

**Computer Lab Week 4**

1.
  - (a) Generate 100 iid  $\text{Unif}(0,1)$  (use `runif`) random variables and store them in `u`. Apply the function  $-\log(1-u)$  to each element, and store the results in `x`.
  - (b) Plot the histogram of `x` and overlay it with the density curve of  $\text{exponential}(1)$  (use `dexp(x,rate=1)`). Why do we have good agreement here? (Hint:  $-\log(1-u)$  is the inverse function of the c.d.f. of  $\text{exponential}(1)$ .)
2. Transformation of random variables.
  - (a) Generate 100 random variables from a  $t$  distribution with 5 degrees of freedom (use `rt(100,df=5)`). Store them in `t`. Make another vector `f` by `f <- t^2`. Overlay the histogram of `f` with the density curve of a  $F_{1,5}$  distribution (use `df(x, df1=1, df2=5)`). Comment on the plot.
  - (b) Generate 100 random variables from a  $F_{5,2}$  distribution (use `rf(100, df1=5, df2=2)`). Store them in `y`. Make another vector `w <- 1/y`. Overlay the histogram of `w` with the density curve of a  $F_{2,5}$  distribution. Comment on the plot.
  - (c) Generate 100 random variables from a  $\text{beta}(2,1)$  distribution (use `rbeta(100, shape1=2, shape2=1)`). Store them in `z`. Make another vector `v <- 2*z/(4*(1-z))`. Overlay the histogram of `v` with the density curve of a  $F_{4,2}$  distribution. Comment on the plot.