

# Optimal monetary and fiscal policy without fiscal backing for the central bank

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# Introduction

- The Fed runs a large loss by paying interest on reserves after 2022.
  - Expenditure = Interest rate (5p.p.) \* Reserve (15% of GDP)
  - Fed's loss / Treasury's tax revenue (2022 Q4 – 2024 Q3) = 2.5%
- The Fed transferred all profits to the Treasury before 2022.
- The Treasury does not offset the Fed's losses now.
- However, conventional macroeconomic models assume a consolidated government budget (Sargent and Wallace 1981).

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# Research Question

Do the **unconsolidated government budgets** change monetary-fiscal policy?

Treasury cannot provide the **optimal fiscal support** to the central bank.

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# What I do

## Optimal monetary and fiscal Policy without commitment

The decision-making problem for the government.

- Maximize the household utility subject to the equilibrium conditions.
  1. NK model with two interest-bearing liabilities, reserves and Government bonds.
  2. Constraint an optimal resource allocation from Treasury to the central bank.

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# What I find

1. Study the inflationary episode after 2022 and negative productivity shock.

## Question.

How does the impulse responses change when the central bank lacks fiscal backing?

## Answer.

The central bank without fiscal backing tolerates higher inflation.

The key is the large reserves as an initial condition.

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# What I find

1. Study the inflationary episode after 2022 and negative productivity shock.
2. Quantitatively characterize the dynamic property of the optimal policy.

## Question.

Does the lack of fiscal support make the optimal monetary-fiscal policy volatile?

## Answer.

Inflation is more volatile by 3% without the fiscal backing.

Tax is more volatile for productivity and government expenditure shocks, but less for cost-push.

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# What I find

1. Study the inflationary episode after 2022 and negative productivity shock.
2. Quantitatively characterize the dynamic property of the optimal policy.
3. **Question**

From a normative point, should the Treasury support the central bank?

## **Answer.**

The welfare gain of fiscal backing is small in the typical business cycle.

<0.01% in consumption equivalence

The key is 1. “typical” business cycle VS. Large reserves as an initial condition.

2. Stochastic steady-state VS Dynamics.

# Model



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# Environment

- **Time.** Discrete, Infinite horizon.

- **Agents**

**Household** consumes, works, and trades reserves and government bonds. Appreciate reserves and bonds as a liquidity value.

**Producers** are the simple New-Keynesian style.

**Treasury** provides public expenditure. Finance by distortionary sales tax, government bonds, and remittance from the central bank.

**Central bank** provides reserves. Purchases government bonds to stabilize net worth.

- **Market.** Reserves and government bonds are traded. They differ in duration and liquidity value.

# Household

$$\max_{C_t, N_t(j), B_t^H, D_t^H} \sum_{t=0}^{\infty} \beta^t \left[ \frac{1}{1-\sigma} C_t^{1-\sigma} - \frac{1}{1+\nu} N_t^{1+\nu} + \frac{\chi_1}{1-\gamma_1} (Q_t^d D_t^H)^{1-\gamma_1} + \frac{\chi_2}{1-\gamma_2} (Q_t^b B_t^H)^{1-\gamma_2} \right]$$

s.t.

$$P_t C_t + Q_t^d D_t^H + Q_t^b B_t^H = D_{t-1}^H + (1 + \rho^T Q_t^b) B_{t-1}^H + P_t w_t \int_0^1 N_t(j) dj + P_t \Phi_t,$$

- $D_t^H$  is **reserves** directly held by the household and issued by the central bank.
- $B_t^H$  is a long-duration government bond. Duration is given by  $\rho^T$ .
- $\Phi$  is the firm's profit.

# Firms

- Standard set up of the adjustment cost model.

$$\max_{p_t(i)} E_t \sum_{T=t}^{\infty} \beta^T \Lambda_t \left( \underbrace{(1 - \tau_t)p_t(i)y_t(i)}_{\text{Sales tax}} - \underbrace{\mu_t^w w_t N_t(i)}_{\substack{\text{Exogenous} \\ \text{Cost-push shock}}} - P_t \frac{\varphi}{2} \left( \frac{p_t(i)}{p_{t-1}(i)} - 1 \right)^2 Y_t \right)$$

Production function  $y_t(i) = \underbrace{A_t}_{\substack{\text{Exogenous} \\ \text{Productivity}}} N_t(i)$

# Government

- Treasury's budget

Remittance from CB

$$Q_t^b B_t^T + P_t \tau_t Y_t + \overbrace{P_t H_t}^{\text{Remittance from CB}} = (1 + \rho^T Q_t^b) B_{t-1}^T + P_t G_t$$

$B^T$  is the total supply of government bonds. The government expenditure,  $G_t$ , is exogenous.

- Central bank's budget

Remittance to Treasury

$$Q_t^d D_t^C + (1 + \rho^T Q_t^b) B_{t-1}^C = D_{t-1}^C + Q_t^b B_t^C + \overbrace{P_t H_t}^{\text{Remittance to Treasury}}$$

$D^C$  is reserves.  $B^C$  is a Treasury's bond held by the central bank.

$$B_t^C = \alpha B_t^T$$

- Inequality constraint on the remittance

$$H_t \geq H^*$$

# Equilibrium

- Market Clearing Condition

$$\text{(Goods)} \quad Y_t = C_t + G_t + \frac{\varphi}{2} (\pi_t - 1)^2 Y_t$$

$$\text{(Reserves)} \quad D_t^H = D_t^C$$

$$\text{(Government bonds)} \quad B_t^H + B_t^C = B_t^T$$

# Optimal Policy (Discretion) - Unconsolidated Budgets

$$\max E_0 \sum_{t=0}^{\infty} \beta^t \left[ \frac{1}{1-\sigma} C_t^{1-\sigma} - \frac{1}{1+\nu} N_t^{1+\nu} + \frac{\chi_1}{1-\gamma_1} (Q_t^C b_t^C)^{1-\gamma_1} + \frac{\chi_2}{1-\gamma_2} ((1-\alpha) Q_t^T b_t^T)^{1-\gamma_2} \right]$$

Choice

$C_t, N_t, \pi_t$ , Sales Tax  
Two liabilities  
Prices of liabilities  
Remittance

Euler Equations

NKPC

Market Clearing

Treasury

$$Q_t^b B_t^T + P_t \tau_t Y_t + P_t H_t = (1 + \rho^T Q_t^b) B_{t-1}^T + P_t G_t.$$

CB

$$Q_t^d D_t^C + (1 + \rho^T Q_t^b) B_{t-1}^C = D_{t-1}^C + Q_t^b B_t^C + P_t H_t$$

$$H_t \geq H^*$$

Remittance

# Optimal Policy (Discretion) - Unconsolidated Budgets

$$\max E_0 \sum_{t=0}^{\infty} \beta^t \left[ \frac{1}{1-\sigma} C_t^{1-\sigma} - \frac{1}{1+\nu} N_t^{1+\nu} + \frac{\chi_1}{1-\gamma_1} (Q_t^C b_t^C)^{1-\gamma_1} + \frac{\chi_2}{1-\gamma_2} ((1-\alpha) Q_t^T b_t^T)^{1-\gamma_2} \right]$$

**Choice**

$C_t, N_t, \pi_t$ , Sales Tax  
Two liabilities  
Prices of liabilities  
Remittance

Euler Equations

NKPC

Market Clearing

Treasury

$$Q_t^b B_t^T + P_t \tau_t Y_t + P_t H_t = (1 + \rho^T Q_t^b) B_{t-1}^T + P_t G_t.$$

CB

$$Q_t^d D_t^C + (1 + \rho^T Q_t^b) B_{t-1}^C = D_{t-1}^C + Q_t^b B_t^C + P_t H_t$$

Remittance

$$H_t \geq H^*$$

**Optimal resource allocation through remittance**

For CB, Reduce abundant reserves & Increase scarce reserves.  
For Treasury, help tax smoothing.

# Optimal Policy (Discretion) - Consolidated Budgets

$$\max E_0 \sum_{t=0}^{\infty} \beta^t \left[ \frac{1}{1-\sigma} C_t^{1-\sigma} - \frac{1}{1+\nu} N_t^{1+\nu} + \frac{\chi_1}{1-\gamma_1} (Q_t^C b_t^C)^{1-\gamma_1} + \frac{\chi_2}{1-\gamma_2} ((1-\alpha) Q_t^T b_t^T)^{1-\gamma_2} \right]$$

Choice

$C_t, N_t, \pi_t$ , Sales Tax  
Two liabilities  
Prices of liabilities  
Remittance

Euler Equations

NKPC

Market Clearing

Consolidated  
Government

$$Q_t^d D_t^C + Q_t^b (1-\alpha) B_t^T + \tau_t P_t Y_t = D_{t-1}^C + (1 + \rho^T Q_t^b) (1-\alpha) B_{t-1}^T + P_t G_t.$$



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## Solution

- **Discretion.** Markov-perfect equilibrium.
- State variables ... Shock, reserves, Treasury bond
- Shock... Cost-push, productivity, and government expenditure.
  - Include one shock and exclude the other two.
- **Globally** solve the model.
  - Occasionally binding constraints,  $H_t \geq H^*$ .
  - The steady state is a priori unknown (The steady state depends on  $\frac{\partial \text{Expectations}}{\partial \text{state variables}}$ ).

