

Pre-lab Questions

Question 1

An audio signal $y(t)$ is sampled with $f_s=32$ kHz. What sampling period does that correspond to? If you mistakenly play the signal with $f_s=16$ kHz, will it be shorter or longer than the original? How else will it sound different?

Answer:

The sampling period is the inverse of the sampling frequency (f_s).

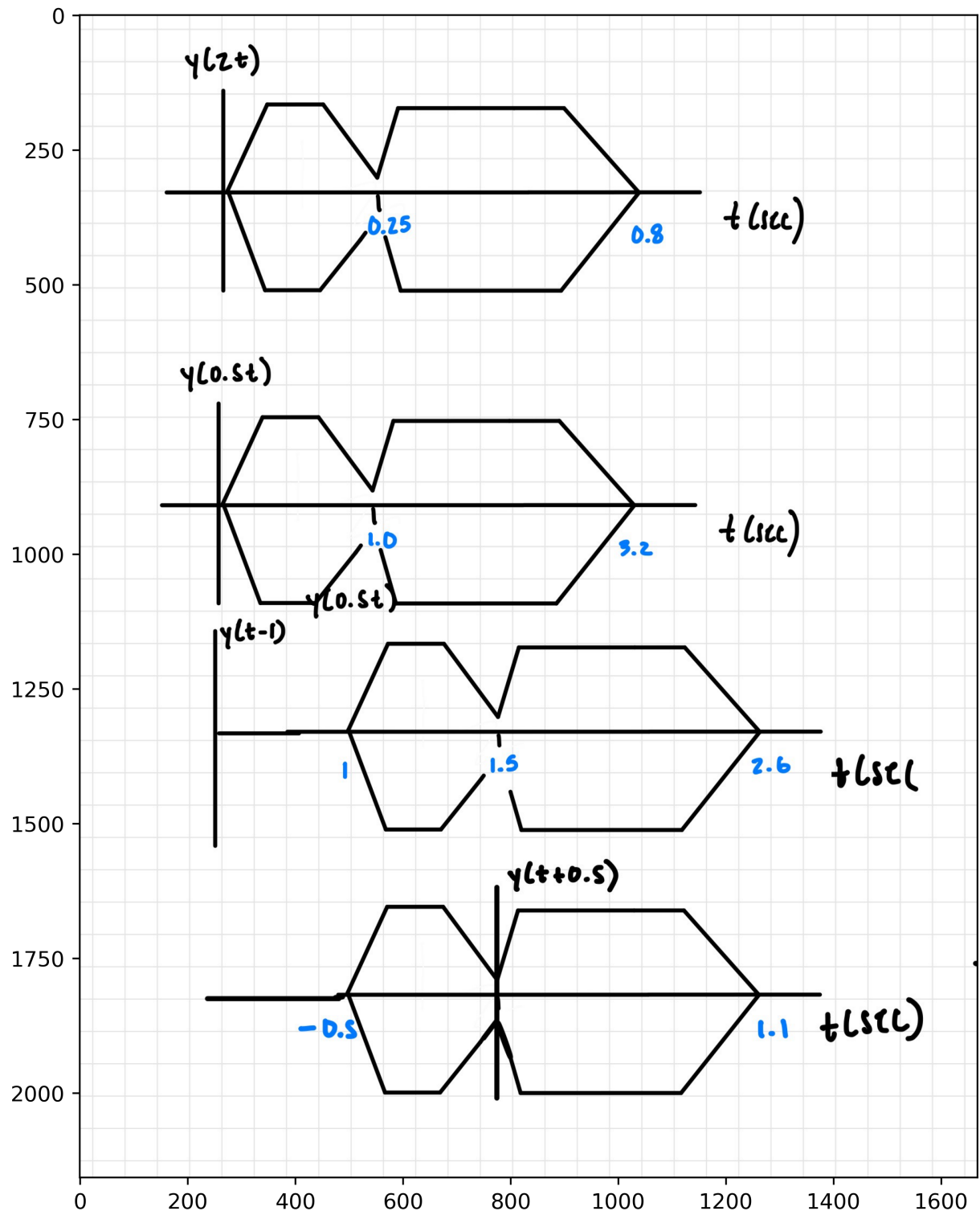
Sampling period (T) = $1/f_s = 1/32000 = 31.25 \mu\text{s}$

If you mistakenly play the signal with $f_s=16$ kHz, it will be longer than the original. The duration will be doubled, as the sampling rate is halved. The sound will also be different, with a lower pitch, as the frequency content of the signal will be stretched out.

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In [ ]: # the answer is stored in PreLabP2.jpg
        # Use python to display the image

import matplotlib.pyplot as plt
import matplotlib.image as mpimg
import numpy as np

plt.figure(figsize=(10,10), dpi=400)
img = mpimg.imread('PreLabP2.jpg')
plt.imshow(img)
plt.show()
```



Question 3

When the signal is digitized, you need to implement the time shift in terms of the number of samples: $y[n-n_1]$ and $y[n+n_2]$. Find n_1 and n_2 (corresponding to $t_1=1$ and $t_2=0.5$, respectively) for the case when $f_s=32\text{kHz}$.

Answer:

For $f_s = 32\text{ kHz}$, the time shifts are $t_1 = 1\text{ s}$ and $t_2 = 0.5\text{ s}$.

$$n_1 = t_1 f_s = 1 \cdot 32,000 = 32,000 \text{ samples} \quad n_2 = t_2 f_s = 0.5 \cdot 32,000 = 16,000 \text{ samples}$$

Question 4

On a computer, we may have the constraint of keeping the time window fixed. Assuming the time window is constrained to be $[0, 3]$ sec, which of the time transformations in part 1 will require you to throw away some of the transformed signal? If you were to implement $y(t) = x(2(t+1.5))$ with a fixed time window, would it be better to scale first or shift first, or does it not matter?

Answer:

For a fixed time window of $[0, 3]$ seconds, any time transformation that extends the signal outside this window would require us to throw away some of the transformed signal. In this case, the transformation $y(t) = x(2(t+1.5))$ involves both scaling and shifting.

To determine if it's better to scale first or shift first, we can analyze both options:

- Scaling first ($y(t) = x(2t)$): The signal is compressed along the time axis, fitting within the $[0, 3]$ seconds window.
- Shifting after scaling ($y(t) = x(2t+1.5)$): The signal is shifted by 1.5 seconds. Since the scaled signal is shorter, it still fits within the $[0, 3]$ seconds window.
- Shifting first ($y(t) = x(t+1.5)$): The signal is shifted by 1.5 seconds, extending beyond the $[0, 3]$ seconds window.
- Scaling after shifting ($y(t) = x(2(t+1.5))$): The signal is compressed along the time axis, fitting within the $[0, 3]$ seconds window.

Considering both options, it doesn't matter if you scale first or shift first. In both cases, the transformed signal fits within the fixed time window of $[0, 3]$ seconds.