

# Optimal monetary and fiscal policy without fiscal backing for the Central Bank

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# Introduction

- The Fed runs a large loss by paying interest on reserves after 2022.
  - Expenditure = Interest rate (5p.p.) \* Reserves (15% of GDP)
  - Fed's loss / Treasury's tax revenue (2022 Q4 – 2024 Q3) = 2.5%
- Asymmetric resource allocation between Treasury and Central Bank:
  - The Fed transferred all profits to the Treasury before 2022.
  - The Treasury does not offset the Fed's losses now.
- Conventional macroeconomic models assume a consolidated government budget  
(Sargent and Wallace 1981).

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# Research Question

If the government budgets are **unconsolidated**,  
(Treasury does not provide the **optimal fiscal support** to Central Bank)  
does the optimal monetary-fiscal policy change?

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# What I do

## Optimal monetary and fiscal policy without commitment

As in the literature,

- NK model where the government chooses policies to maximize the household utility subject to the equilibrium conditions.

New

1. Two interest-bearing liabilities, reserves and government bonds.
2. Constraint on transfers from Treasury to Central Bank.

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# What I find

Without the fiscal backing,

1. Central Bank tolerates higher inflation in response to the cost-push shock.
  - Key: An initial condition with large reserves

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# What I find

Without the fiscal backing,

1. Central Bank tolerates higher inflation in response to the cost-push shock.
2. Inflation rate is 3% more volatile over the business cycle.

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# What I find

Without the fiscal backing,

1. Central Bank tolerates higher inflation in response to the cost-push shock.
2. Inflation rate is 2-3% more volatile over the business cycle.
3. The welfare loss is small ( $<0.01\%$  of consumption) in the typical business cycle.

Conditional on a large cost-push shock, the fiscal backing reduces the welfare cost by 20%

# Model



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# Environment

- **Time.** Discrete, infinite horizon.
- **Assets.** Reserves and government bonds (Differ in duration and liquidity value).
- **Agents**

**Household** consumes and works. Trades assets. Get a convenience yield.

**Producers** are NK model, facing cost-push and productivity shock.

**Treasury** finances public expenditure by a linear sales tax, government bonds, and remittance from Central Bank.

**Central Bank** issues reserves and buys government bonds.

# Household

$$\max_{C_t, N_t(j), B_t, D_t} \sum_{t=0}^{\infty} \beta^t \left[ \frac{1}{1-\sigma} C_t^{1-\sigma} - \frac{1}{1+\nu} N_t^{1+\nu} + \frac{\chi_1}{1-\gamma_1} \left( Q_t^C \frac{D_t}{P_t} \right)^{1-\gamma_1} + \frac{\chi_2}{1-\gamma_2} \left( Q_t^T \frac{B_t}{P_t} \right)^{1-\gamma_2} \right]$$

s.t.

$$P_t C_t + Q_t^C D_t + Q_t^T B_t = D_{t-1} + (1 + \rho Q_t^T) B_{t-1} + P_t w_t \int_0^1 N_t(j) dj + P_t \Phi_t,$$

- $D_t$  is **reserves** directly held by the household and issued by Central Bank.
- $B_t$  is long-duration **government bonds**. Duration is given by  $\rho$ .
- $\Phi$  is the firm's profit.

# Firms

- Standard set up of the adjustment cost model.

$$\max_{p_t(i)} E_t \sum_{T=t}^{\infty} \beta^T \Lambda_t \left( \underbrace{(1 - \tau_t)p_t(i)y_t(i)}_{\text{Sales tax}} - \underbrace{\mu_t^w w_t N_t(i)}_{\substack{\text{Exogenous} \\ \text{Cost-push shock}}} - P_t \frac{\varphi}{2} \left( \frac{p_t(i)}{p_{t-1}(i)} - 1 \right)^2 Y_t \right)$$

Production function  $y_t(i) = \underbrace{A_t}_{\substack{\text{Exogenous} \\ \text{Productivity}}} N_t(i)$

# Government

- Treasury's budget

$$Q_t^T B_t^T + P_t \tau_t Y_t + \overbrace{P_t H_t}^{\text{Remittance from CB}} = (1 + \rho Q_t^T) B_{t-1}^T + P_t G_t$$

$B^T$  is the total supply of government bonds. The government expenditure,  $G_t$ , is exogenous.

- Central Bank trades reserves and government bonds.

$$\begin{array}{c} \text{Trade reserves} \quad \text{Trade government bonds} \quad \text{Remittance to Treasury} \\ \swarrow \quad \searrow \quad \downarrow \\ Q_t^C D_t + (1 + \rho Q_t^T) B_{t-1}^C = D_{t-1} + Q_t^T B_t^C + \overbrace{P_t H_t} \end{array}$$

$D$  is reserves.  $B^C$  is government bonds held by Central Bank.

- Inequality constraint on the remittance

$$H_t \geq H^*$$

# Central Bank's Asset Purchase Policy

- Assume an exogenous asset purchase rule.

$$B_t^C = \alpha B_t^T$$

- $B^C$  is government bonds held by Central Bank.
  - $B^T$  is total supply of government bonds.
  - $\alpha$  is a parameter.
- Reduces the size of the state space (4 states  $\rightarrow$  3 states).
  - The goal of Central Bank's asset purchase policy is to stabilize the financial market.

# Equilibrium

- Market Clearing Condition

$$\text{(Goods)} \quad Y_t = C_t + G_t + \frac{\varphi}{2} (\pi_t - 1)^2 Y_t$$

$$\text{(Government bonds)} \quad B_t^H + B_t^C = B_t^T$$

# Optimal Policy (Discretion) – Unconsolidated Model

$$\max E_0 \sum_{t=0}^{\infty} \beta^t \left[ \frac{1}{1-\sigma} C_t^{1-\sigma} - \frac{1}{1+\nu} N_t^{1+\nu} + \frac{\chi_1}{1-\gamma_1} \left( Q_t^C \frac{D_t}{P_t} \right)^{1-\gamma_1} + \frac{\chi_2}{1-\gamma_2} \left( (1-\alpha) Q_t^T \frac{B_t}{P_t} \right)^{1-\gamma_2} \right]$$

## Choice

$C_t, N_t, \pi_t$ , Sales Tax  
Two liabilities  
Prices of liabilities  
Remittance

Euler Equations

NKPC

Market Clearing

Treasury

CB

Remittance  $H_t \geq H^*$

# Optimal Policy (Discretion) – Unconsolidated Model

$$\max E_0 \sum_{t=0}^{\infty} \beta^t \left[ \frac{1}{1-\sigma} C_t^{1-\sigma} - \frac{1}{1+\nu} N_t^{1+\nu} + \frac{\chi_1}{1-\gamma_1} \left( Q_t^C \frac{D_t}{P_t} \right)^{1-\gamma_1} + \frac{\chi_2}{1-\gamma_2} \left( (1-\alpha) Q_t^T \frac{B_t}{P_t} \right)^{1-\gamma_2} \right]$$

## The role of remittance when there is fiscal backing

- Relax one budget by tightening the other.

## Why is Central Bank's loss an issue?

- Large reserves  $\rightarrow$  Central Bank's loss.
- Downward-sloping demand curve.
- Price of reserves ( = nominal interest rate ) drops.

## Why is the lack of fiscal support an issue?

- To reduce large reserves, funds from Treasury are required.

Euler Equations

NKPC

Market Clearing

Treasury

CB

Remittance  $H_t \geq H^*$



# Optimal Policy (Discretion) – Consolidated Model

$$\max E_0 \sum_{t=0}^{\infty} \beta^t \left[ \frac{1}{1-\sigma} C_t^{1-\sigma} - \frac{1}{1+\nu} N_t^{1+\nu} + \frac{\chi_1}{1-\gamma_1} \left( Q_t^C \frac{D_t}{P_t} \right)^{1-\gamma_1} + \frac{\chi_2}{1-\gamma_2} \left( (1-\alpha) Q_t^T \frac{B_t}{P_t} \right)^{1-\gamma_2} \right]$$

Euler Equations

NKPC

Market Clearing

Consolidated  
Government

$$Q_t^C D_t + Q_t^T (1-\alpha) B_t + \tau_t P_t Y_t = D_{t-1} + (1 + \rho Q_t^T) (1-\alpha) B_{t-1} + P_t G_t.$$

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## Solution

- **Discretion**. Markov-perfect equilibrium.
- State variables: Shock, reserves, and government bonds.
- Shock: Cost-push, productivity, or government expenditure.
- **Globally** solve the model.
  - Occasionally binding constraints,  $H_t \geq H^*$ .

