



# Power Electronics

EE312

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## Selective Harmonic Elimination based PWM

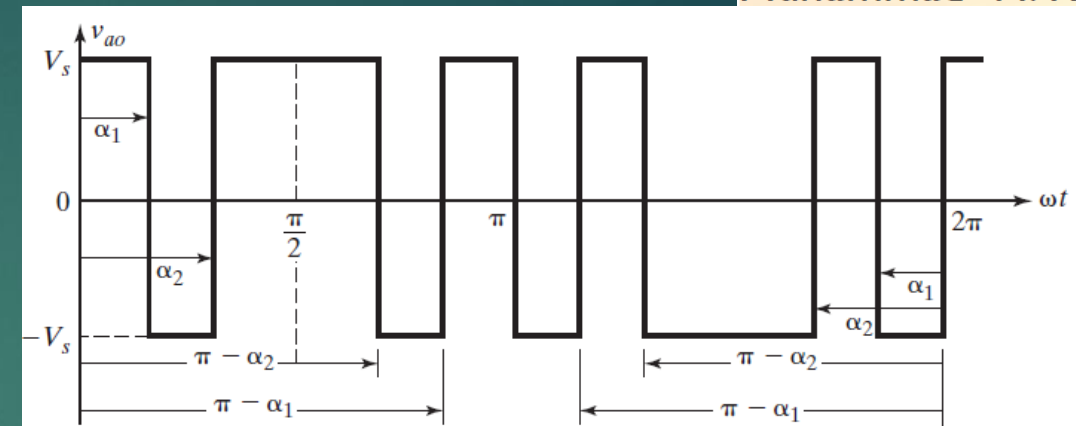
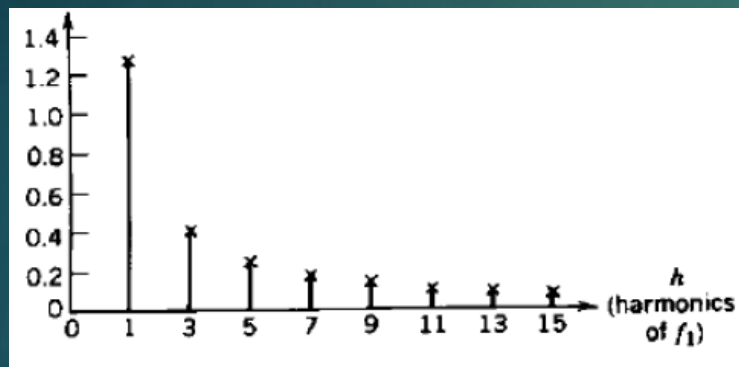
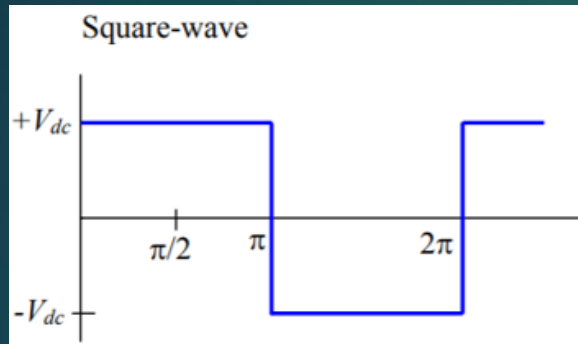
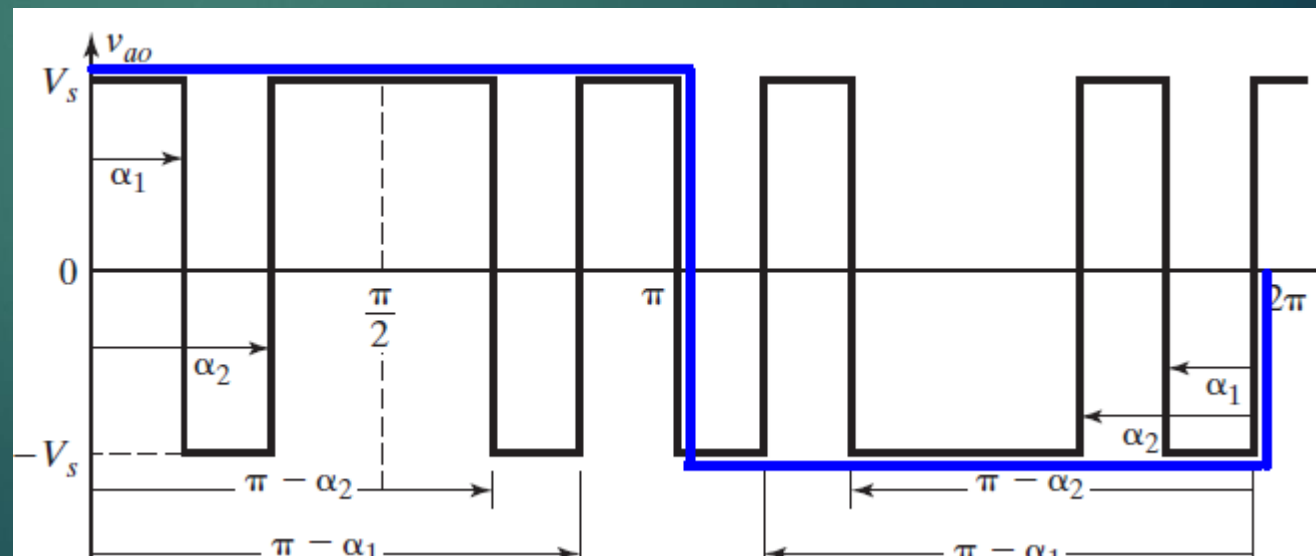


FIGURE 6.32

Output voltage with two bipolar notches per half-wave.



$$v_o = \sum_{n=1,3,5,\dots}^{\infty} B_n \sin n\omega t$$

$$B_n = \frac{4V_s}{\pi} \left[ \int_0^{\alpha_1} \sin n\omega t d(\omega t) - \int_{\alpha_1}^{\alpha_2} \sin n\omega t d(\omega t) + \int_{\alpha_2}^{\pi/2} \sin n\omega t d(\omega t) \right]$$

$$= \frac{4V_s}{\pi} \frac{1 - 2 \cos n\alpha_1 + 2 \cos n\alpha_2}{n} \quad (6.92)$$

