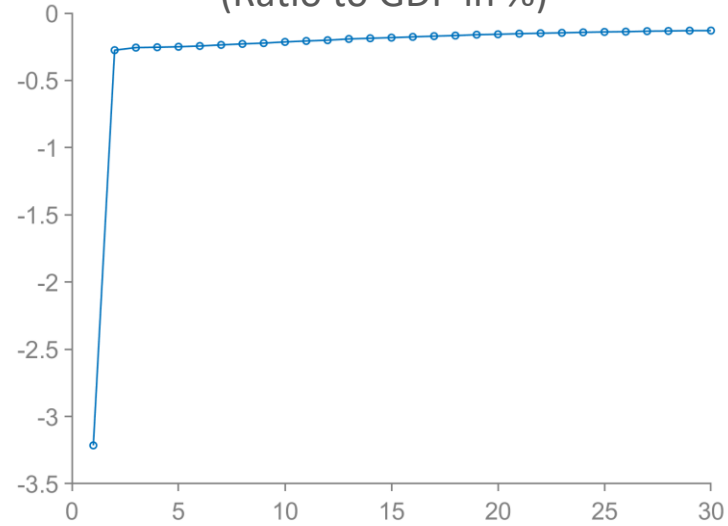
- Transition dynamics following a decline of productivity by 5%.
- The marginal cost increases and consumption drops.
- Optimal to raise nominal interest rate, leading to higher interest expenses.
- The initial state variables are large reserves (90<sup>th</sup> percentile of simulated reserves).
  - The economy moves even when the shock does not hit.

# Negative productivity shock in consolidated model

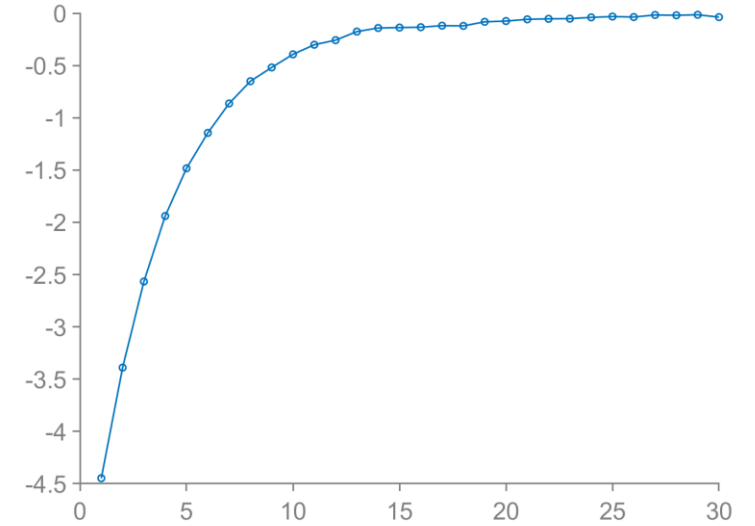
**Nominal interest on  
reserves**



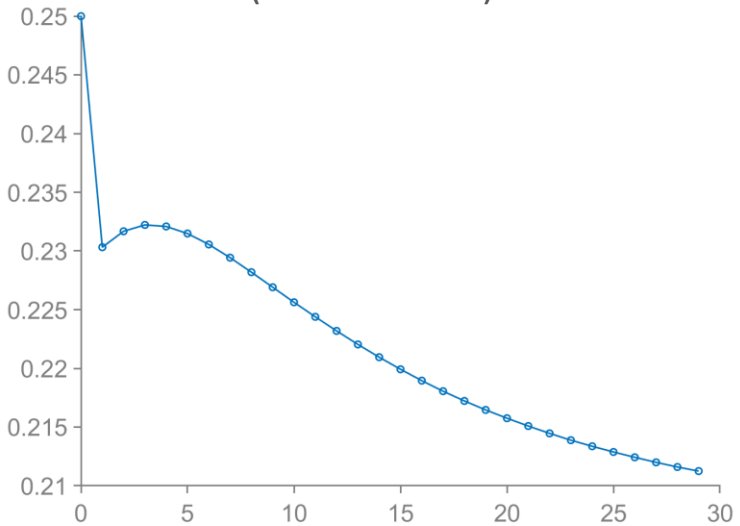
**Remittance from CB to Treasury  
(Ratio to GDP in %)**