# Calibration

Variable	Value	Description	Target	Model	Data
Standard NK	$\beta$	0.995	Discount factor	-	-
	$\sigma$	2	Risk aversion	-	-
	$\nu$	7	Frisch Elasticity	Frisch Elasticity	1/7
	$\theta$	10	Elasticity of substitution among goods	Mark up	7%
	$\varphi$	100	Price adjustment cost	Slope of NKPC	0.05
$\rho^T$	0.9	Duration of Treasury	Average Maturity	10 quarters	32 quarters
$\chi_1$	0.0002	Utility from reserves	Steady-state reserves	15% of GDP	15% of GDP
$\chi_2$	0.0015	Utility from Treasury bond	Steady state Treasury	30% of GDP	80% of GDP
$\gamma_1$	2	Curvature of utility from reserves	$\frac{\partial Q^d}{\partial d}$	0.2	0.05~0.2
$\gamma_2$	2	Curvature of utility from Treasury	$\frac{\partial Q^b}{\partial b}$	0.2	0.2~0.5
$\alpha$	0.4	CB's asset holding	CB's Net worth	1	1
$H^*$	-0.01	Lower bound on remittance	-	-1% of GDP	-

# Results

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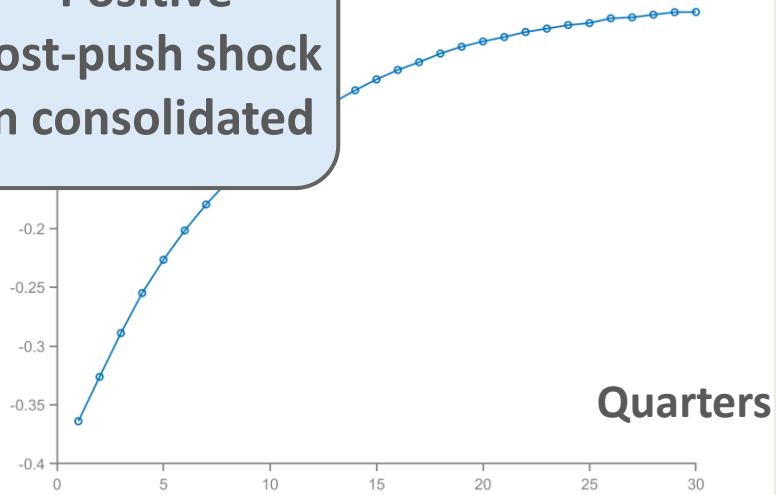
## Simulation

- The initial state variables are large reserves (90<sup>th</sup> percentile of simulated reserves).
- The size of the shock is small (-0.3% of output decline and 0.2% of inflation increase).
  - I do not finish solving the model with large shock.

## Consumption

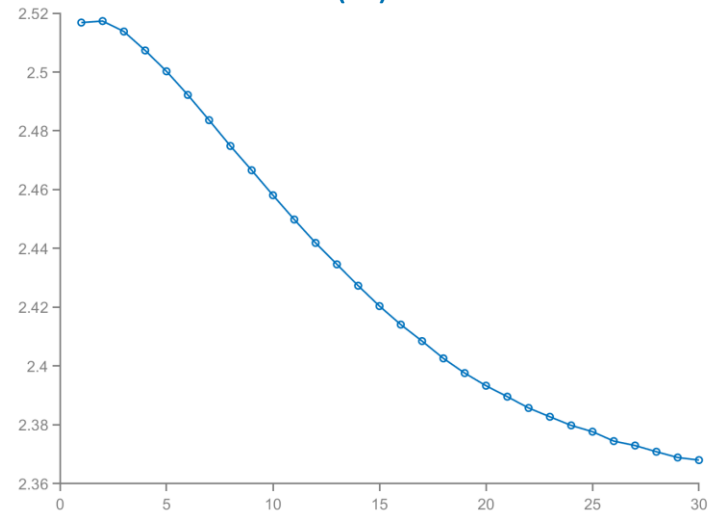
(SS deviation in %)

**Positive  
cost-push shock  
in consolidated**



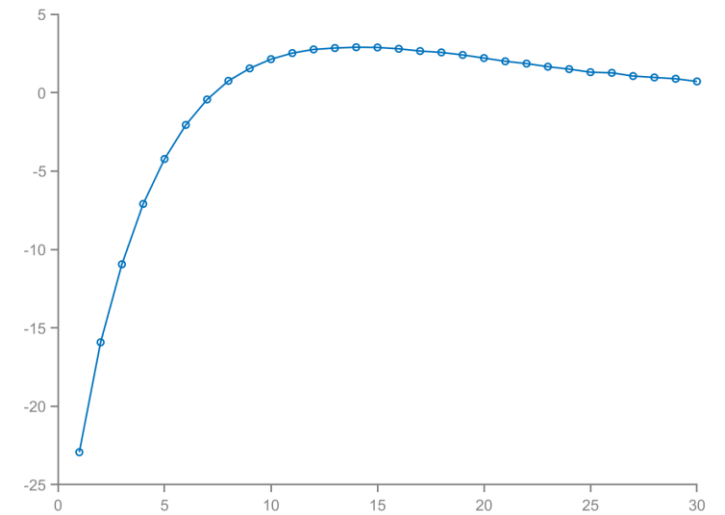
## Inflation

(%)



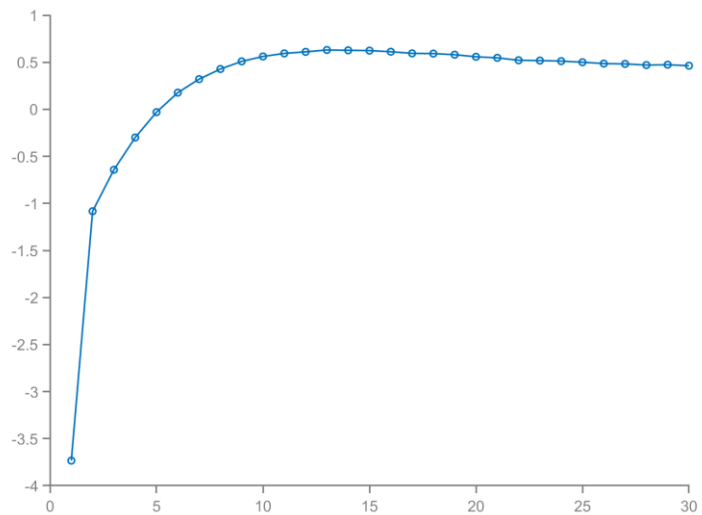
## Tax rate

(SS deviation in %)



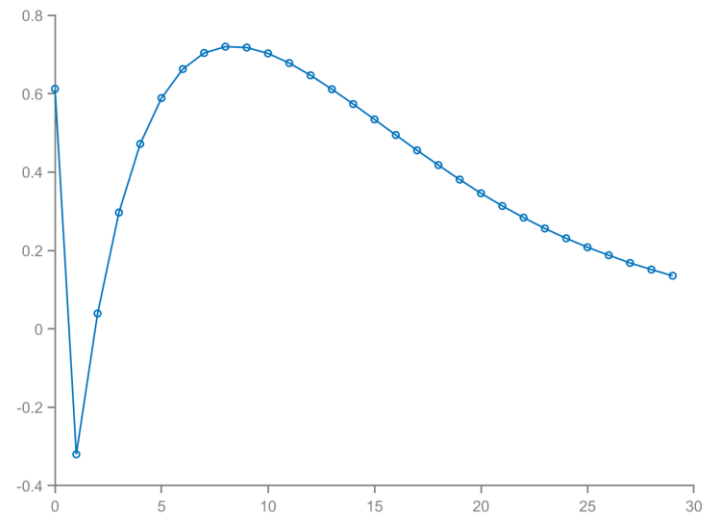
## Remittance

(Ratio to GDP in %)



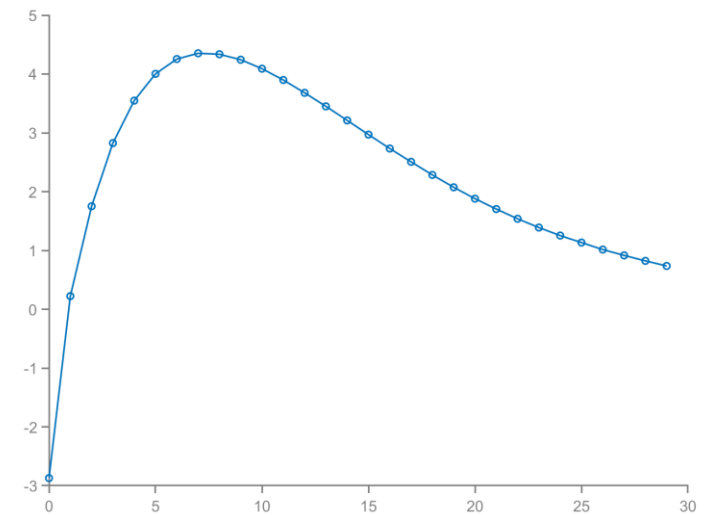
## Reserves

(SS deviation in %)