$$a_n = \frac{1}{\pi} \int_0^{2\pi} v_o(\omega t) \cos n\omega t d(\omega t)$$

$$b_n = \frac{1}{\pi} \int_0^{2\pi} v_o(\omega t) \sin n\omega t d(\omega t)$$

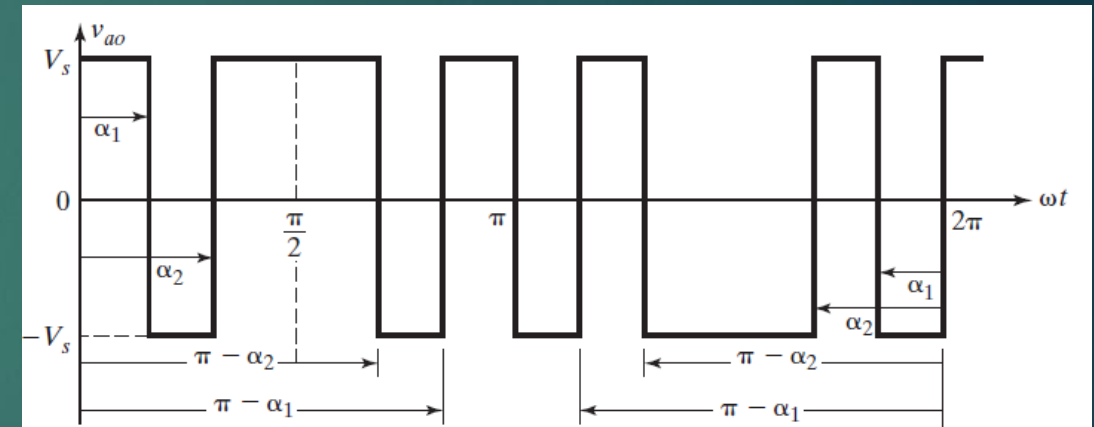
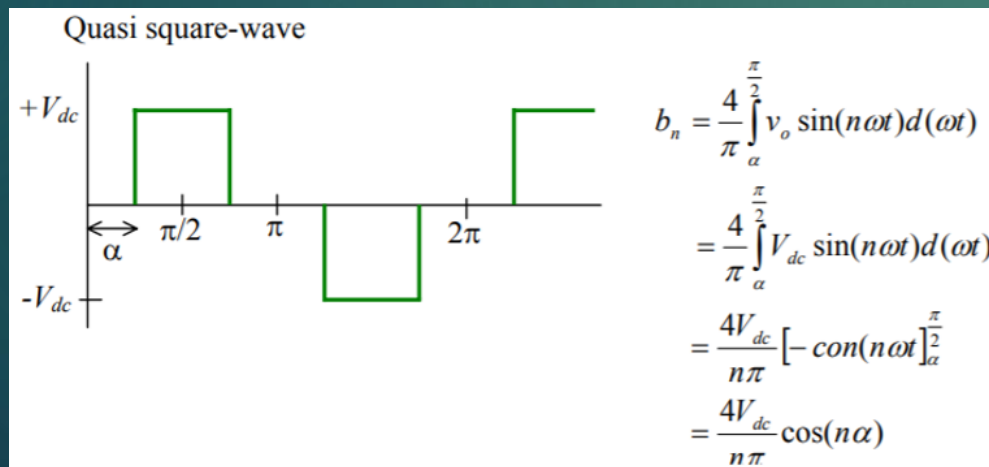


FIGURE 6.32

Output voltage with two bipolar notches per half-wave.





$$B_n = \frac{4V_s}{\pi} \left[ \int_0^{\alpha_1} \sin n\omega t d(\omega t) - \int_{\alpha_1}^{\alpha_2} \sin n\omega t d(\omega t) + \int_{\alpha_2}^{\pi/2} \sin n\omega t d(\omega t) \right]$$

$$= \frac{4V_s}{\pi} \frac{1 - 2 \cos n\alpha_1 + 2 \cos n\alpha_2}{n} \quad (6.92)$$

$$B_3 = B_5 = 0$$

$$1 - 2 \cos 3\alpha_1 + 2 \cos 3\alpha_2 = 0 \quad \text{or} \quad \alpha_2 = \frac{1}{3} \cos^{-1}(\cos 3\alpha_1 - 0.5)$$

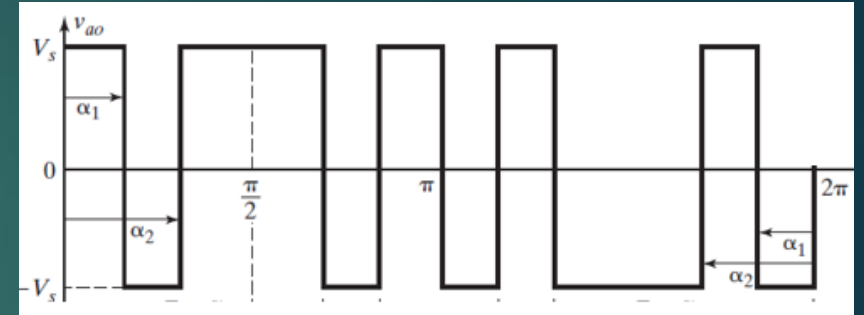
$$1 - 2 \cos 5\alpha_1 + 2 \cos 5\alpha_2 = 0 \quad \text{or} \quad \alpha_1 = \frac{1}{5} \cos^{-1}(\cos 5\alpha_2 + 0.5)$$

$$\alpha_1 = 23.62^\circ \text{ and } \alpha_2 = 33.3^\circ$$

half

m notches per quarter cycle → m harmonics removable

$$B_n = \frac{4V_s}{n\pi} (1 - 2 \cos n\alpha_1 + 2 \cos n\alpha_2 - 2 \cos n\alpha_3 + 2 \cos n\alpha_4 - \dots) \quad (6.93)$$



$$B_n = \frac{4V_s}{n\pi} (1 - 2 \cos n\alpha_1 + 2 \cos n\alpha_2 - 2 \cos n\alpha_3 + 2 \cos n\alpha_4 - \cdots) \quad (6.93)$$

### Example 6.6 Finding the Number of Notches and Their Angles

A single-phase full-wave inverter uses multiple notches to give bipolar voltage as shown in Figure 6.32, and is required to eliminate the fifth, seventh, eleventh, and thirteenth harmonics from the output wave. Determine the number of notches and their angles.

#### Solution

For elimination of the fifth, seventh, eleventh, and thirteenth harmonics,  $A_5 = A_7 = A_{11} = A_{13} = 0$ ; that is,  $m = 4$ . Four notches per quarter-wave would be required. Equation (6.93) gives the following set of nonlinear simultaneous equations to solve for the angles.

$$\begin{aligned} 1 - 2 \cos 5\alpha_1 + 2 \cos 5\alpha_2 - 2 \cos 5\alpha_3 + 2 \cos 5\alpha_4 &= 0 \\ 1 - 2 \cos 7\alpha_1 + 2 \cos 7\alpha_2 - 2 \cos 7\alpha_3 + 2 \cos 7\alpha_4 &= 0 \\ 1 - 2 \cos 11\alpha_1 + 2 \cos 11\alpha_2 - 2 \cos 11\alpha_3 + 2 \cos 11\alpha_4 &= 0 \\ 1 - 2 \cos 13\alpha_1 + 2 \cos 13\alpha_2 - 2 \cos 13\alpha_3 + 2 \cos 13\alpha_4 &= 0 \end{aligned}$$

Solution of these equations by iteration using a Mathcad program yields

$$\alpha_1 = 10.55^\circ \quad \alpha_2 = 16.09^\circ \quad \alpha_3 = 30.91^\circ \quad \alpha_4 = 32.87^\circ$$