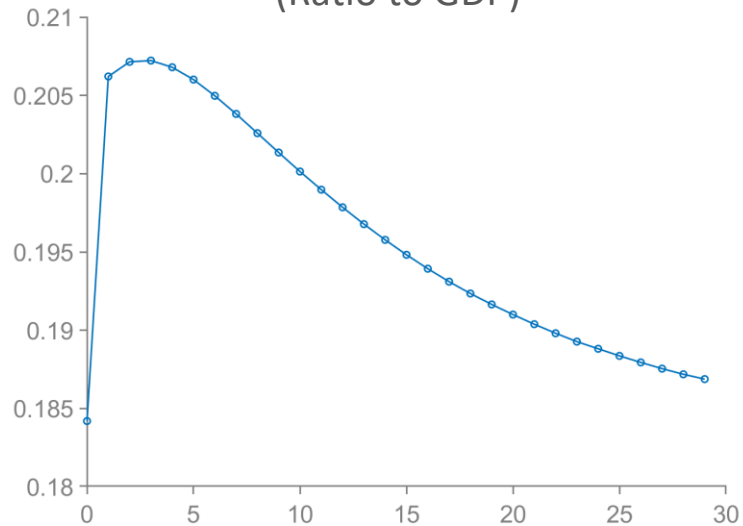
**Consumption  
(SS deviation in %)**



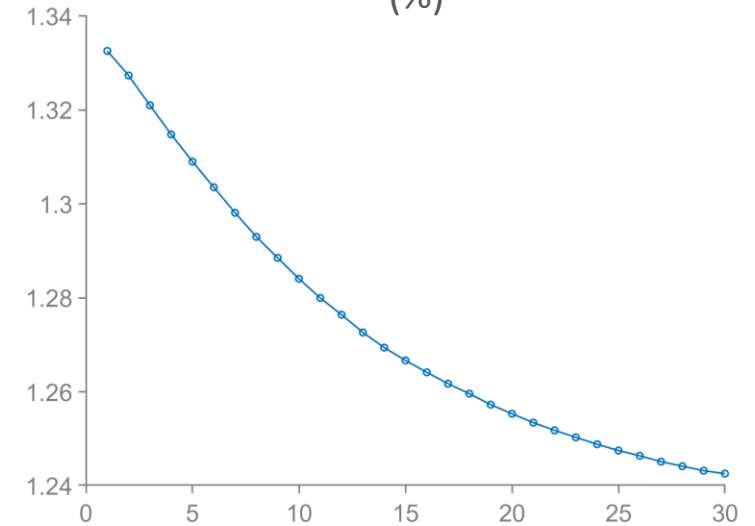
**Reserves  
(Ratio to GDP)**



**Government bonds  
(Ratio to GDP)**

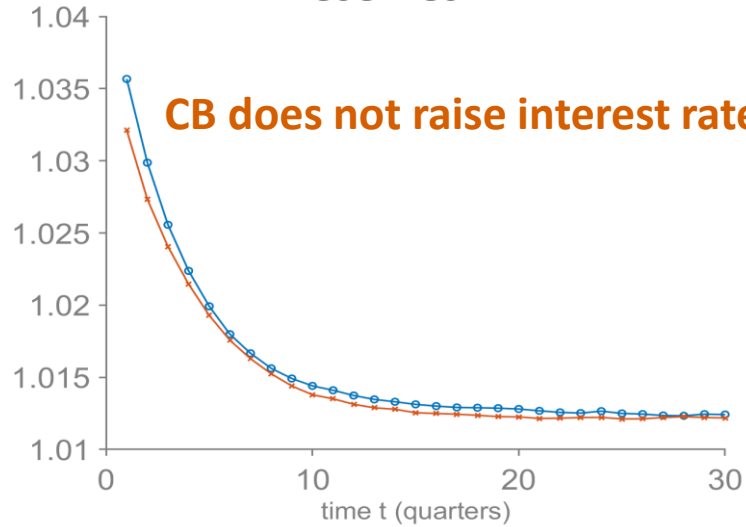


**Inflation  
(%)**

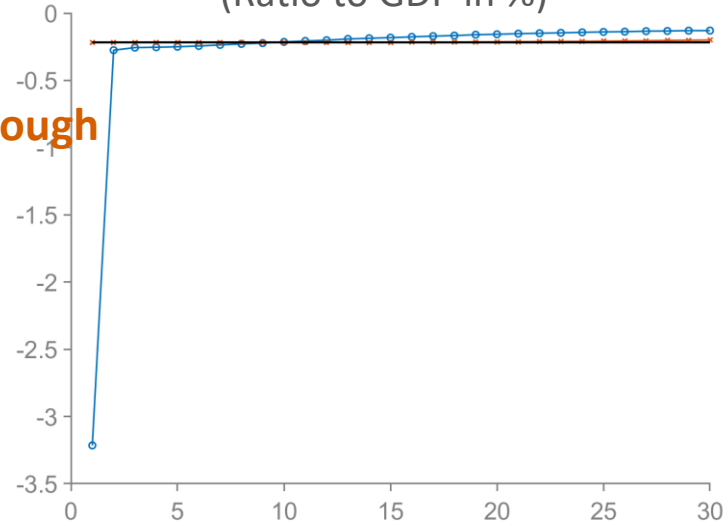