# Calibration

	Variable	Value	Description	Target	Model	Data
Standard NK	$\beta$	0.995	Discount factor	-	-	-
	$\sigma$	2	Risk aversion	-	-	-
	$\nu$	7	Frisch Elasticity	Frisch Elasticity	1/7	-
	$\theta$	10	Elasticity of substitution	Mark up	7%	-
	$\varphi$	100	Price adjustment cost	Slope of NKPC	0.05	-
	$\rho^T$	0.94	Duration of Treasury	Average maturity	4 years	4 years
	$\chi_1$	0.0006	Utility from reserves	Steady-state reserves	15% of GDP	15% of GDP
	$\chi_2$	0.0014	Utility from Treasury bond	Steady state Treasury	40% of GDP	80% of GDP
$(Q^c d)^{1-\gamma_1}$	$\gamma_1$	1.7	Curvature of utility from reserves	$\frac{\partial Q^c}{\partial d}$	0.1	0.05~0.2
$(Q^T b)^{1-\gamma_2}$	$\gamma_2$	1.5	Curvature of utility from Treasury	$\frac{\partial Q^T}{\partial b}$	0.05	0~0.1
	$\alpha$	0.4	CB's asset holding	CB's Net worth	1	1
	$H^*$	-0.005	Lower bound on remittance	-	-0.5% of GDP	-

# Results

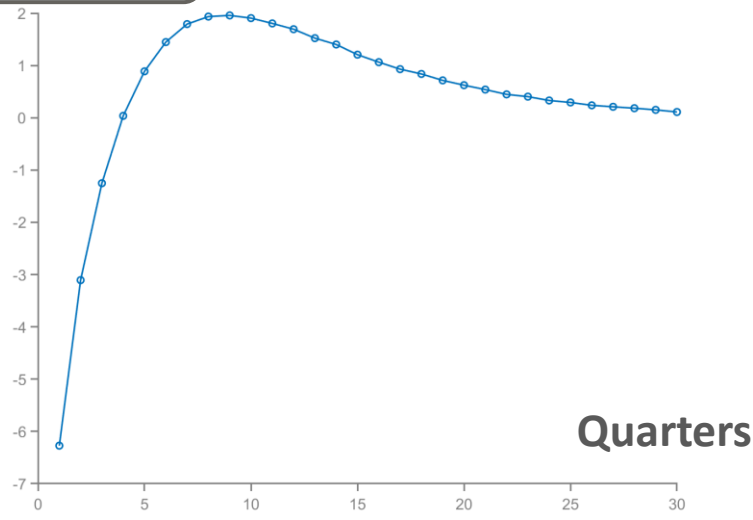
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## Simulation

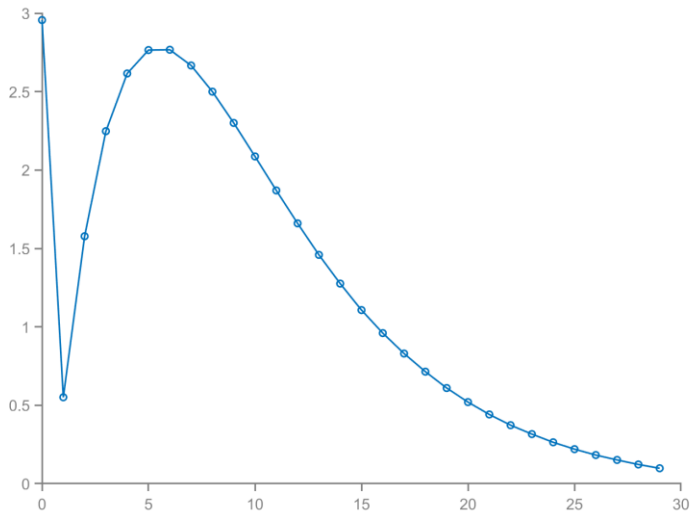
- Positive cost-push shock. 9% increase in wage mark-up.
- The size of the response is small (0.8% of the fall in output and 0.4% of the rise in inflation).
  - I do not finish solving the model with large shock.
- The initial state variables are large reserves (90<sup>th</sup> percentile of simulated reserves).

Cost-push shock  
Consolidated

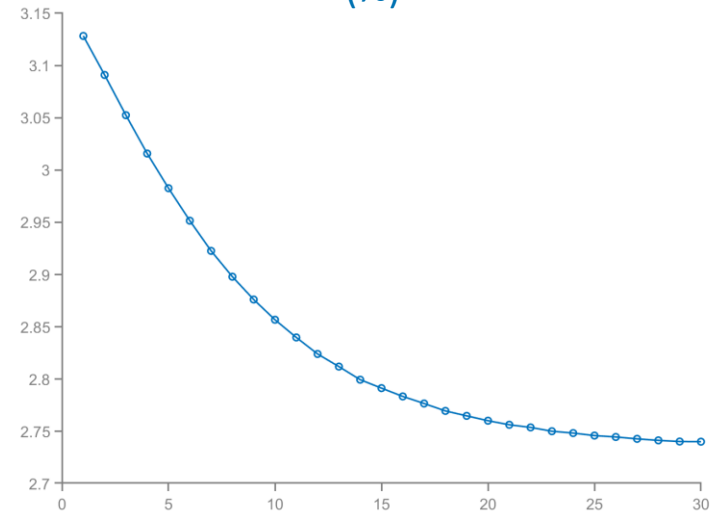
**Tax rate**  
(SS deviation in %)



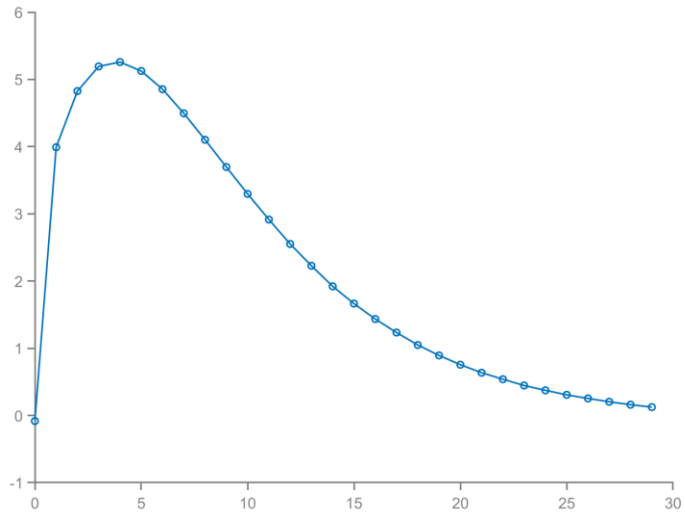
**Reserves**  
(SS deviation in %)



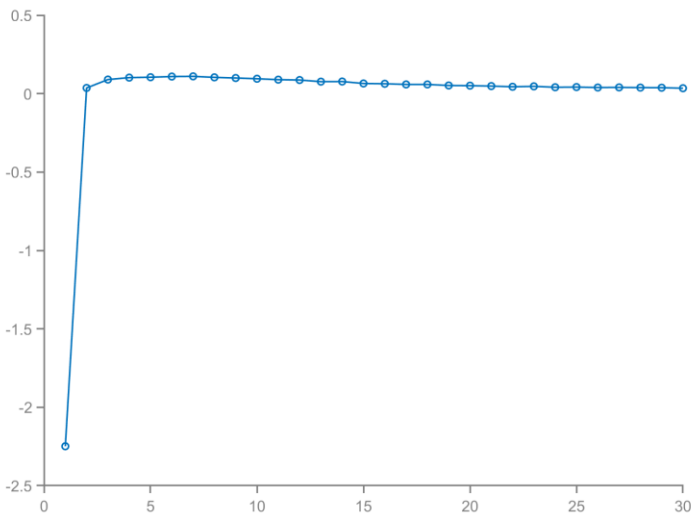
**Inflation**  
(%)