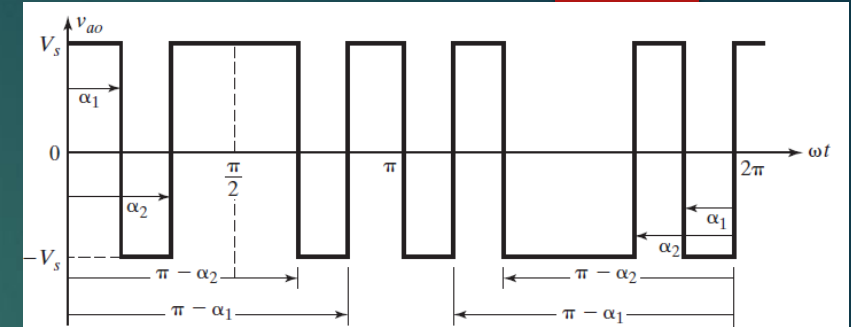
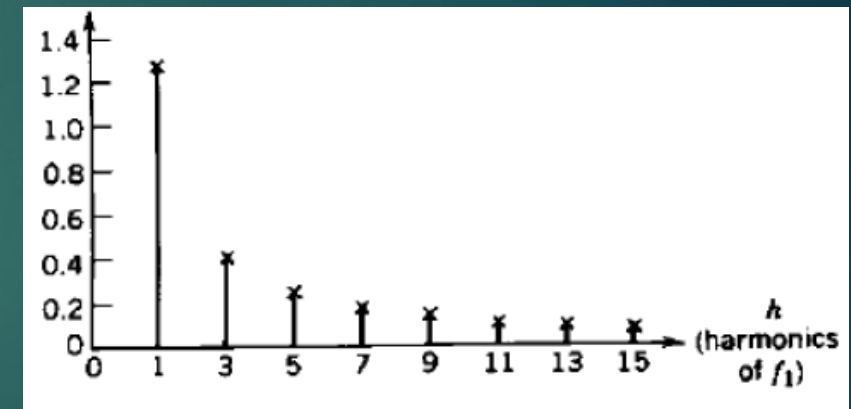


FIGURE 6.32

Output voltage with two bipolar notches per half-wave.



### 8-6-3 CURRENT-REGULATED (CURRENT-MODE) MODULATION

#### 8-6-3-1 Tolerance Band Control

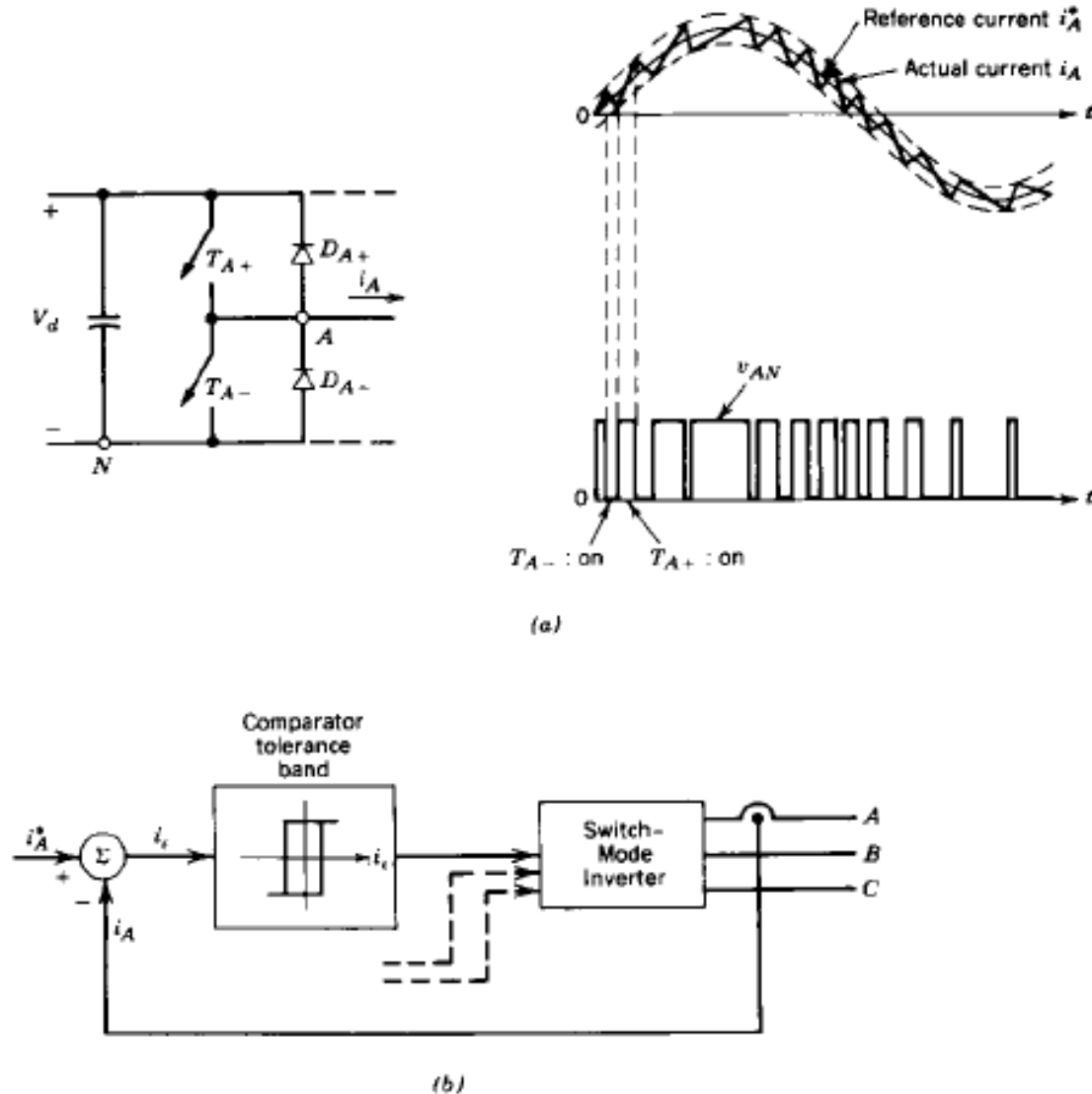


Figure 8-35 Tolerance band current control.