## Consolidated (blue) and unconsolidated (red)

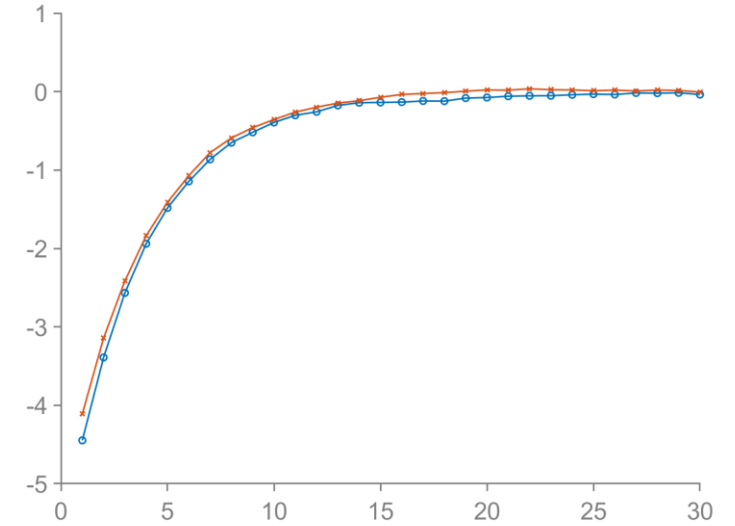
### Nominal interest on reserves



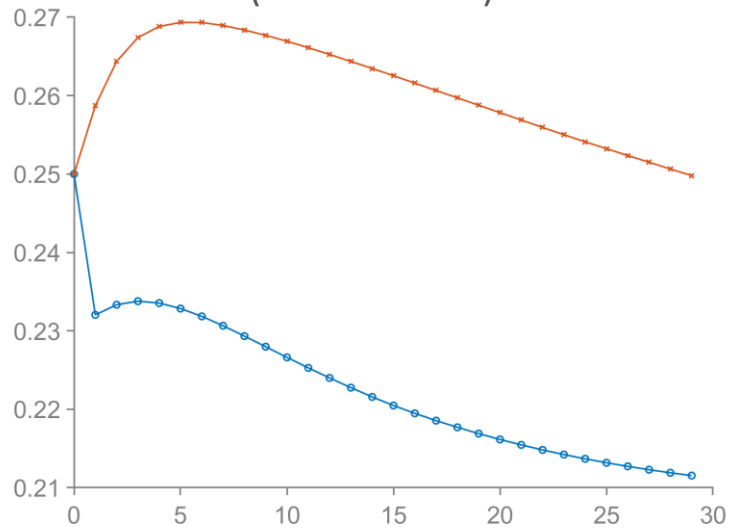
### Remittance from CB to Treasury (Ratio to GDP in %)



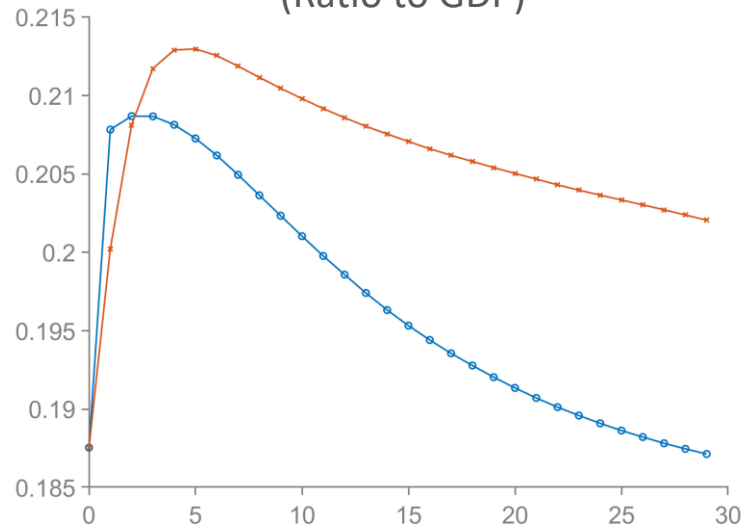
### Consumption (SS deviation in %)



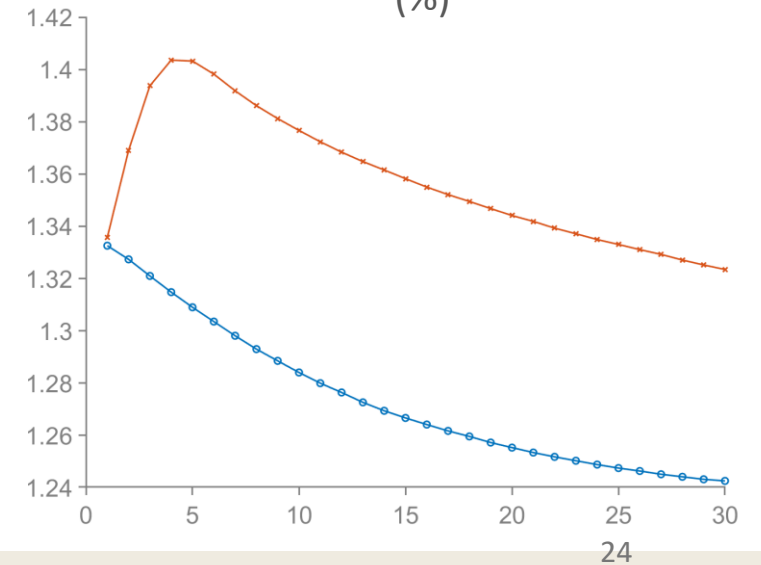
### Reserves (Ratio to GDP)



