



# Power Electronics

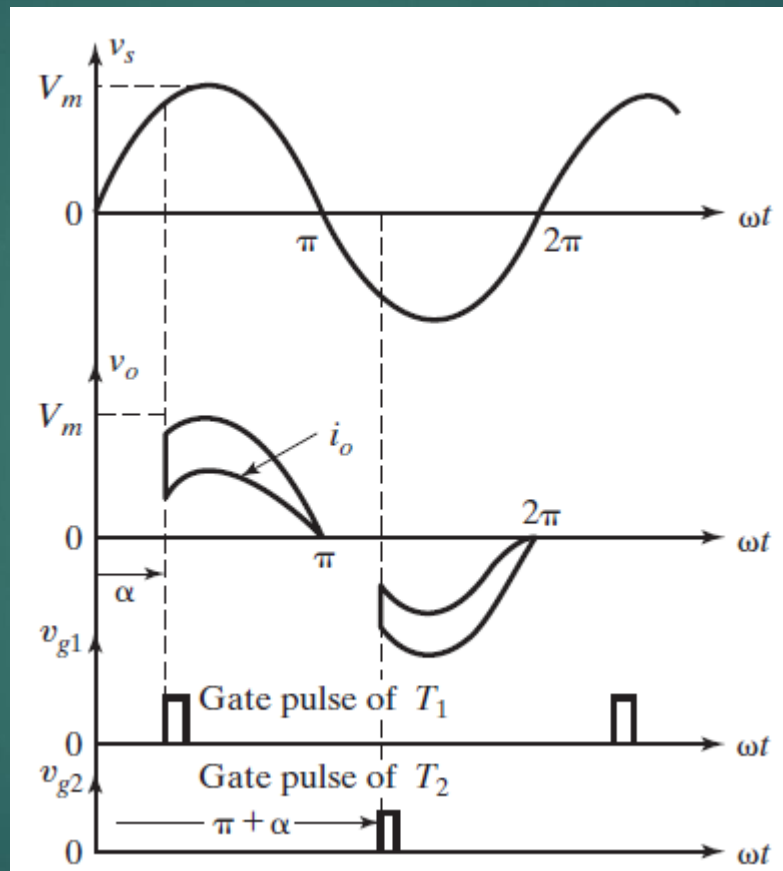
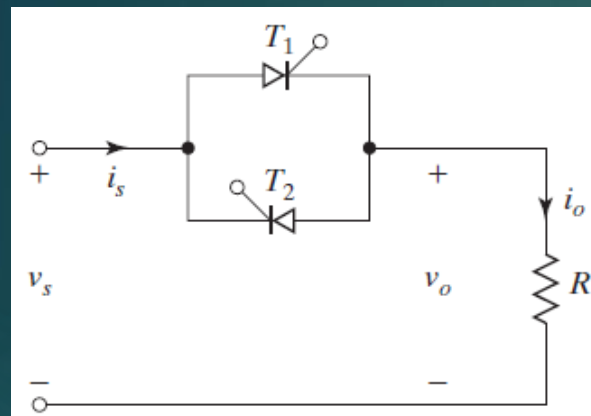
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## AC Voltage Controllers

### 11.3 SINGLE-PHASE FULL-WAVE CONTROLLERS WITH RESISTIVE LOADS

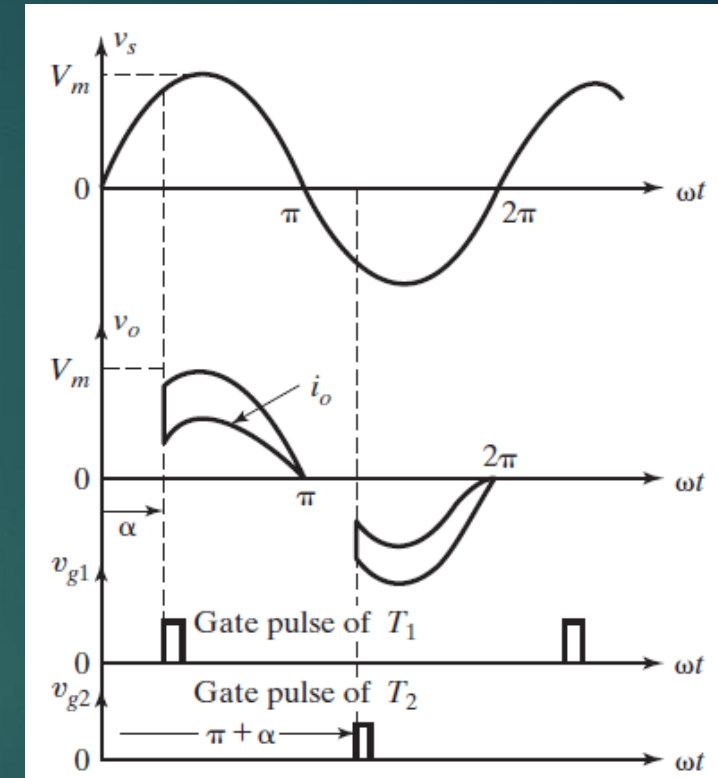


$$v_s = \sqrt{2}V_s \sin \omega t$$

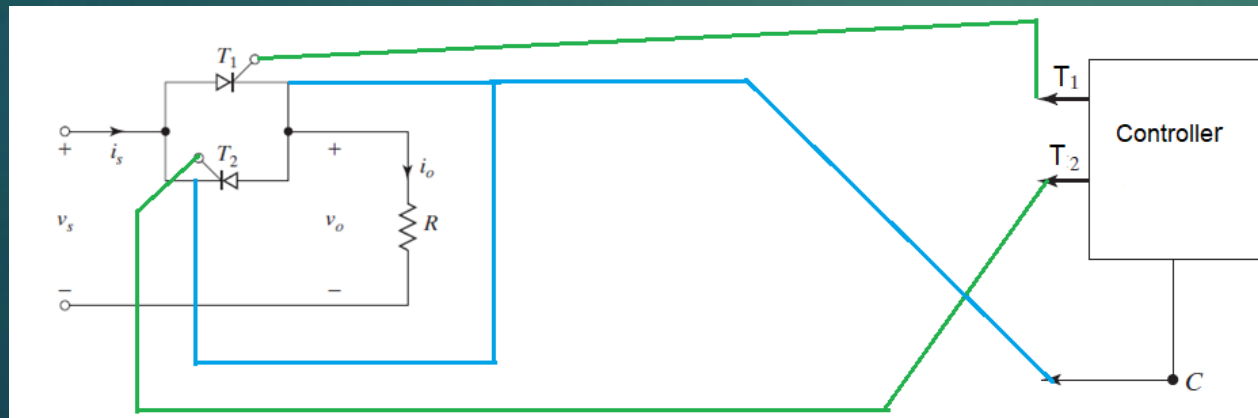
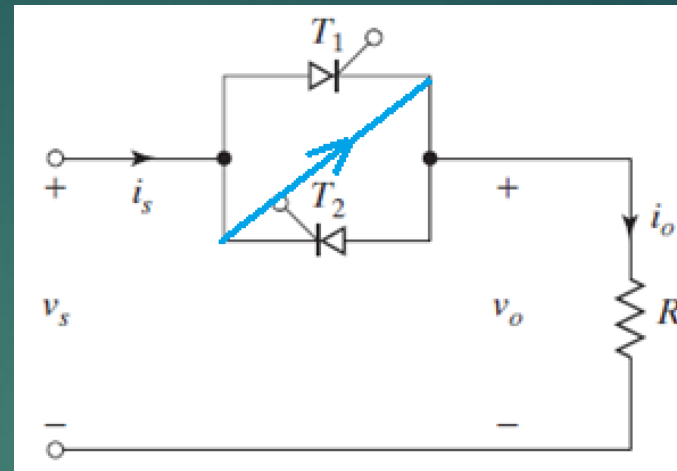
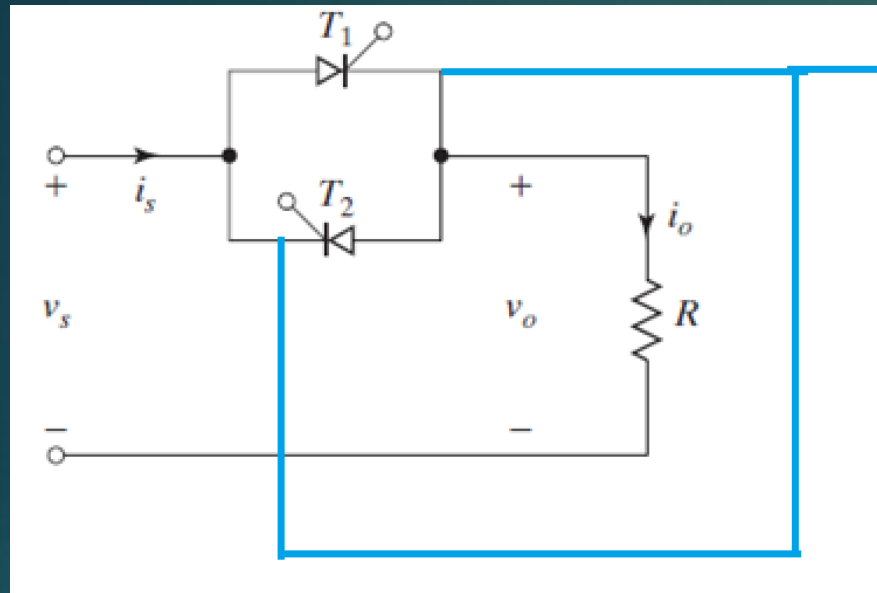
$$\begin{aligned} V_o &= \left\{ \frac{2}{2\pi} \int_{\alpha}^{\pi} 2V_s^2 \sin^2 \omega t d(\omega t) \right\}^{1/2} \\ &= \left\{ \frac{4V_s^2}{4\pi} \int_{\alpha}^{\pi} (1 - \cos 2\omega t) d(\omega t) \right\}^{1/2} \\ &= V_s \left[ \frac{1}{\pi} \left( \pi - \alpha + \frac{\sin 2\alpha}{2} \right) \right]^{1/2} \quad (11.1) \end{aligned}$$