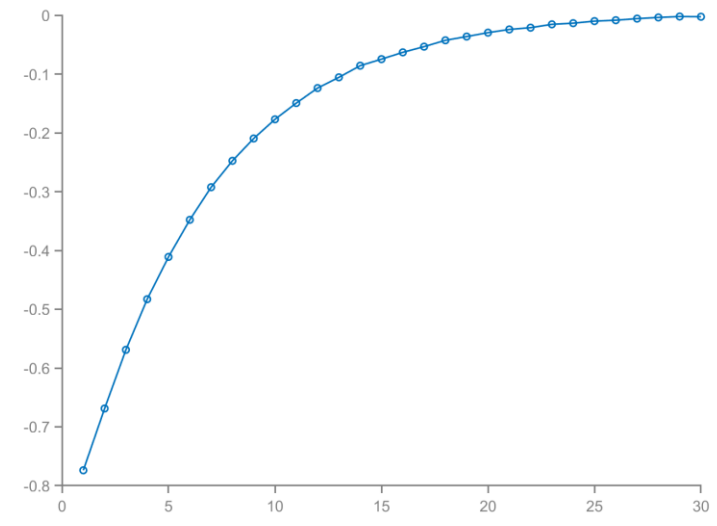
**Government bonds**  
(SS deviation in %)



**Remittance**  
(Ratio to GPD in %)

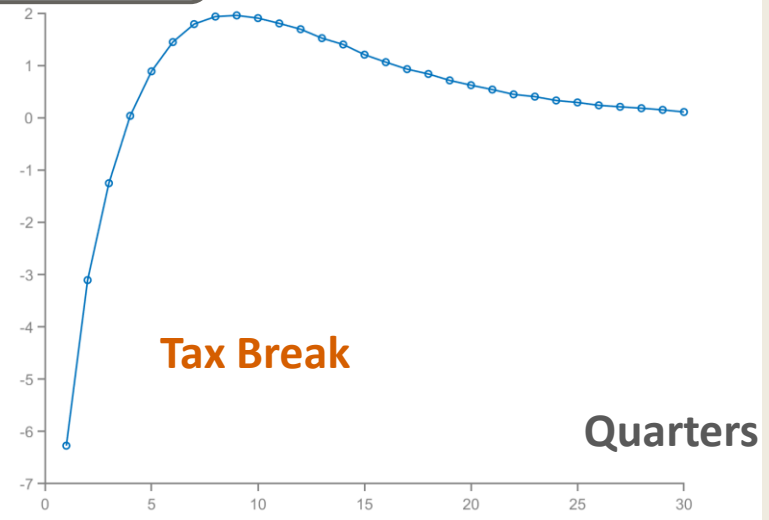


**Consumption**  
(SS deviation in %)

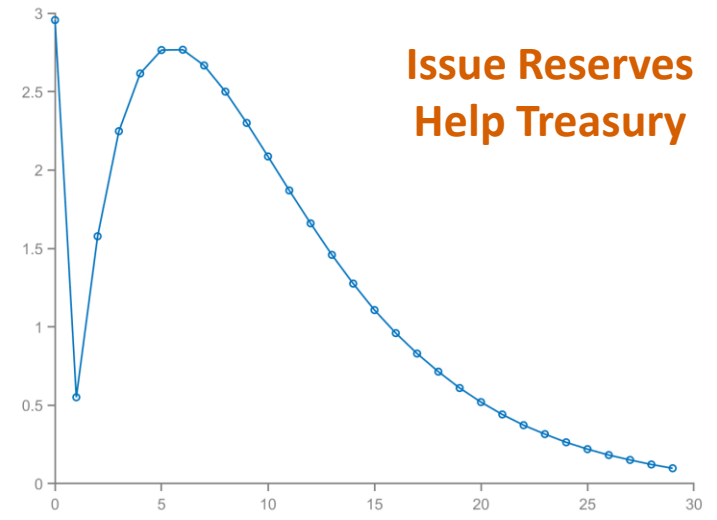


Cost-push shock  
Consolidated

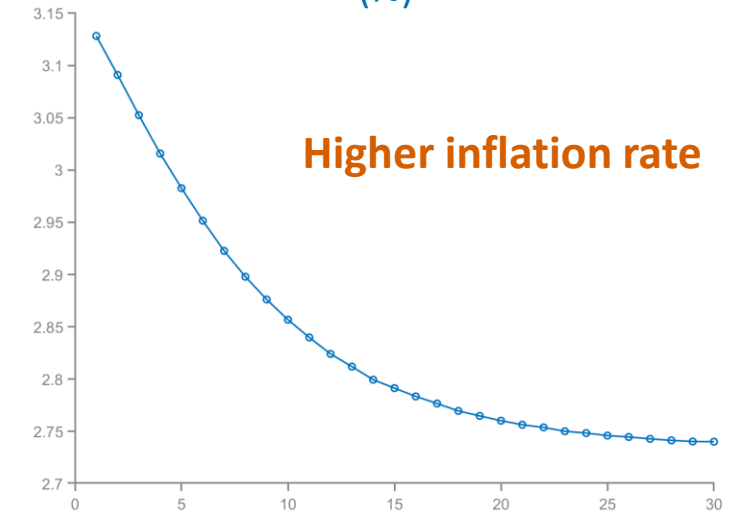
**Tax rate**  
(SS deviation in %)



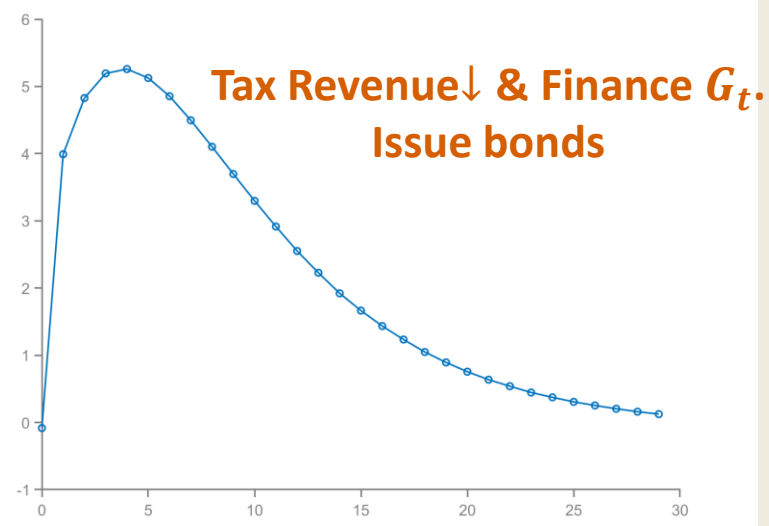
**Reserves**  
(SS deviation in %)



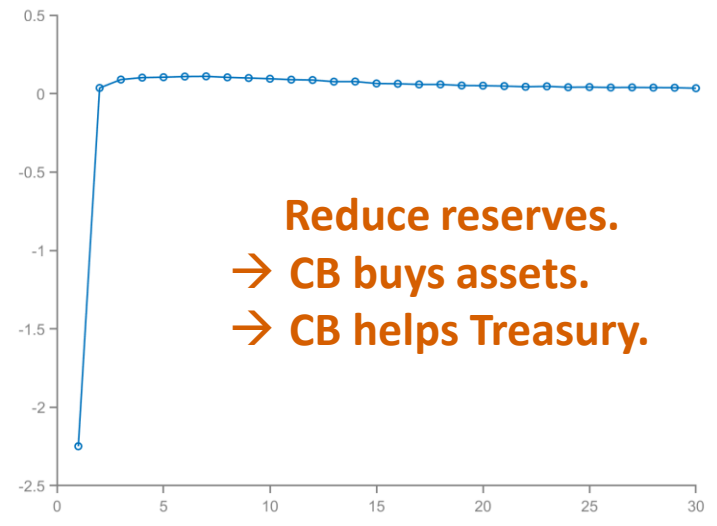
**Inflation**  
(%)



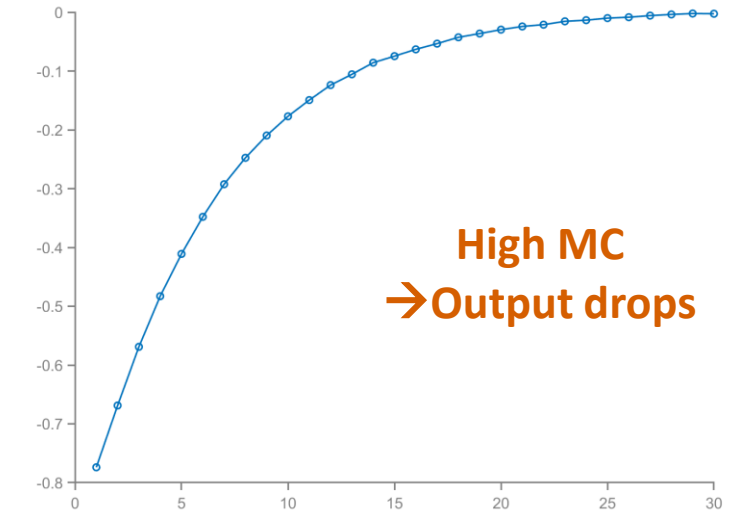
**Government bonds**  
(SS deviation in %)