### Government bonds (Ratio to GDP)

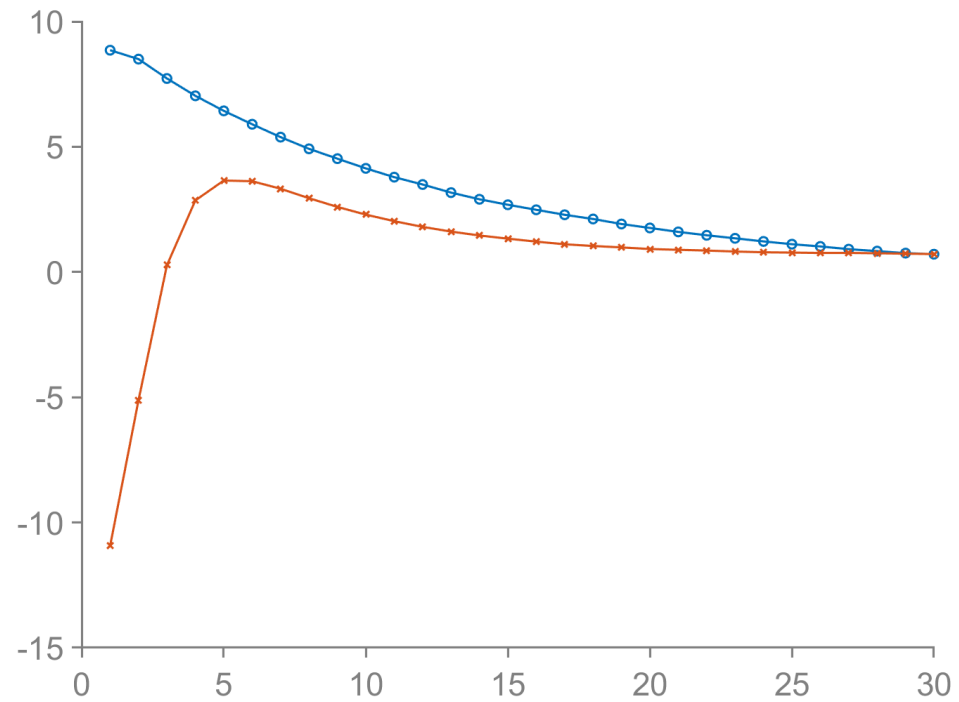


### Inflation (%)

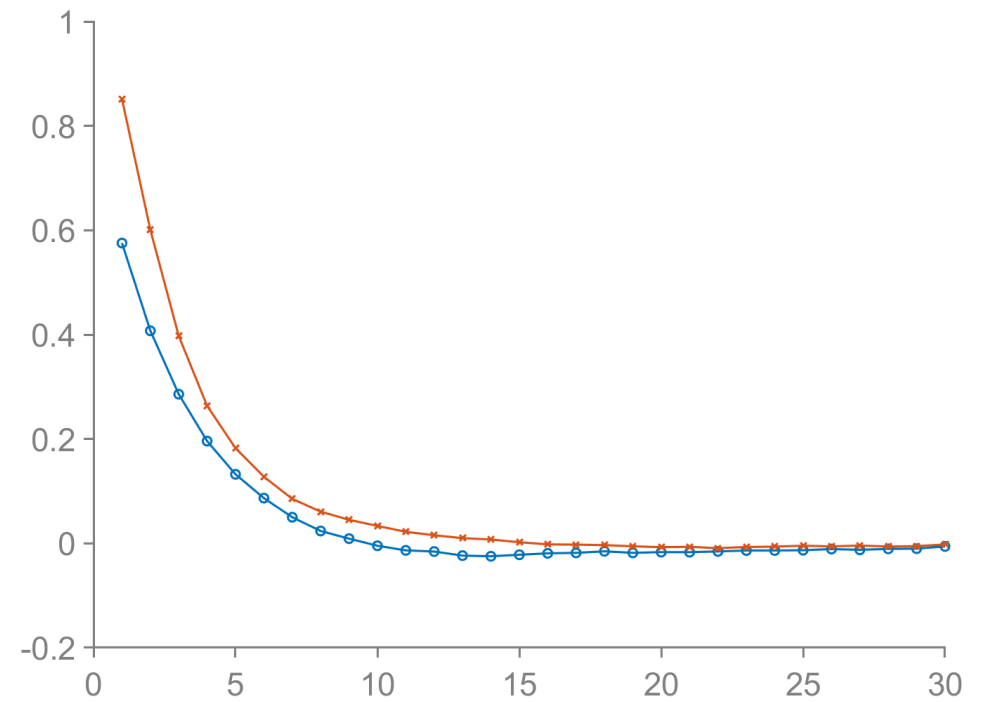




**Tax rate on sales  
SS deviation**



**Labor supply  
SS deviation**



# Intuition & Takeaway

## Finding

- **Optimally not to raise** the interest rate as much as with fiscal backing.