$$RMS \text{ Value} = \sqrt{\frac{1}{T} \int_0^T [f(x)]^2 dx}$$

$$\sin \frac{\theta}{2} = \pm \sqrt{\frac{1 - \cos \theta}{2}}$$







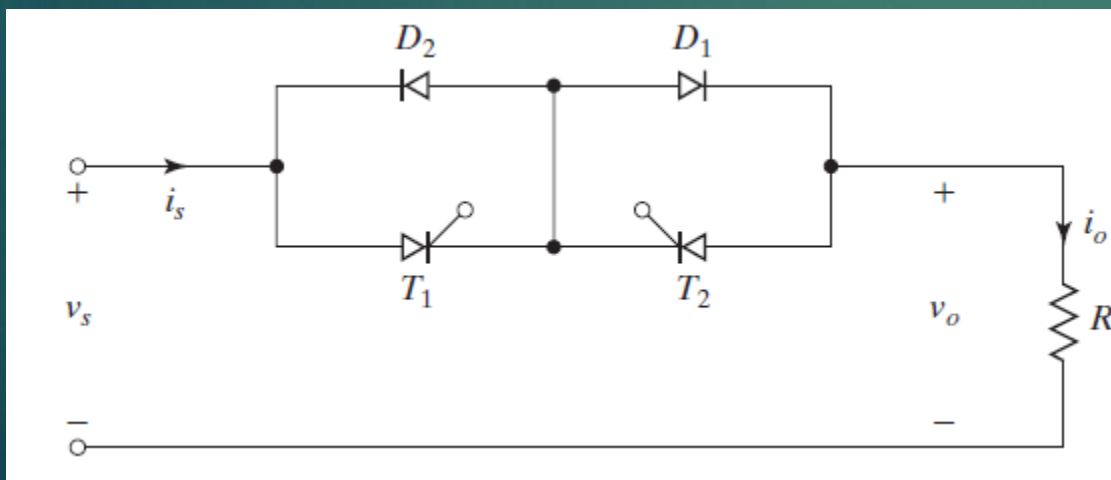
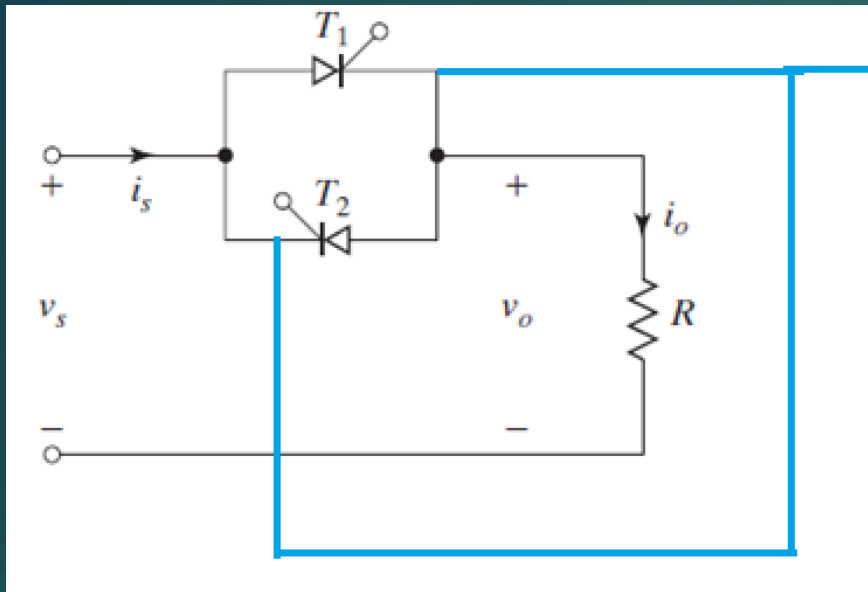


FIGURE 11.3

Single-phase full-wave controller with common cathode.



## Example 11.1 Finding the Performance Parameters of a Single-Phase Full-Wave Controller

A single-phase full-wave ac voltage controller in Figure 11.2a has a resistive load of  $R = 10\ \Omega$  and the input voltage is  $V_s = 120\text{ V}$  (rms), 60 Hz. The delay angles of thyristors  $T_1$  and  $T_2$  are equal:  $\alpha_1 = \alpha_2 = \alpha = \pi/2$ . Determine (a) the rms output voltage  $V_o$ , (b) the input PF, (c) the average current of thyristors  $I_A$ , and (d) the rms current of thyristors  $I_R$ .

### Solution

$R = 10\ \Omega$ ,  $V_s = 120\text{ V}$ ,  $\alpha = \pi/2$ , and  $V_m = \sqrt{2} \times 120 = 169.7\text{ V}$ .

- a. From Eq. (11.1), the rms output voltage

$$V_o = \frac{120}{\sqrt{2}} = 84.85\text{ V}$$

- b. The rms value of load current is  $I_o = V_o/R = 84.85/10 = 8.485\text{ A}$  and the load power is  $P_o = I_o^2 R = 8.485^2 \times 10 = 719.95\text{ W}$ . Because the input current is the same as the load current, the input VA rating is

$$\text{VA} = V_s I_s = V_s I_o = 120 \times 8.485 = 1018.2\text{ W}$$

The input PF is

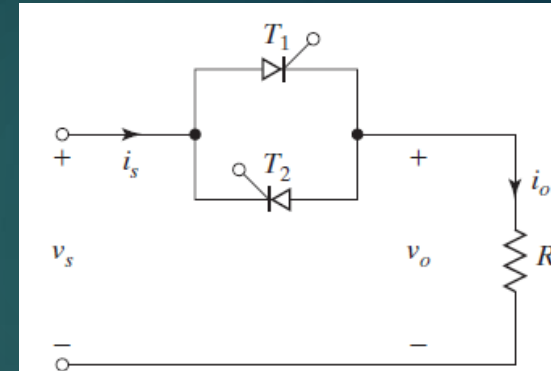
$$\begin{aligned} \text{PF} &= \frac{P_o}{\text{VA}} = \frac{V_o}{V_s} = \left[ \frac{1}{\pi} \left( \pi - \alpha + \frac{\sin 2\alpha}{2} \right) \right]^{1/2} \\ &= \frac{1}{\sqrt{2}} = \frac{719.95}{1018.2} = 0.707 \text{ (lagging)} \end{aligned}$$

- c. The average thyristor current

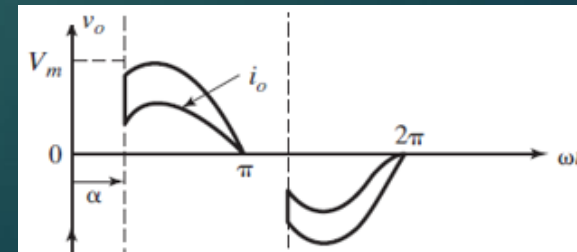
$$\begin{aligned} I_A &= \frac{1}{2\pi R} \int_{\alpha}^{\pi} \sqrt{2} V_s \sin \omega t \, d(\omega t) \\ &= \frac{\sqrt{2} V_s}{2\pi R} (\cos \alpha + 1) \\ &= \sqrt{2} \times \frac{120}{2\pi \times 10} = 2.7\text{ A} \end{aligned}$$

- d. The rms value of the thyristor current

$$\begin{aligned} I_R &= \left[ \frac{1}{2\pi R^2} \int_{\alpha}^{\pi} 2V_s^2 \sin^2 \omega t \, d(\omega t) \right]^{1/2} \\ &= \left[ \frac{2V_s^2}{4\pi R^2} \int_{\alpha}^{\pi} (1 - \cos 2\omega t) \, d(\omega t) \right]^{1/2} \\ &= \frac{V_s}{\sqrt{2} R} \left[ \frac{1}{\pi} \left( \pi - \alpha + \frac{\sin 2\alpha}{2} \right) \right]^{1/2} \\ &= \frac{120}{2 \times 10} = 6\text{ A} \end{aligned}$$



$$V_o = V_s \left[ \frac{1}{\pi} \left( \pi - \alpha + \frac{\sin 2\alpha}{2} \right) \right]^{1/2} \quad (11.1)$$



## 11.4 SINGLE-PHASE FULL-WAVE CONTROLLERS WITH INDUCTIVE LOADS

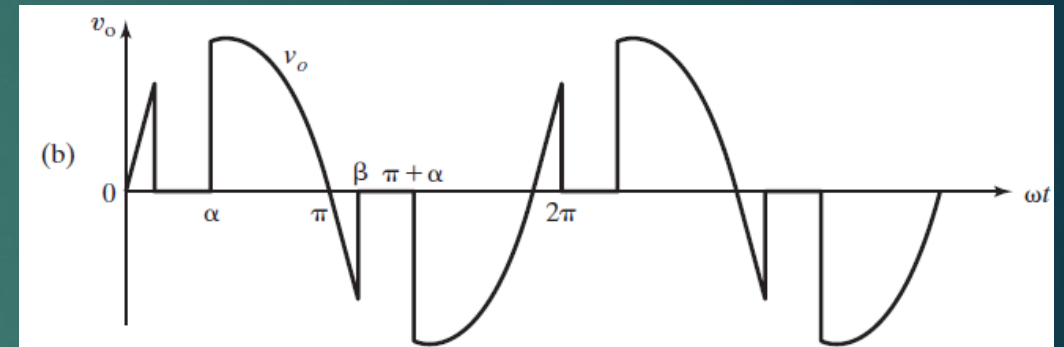
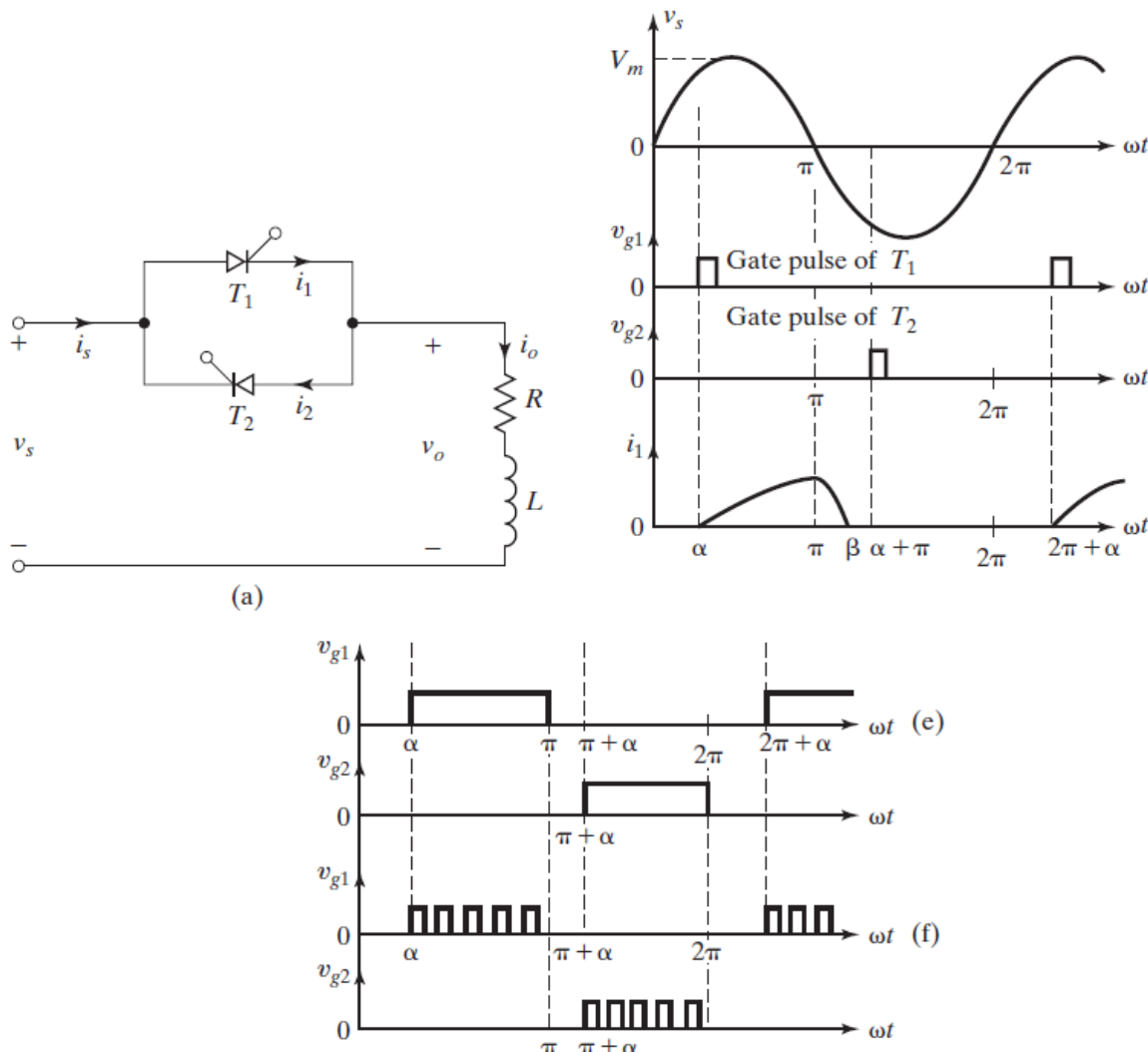