**Remittance**  
(Ratio to GPD in %)

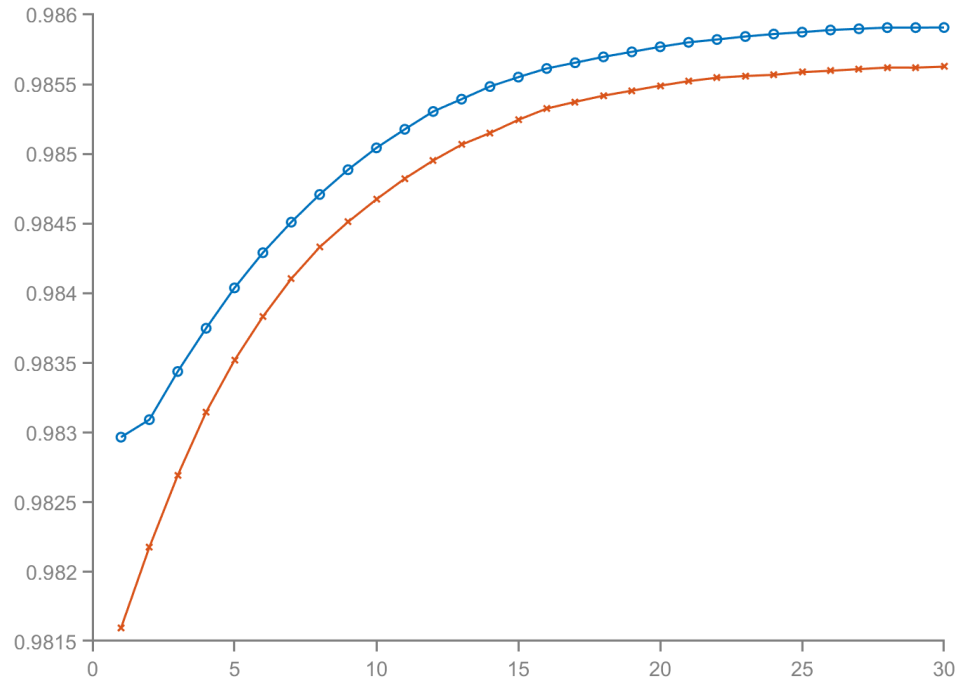


**Consumption**  
(SS deviation in %)

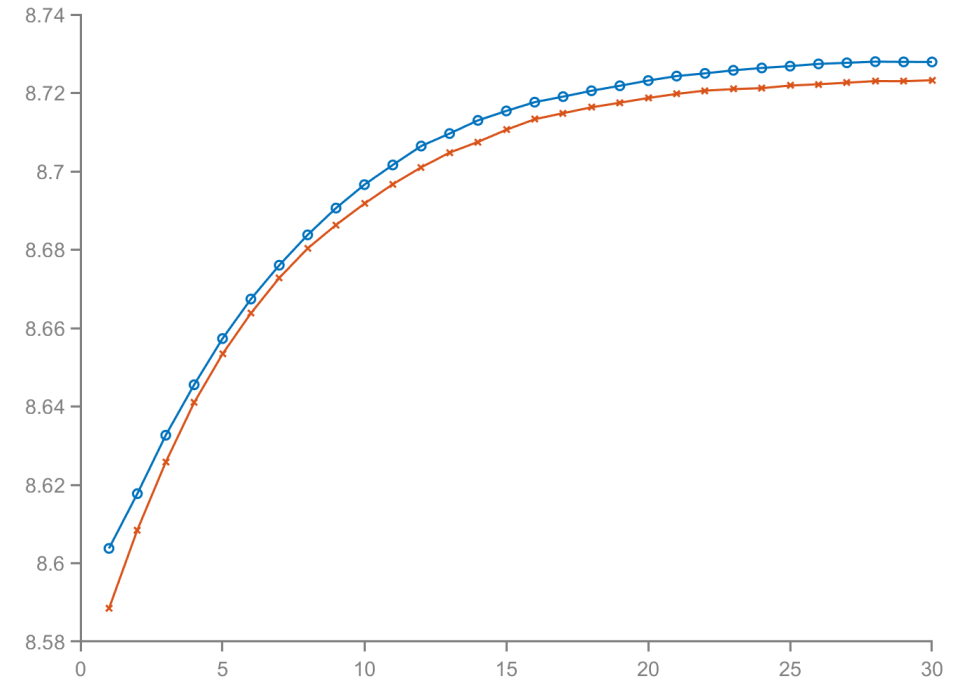


CB receives

## Price of reserves



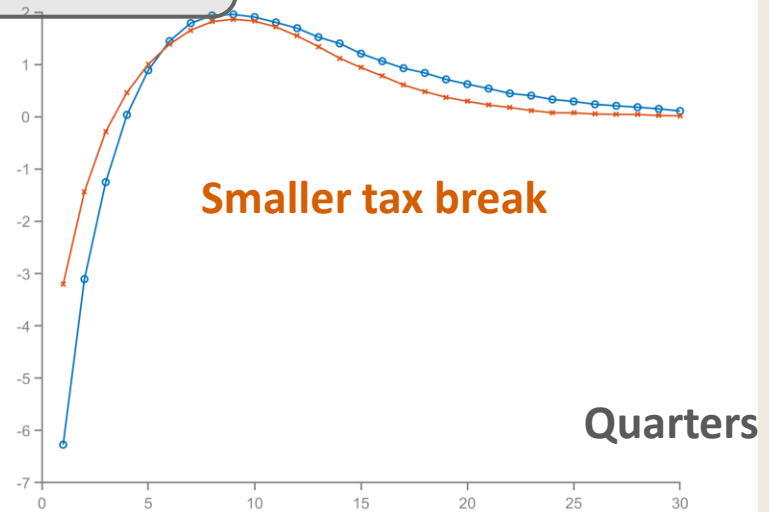
## Price of government bonds



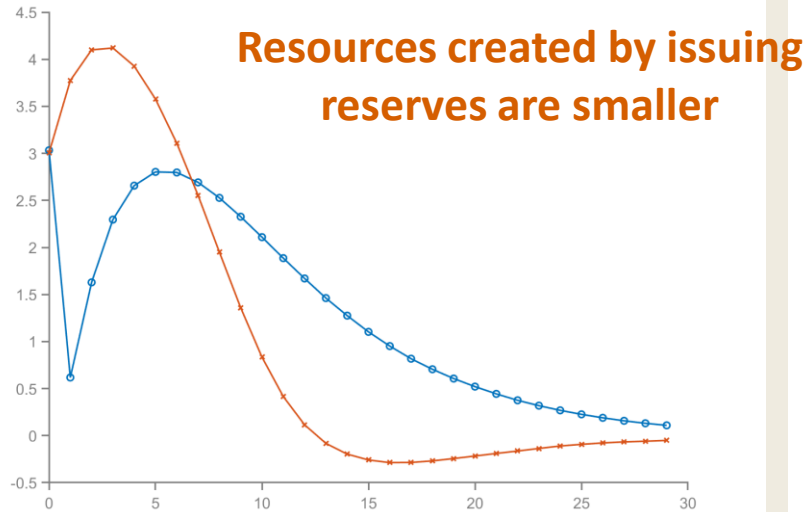


Unconsolidated  
Consolidated

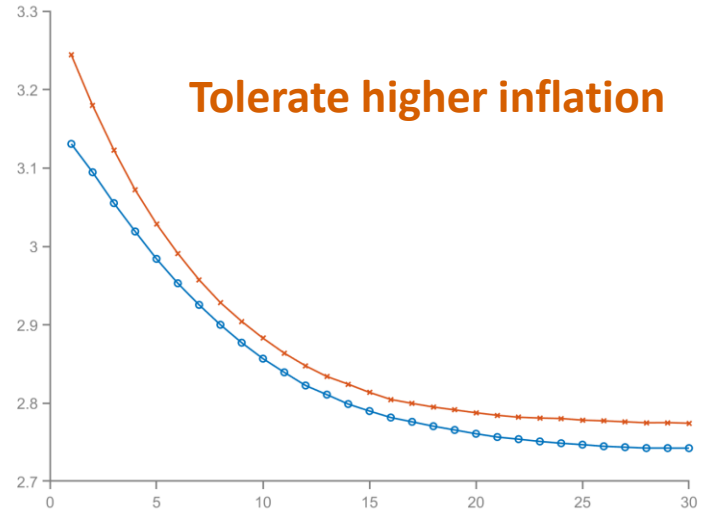
### Tax rate



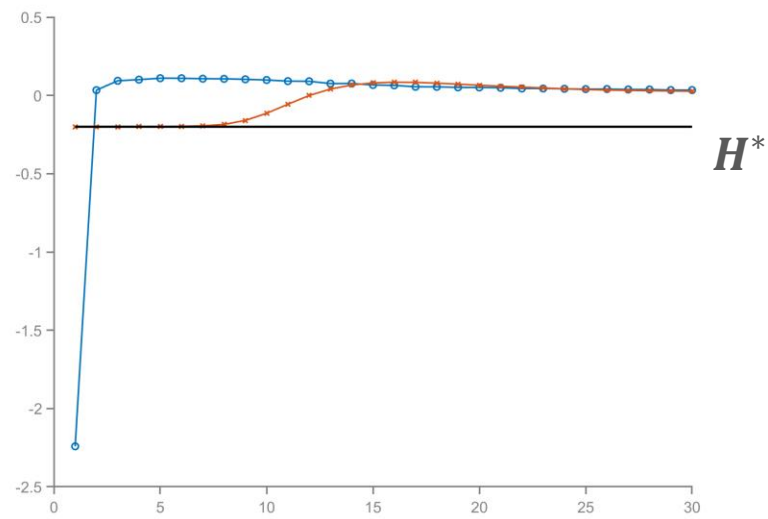
### Reserves



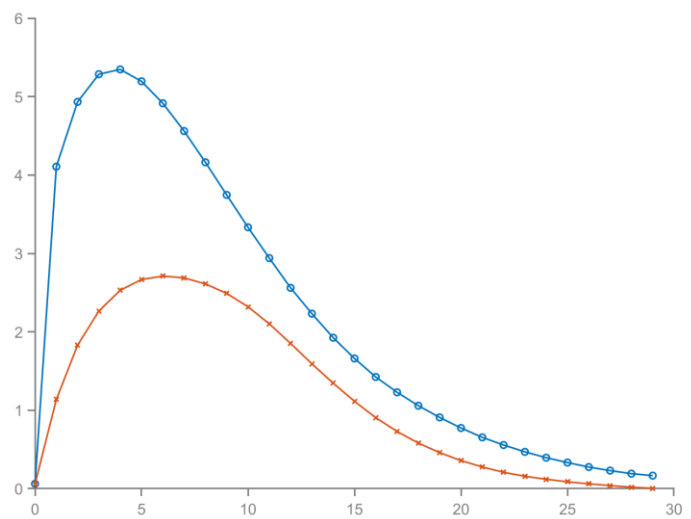
### Inflation



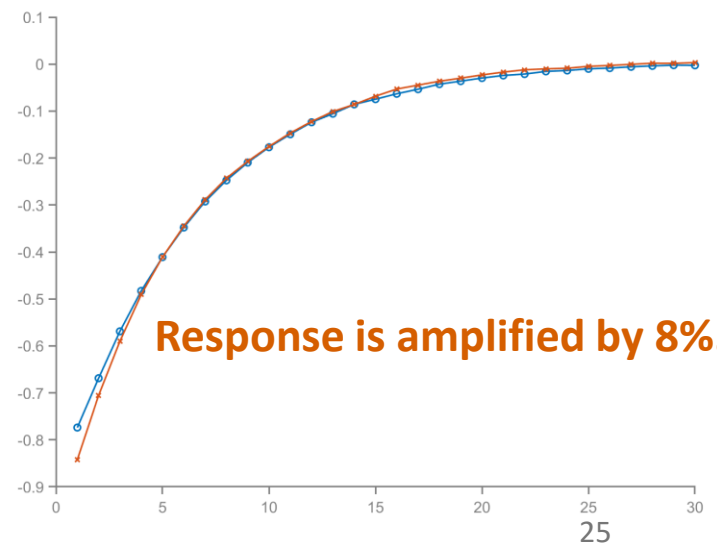