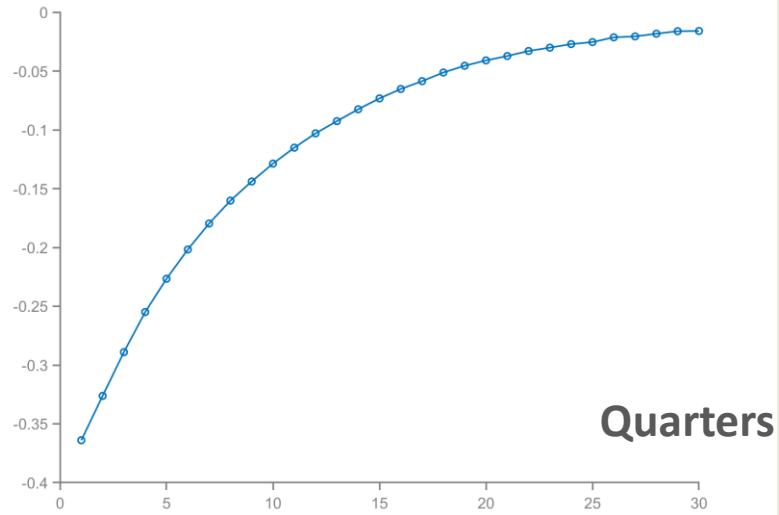


## Treasury liability

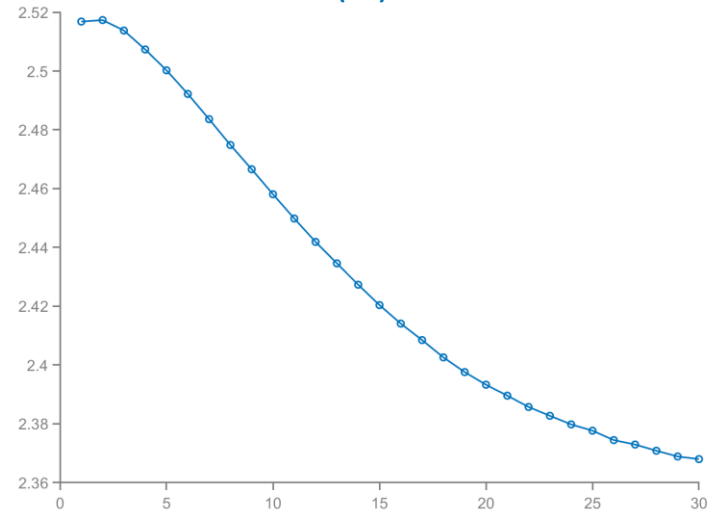
(SS deviation in %)



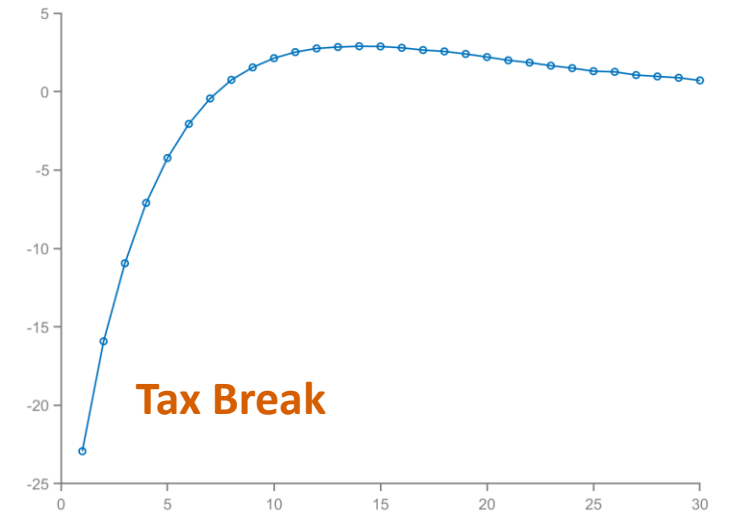
**Consumption**  
(SS deviation in %)



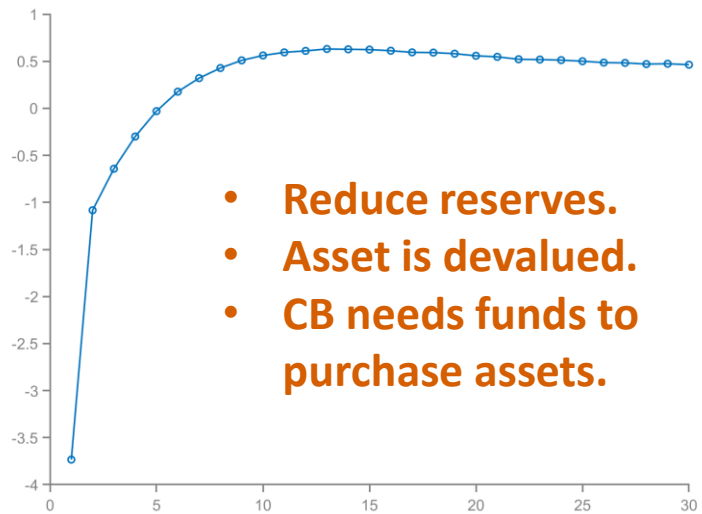
**Inflation**  
(%)



**Tax rate**  
(SS deviation in %)

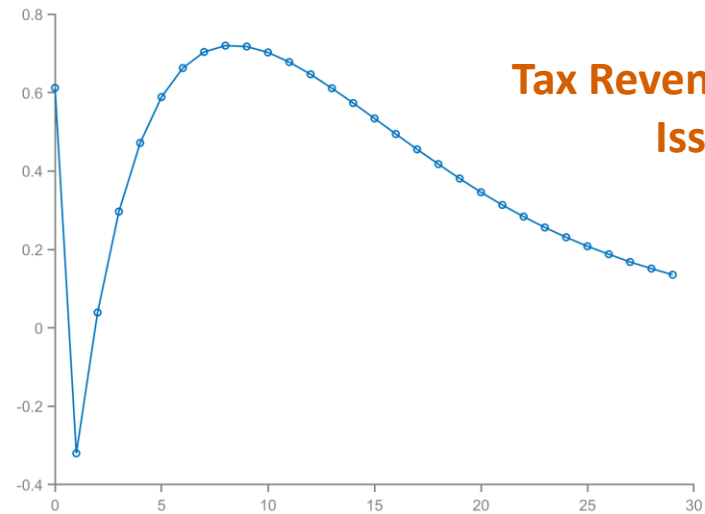


**Remittance**  
(Ratio to GDP in %)



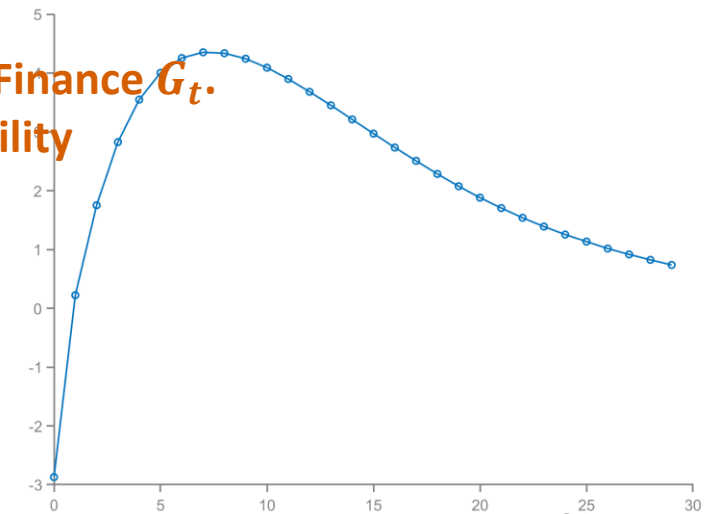
- **Reduce reserves.**
- **Asset is devalued.**
- **CB needs funds to purchase assets.**

**Reserves**  
(SS deviation in %)

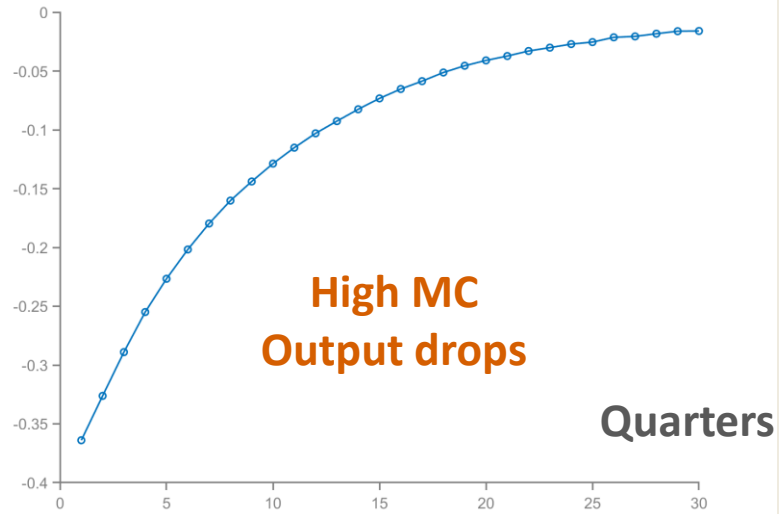


**Tax Revenue↓ & Finance  $G_t$ .  
Issue Liability**

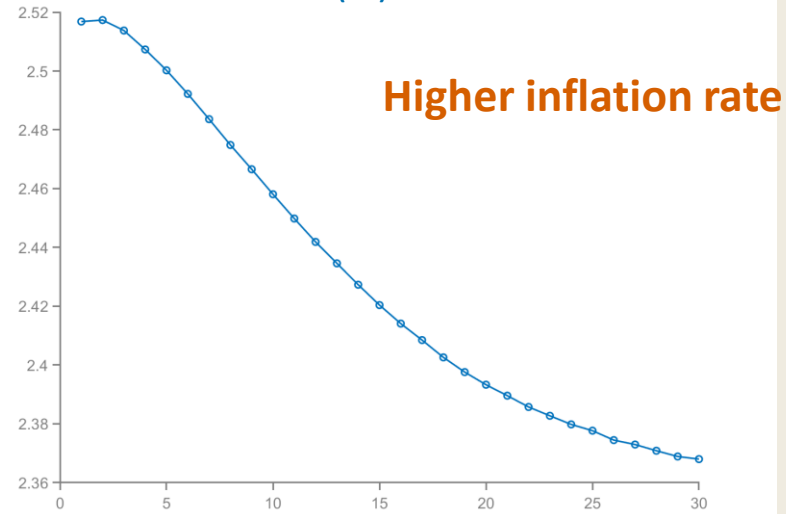
**Treasury liability**  
(SS deviation in %)