FIGURE 11.6

Typical waveforms of single-phase ac voltage controller with an  $RL$  load. (a) Input supply voltage and output current, (b) Output voltage, and (c) Voltage across thyristor  $T_1$ .

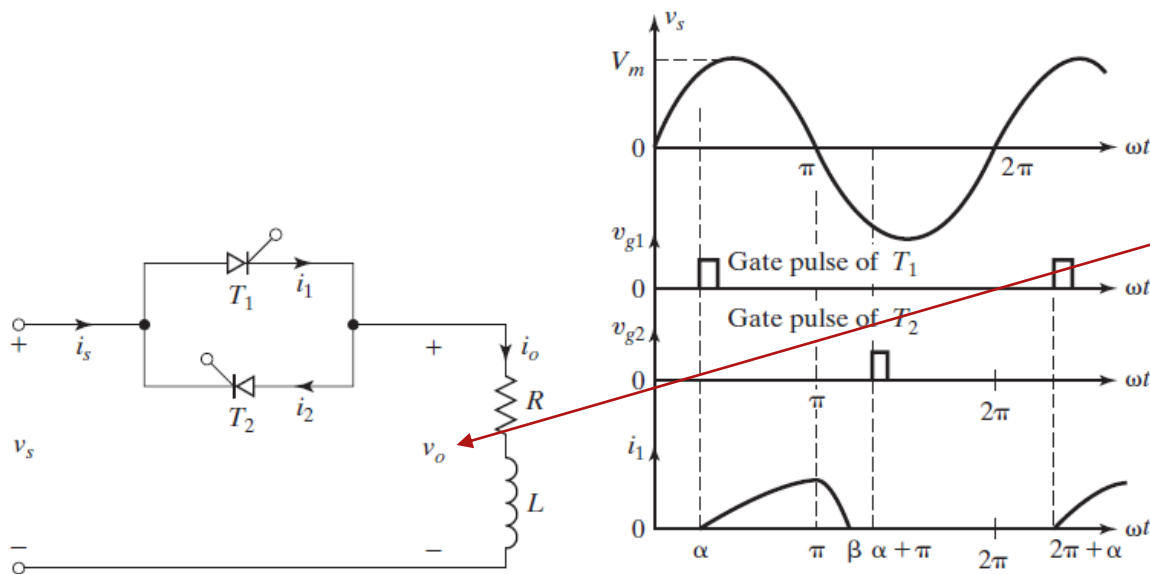
$$i_1 = \frac{\sqrt{2}V_s}{Z} [\sin(\omega t - \theta) - \sin(\alpha - \theta)e^{(R/L)(\omega t - \alpha)}] \quad (11.8)$$

$$\sin(\beta - \theta) = \sin(\alpha - \theta)e^{(R/L)(\alpha - \beta)/\omega} \quad (11.9)$$





## 11.4 SINGLE-PHASE FULL-WAVE CONTROLLERS WITH INDUCTIVE LOADS



$v_o(t)$  may be evaluated via

$$v_o = L \frac{di_1}{dt} + Ri_1$$

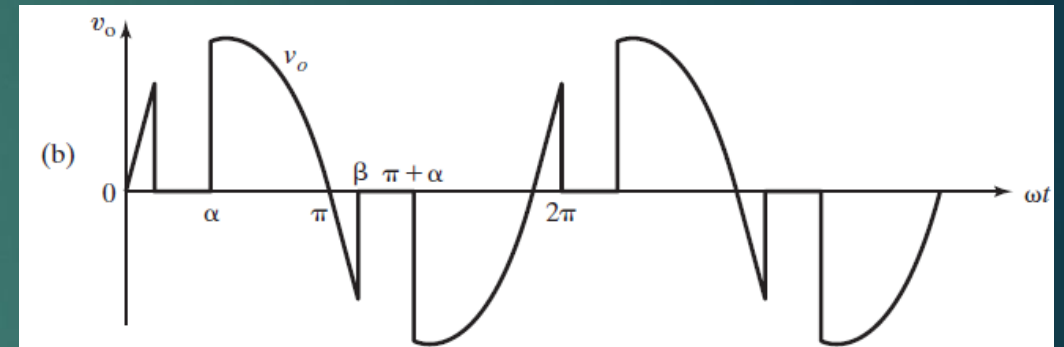


FIGURE 11.6

Typical waveforms of single-phase ac voltage controller with an  $RL$  load. (a) Input supply voltage and output current, (b) Output voltage, and (c) Voltage across thyristor  $T_1$ .

$$i_1 = \frac{\sqrt{2}V_s}{Z} [\sin(\omega t - \theta) - \sin(\alpha - \theta)e^{(R/L)(\omega t - \alpha)}] \quad (11.8)$$

$$\sin(\beta - \theta) = \sin(\alpha - \theta)e^{(R/L)(\alpha - \beta)/\omega} \quad (11.9)$$



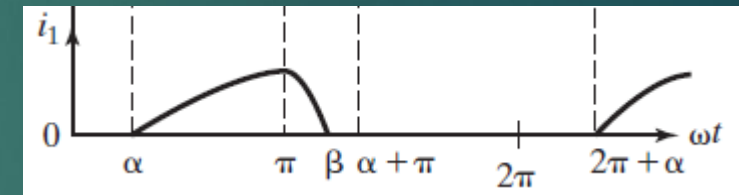
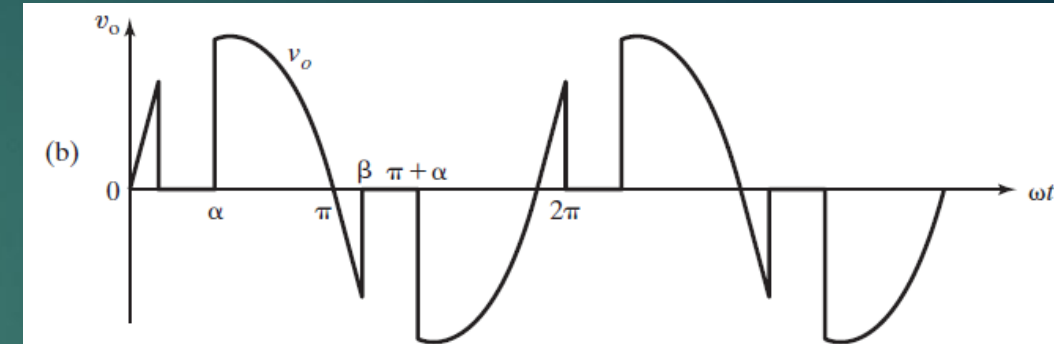
## Mathematical expressions for AC/AC conv. with RL load

$$\begin{aligned}
 V_o &= \left[ \frac{2}{2\pi} \int_{\alpha}^{\beta} 2V_s^2 \sin^2 \omega t d(\omega t) \right]^{1/2} \\
 &= \left[ \frac{4V_s^2}{4\pi} \int_{\alpha}^{\beta} (1 - \cos 2\omega t) d(\omega t) \right]^{1/2} \\
 &= V_s \left[ \frac{1}{\pi} \left( \beta - \alpha + \frac{\sin 2\alpha}{2} - \frac{\sin 2\beta}{2} \right) \right]^{1/2} \quad (11.11)
 \end{aligned}$$

$$\begin{aligned}
 I_R &= \left[ \frac{1}{2\pi} \int_{\alpha}^{\beta} i_1^2 d(\omega t) \right]^{1/2} \\
 &= \frac{V_s}{Z} \left[ \frac{1}{\pi} \int_{\alpha}^{\beta} \left\{ \sin(\omega t - \theta) - \sin(\alpha - \theta) e^{(R/L)(\alpha/\omega - t)} \right\}^2 d(\omega t) \right]^{1/2} \quad (11.12)
 \end{aligned}$$

$$I_o = (I_R^2 + I_R^2)^{1/2} = \sqrt{2} I_R \quad (11.13)$$

$$\begin{aligned}
 I_A &= \frac{1}{2\pi} \int_{\alpha}^{\beta} i_1 d(\omega t) \\
 &= \frac{\sqrt{2}V_s}{2\pi Z} \int_{\alpha}^{\beta} \left[ \sin(\omega t - \theta) - \sin(\alpha - \theta) e^{(R/L)(\alpha/\omega - t)} \right] d(\omega t) \quad (11.14)
 \end{aligned}$$



$$\begin{aligned}
 V_o &= \left\{ \frac{2}{2\pi} \int_{\alpha}^{\pi} 2V_s^2 \sin^2 \omega t d(\omega t) \right\}^{1/2} \\
 &= \left\{ \frac{4V_s^2}{4\pi} \int_{\alpha}^{\pi} (1 - \cos 2\omega t) d(\omega t) \right\}^{1/2} \\
 &= V_s \left[ \frac{1}{\pi} \left( \pi - \alpha + \frac{\sin 2\alpha}{2} \right) \right]^{1/2} \quad (11.1)
 \end{aligned}$$



### Example 11.2 Finding the Performance Parameters of a Single-Phase Full-Wave Controller with an $RL$ Load

The single-phase full-wave controller in Figure 11.5a supplies an  $RL$  load. The input rms voltage is  $V_s = 120$  V, 60 Hz. The load is such that  $L = 6.5$  mH and  $R = 2.5$   $\Omega$ . The delay angles of thyristors are equal:  $\alpha_1 = \alpha_2 = \pi/2$ . Determine (a) the conduction angle of thyristor  $T_1$ ,  $\delta$ ; (b) the rms output voltage  $V_o$ ; (c) the rms thyristor current  $I_R$ ; (d) the rms output current  $I_o$ ; (e) the average current of a thyristor  $I_A$ ; and (f) the input PF.