### Remittance



### Government Bonds



### Consumption



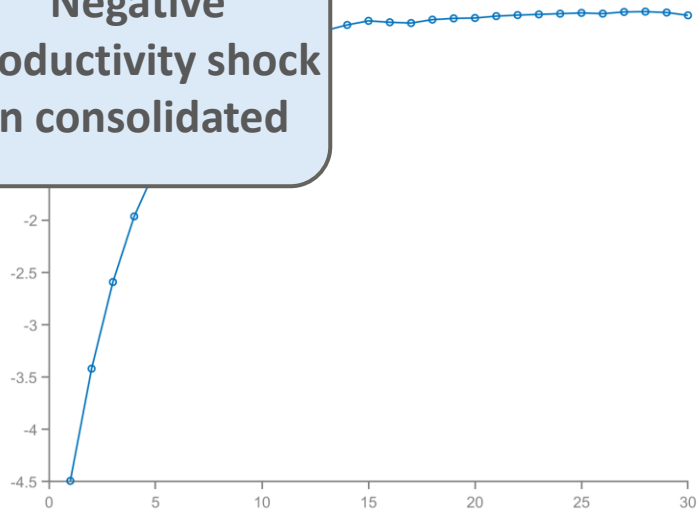
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# Primary Policy Tool and Central Bank's Role

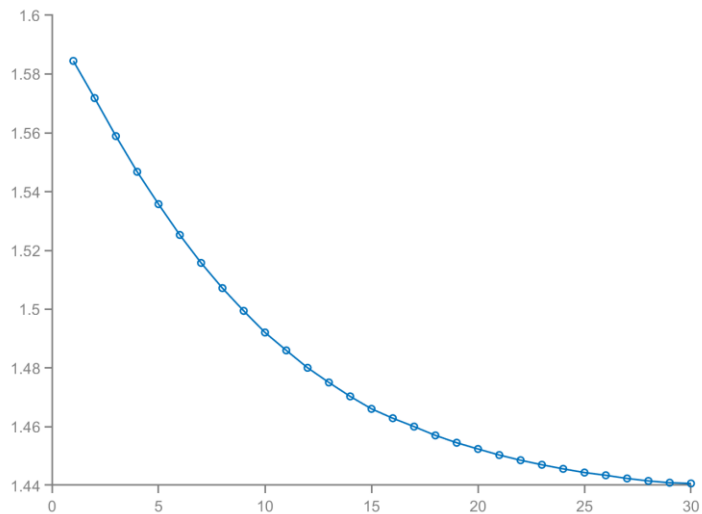
- After cost-push shock, the primary policy tool is tax break.
- **Central Bank's role to issue reserves helps tax break.**
- After productivity shock, **Central Bank's role is to raise nominal interest rate enough.**
- When the household cannot absorb large reserves, the unconsolidated model gives difference.

### Consumption

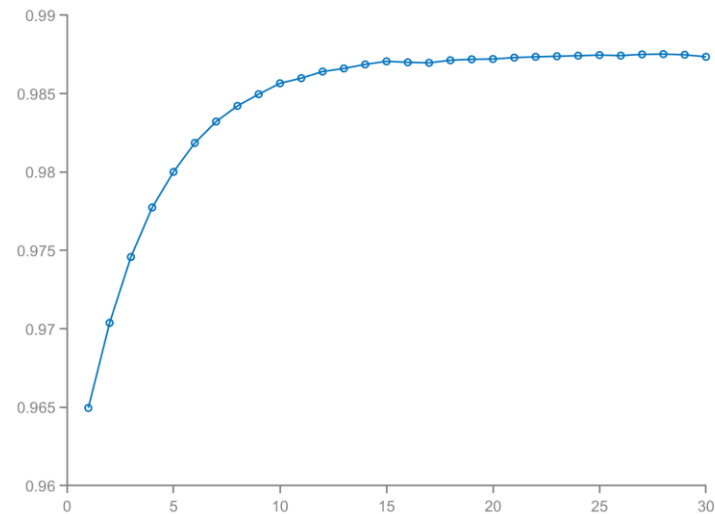
Negative productivity shock in consolidated