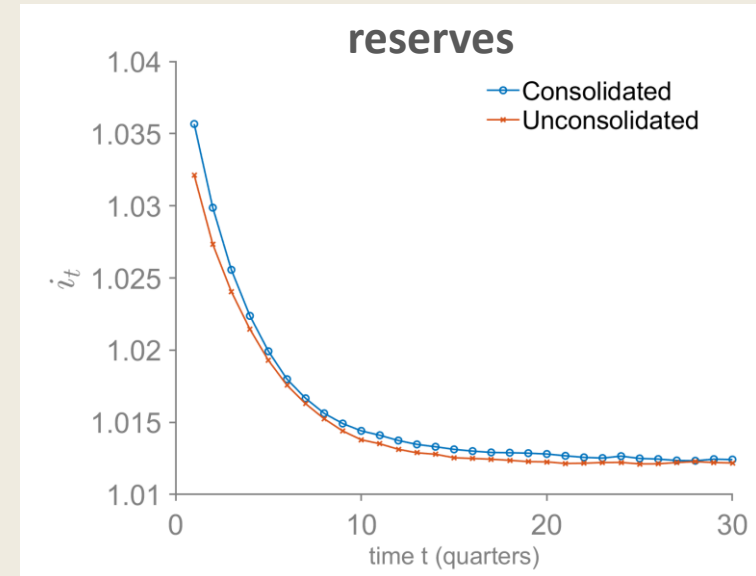
## Intuition

- Suppose the nominal interest rate is high in the unconsolidated regime.
- No fiscal backing to reduce reserves. → Larger reserves.
- Higher nominal interest rates are required because of the downward-slope demand curve.

## Takeaway

- Lower nominal interest rate and tolerate higher inflation rate is optimal.

Nominal interest on  
reserves



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# Second Finding

Without fiscal backing,

## Fiscal Policy

- Tax rate is more volatile over the business cycle.
- The central bank is limited to helping the Treasury finance government spending.

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## Procedure

- I feed the exogenous path of **public expenditure ( $G_t$ )** that follows AR(1) with a shock.
- I simulate the economy in the consolidated and unconsolidated regimes for 1000 periods.
- Compute the variance of tax rate on sales.

## Intuition in the consolidated regime.

- Positive shock to public expenditure ( $G_t$ ).
- The government wants to smooth tax distortion ( $\tau_t$ ) over time by issuing liabilities.
- The Treasury can issue bonds ( $B_t$ ). The central bank can issue reserves ( $D_t$ ).
- The Treasury receives funds from the central bank ( $H_t$ ) and finance  $G_t$ .

Treasury

$$Q_t^T B_t^T + P_t \tau_t A_t N_t + P_t H_t = (1 + \rho Q_t^T) B_{t-1}^T + P_t G_t$$

CB

$$Q_t^C D_t = D_{t-1} + P_t H_t$$

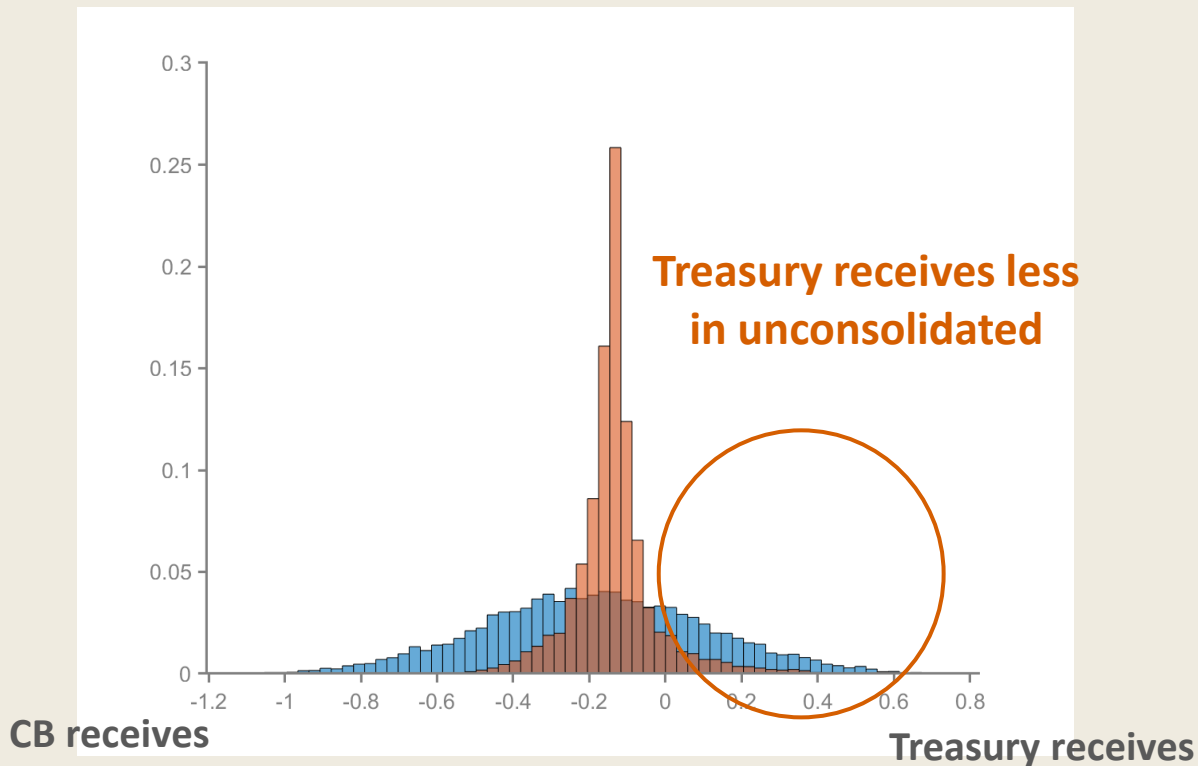
- Show standard deviation in the consolidated and unconsolidated regimes.