#### Solution

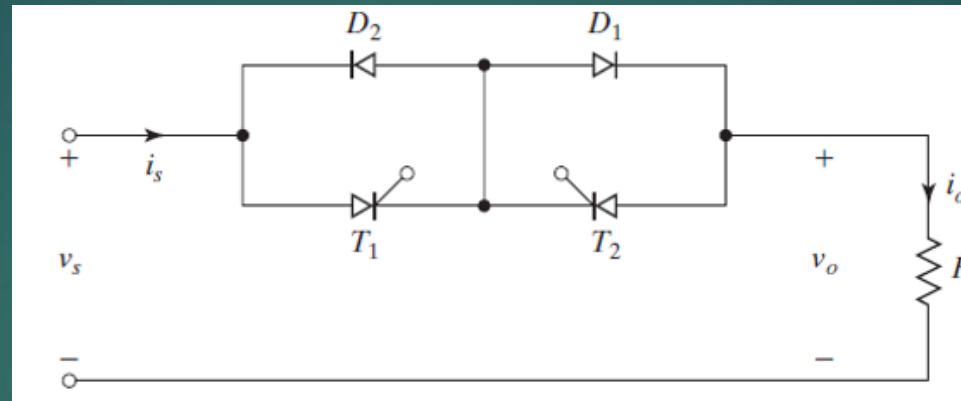
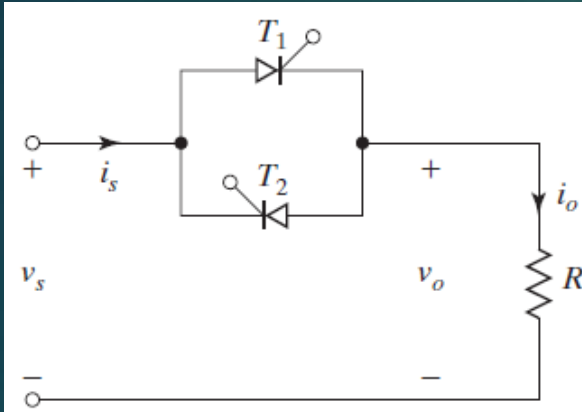
$R = 2.5$   $\Omega$ ,  $L = 6.5$  mH,  $f = 60$  Hz,  $\omega = 2\pi \times 60 = 377$  rad/s,  $V_s = 120$  V,  $\alpha = 90^\circ$ , and  $\theta = \tan^{-1}(\omega L/R) = 44.43^\circ$ .

- The extinction angle can be determined from the solution of Eq. (11.9) and an iterative solution yields  $\beta = 220.35^\circ$ . The conduction angle is  $\delta = \beta - \alpha = 220.35 - 90 = 130.35^\circ$ .
- From Eq. (11.11), the rms output voltage is  $V_o = 68.09$  V.
- Numerical integration of Eq. (11.12) between the limits  $\omega t = \alpha$  to  $\beta$  gives the rms thyristor current as  $I_R = 15.07$  A.
- From Eq. (11.13),  $I_o = \sqrt{2} \times 15.07 = 21.3$  A.
- Numerical integration of Eq. (11.14) yields the average thyristor current as  $I_A = 8.23$  A.
- The output power  $P_o = 21.3^2 \times 2.5 = 1134.2$  W, and the input VA rating is  $VA = 120 \times 21.3 = 2556$  W; therefore,

$$PF = \frac{P_o}{VA} = \frac{1134.200}{2556} = 0.444 \text{ (lagging)}$$



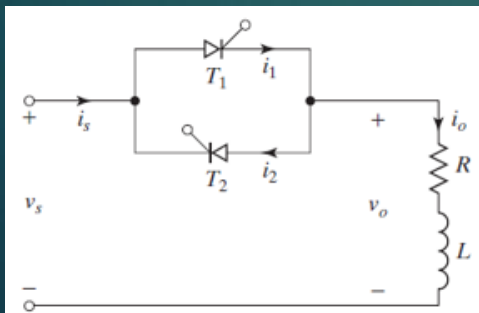
## Evaluate/Assess AC/AC converters



Give a comparative evaluation of the above two ac/ac converters w.r.t. output voltage magnitude and power efficiency.

Evaluate the suitability of the above converters in comparison to an AC/DC/AC power conversion.

Assess the selection of the given SCR for use in an ac/ac general purpose fan dimmer.



Type:	Phase Control
Case:	Disc
$V_{RRM}/V_{DRM}$ :	400V
$I_{T(av)}$ :	0.1 A
$I_{T(rms)}$ :	0.17 A
$I_{TSM}$ :	4 A
$I^2t$ :	$11.3 \times 10^6 \text{ A}^2\text{s}$
$V_{TM}$ :	2 V
$I_{RRM}/I_{DRM}$ :	1 A
$t_{ON}$ :	3 $\mu\text{s}$
$t_{OFF}$ :	1080 $\mu\text{s}$
$I_{GT}$ :	400 mA
$V_{GT}$ :	2.6 V
Diameter:	150 mm
Thickness:	27 mm