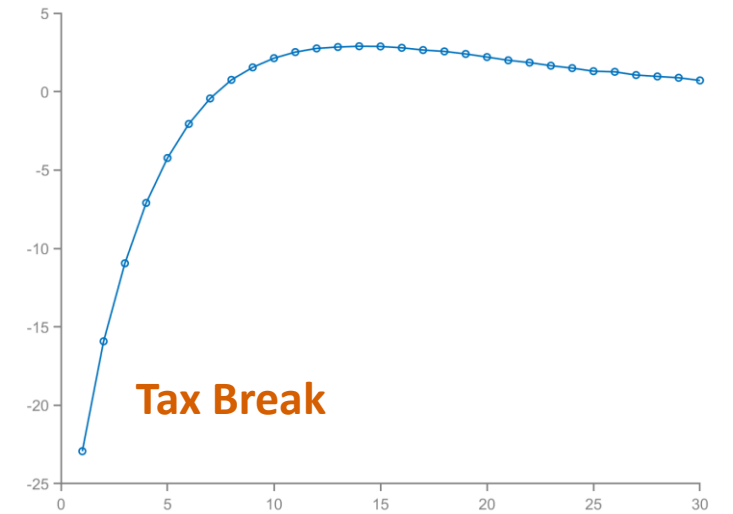
**Consumption**  
(SS deviation in %)



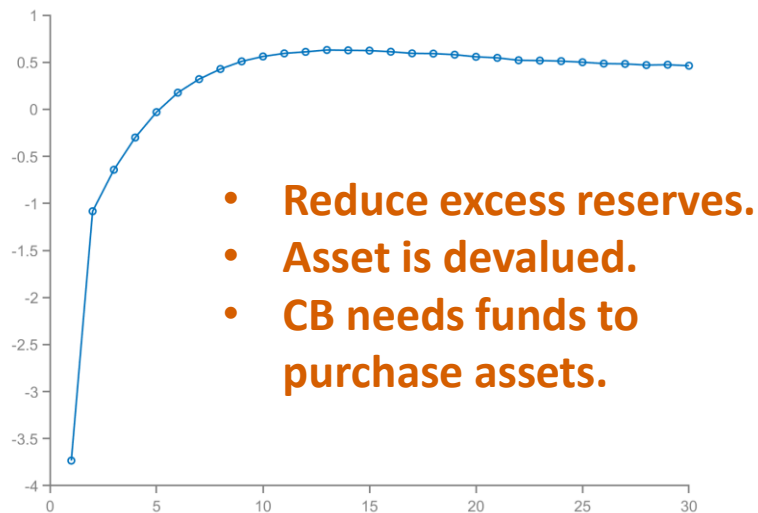
**Inflation**  
(%)



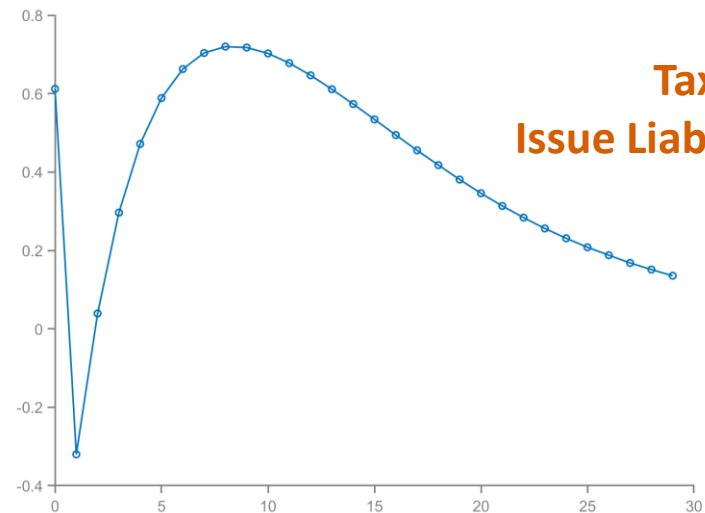
**Tax rate**  
(SS deviation in %)



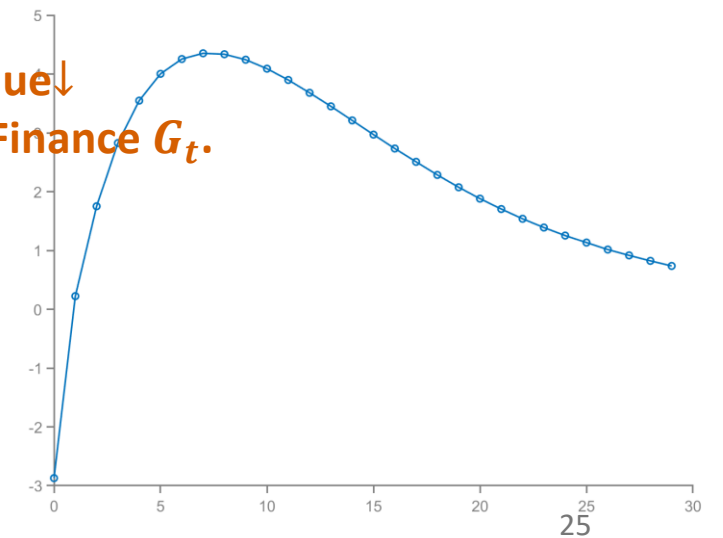
**Remittance**  
(Ratio to GDP in %)



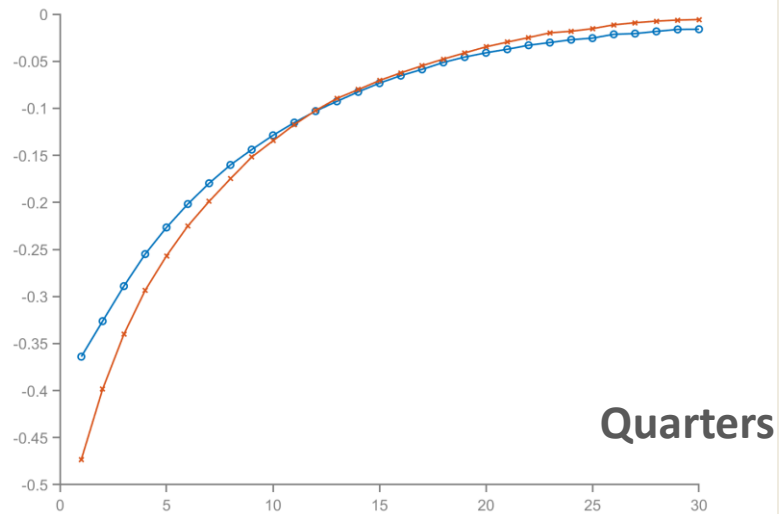
**Reserves**  
(SS deviation in %)



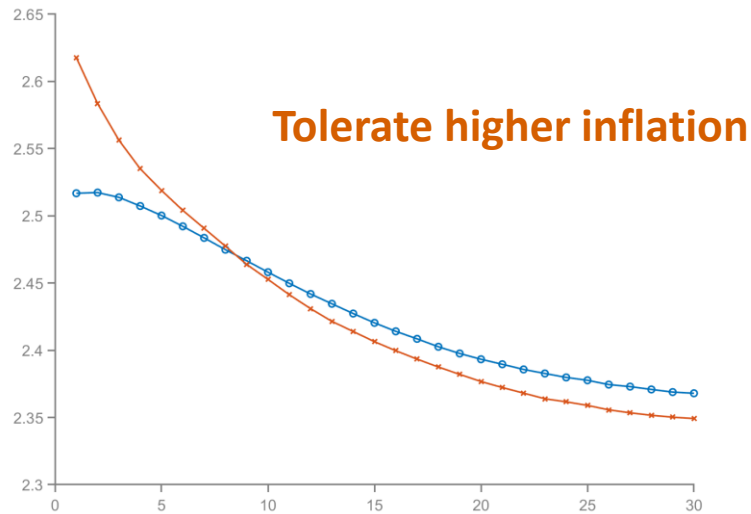
**Treasury liability**  
(SS deviation in %)