## AC Motor Drives

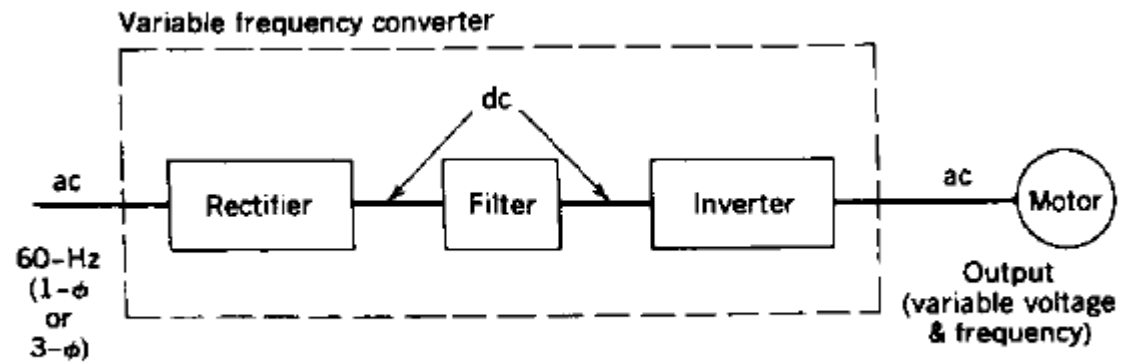
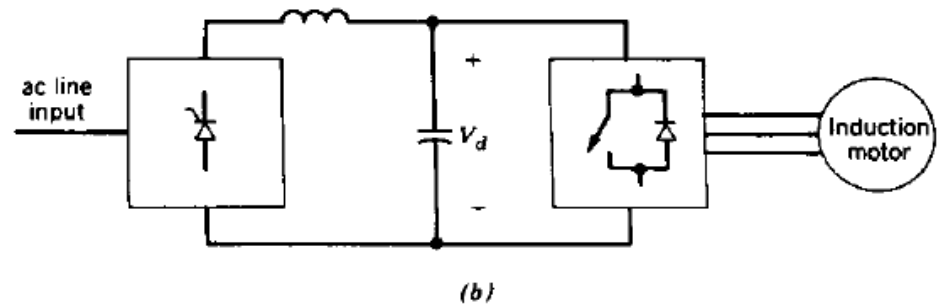
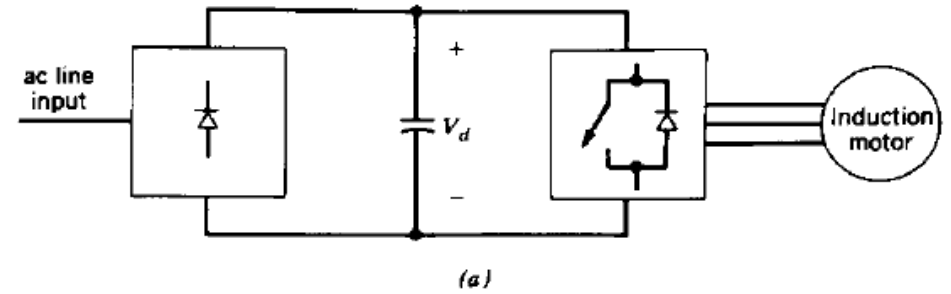
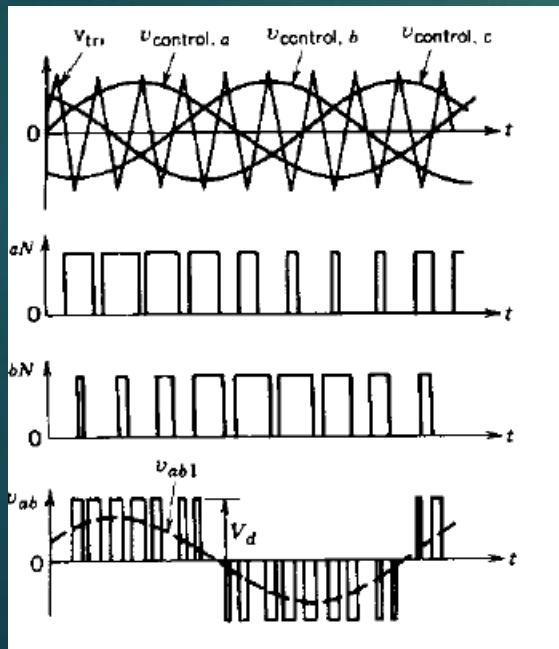
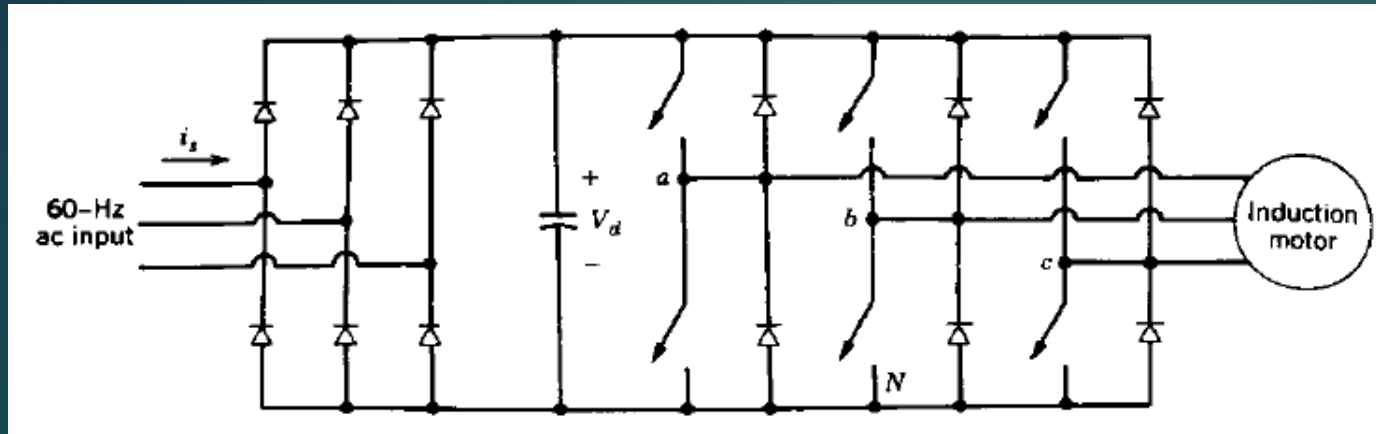


Figure 14-17 Variable-frequency converter.