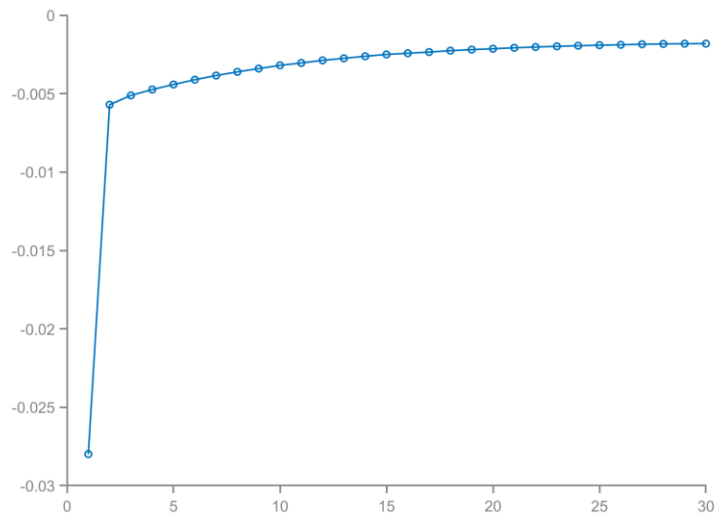
### Inflation



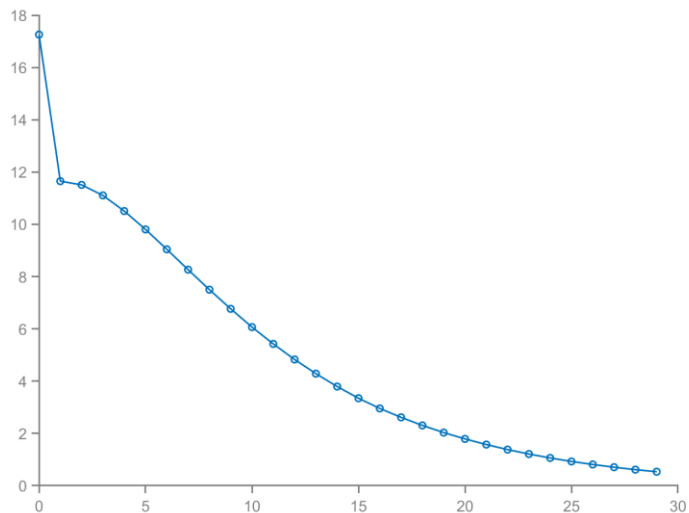
### Price of Reserves



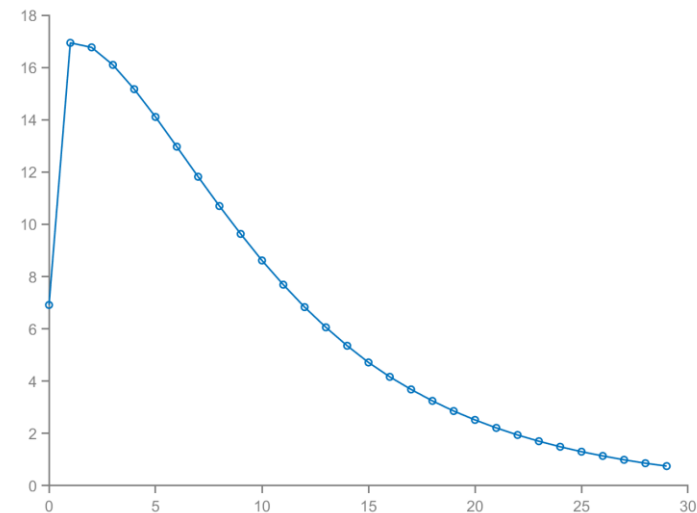
### Remittance



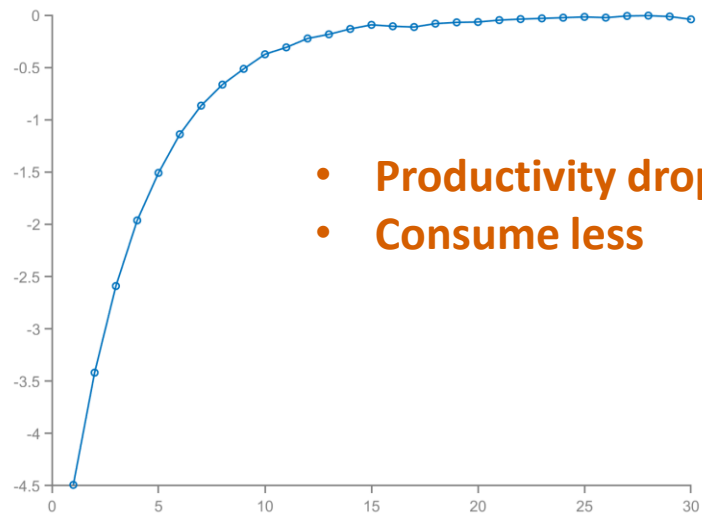
### Reserves



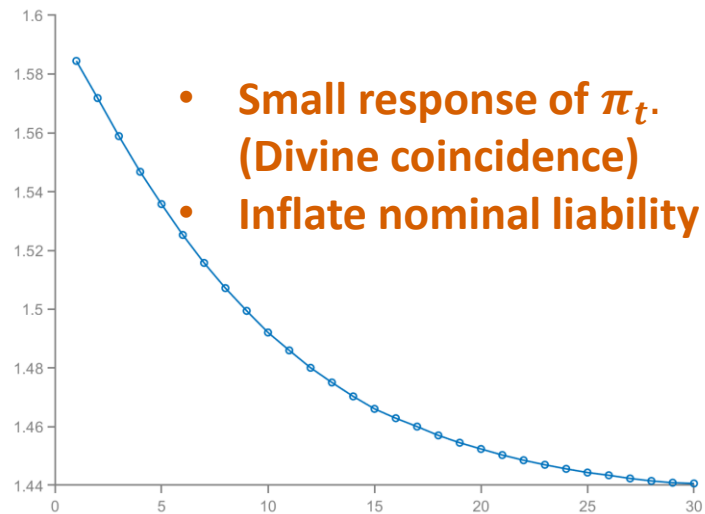
### Treasury liability



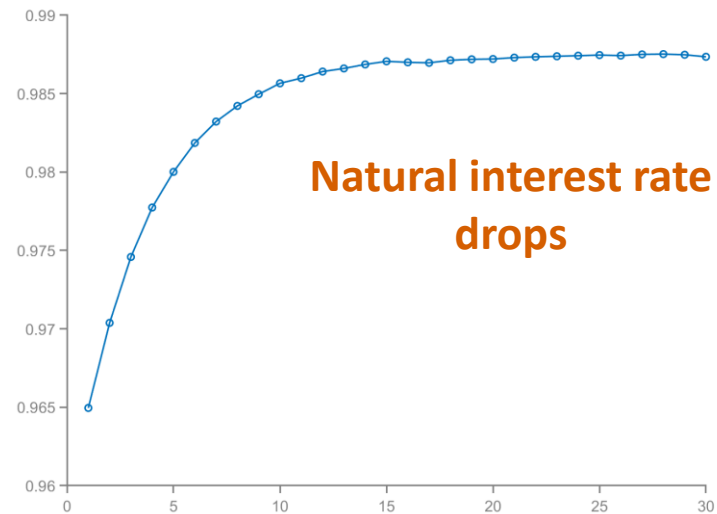
## Consumption



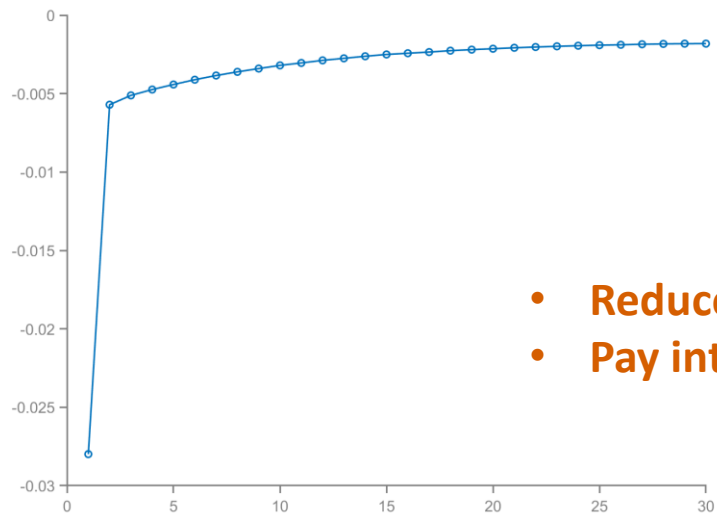
## Inflation



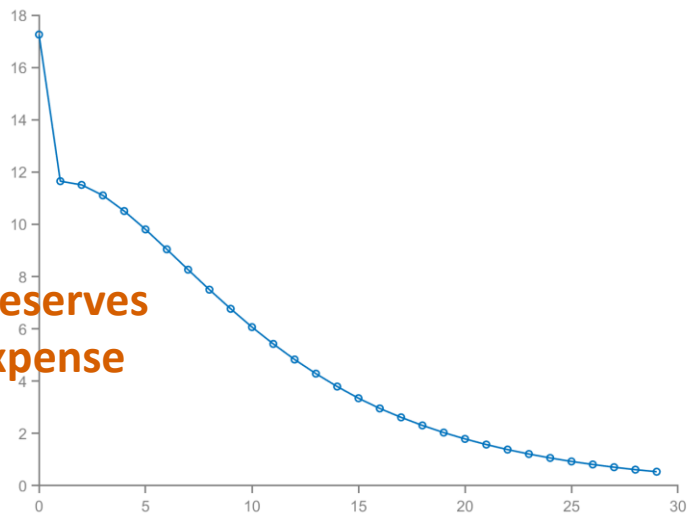
## Price of Reserves



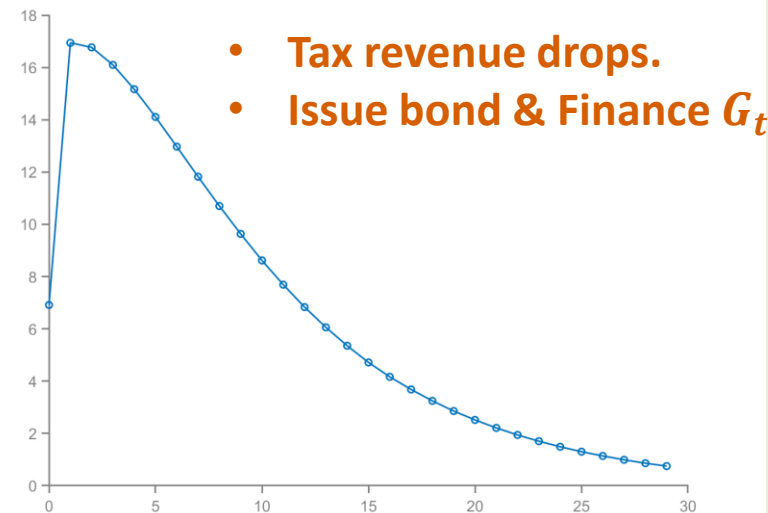
## Remittance



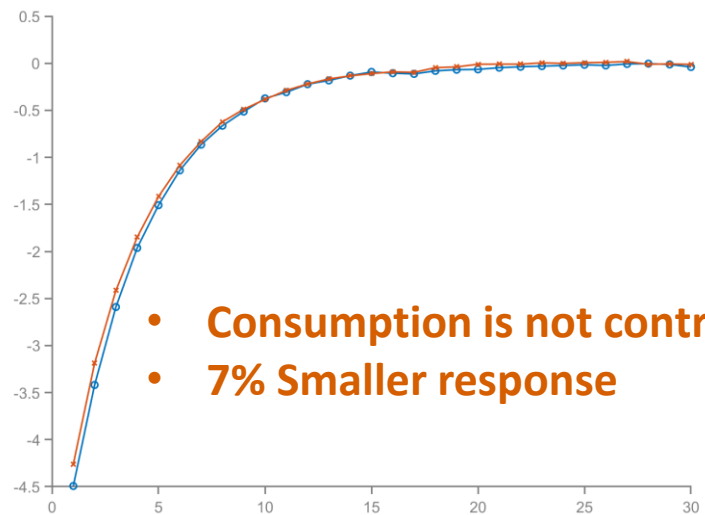
## Reserves



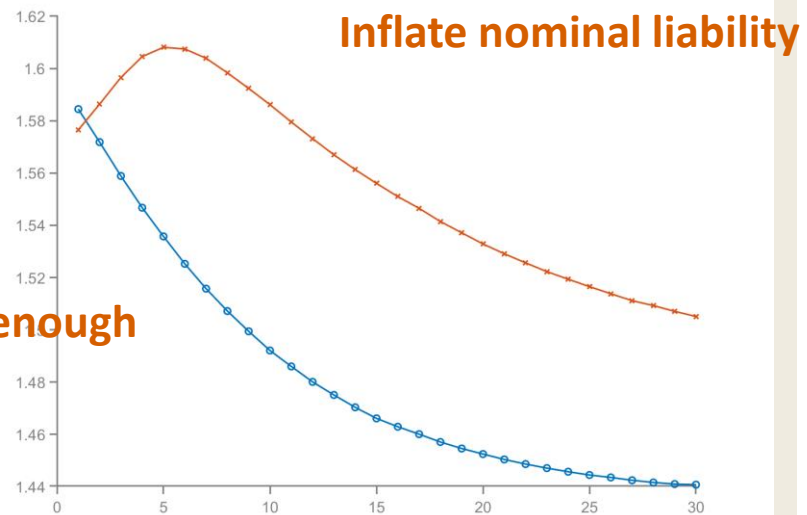
## Treasury liability



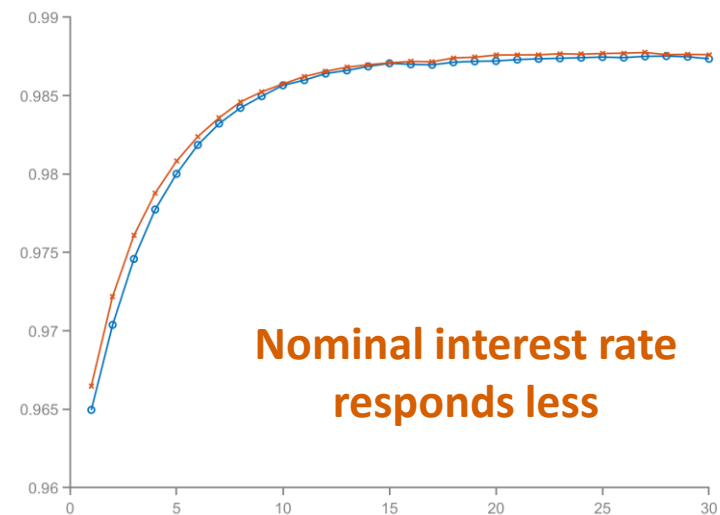
## Consumption



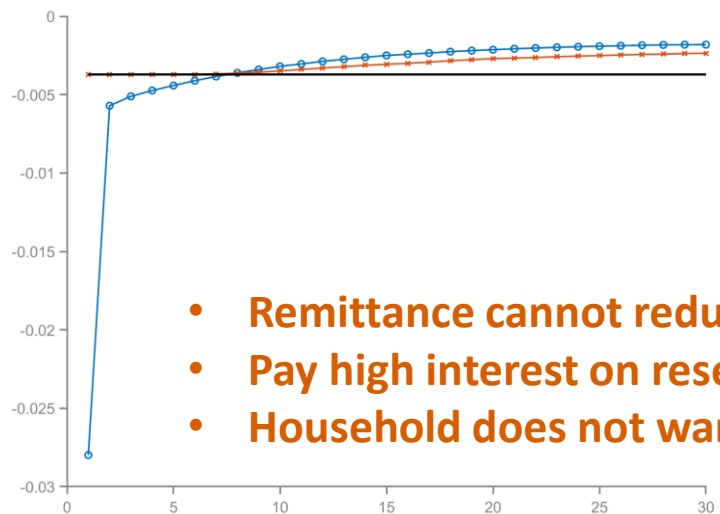
## Inflation



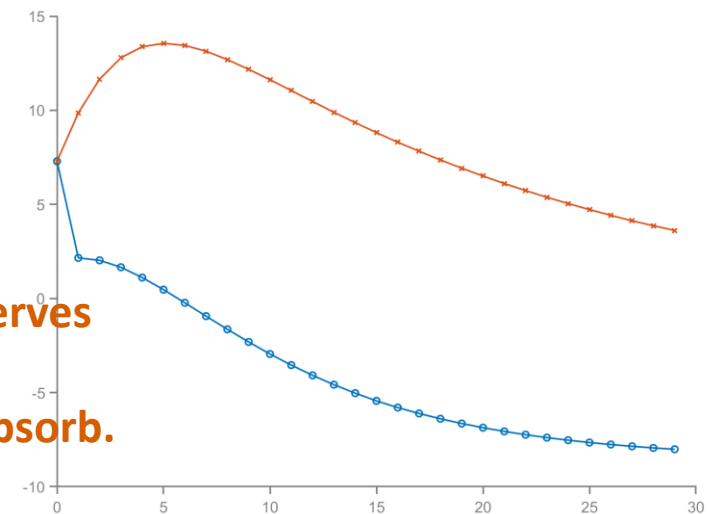
## Price of Reserves



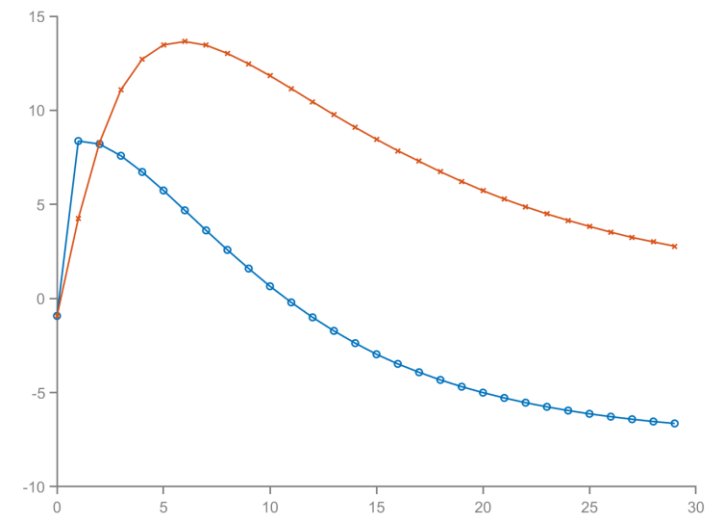
## Remittance



## Reserves



## Treasury liability



# Dynamic Properties of the Optimal Policy

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## Does the fiscal backing affect dynamic properties of the optimal policy?