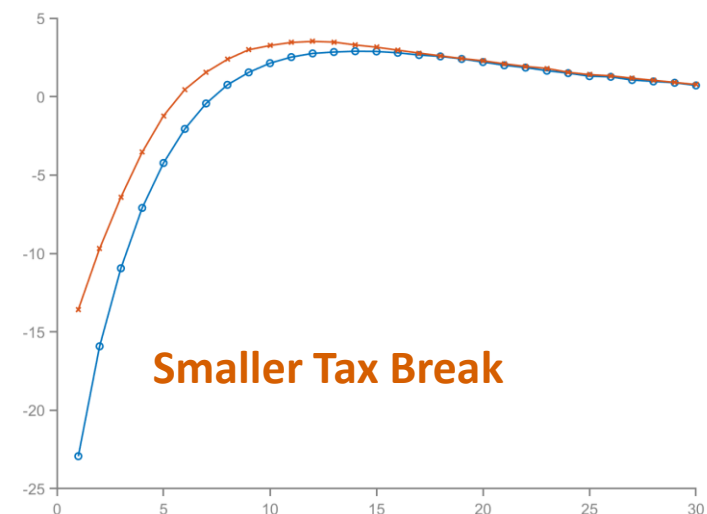
## Consumption



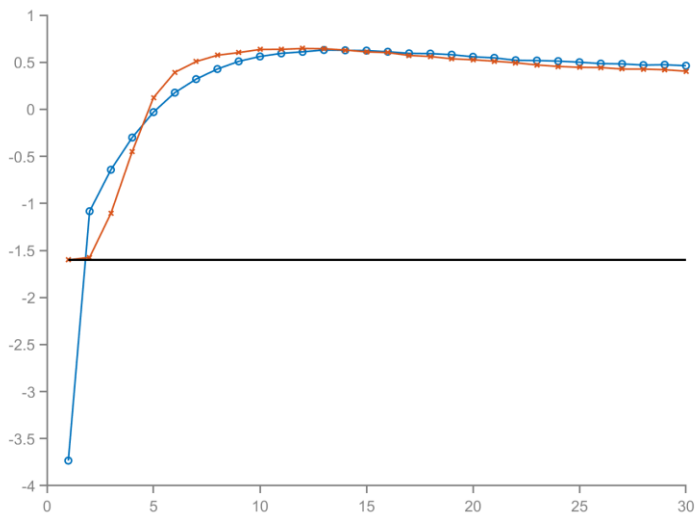
## Inflation



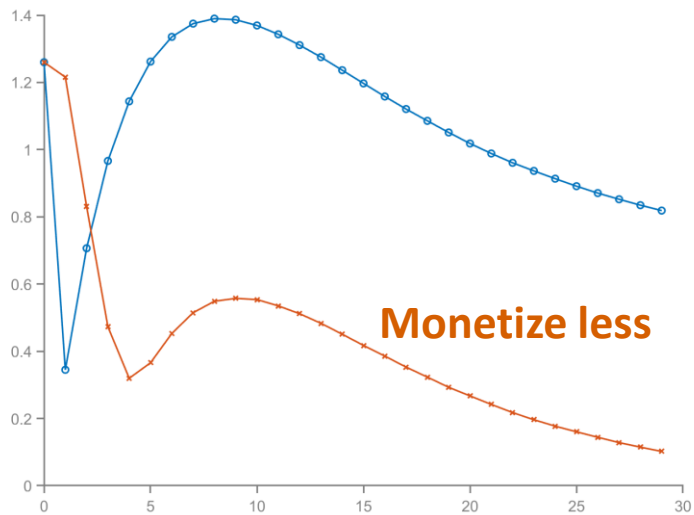
## Tax rate



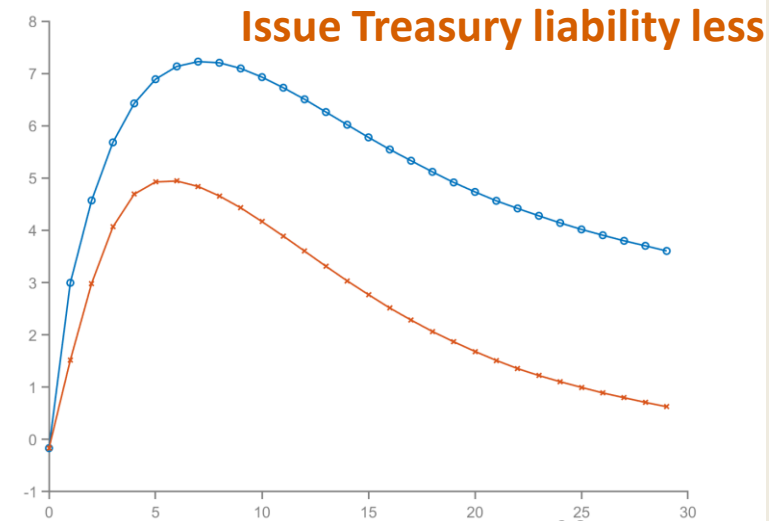
## Remittance



## Reserves



## Treasury liability



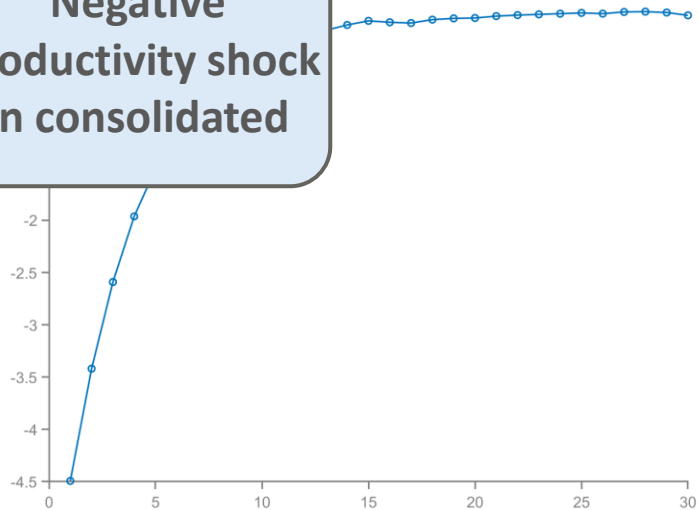


# Primary Policy Tool and Central Bank's Role

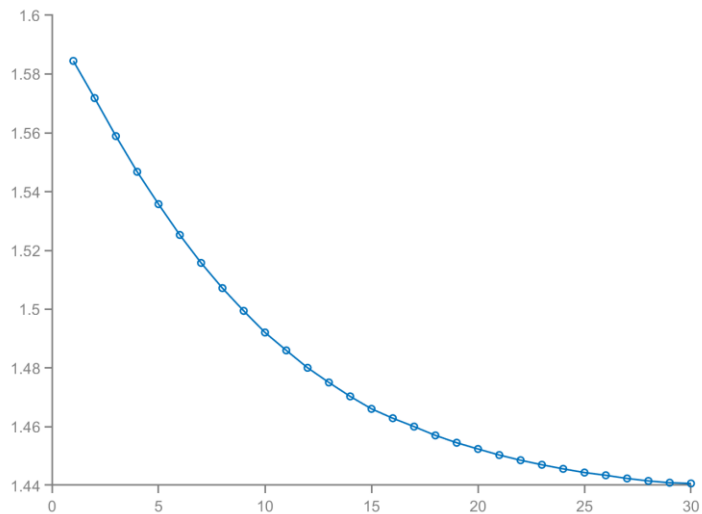
- After cost-push shock, the primary policy tool is tax break.
- **The central bank's role to issue reserves helps tax break.**
  - The key parameter is Frisch elasticity and  $(Q^C b^C)^{1-\gamma}$ .
- After productivity shock, **the central bank's role is to raise nominal interest rate enough.**
- When the household cannot absorb large reserves, the unconsolidated model gives difference.
  - The key parameter is risk aversion and  $(Q^C b^C)^{1-\gamma}$ .

### Consumption

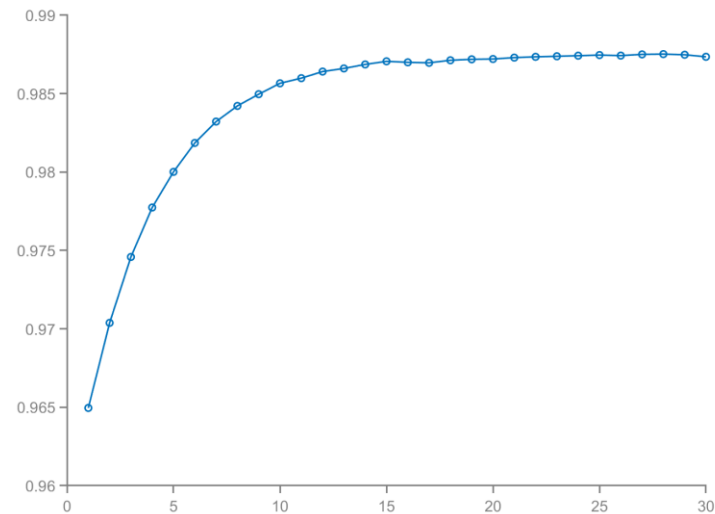
Negative productivity shock in consolidated