## 11.5 THREE-PHASE FULL-WAVE CONTROLLERS

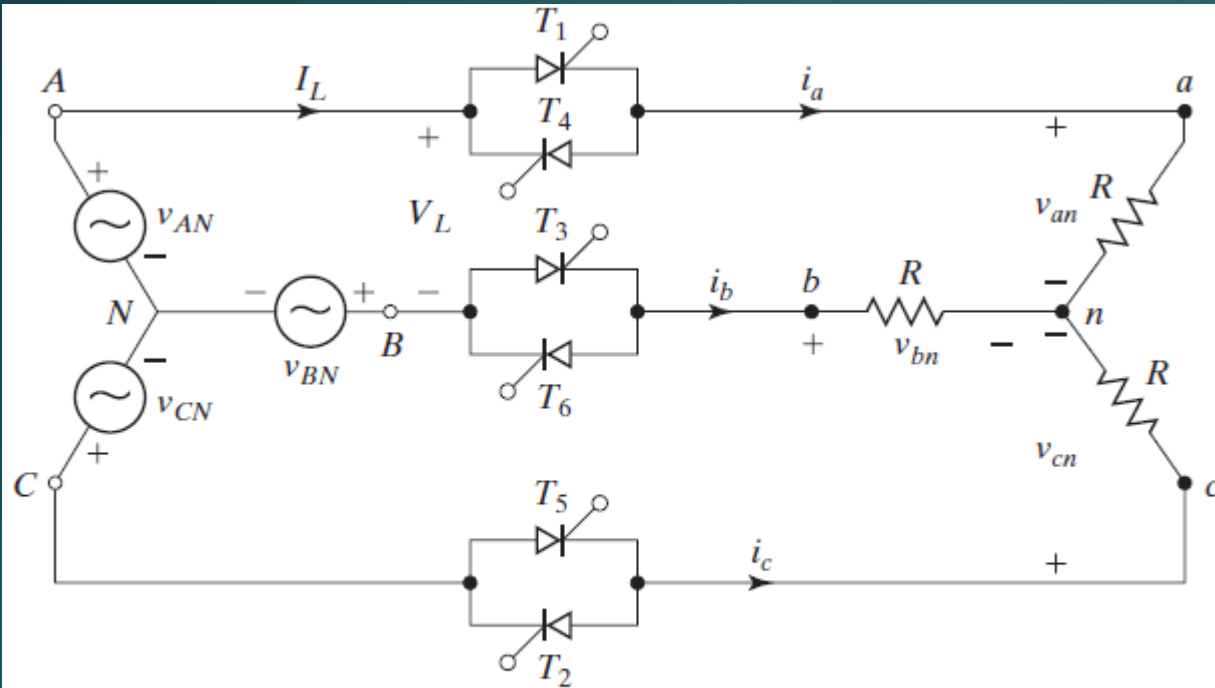
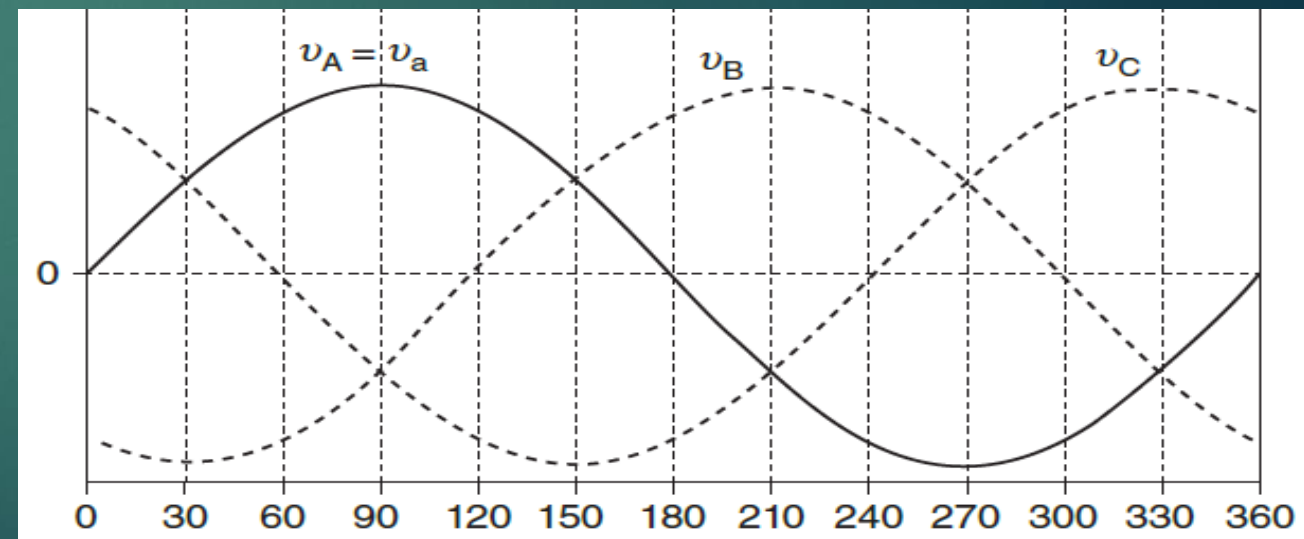
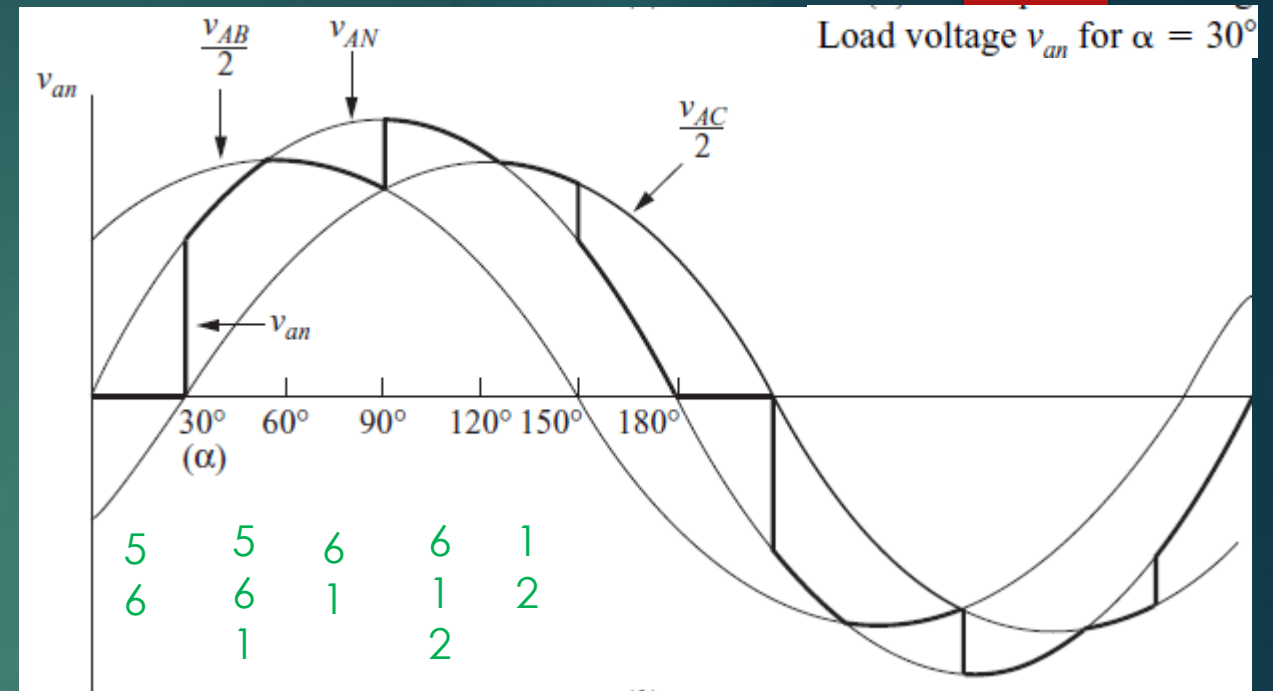
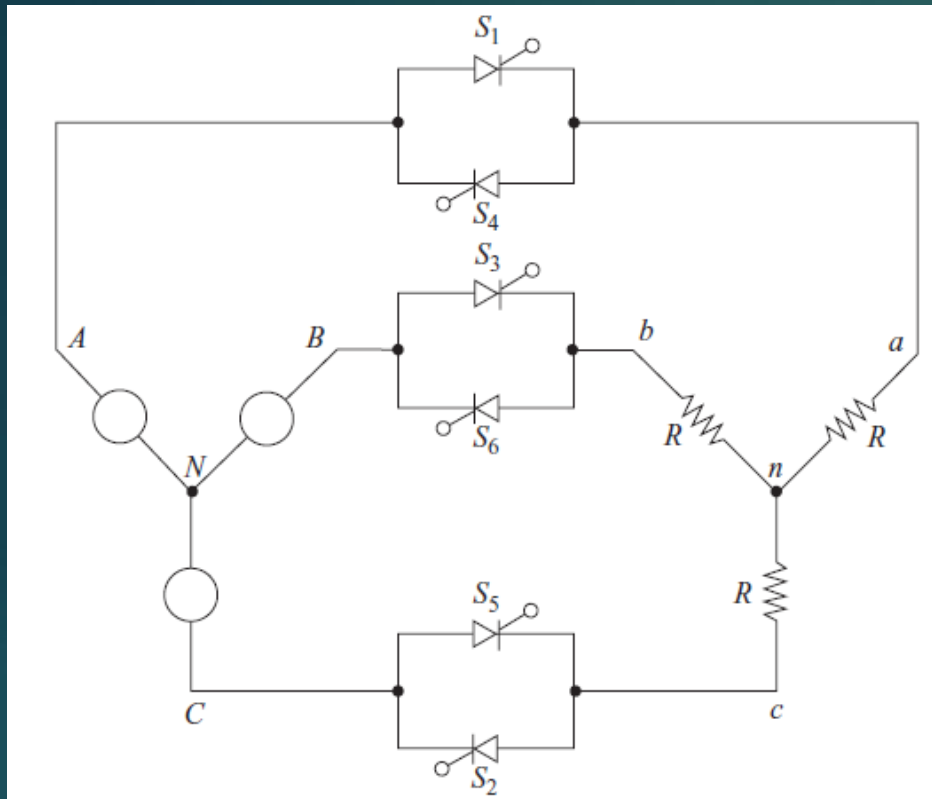


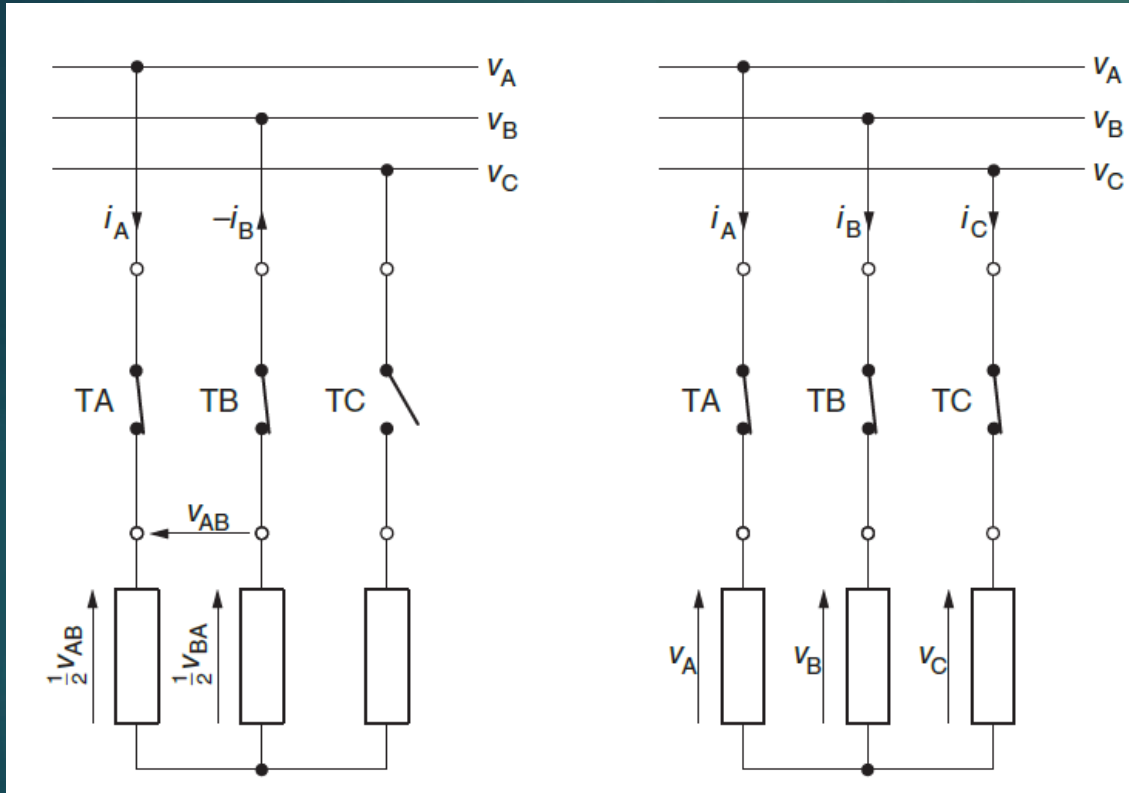
FIGURE 11.7

Three-phase bidirectional controller.