	Consolidated	Unconsolidated
Tax rate on sales (percent)	<b>0.57</b>	<b>0.60</b>
Reserve (ratio to GDP in %)	<b>4.1</b>	<b>1.1</b>
Bonds (ratio to GDP in %)	<b>4.1</b>	<b>6.3</b>

## Intuition - Forward looking decision-making

- A lower bound on remittance motivates the central bank to reduce remittance.
- Large reserves cannot be reduced through remittance later.

Histogram for remittance in **consolidated** and **unconsolidated**.



$$Q_t^T B_t^T + P_t \tau_t A_t N_t + \underbrace{P_t H_t}_{\text{Less help from CB}} = (1 + \rho Q_t^T) B_{t-1}^T + \overset{\text{Treasury}}{\underset{\uparrow}{P_t G_t}}$$

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# Policy Implications and Takeaway

## Policy in practice

- The central bank's profit finances public expenditure.
  - Fed's profits / Federal expenditure = 2% (2010-2022).
- The central banks have motive to retain earnings.
  - Bank of Japan **retains 5% of profits** and transfers the rest to the Treasury.
  - Bank of England retains profits if its net worth is below a threshold.

## Takeaway

- The lack of *fiscal* backing constraints optimal *fiscal* policy.



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# Additional Findings

## 1. Non-linearity of the model

- The higher inflation due to lack of fiscal backing is exacerbated by (i) larger shocks and (ii) higher initial reserves.

## 2. The conditional welfare gain after a large shock is substantial.

- Following a shock that increases the wage mark-up by 10%, the welfare loss from the shock is 20% lower in the unconsolidated model compared to the consolidated model