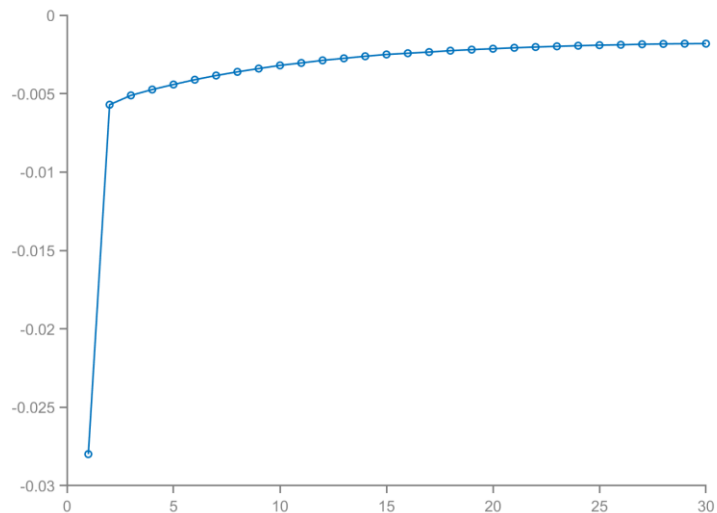
### Inflation



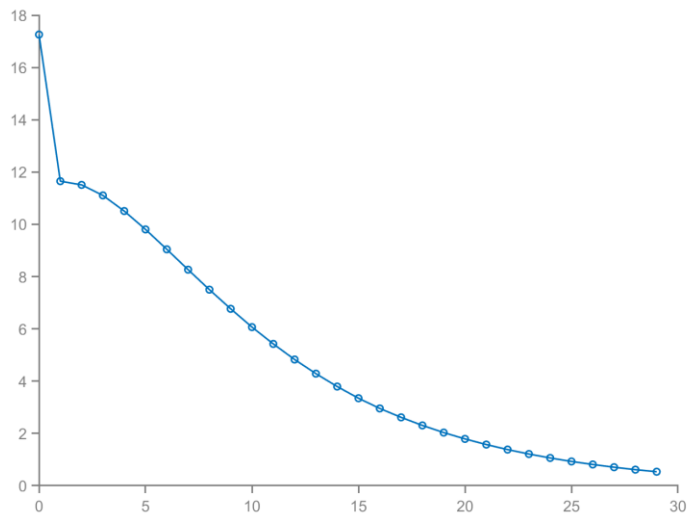
### Price of Reserves



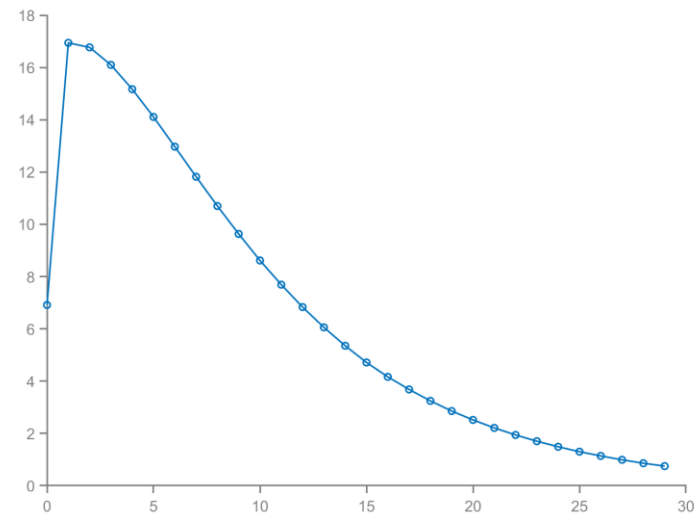
### Remittance



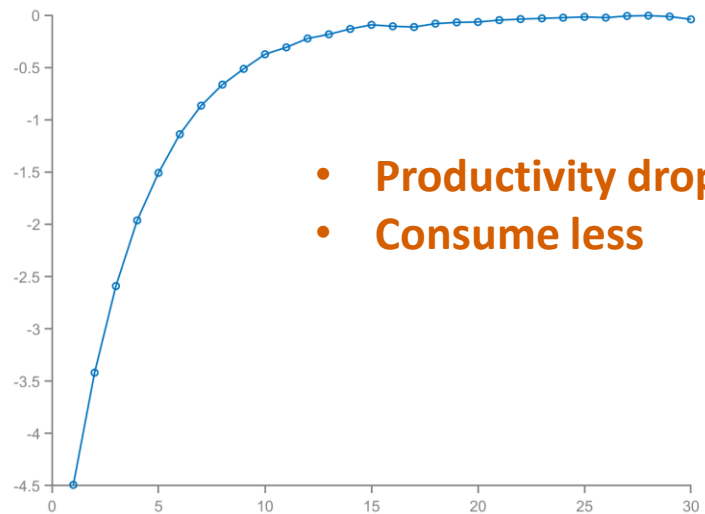
### Reserves



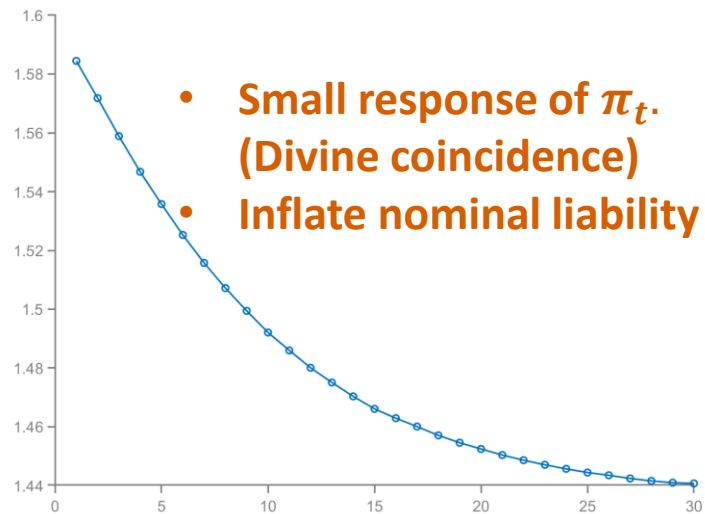
### Treasury liability



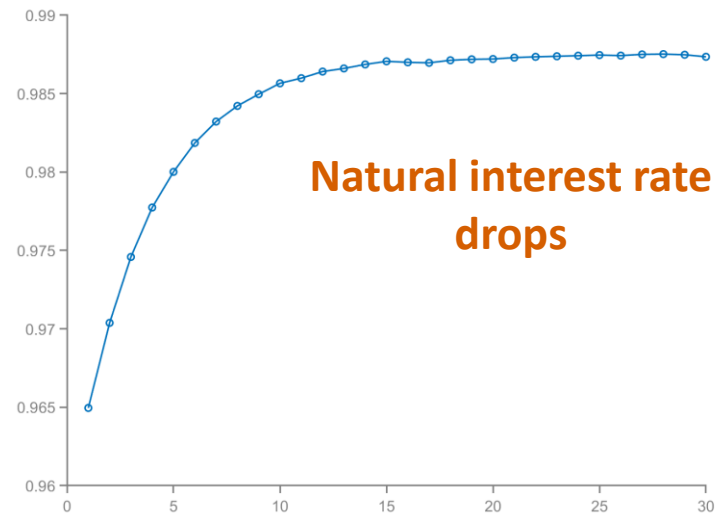
## Consumption



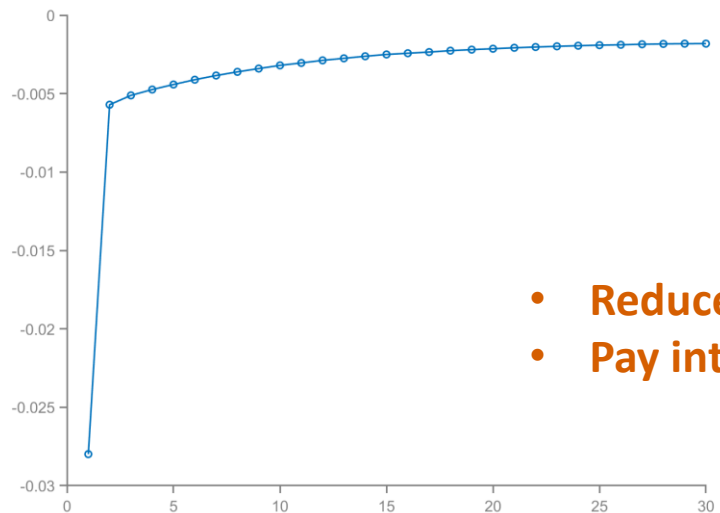
## Inflation



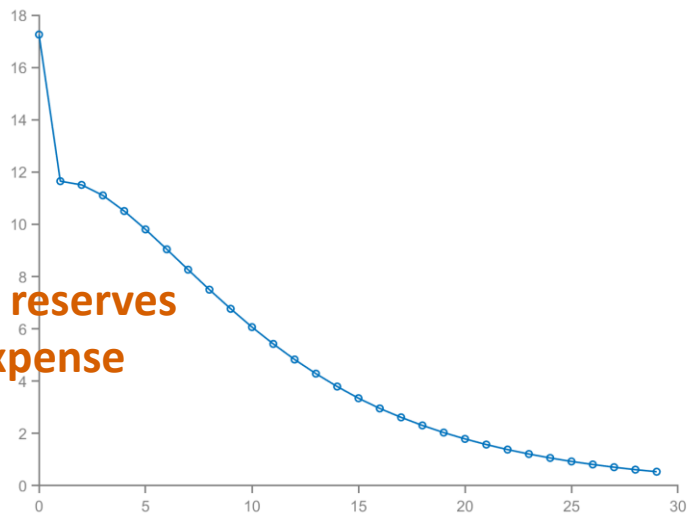
## Price of Reserves



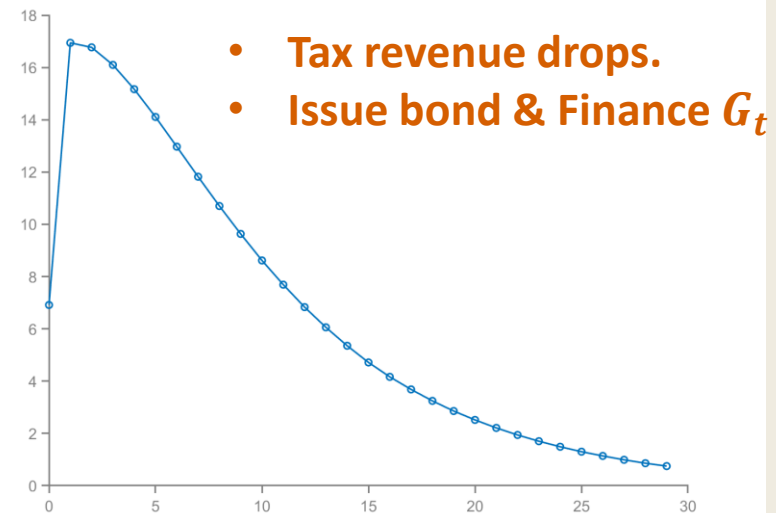
## Remittance



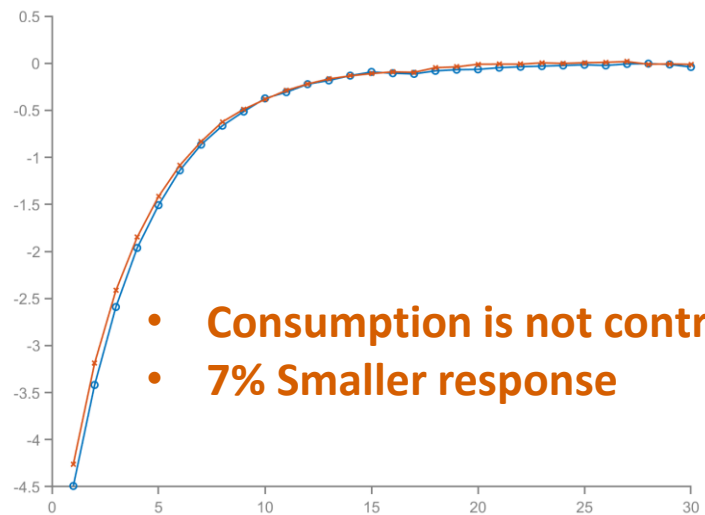
## Reserves



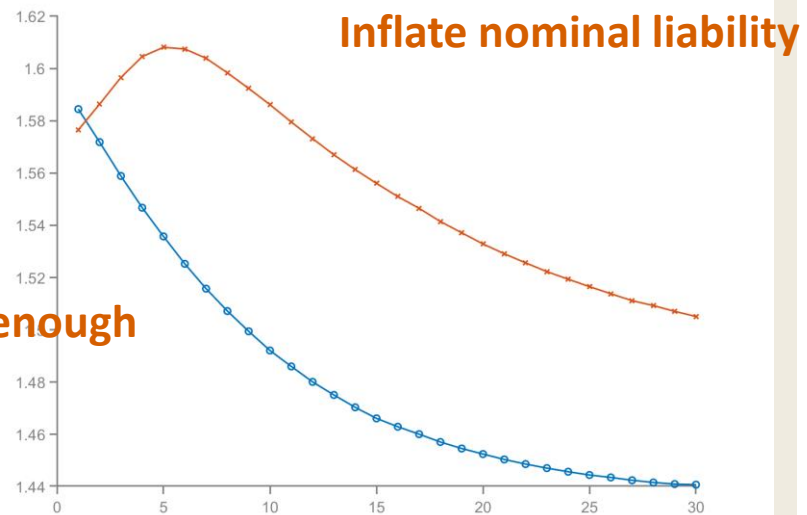
## Treasury liability



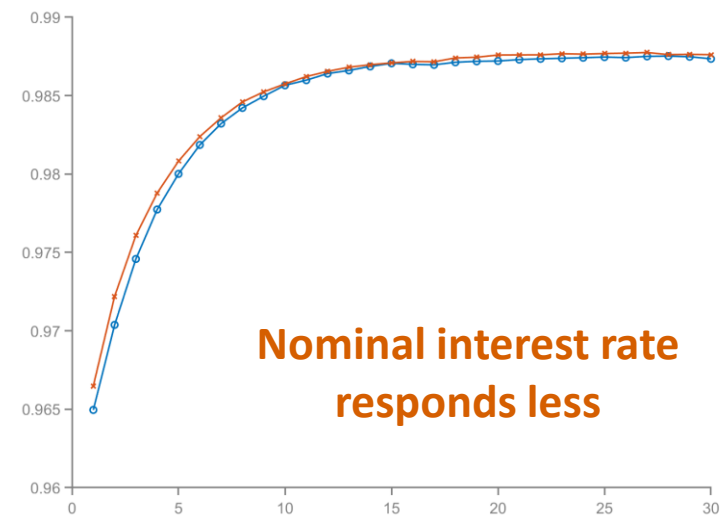
## Consumption



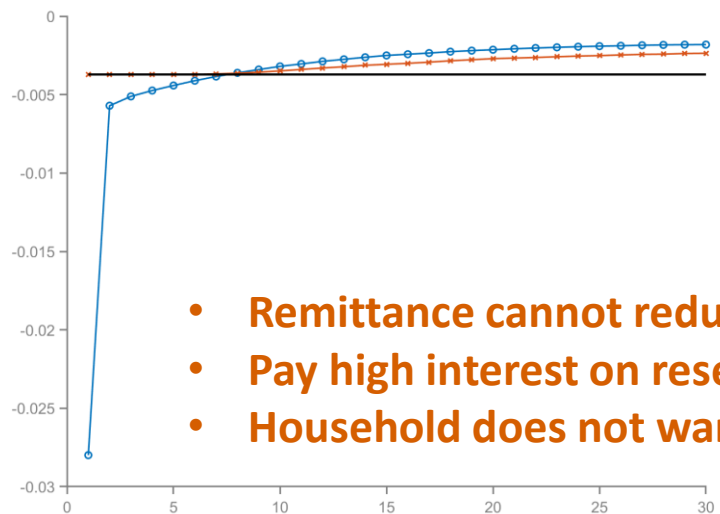
## Inflation



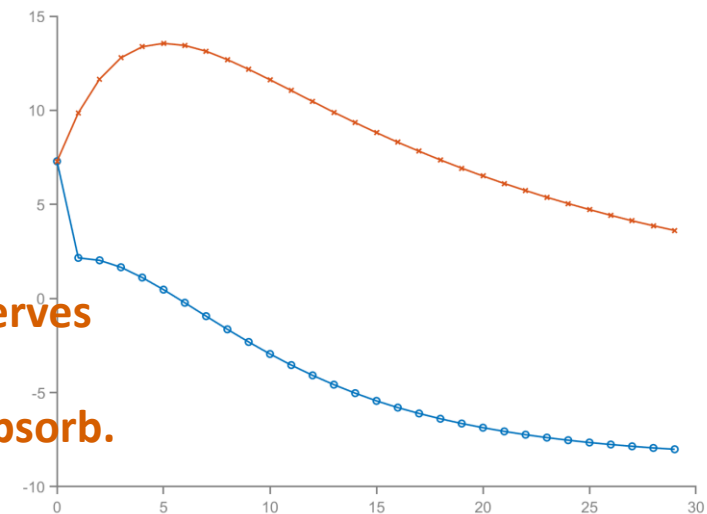
## Price of Reserves



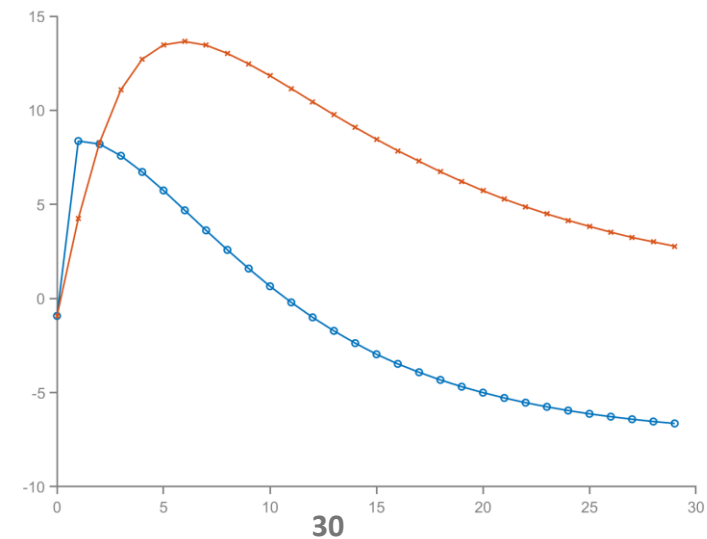
## Remittance



## Reserves



## Treasury liability



# Dynamic Property of the Optimal Policy

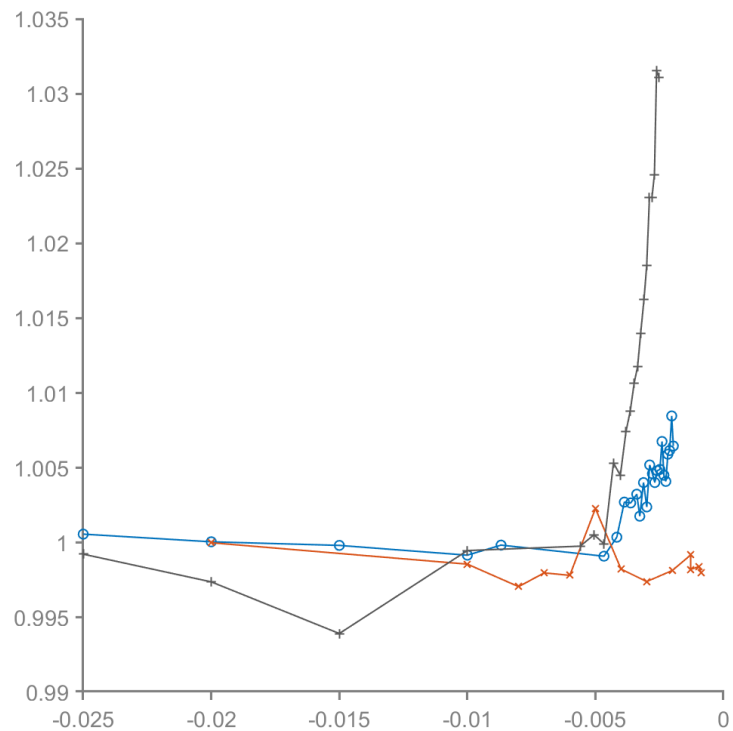
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## Does the fiscal backing affect dynamic property of the optimal policy?

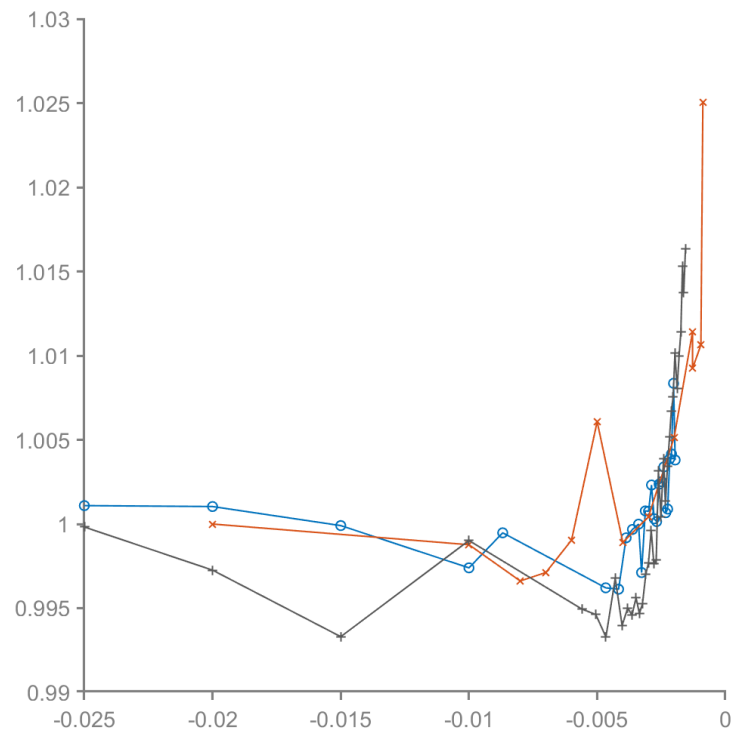