## 14-7 VARIABLE-FREQUENCY PWM-VSI DRIVES



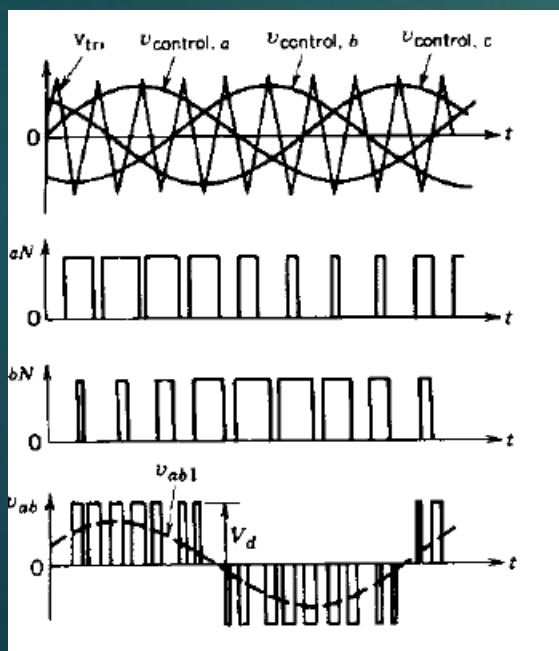
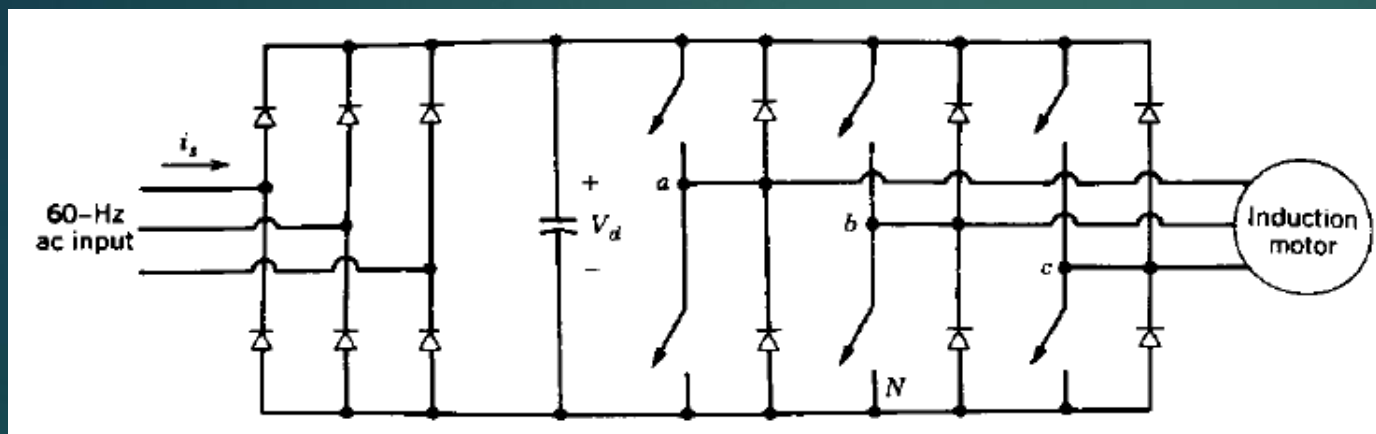
$$P_h/m^3 = \eta B_{\max}^{1.6} f \quad \text{Watts}$$

Or

$$P_h = \eta B_{\max}^{1.6} f V \quad \text{Watts}$$



## 14-7 VARIABLE-FREQUENCY PWM-VSI DRIVES



$$P_h / m^3 = \eta B_{\max}^{1.6} f \quad \text{Watts}$$

Or

$$P_h = \eta B_{\max}^{1.6} f V \quad \text{Watts}$$

Eddy Current Loss,

$$W_e = K_e B_m^2 t^2 f^2 V$$

Where,

$K_e$  = co-efficient of eddy current

$B_m$  – maximum value of flux density in wb/m<sup>2</sup>

$T$  – thickness of lamination in meters

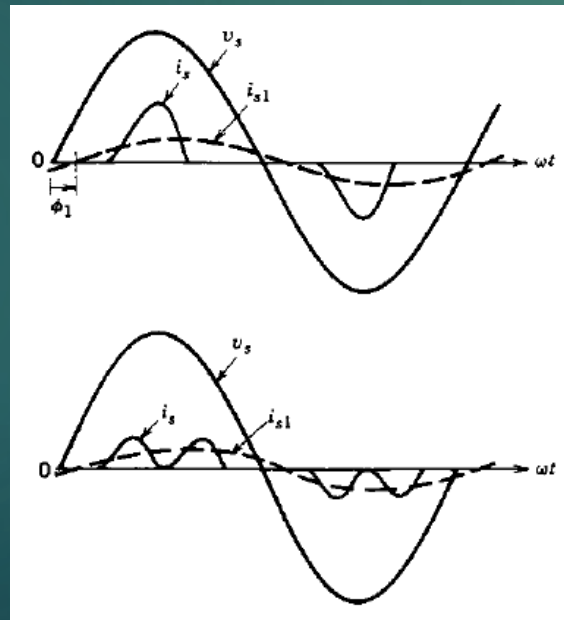
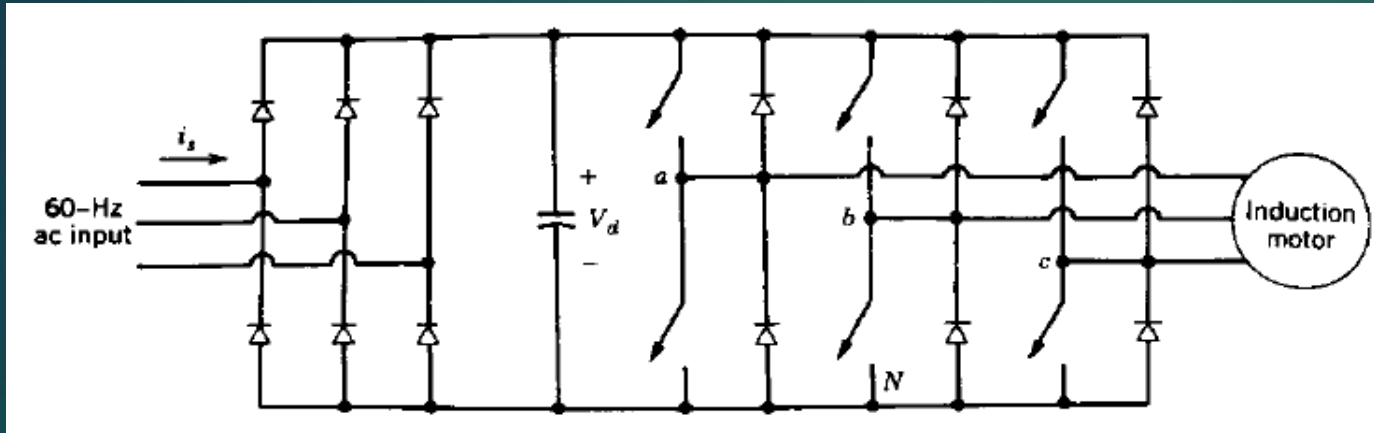
$F$  – frequency in Hz

$V$  – volume of magnetic material in m<sup>3</sup>



## 14-7 VARIABLE-FREQUENCY PWM-VSI DRIVES

The input current



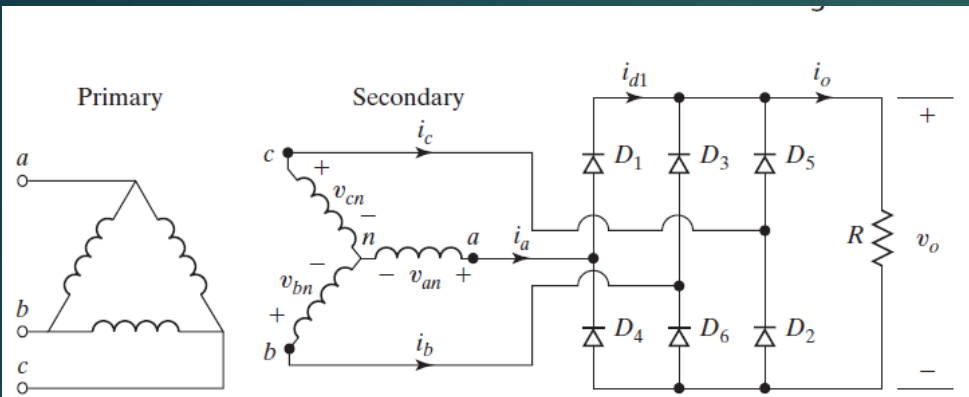


FIGURE 3.11  
Three-phase bridge rectifier.