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# Additional Findings

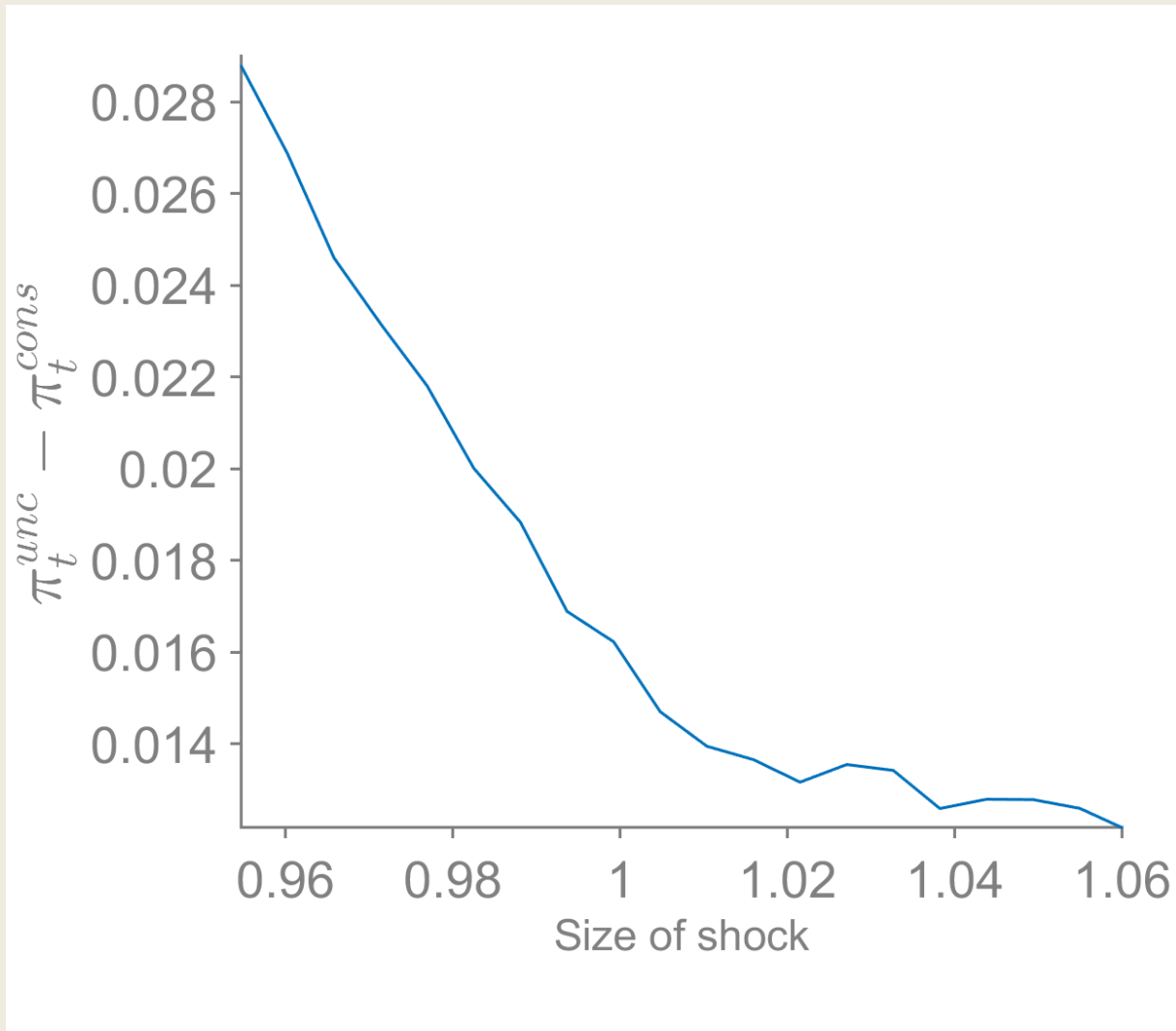
## 1. Non-linearity of the model

- The higher inflation due to lack of fiscal backing is exacerbated by (i) larger shocks and (ii) higher initial reserves.
- If the inflationary shock is small or the central bank holds small reserves, the inequality constraint on transfers is not binding;  $H_t \geq H^*$ .

## Simulation

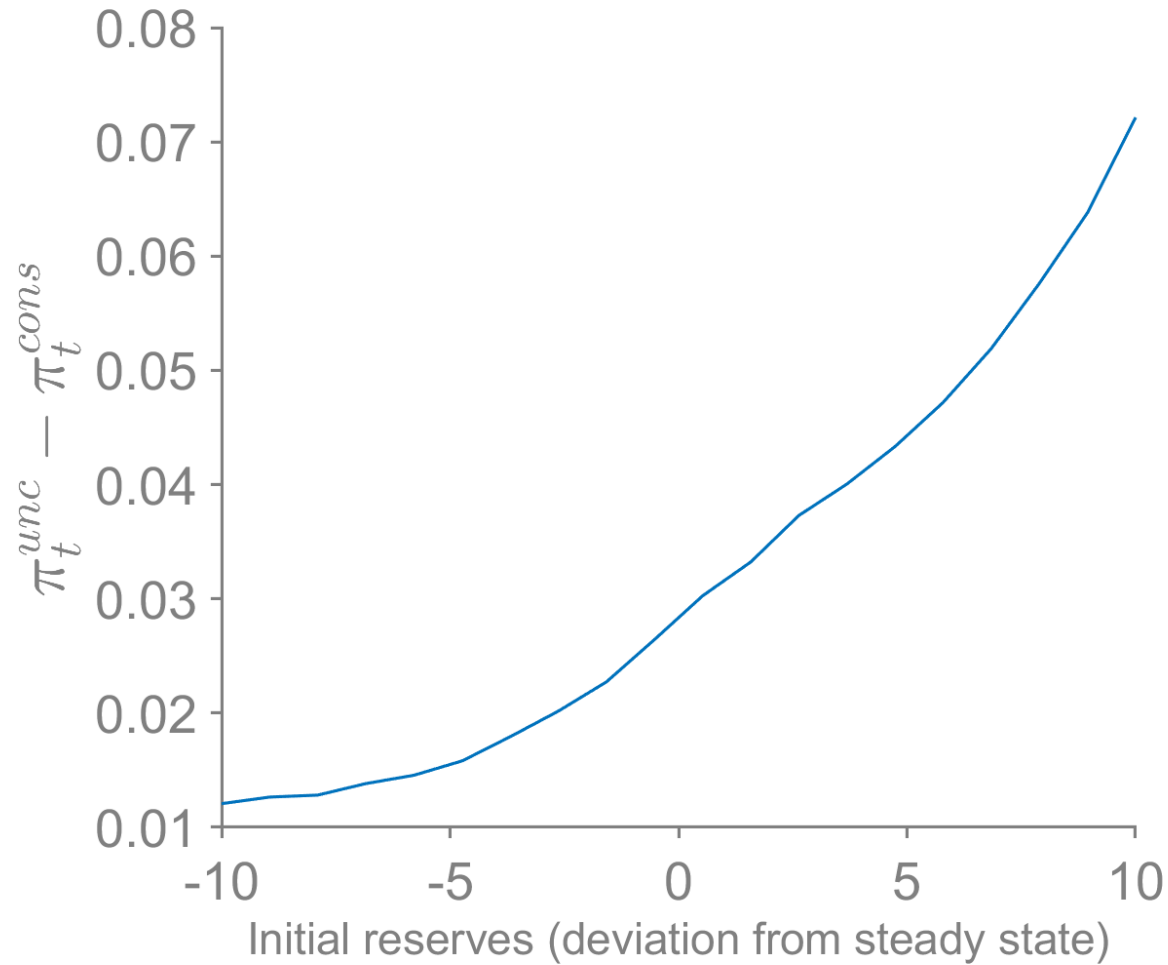
- Compute the response of inflation rate for both regimes (i) following the different size of shock (ii) different size of initial condition for reserves.