- I simulate the economy in the consolidated and unconsolidated model.
- Compute the variance of consumption, inflation, and tax rate.

- Show the change in volatility in the unconsolidated model compared to the consolidated model.

	Cost-push shocks	Government expenditure shock
Consumption	<b>+3%</b>	<b>+0.6%</b>
Tax	<b>-10%</b>	<b>+2%</b>
Inflation	<b>+3%</b>	<b>+2%</b>

**The lack of fiscal backing constrains the size of tax break**

**The lack of fiscal backing limits tax smoothing**



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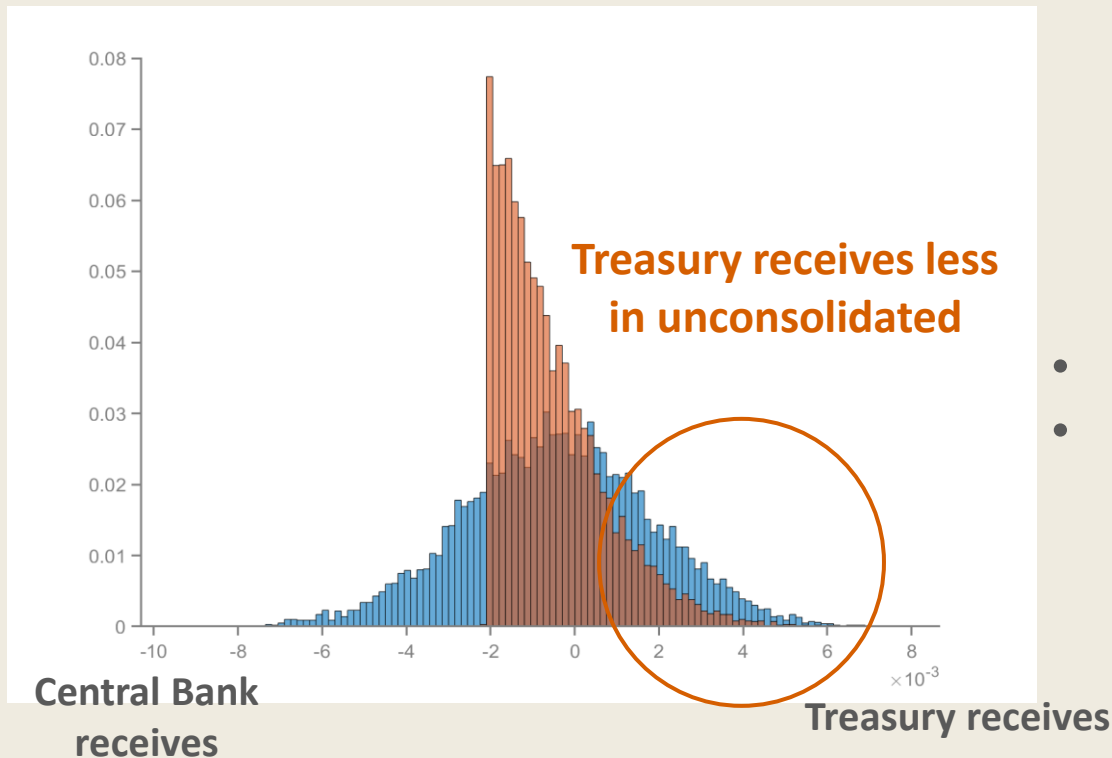
# Retained Earnings by Central Banks

- Bank of Japan **retains 5% of profits** and transfers the rest to the Treasury.
- Bundesbank uses its financial buffers to cushion burdens.
- No reason to retain earnings if Central Bank and Treasury are consolidated.

# Why do Central Banks transfer less?

## Model implications

- A lower bound on remittance makes the upper tail thinner.
- Central Bank knows large reserves cannot be reduced through remittance.