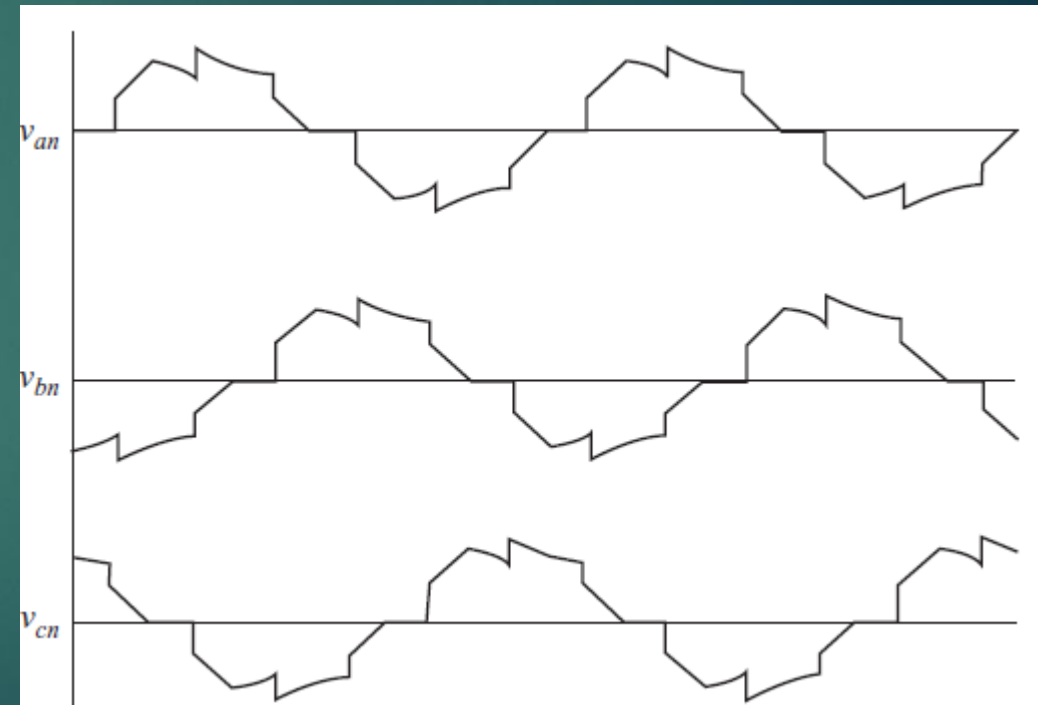
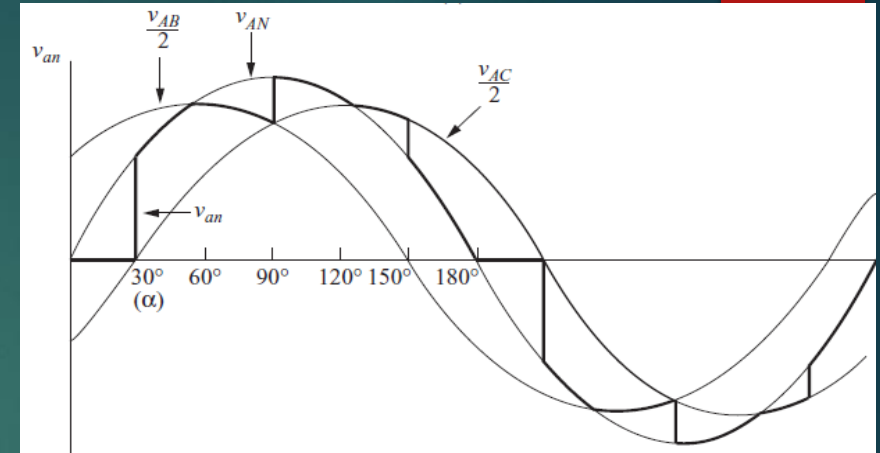




To show reduction of  $v_{an}$  to  $\frac{1}{2}(v_{ab})$

$$V_o = V_i \sqrt{\frac{1}{\pi} \left[ \pi - \frac{3}{2} \alpha_f + \frac{3}{4} \sin(2\alpha_f) \right]}$$

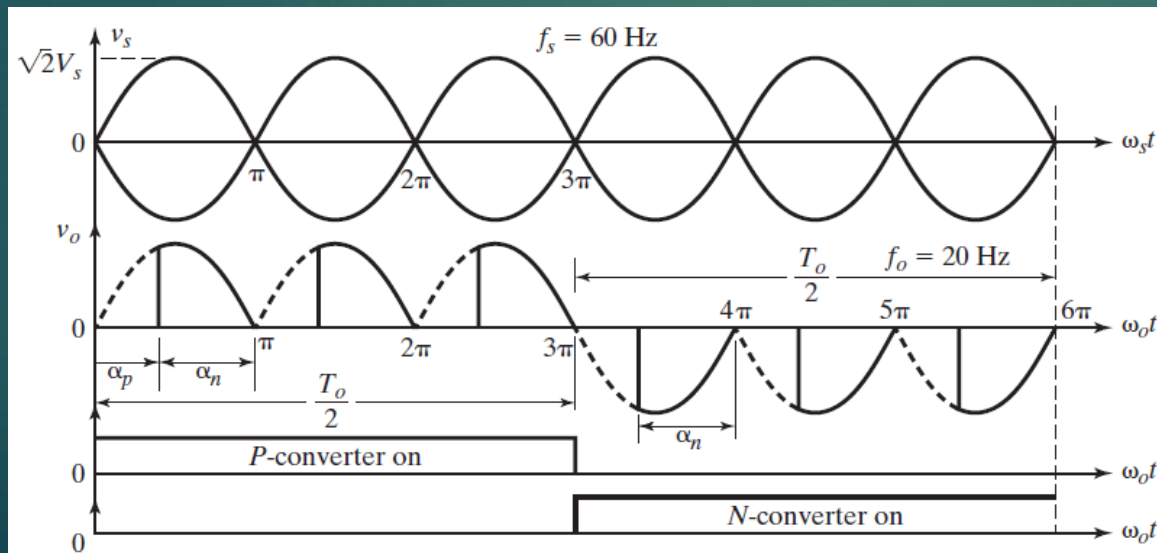
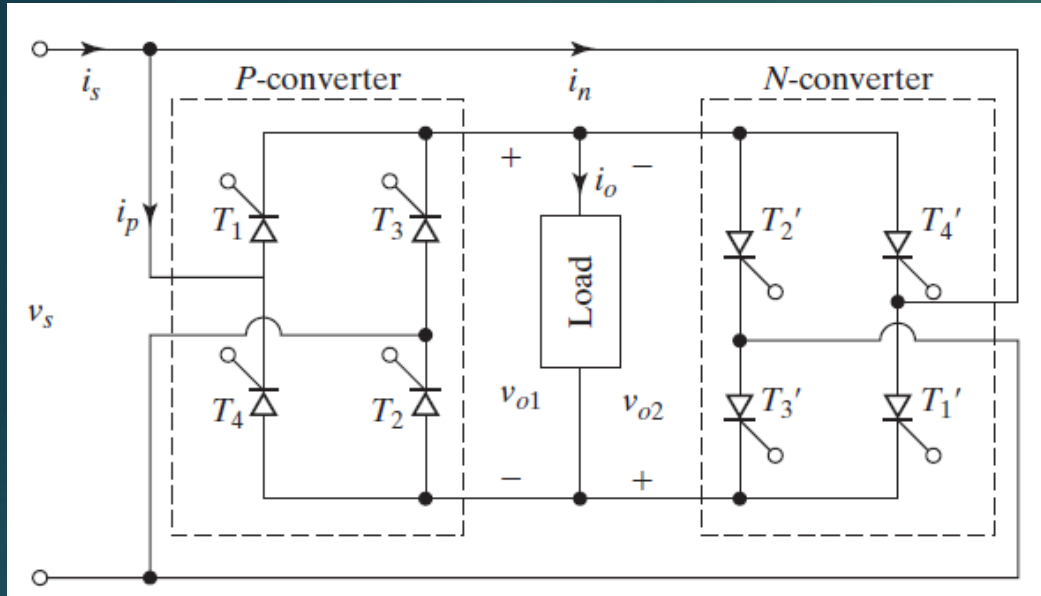
for  $0 \leq \alpha_f < 60^\circ$



Line-neutral voltages for 30 deg firing angle



## Cyclo-converters



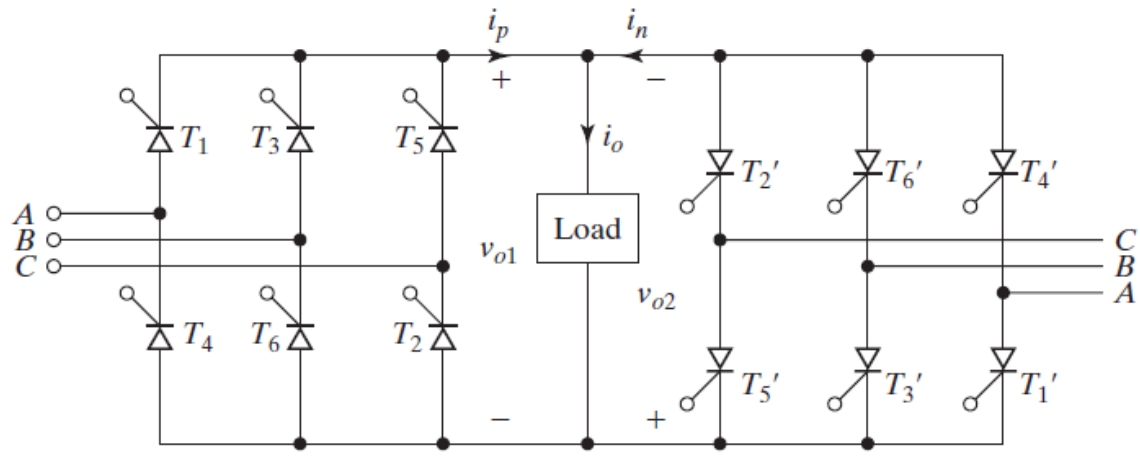
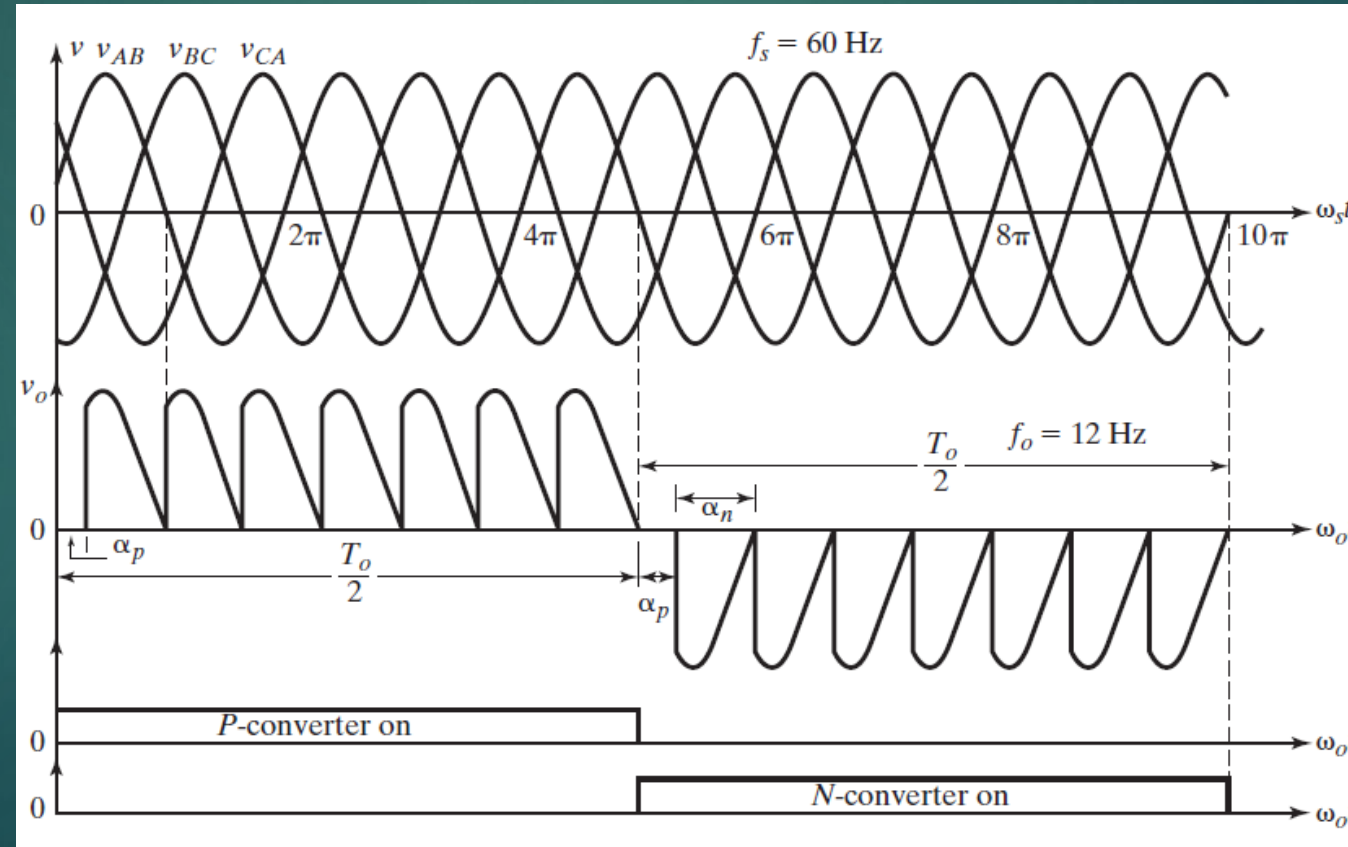


