Test of Biomass as Covariate in Aster Models for Lifetime Fitness

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Introduction

The following code tests, on the advice of Dr. Daniel Bolnick and Dr. Lynda Delph, the effect of biomass on female and male fitness, as determined with aster models.

Preliminaries

Set working directory and load data.

Examine data

```
fin<- read.csv("data/aster.dat.csv")</pre>
names(fin)
    [1] "Treat"
                      "plotID"
                                                             "plantID"
##
                                   "Den"
                                                "Gen"
                      "surv"
                                                             "frt.2"
##
   [6] "familyID"
                                   "flw"
                                                "frt"
## [11] "seeds"
                      "aborted"
                                   "rel.seeds" "seed.wt"
                                                             "mass.a"
## [16] "mass.b"
head(fin)
     Treat plotID Den Gen plantID familyID surv flw frt frt.2 seeds aborted
## 1
      HDHG
                 5
                     Η
                        HG
                                  1
                                            4
                                                  1
                                                      1
                                                          3
                                                                 2
                                                                       33
      HDHG
                 5
                     H HG
                                  2
                                            6
                                                      1
                                                         21
                                                                       69
                                                                               22
## 2
                                                  1
                                                                 6
      HDHG
                     H HG
                                  3
                                                      1
                                                                 7
                                                                      73
                                                                               19
## 3
                                           11
                                                  1
                                                                               23
      HDHG
                 5
                     H HG
                                  4
                                           14
                                                      1
                                                         18
                                                                     107
## 4
                                                  1
                                                                 8
                 5
                     Н
## 5
      HDHG
                        HG
                                  5
                                            6
                                                  1
                                                      1
                                                          1
                                                                 1
                                                                       16
                                                                                4
      HDHG
                 5
                     H HG
                                  6
                                           14
                                                          0
                                                                                0
## 6
                                                                        0
     rel.seeds seed.wt mass.a mass.b
## 1 0.5714286
                  6.792
                            5.8
                                    0.8
## 2 1.1948052
                  6.995
                            1.9
                                    0.2
## 3 1.2640693
                  7.413
                           20.8
                                    1.3
## 4 1.8528139
                  8.554
                           18.2
                                    1.1
## 5 0.2770563
                  7.771
                           65.8
                                    6.1
## 6 0.0000000
                  0.000
                            6.6
                                    1.2
```

Make sure Den (density treatment), Gen (N_e treatment), plotID, plantID, and familyID are all classified as factors. Otherwise

```
fin$Den<- as.factor(fin$Den)
fin$Gen<- as.factor(fin$Gen)
fin$plotID<- as.factor(fin$plotID)
fin$plantID<- as.factor(fin$plantID)
fin$familyID<- as.factor(fin$familyID)</pre>
```

Setting up for aster analyses

Load aster package (make sure you have most current version)

```
library(aster)
```

Begin by naming variables that will be used in the graphical model of the aster analyses:

 ${f flw}$ - total number of flowers produced ${f frt}$ - total number of fruits produced ${f frt.2}$ - subsetted number of fruits collected ${f seeds}$ - total number of seeds collected from subsetted fruits

```
vars<- c( "flw", "frt", "frt.2", "seeds")</pre>
```

Reshape the data so that all response variables are located in a single vector, in a new data set called "redata"

```
redata <- reshape(fin, varying = list(vars), direction = "long",timevar = "varb", times = as.factor(var</pre>
```

Designate the terminal fitness variable "seeds" (make it numberic), and then add it to the reshaped data

```
fit <- grepl("seeds", as.character(redata$varb))
fit<- as.numeric(fit)
redata$fit <- fit</pre>
```

Check

```
with(redata, sort(unique(as.character(varb)[fit == 0])))
```

```
## [1] "flw" "frt" "frt.2"
with(redata, sort(unique(as.character(varb)[fit == 1])))
```

```
## [1] "seeds"
```

Add a variable "root" to redata, where value is 1. This is the "starting point" of the aster graphical model (i.e. a seed planted)

```
redata<- data.frame(redata, root=1)
```

Set up the graphical model and designate the statistical distribution for each node. This graphical model has four nodes (in object pred) described earlier. Statistical family for each node is described by object fam.

```
pred<- c(0,1,2,3)
fam<- c(1,2,2,2)
```