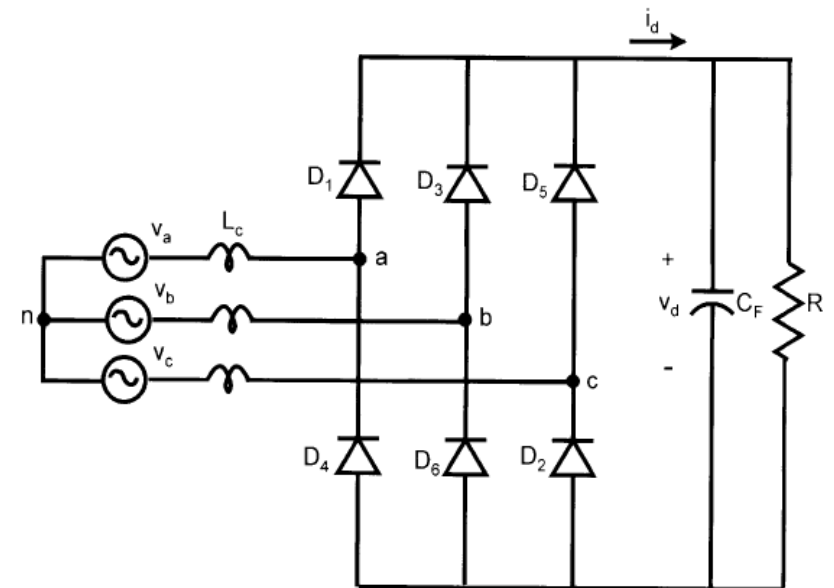
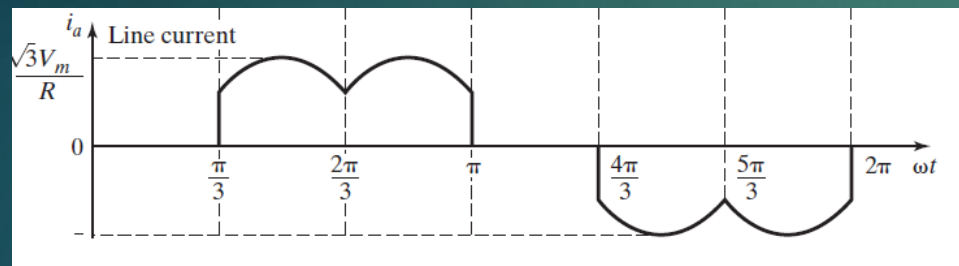
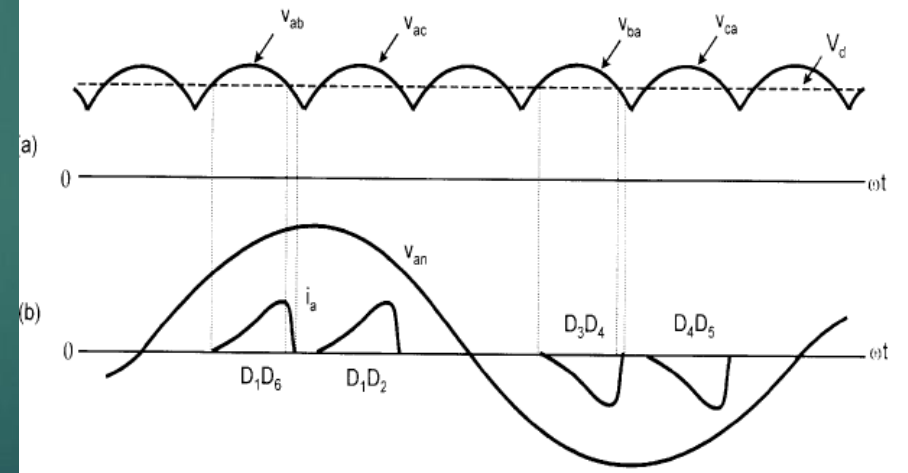
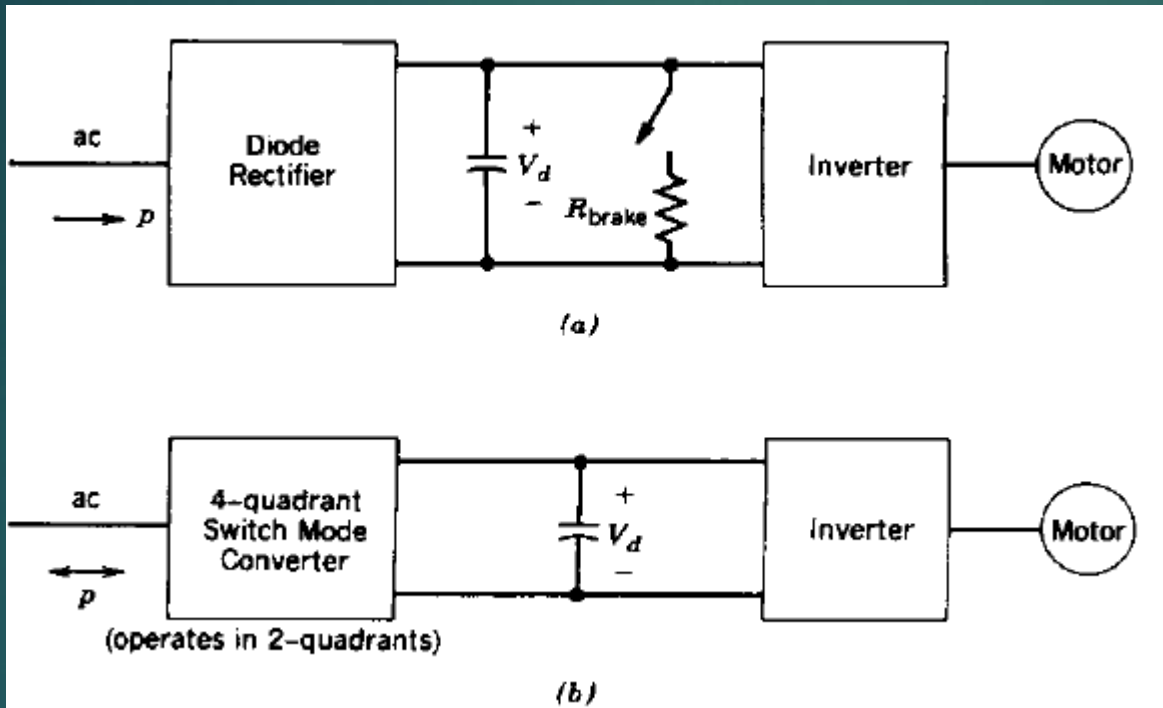