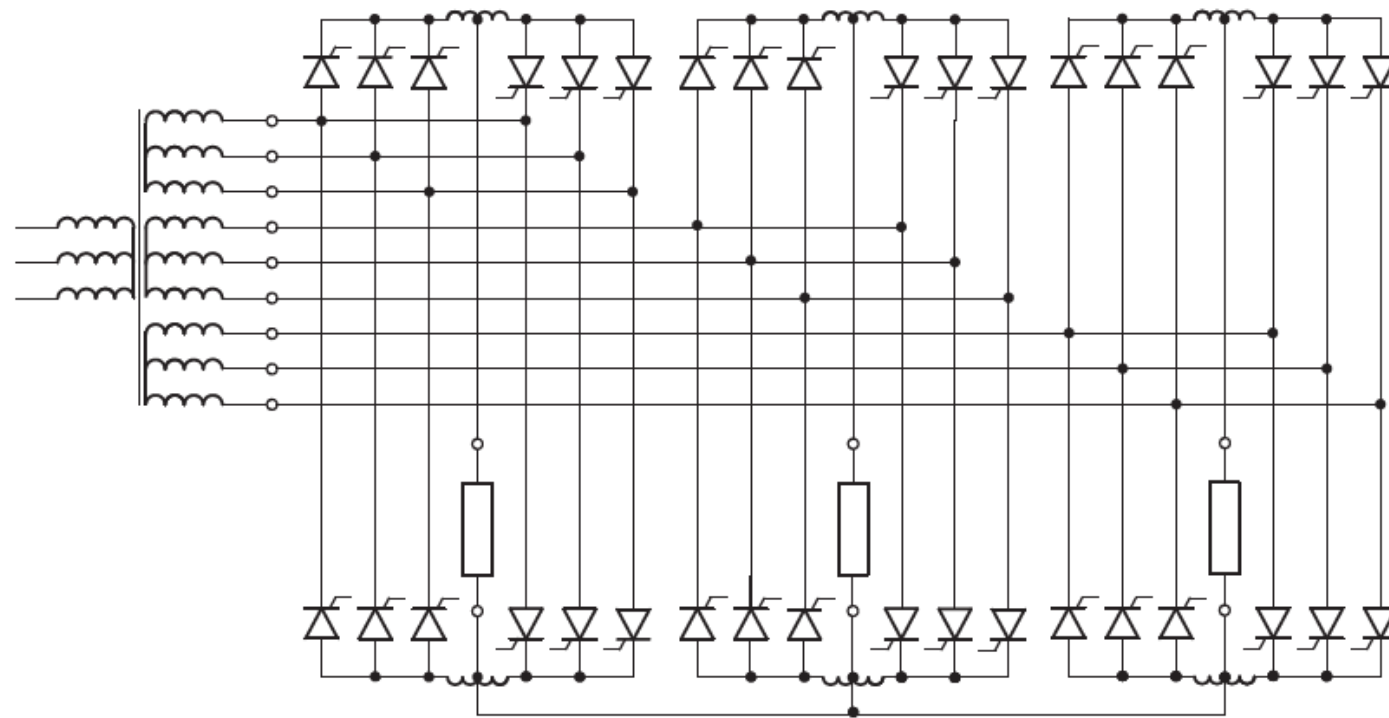
FIGURE 11.18  
Three-phase/single-phase cycloconverter.



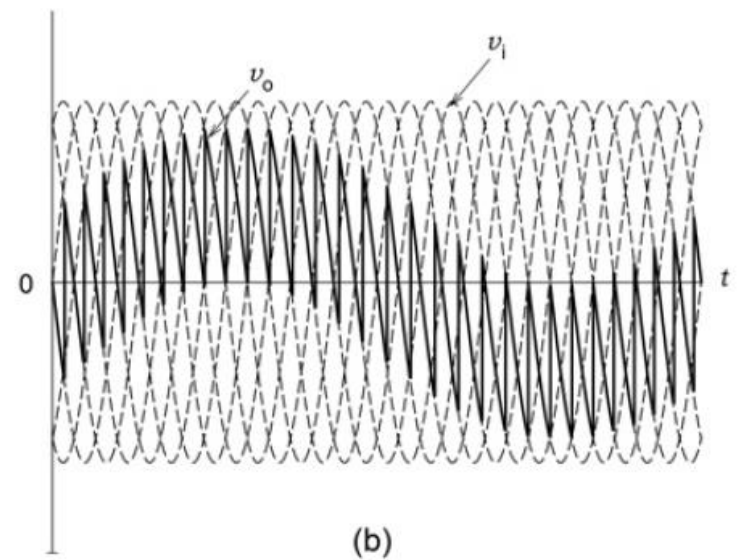
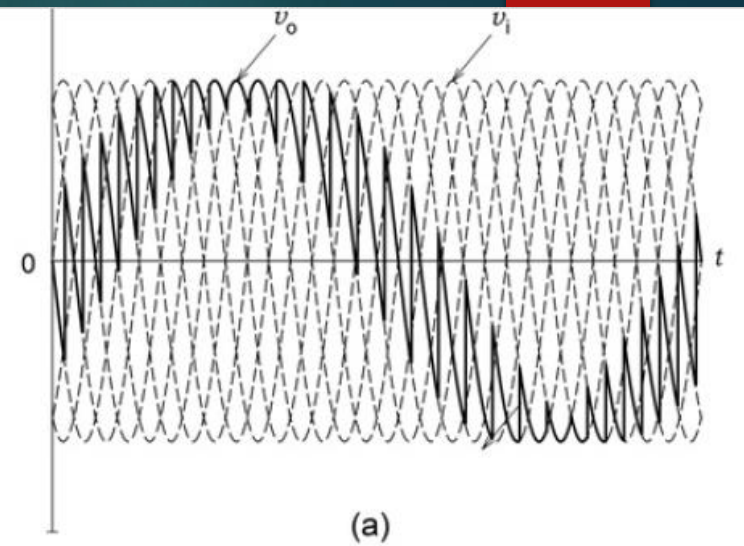
$10\pi \rightarrow 5 \text{ cycles}$