Show distribution family for each node

```
sapply(fam.default(), as.character)[fam]
```

```
## [1] "bernoulli" "poisson" "poisson" "poisson"
```

Main Aster Analyses for Female Fitness (Seeds set)

First aster analysis with only fitness data. Note, aster reads the redata version of the data.

```
aout<- aster(resp~varb, pred, fam, varb, id, root, data=redata)
aout1<- aster(resp~varb + fit:(familyID), pred, fam, varb, id, root, data=redata)
aout2<- aster(resp~varb + fit:(familyID + Gen), pred, fam, varb, id, root, data=redata)
aout3<- aster(resp~varb + fit:(familyID + Gen + Den), pred, fam, varb, id, root, data=redata)</pre>
```

```
aout4<- aster(resp~varb + fit:(familyID + Gen + Den + Gen*Den), pred, fam, varb, id, root, data=redata
aout5<- aster(resp~varb + fit:(familyID + Gen + Den + Gen*Den + mass.a) , pred, fam, varb, id, root, da
anova(aout, aout1, aout2, aout3, aout4, aout5)
## Analysis of Deviance Table
##
## Model 1: resp ~ varb
## Model 2: resp ~ varb + fit:(familyID)
## Model 3: resp ~ varb + fit:(familyID + Gen)
## Model 4: resp ~ varb + fit:(familyID + Gen + Den)
## Model 5: resp ~ varb + fit:(familyID + Gen + Den + Gen * Den)
## Model 6: resp ~ varb + fit:(familyID + Gen + Den + Gen * Den + mass.a)
     Model Df Model Dev Df Deviance P(>|Chi|)
## 1
           4
                132606
## 2
           15
                 132996 11
                             389.52 < 2.2e-16 ***
## 3
          16
                133274 1
                            277.97 < 2.2e-16 ***
## 4
          18
                133816 2
                            542.55 < 2.2e-16 ***
## 5
          20
                133935 2
                            118.54 < 2.2e-16 ***
## 6
          21
                134028 1
                             93.14 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Interpretation

Sequential addition of familyID, Gen (Ne), Den (density), Gen * Den (Gen by Den interaction), and finally mass.a (above ground biomass) consistently explained more variation in total lifetime fitness. Next, move on to specific models to estimate fitness across treatments.

First, isloate high (HG) and low (LG) data from the main redata file, and drop unused levels. Therefore, don't have to do "reshape" data step. $HG/hg = High N_e$, $LG/lg = Low N_e$

```
redataHG<- subset(redata, Gen=="HG")
redataLG<- subset(redata, Gen=="LG")

redataHG<- droplevels(redataHG)
redataLG<- droplevels(redataLG)</pre>
```

Perform aster analysis on HG and LG data with just fitness data (no predictors), then add Den and perform a liklihood ratio test.

```
aoutHG<- aster(resp~varb, pred, fam, varb, id, root, data=redataHG)
aoutHG2<- aster(resp~varb + fit:(familyID), pred, fam, varb, id, root, data=redataHG)
aoutHG3<- aster(resp~varb + fit:(familyID + Den), pred, fam, varb, id, root, data=redataHG)
aoutHG4<- aster(resp~varb + fit:(familyID + Den + mass.a), pred, fam, varb, id, root, data=redataHG)
anova(aoutHG, aoutHG2, aoutHG3, aoutHG4)</pre>
```

```
## Analysis of Deviance Table
##
## Model 1: resp ~ varb
## Model 2: resp ~ varb + fit:(familyID)
## Model 3: resp ~ varb + fit:(familyID + Den)
## Model 4: resp ~ varb + fit:(familyID + Den + mass.a)
```