- Suppose the central bank has less fiscal support from the Treasury.
  - Increase the lower bound on remittance,  $H^*$ . ( $H_t \geq H^*$ )
- For each  $H^*$  and shock, I solve the model and simulate the economy.
- Compute the mean and variance of consumption, inflation, and tax rate.

- Horizontal is  $H^*$ . Vertical is **the volatility**. Normalized by the volatility in the consolidated model.
- Government expenditure (blue). Productivity (red). Cost-push (black).

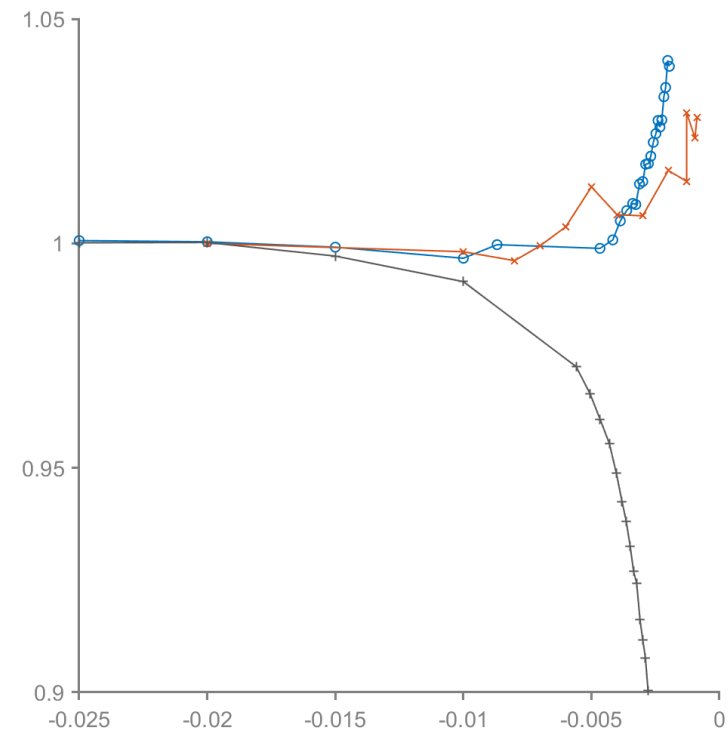
Consumption



Inflation



Tax rate



- How each variable's volatility changes as fiscal backing for the central bank decreases (i.e.,  $H^* \uparrow$ ).

	Cost-push	Government expenditure
Consumption	<b>+3%</b>	<b>+1%</b>
Tax	<b>-10%</b>	<b>+3%</b>
Inflation	<b>+1%</b>	<b>+2%</b>

**Fiscal backing allows  
tax break**



- How each variable's volatility changes as fiscal backing for the central bank decreases (i.e.,  $H^* \uparrow$ ).

	Cost-push	Government expenditure
Consumption	<b>+3%</b>	<b>+1%</b>
Tax	<b>-10%</b>	<b>+3%</b>
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**Fiscal backing allows  
tax break**

**Fiscal backing allows  
tax smoothing**