$60/5 = 12 \text{ Hz}$



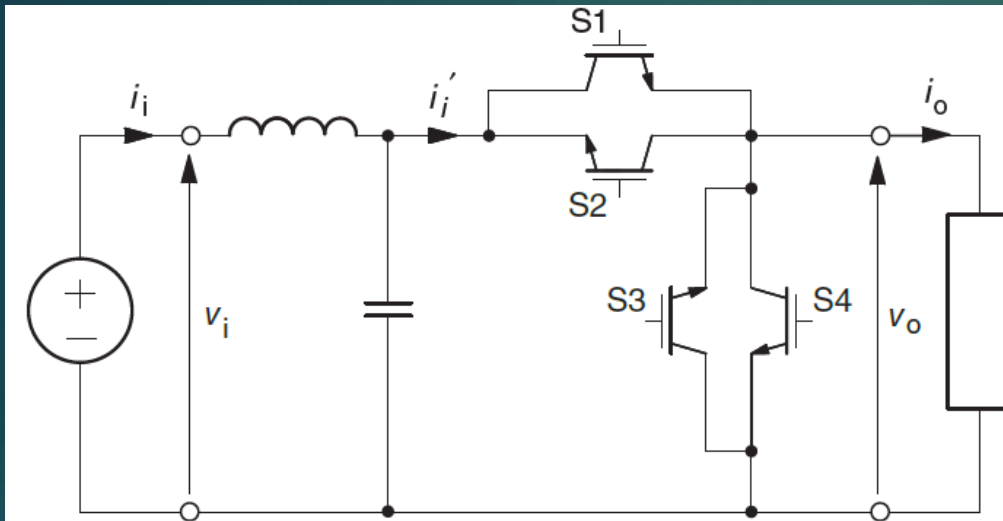


**Figure 5.23** Three-phase six-pulse cycloconverter with interconnected phase loads.





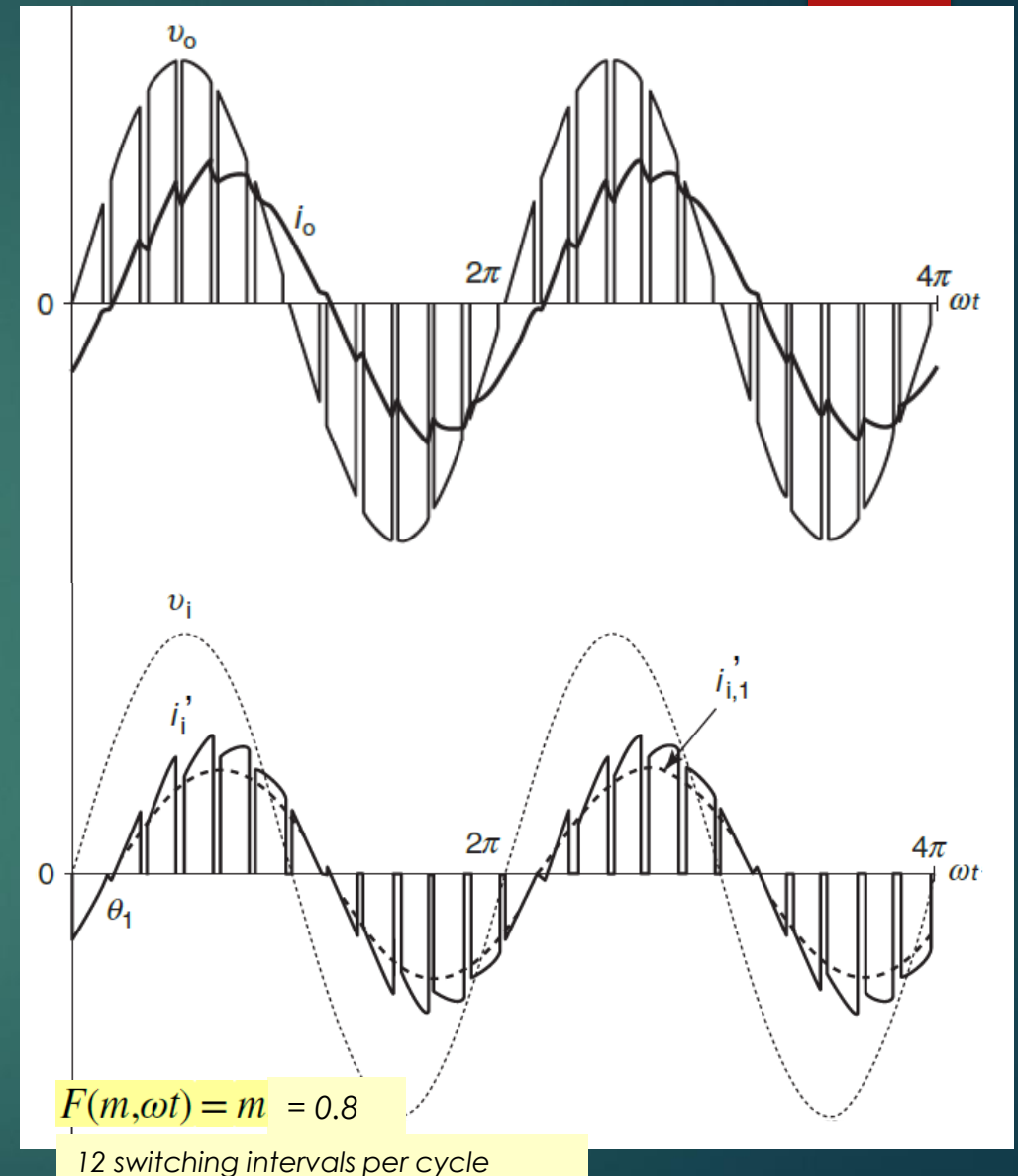
### 5.1.3 PWM AC Voltage Controllers



**Figure 5.16** Single-phase ac chopper with input filter.

$$\begin{aligned} x_3 &= \bar{x}_1 \\ x_4 &= \bar{x}_2 \end{aligned}$$

S3, S4 are free  
wheeling switches



**Figure 5.17** Waveforms of voltages and currents in a single-phase ac chopper: (a) output voltage and current, (b) input voltage and current (after the input filter) and the fundamental output current.



This is the value of the modulating function  $F(m, \omega t)$  at  $\omega t = \alpha_n$ .

$$d_{1,n} = \begin{cases} F(m, \alpha_n) & \text{for } 0 < \alpha_n \leq \pi \\ 0 & \text{otherwise} \end{cases}$$

$$d_{2,n} = \begin{cases} F(m, \alpha_n) & \text{for } \pi < \alpha_n \leq 2\pi \\ 0 & \text{otherwise} \end{cases}$$

Duty ratios of S1 and S2 for the  $n$ th switching interval.

$$d_{1,n}^* = d_{2,n}^* = F(m, \alpha_n)$$

$$x_3^* = x_4^* = \bar{x}_1^*$$

For  $F(m, \omega t) = m = 0.8$

$$d_{1,n} = 0.8$$

i.e. duty cycle in every switching interval is fixed equal to 0.8

$$V_o = \sqrt{m} V_i$$

$$F(\omega t) = m$$

$$F(\omega t) = m |\sin(\omega t)|$$

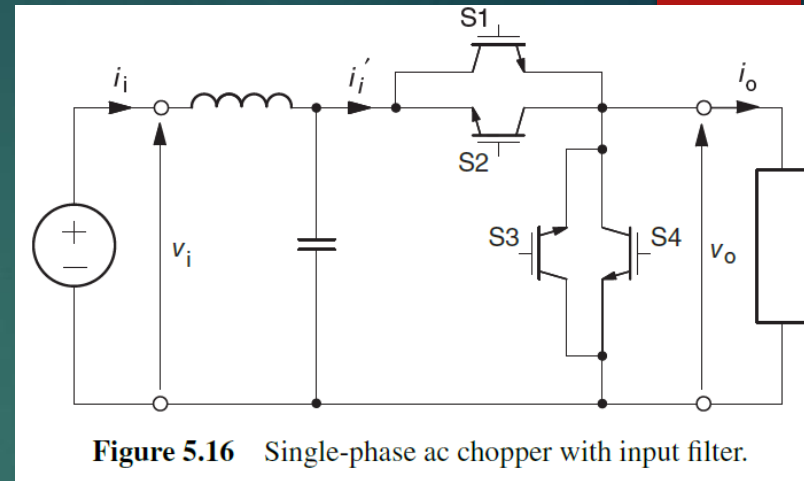
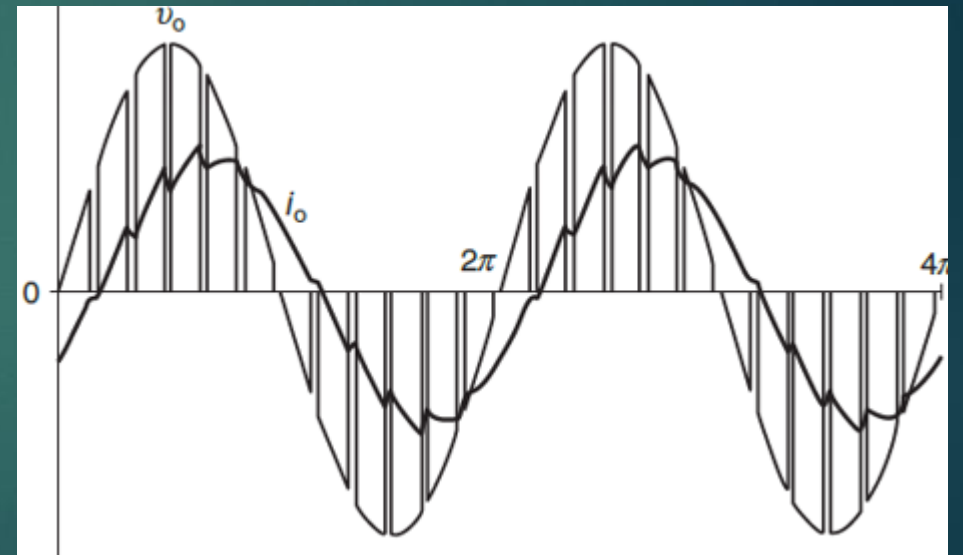


Figure 5.16 Single-phase ac chopper with input filter.

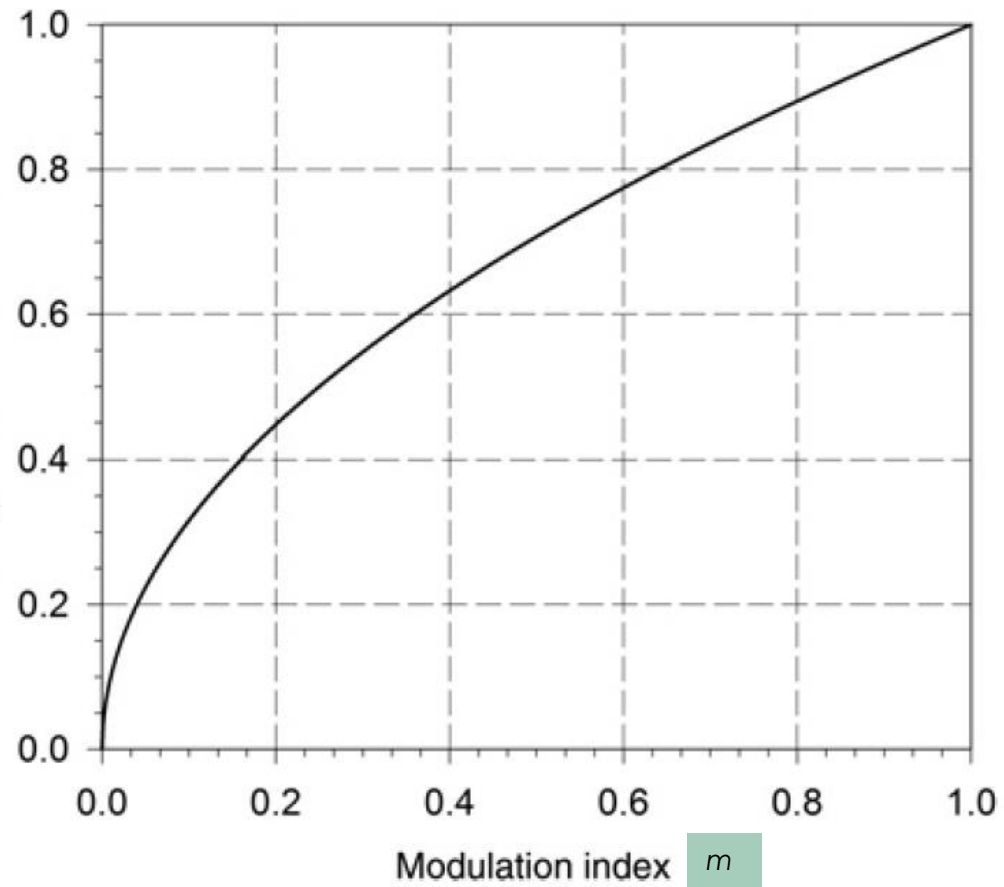


$$F(m, \omega t) = m = 0.8$$



$V_{o-rms} / V_{in-rms}$

Magnitude control ratio



$$V_o = \sqrt{m} V_i$$