```
Model Df Model Dev Df Deviance P(>|Chi|)
## 1
           4
                 89573
## 2
          13
                 90086 9
                            512.72 < 2.2e-16 ***
## 3
          15
                 90599 2
                            513.25 < 2.2e-16 ***
## 4
          16
                 90785 1
                            185.98 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
summary(aoutHG4, show.graph=T, info.tol = 1e-9)
##
## Call:
## aster.formula(formula = resp ~ varb + fit:(familyID + Den + mass.a),
      pred = pred, fam = fam, varvar = varb, idvar = id, root = root,
##
      data = redataHG)
##
##
## Graphical Model:
## variable predecessor family
## flw
            root
                        bernoulli
## frt
            flw
                        poisson
## frt.2
            frt
                        poisson
## seeds
            frt.2
                        poisson
##
                   Estimate Std. Error z value Pr(>|z|)
                 -3.623e+01 8.223e-01 -44.060 < 2e-16 ***
## (Intercept)
## varbfrt
                  4.078e+01 8.334e-01 48.933 < 2e-16 ***
## varbfrt.2
                  2.529e+01 8.208e-01 30.808 < 2e-16 ***
## varbseeds
                  3.863e+01 8.226e-01 46.960 < 2e-16 ***
## fit:familyID1
                 5.225e-02 8.080e-03
                                         6.466 1.01e-10 ***
## fit:familyID2
                 6.449e-02 7.678e-03
                                         8.400 < 2e-16 ***
## fit:familyID3
                  2.464e-02 1.174e-02
                                        2.099 0.03585 *
## fit:familyID4 -7.718e-02 1.915e-02 -4.030 5.57e-05 ***
## fit:familyID6 -4.465e-02 1.684e-02 -2.651 0.00802 **
## fit:familyID7
                 6.854e-02 8.245e-03
                                        8.313 < 2e-16 ***
                 1.093e-01 8.229e-03 13.287 < 2e-16 ***
## fit:familyID8
## fit:familyID9
                  2.414e-02 9.139e-03
                                         2.641 0.00827 **
## fit:familyID11 6.367e-02 7.656e-03
                                         8.317
                                               < 2e-16 ***
## fit:DenL
                 -1.268e-01 6.418e-03 -19.755 < 2e-16 ***
## fit:DenM
                 -3.788e-02 3.688e-03 -10.273 < 2e-16 ***
                 -2.000e-03 1.692e-04 -11.819 < 2e-16 ***
## fit:mass.a
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Original predictor variables dropped (aliased)
       fit:familyID14
Perform same sequence of analyses on LG dataset
aoutLG<- aster(resp~varb, pred, fam, varb, id, root, data=redataLG)
aoutLG2<- aster(resp~varb + fit:(familyID), pred, fam, varb, id, root, data=redataLG)
aoutLG3<- aster(resp~varb + fit:(familyID + Den), pred, fam, varb, id, root, data=redataLG)
aoutLG4<- aster(resp~varb + fit:(familyID + Den + mass.a), pred, fam, varb, id, root, data=redataLG)
anova(aoutLG, aoutLG2, aoutLG3, aoutLG4)
```

```
## Analysis of Deviance Table
##
## Model 1: resp ~ varb
## Model 2: resp ~ varb + fit:(familyID)
## Model 3: resp ~ varb + fit:(familyID + Den)
## Model 4: resp ~ varb + fit:(familyID + Den + mass.a)
    Model Df Model Dev Df Deviance P(>|Chi|)
## 1
                 43589
           4
## 2
          13
                 43633 9
                            44.179 1.308e-06 ***
## 3
          15
                            92.203 < 2.2e-16 ***
                 43725 2
## 4
          16
                 43727 1
                             1.989
                                      0.1585
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
summary(aoutLG4, show.graph = T, info.tol = 1e-8)
##
## Call:
## aster.formula(formula = resp ~ varb + fit:(familyID + Den + mass.a),
##
      pred = pred, fam = fam, varvar = varb, idvar = id, root = root,
##
      data = redataLG)
##
##
## Graphical Model:
## variable predecessor family
## flw
            root
                        bernoulli
## frt
            flw
                        poisson
## frt.2
            frt
                        poisson
## seeds
            frt.2
                        poisson
##
                   Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                 -3.898e+01 8.207e-01 -47.487 < 2e-16 ***
## varbfrt
                  4.351e+01 8.334e-01 52.203 < 2e-16 ***
## varbfrt.2
                  2.984e+01 8.228e-01 36.265
                                                < 2e-16 ***
## varbseeds
                  4.116e+01 8.204e-01 50.174
                                               < 2e-16 ***
                  6.275e-03 8.761e-03
## fit:familyID1
                                         0.716
                                                0.4738
## fit:familyID2
                  2.985e-02 1.449e-02
                                         2.061
                                                 0.0393 *
## fit:familyID3 -2.516e-02 1.388e-02 -1.813
                                                0.0698 .
                  5.232e-03 8.770e-03
                                                 0.5508
## fit:familyID7
                                        0.597
## fit:familyID8 -2.565e-02 1.397e-02 -1.836
                                                 0.0663 .
## fit:familyID9
                  1.646e-02 8.517e-03
                                         1.932
                                                 0.0533 .
## fit:familyID10 -3.130e-02 1.381e-02 -2.267
                                                 0.0234 *
## fit:familyID11 1.015e-01 1.323e-02
                                        7.670 1.72e-14 ***
## fit:familyID13 -7.711e-02 1.759e-02 -4.384 1.17e-05 ***
## fit:DenL
                 -7.115e-02 1.024e-02 -6.947 3.73e-12 ***
                                                 0.5758
## fit:DenM
                 -4.016e-03 7.178e-03 -0.559
## fit:mass.a
                  3.282e-04 2.252e-04
                                        1.457
                                                 0.1451
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Original predictor variables dropped (aliased)
       fit:familyID14
##
```

Interpretation

1

Η

418.02778

Interestingly, the addition of mass.a explains significantly more variation in only the high $N_{\rm e}$ treatments. Now generate estimates of fitness (female function - seeds set) for both high and low $N_{\rm e}$.