Figure 3.11 Three-phase diode bridge rectifier with  $CR$  load



### 14-7-3 ELECTROMAGNETIC BRAKING





## Rectifier mode of operation of Inverters

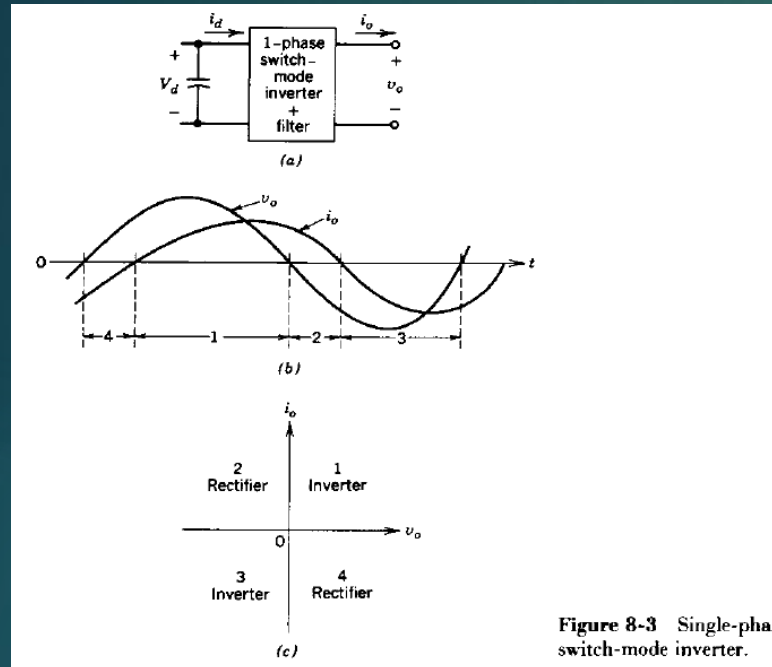
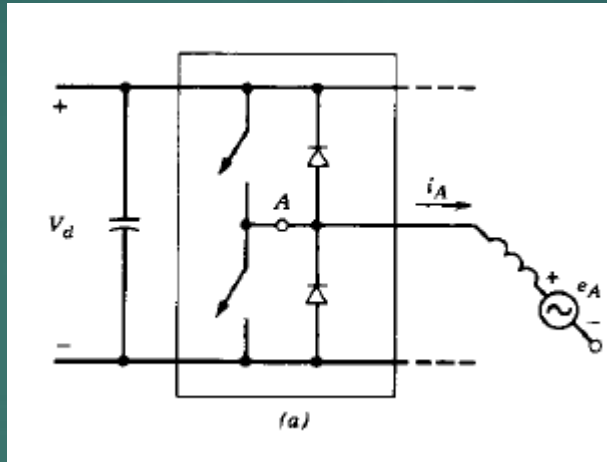
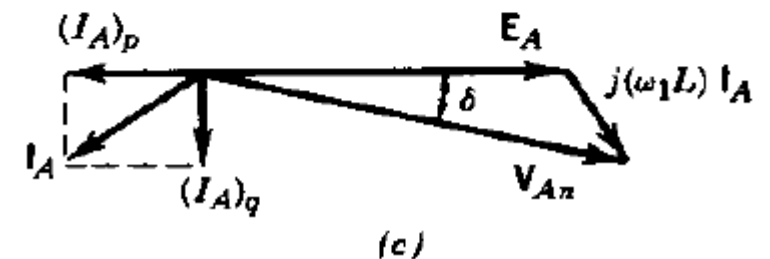
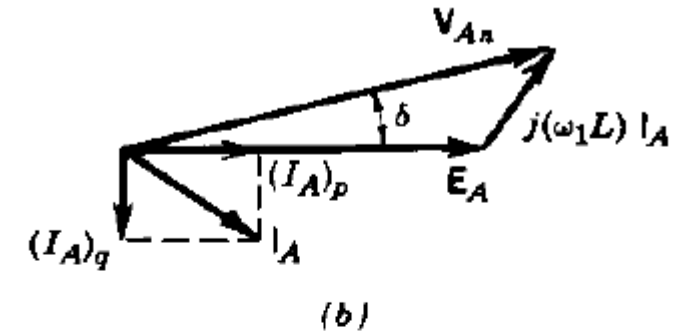


Figure 8-3 Single-phase switch-mode inverter.

### 8-7 RECTIFIER MODE OF OPERATION



$$V_{An} = (j\omega L) I_A + E_A$$

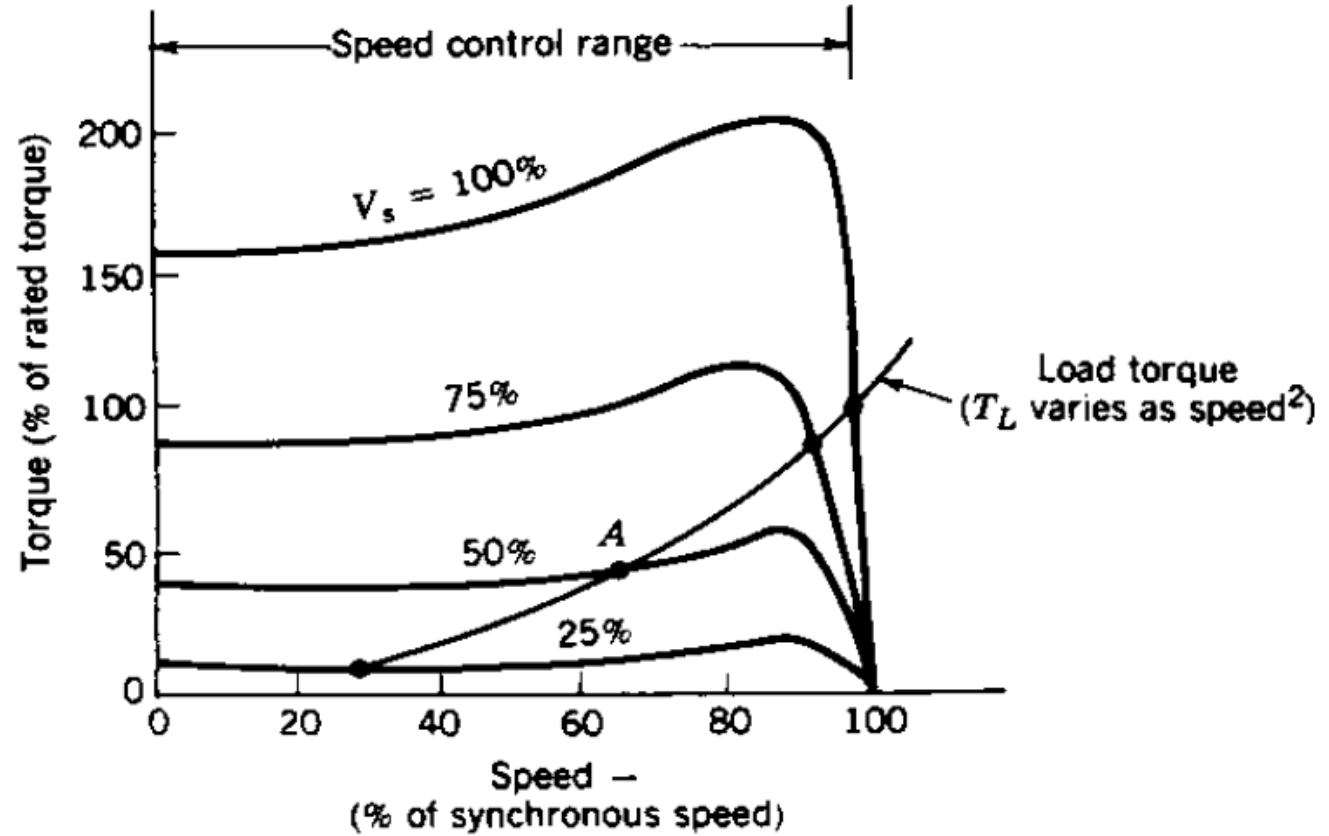
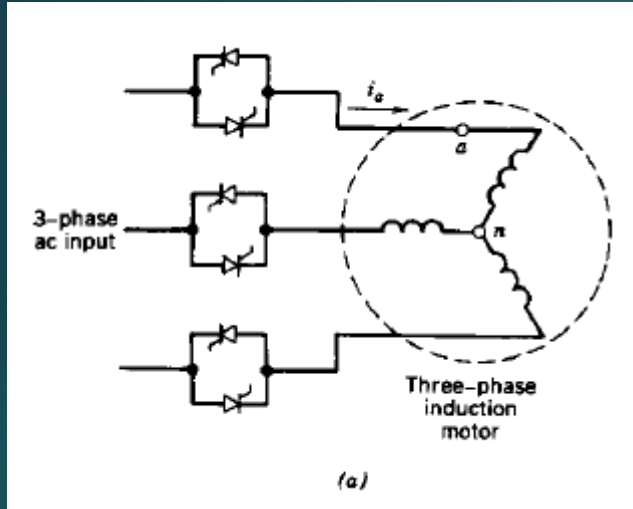