# The size of a shock.



- The horizontal is  $A_t$  at  $t=1$ .
- The vertical is the difference in inflation between two regimes.
- When productivity drops by 4%, the inflation rate is higher by 0.028%.

# The initial condition for reserves

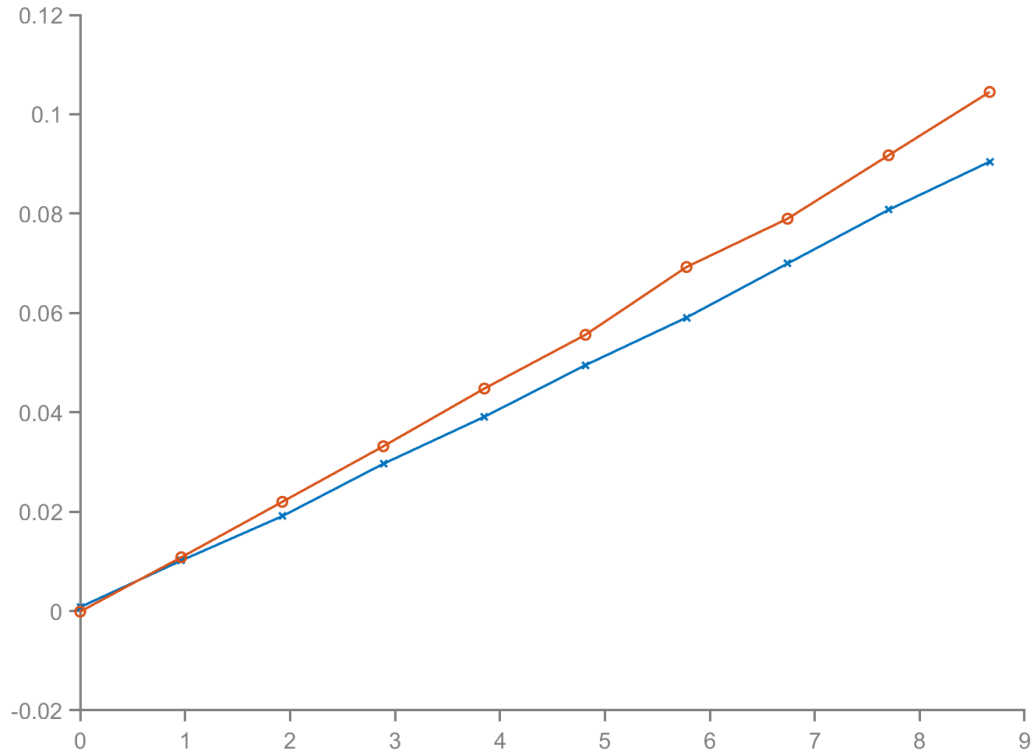


- The horizontal is the initial condition for reserves.
- The vertical is the difference in inflation between two regimes following the decline of productivity by 5%.
- When the central bank holds 10% higher reserves, the difference in inflation is 0.07%.

# The welfare gain of fiscal backing

# The welfare gain of fiscal backing increases with the size of shock.

Welfare cost of  
cost-push shock in  
consumption  
equivalence (%).



Increase in wage mark-up in %.

- Compute the welfare loss of cost-push shock compared to the steady-state.
- Show the welfare loss (horizontal) on the size of shock (vertical) for consolidated and unconsolidated.
- Fiscal backing can reduce the welfare loss by 20%.

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## The welfare gain of fiscal backing $< 0.01\%$ in consumption equivalence.

- I compute the welfare gain of increasing the lower bound on remittance,  $H^*$ .
- Simulate the economy for 1000 periods. Consumption equivalence compared to the case of  $H^* = -\infty$ .

(Intuition)

- Fiscal backing affects the variance but less the mean.