- Less reserves and transfers. **Forward looking decision-making.**

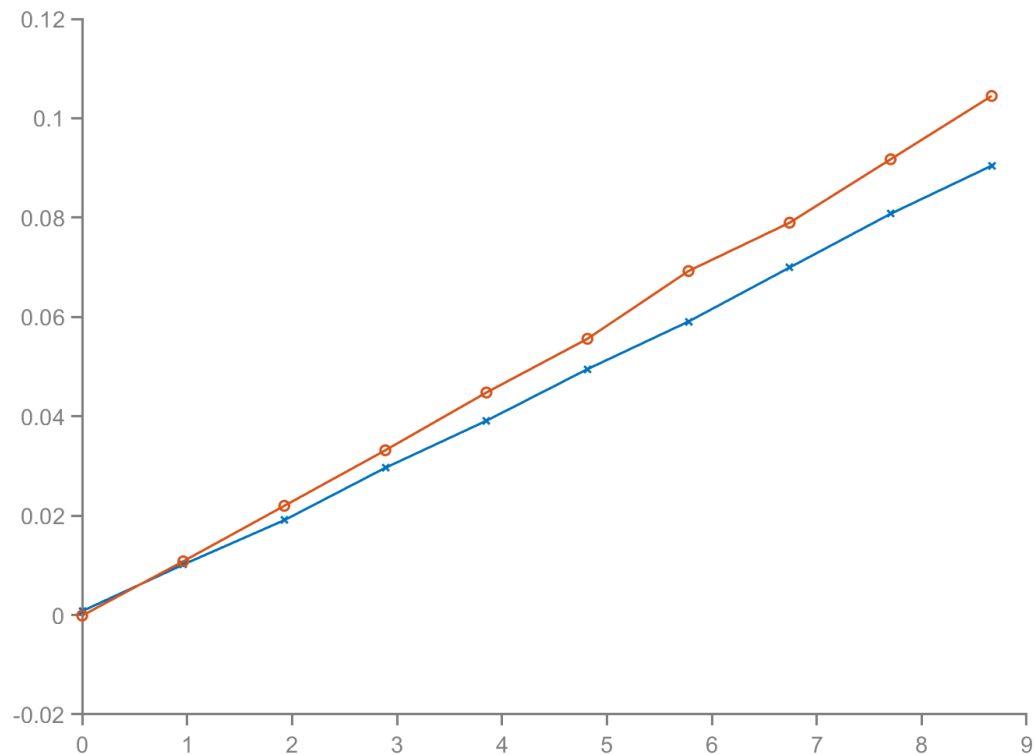


- Simulated the economy with cost-push shock.
- Histogram for remittance in consolidated and unconsolidated.

# The welfare gain of fiscal backing

# The welfare gain of fiscal backing increases with the size of shock.

Welfare cost of  
cost-push shock in  
consumption  
equivalence (%).



Increase in wage mark-up in %.

- Compute the welfare loss of cost-push shock compared to the steady-state.
- Show the welfare loss (horizontal) on the size of shock (vertical) for consolidated and unconsolidated.
- Fiscal backing can reduce the welfare loss by 20%.

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## The welfare gain of fiscal backing $< 0.01\%$ in consumption equivalence.

- I compute the welfare gain of increasing the lower bound on remittance,  $H^*$ .
- Simulate the economy for 1000 periods. Consumption equivalence compared to the case of  $H^* = -\infty$ .

(Intuition)

- Fiscal backing affects the variance but less the mean.