Inverter

Minor mistake in audio – at the start  
Yahan pai samjhaata hoon kai PWM Rectifier ko  
Rectifier mode main kaisai operate kerna hai



## 14-11 LINE-FREQUENCY VARIABLE-VOLTAGE DRIVES



## 14-13 SPEED CONTROL BY STATIC SLIP POWER RECOVERY

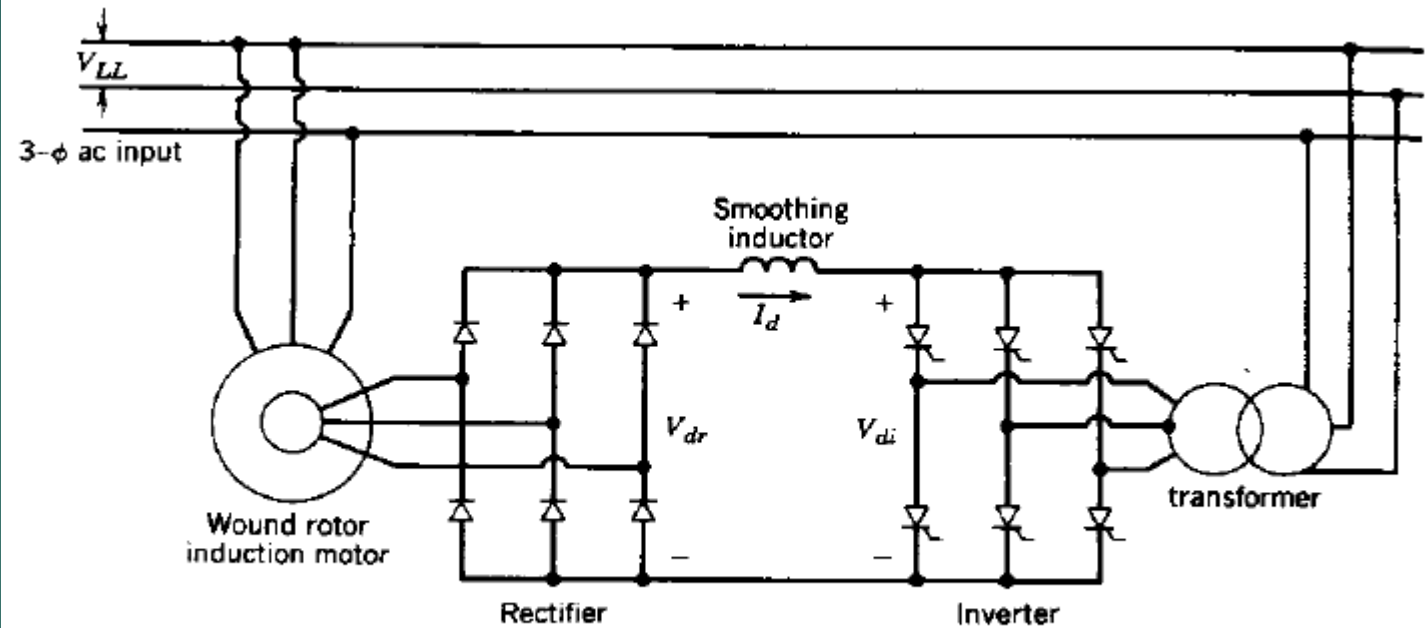
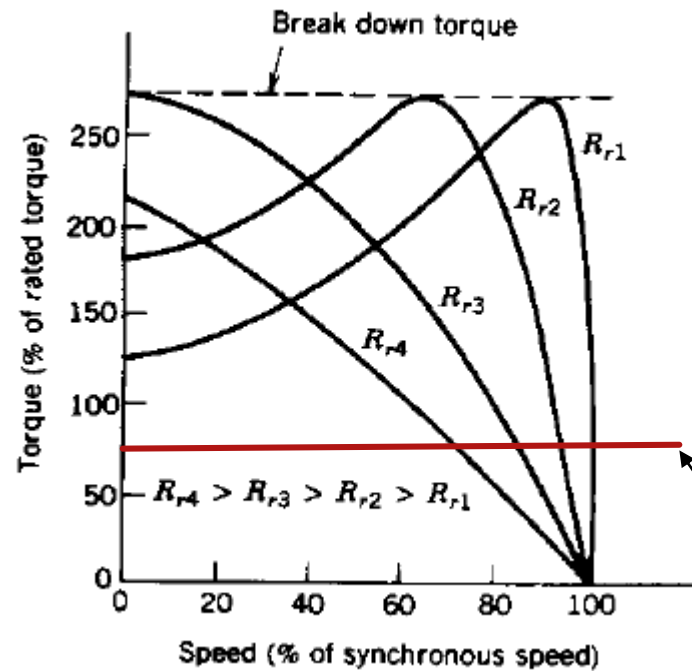
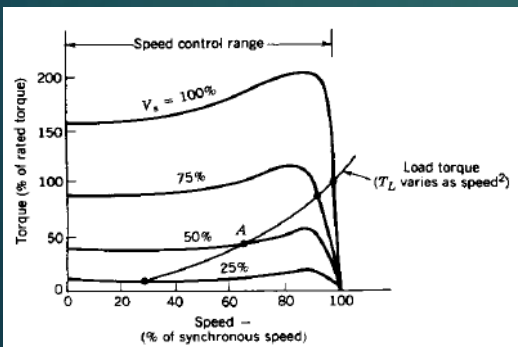


Figure 14-29 Static slip recovery.



Torque speed xtic for a constant torque load. Notice that the operating points (intersection of black lines with brown line) shift back as  $R_r$  increases.