```
pout.HG<- predict(aoutHG4, se.fit=TRUE, info.tol = 1e-9)</pre>
pout.LG<- predict(aoutLG4, se.fit=TRUE, info.tol = 1e-8)</pre>
Playing with predicted values
f<- pout.HG$fit
f<- as.data.frame(f)</pre>
dim(f)
## [1] 432
se<- pout.HG$se.fit
se<- as.data.frame(se)</pre>
dim(se)
## [1] 432
flw.se<- as.data.frame(se$se[1:108])
frt.se<- as.data.frame(se$se[109: 216])</pre>
frt2.se<- as.data.frame(se$se[217:324])</pre>
seeds.se<- as.data.frame(se$se[325:432])</pre>
nodes.se<- cbind(flw.se, frt.se, frt2.se, seeds.se)</pre>
colnames(nodes.se)<- c("flw.se", "frt.se", "frt2.se", "seeds.se")</pre>
hg<- subset(fin, Gen=="HG")
ex.hg<- hg[c("Treat", "familyID", "plotID", "Den")]</pre>
flw.n < -as.data.frame(f f[1:108])
frt.n<- as.data.frame(f$f[109: 216])</pre>
frt2.n<- as.data.frame(f$f[217:324])</pre>
seeds.n<- as.data.frame(f$f[325:432])
nodes<- cbind(flw.n, frt.n, frt2.n, seeds.n)</pre>
colnames(nodes)<- vars</pre>
fit.hg<- cbind(ex.hg, nodes, nodes.se)</pre>
female.fit<- aggregate(fit.hg$seeds, by=list(fit.hg$Den), mean)</pre>
female.se<- aggregate(fit.hg$seeds.se, by=list(fit.hg$Den), mean)</pre>
colnames(female.fit)<- c("Density", "Female.Fitness")</pre>
colnames(female.se)<- c("Density", "SE")</pre>
female.fit
    Density Female.Fitness
```

```
## 2
                    57.83333
## 3
                    180.58333
female.se
##
     Density
## 1
           Н 39.029146
           L 6.429881
## 2
           M 16.527467
## 3
Try the old way until the second 'predict' statement
hg<- subset(fin, Gen=="HG")
hg<- droplevels(hg)
fred.hg <- data.frame( familyID=hg$familyID, Den=hg$Den, mass.a=hg$mass.a, flw=1, frt=1,frt.2=1, seeds=
lg<-subset(fin, Gen=="LG")</pre>
fred.lg <- data.frame( familyID=lg$familyID, Den=lg$Den, mass.a=lg$mass.a, flw=1, frt=1,frt.2=1, seeds=
Reshape the design matrix just as the actual data
renewdata.hg <- reshape(fred.hg, varying = list(vars),</pre>
                       direction = "long", timevar = "varb",
                       times = as.factor(vars), v.names = "resp")
renewdata.lg <- reshape(fred.lg, varying = list(vars),</pre>
                          direction = "long", timevar = "varb",
                          times = as.factor(vars), v.names = "resp")
Make character string from "varb" of renewdata without actual values (i.e., the layers of varb in renewdata),
and add it to each renewdata object
layer<- gsub("[0-9]", "", as.character(renewdata.hg$varb))</pre>
renewdata.hg<- data.frame(renewdata.hg, layer= layer)
renewdata.lg<- data.frame(renewdata.lg, layer= layer)</pre>
Add "seeds" in new layer column of renewdata as numeric, called fit Note: only need one fit object as it is
the same for both High and Low N<sub>e</sub> data, and add to each renew data file
```