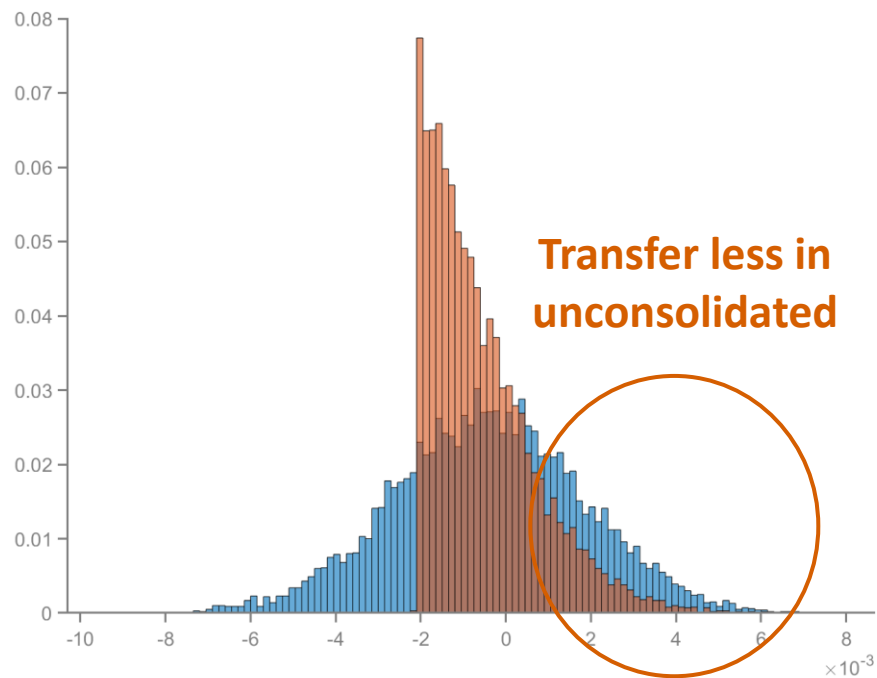
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# Retained Earnings by the central bank

- Bank of Japan **retains 5% of profits** and transfers the rest to the Treasury.
  - Large balance sheet (120% of GDP).
- Bundesbank uses its financial buffers to cushion burdens.
- No reason to retain earnings if the central bank and Treasury are consolidated.

# Why do the central banks retain earnings?

- Lower bound on remittance reduces the upper bound.
- If CB prints reserves and transfer a lot now, increased reserves cannot be reduced through remittance later. → **Forward looking decision-making.**



- Simulated the economy with cost-push shock.
- Remittance as histogram for consolidated and unconsolidated.

# The welfare gain of fiscal backing

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# The welfare gain of fiscal backing is less than 0.01%.

- I compute the welfare gain of increasing the lower bound on remittance,  $H^*$ .
- Consumption equivalence compared to the case of  $H^* = -\infty$ .

(Intuition) Fiscal backing affects the variance but less the mean.

The lack of fiscal backing increases the average inflation by 0.25 bps.