```
fit<- as.numeric(layer=="seeds")
renewdata.hg<- data.frame(renewdata.hg, fit = fit)
renewdata.lg<- data.frame(renewdata.lg, fit = fit)</pre>
```

Rerun prediction of aster analyses, with the reshaped design matrices

Now isolate nodes and se for HG analysis

```
f<- pout.hg$fit
f<- as.data.frame(f)</pre>
dim(f)
## [1] 432
se<- pout.hg$se.fit
se<- as.data.frame(se)</pre>
dim(se)
## [1] 432
flw.se<- as.data.frame(se$se[1:108])
frt.se<- as.data.frame(se$se[109: 216])</pre>
frt2.se<- as.data.frame(se$se[217:324])</pre>
seeds.se<- as.data.frame(se$se[325:432])</pre>
nodes.se<- cbind(flw.se, frt.se, frt2.se, seeds.se)</pre>
colnames(nodes.se)<- c("flw.se", "frt.se", "frt2.se", "seeds.se")</pre>
ex.hg<- hg[c("Treat", "familyID", "plotID", "Den", "mass.a")]</pre>
flw.n < -as.data.frame(f f[1:108])
frt.n<- as.data.frame(f$f[109: 216])</pre>
frt2.n<- as.data.frame(f$f[217:324])</pre>
seeds.n<- as.data.frame(f$f[325:432])</pre>
nodes<- cbind(flw.n, frt.n, frt2.n, seeds.n)</pre>
colnames(nodes)<- vars</pre>
fit.hg<- cbind(ex.hg, nodes, nodes.se)</pre>
female.fit<- aggregate(fit.hg$seeds, by=list(fit.hg$Den), mean)</pre>
female.se<- aggregate(fit.hg$seeds.se, by=list(fit.hg$Den), mean)</pre>
colnames(female.fit)<- c("Density", "Female.Fitness")</pre>
colnames(female.se)<- c("Density", "SE")</pre>
female.fit
##
     Density Female.Fitness
## 1
           Η
                   418.02778
## 2
            L
                    57.83333
## 3
                   180.58333
female.se
## Density
                     SE
## 1
      Н 39.029146
## 2
          L 6.429881
## 3
          M 16.527467
```

Now isolate nodes and se for LG analysis

```
f<- pout.lg$fit
f<- as.data.frame(f)
dim(f)
## [1] 432
se<- pout.lg$se.fit</pre>
se<- as.data.frame(se)</pre>
dim(se)
## [1] 432
flw.se<- as.data.frame(se$se[1:108])
frt.se<- as.data.frame(se$se[109: 216])</pre>
frt2.se<- as.data.frame(se$se[217:324])</pre>
seeds.se<- as.data.frame(se$se[325:432])</pre>
nodes.se<- cbind(flw.se, frt.se, frt2.se, seeds.se)</pre>
colnames(nodes.se)<- c("flw.se", "frt.se", "frt2.se", "seeds.se")</pre>
ex.lg<- lg[c("Treat", "familyID", "plotID", "Den", "mass.a")]</pre>
flw.n<- as.data.frame(f$f[1:108])</pre>
frt.n<- as.data.frame(f$f[109: 216])</pre>
frt2.n<- as.data.frame(f$f[217:324])</pre>
seeds.n<- as.data.frame(f$f[325:432])
nodes<- cbind(flw.n, frt.n, frt2.n, seeds.n)</pre>
colnames(nodes)<- vars</pre>
fit.lg<- cbind(ex.lg, nodes, nodes.se)</pre>
female.fit<- aggregate(fit.lg$seeds, by=list(fit.lg$Den), mean)</pre>
female.se<- aggregate(fit.lg$seeds.se, by=list(fit.lg$Den), mean)</pre>
colnames(female.fit)<- c("Density", "Female.Fitness")</pre>
colnames(female.se)<- c("Density", "SE")</pre>
female.fit
##
     Density Female.Fitness
## 1
         Η
                   122.91666
## 2
           L
                    67.86112
## 3
           М
                   102.75000
female.se
## Density
## 1 H 14.72894
## 2
          L 12.05069
## 3
         M 12.60316
```