Lasso Regularization, Logistic Regression, and Random Forest

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Logistic Regression

We are working with the "bank-additional-full.csv" dataset. In order to select which features matter the most, we will use Lasso Regularization on our Logistic Regression Model.

The equation for Logistic Regression is:

```
P = \frac{e^{\beta_0 + \beta_1 X}}{1 + e^{\beta_0 + \beta_1 X}}
```

[1] 28831

21

Where P is our target variable which varies from 0 to 1, and the β_0 , β_1 , and X are the independent Variables.

Or similarly, $log(\frac{p_i}{1-p_i}) = \beta_0 + \beta_1 X_1 + \beta_2 X_2 ... \beta_k X_k$ Where $log(\frac{p_i}{1-p_i})$ is the Log Likelihood.

We first index the data into a Training Set and a Testing Set using the sample function.

```
library(glmnet)
## Loading required package: Matrix
## Loaded glmnet 4.0-2
library(tidyr)
## Attaching package: 'tidyr'
## The following objects are masked from 'package:Matrix':
##
##
       expand, pack, unpack
library(ggplot2)
library(data.table)
library(gbm)
## Loaded gbm 2.1.8
library(class)
library(glmnet)
set.seed(1)
#Load Data
setwd("/Users/masondelrio/Desktop/Fall 2020 Files/Fall 2020 Handouts/STA 141A/STA 141A Datasets")
bank.data = read.csv("bank-additional-full.csv", sep = ";")
index = sample(1:nrow(bank.data), 0.7*nrow(bank.data))
train = bank.data[index,]
test = bank.data[-index,]
dim(train)
```

dim(test)

```
## [1] 12357 21
```

As we can see, 70% of our data was split for indexing to our training and testing data.

```
28831/41188 = 0.69999854
```

We now have our data split up, randomly, most importantly, and we can fit our logistic model to the training data using the glm() function.

```
glm_model <- glm(y~., family = binomial, data = train)
glm_model</pre>
```

```
##
##
  Call:
          glm(formula = y ~ ., family = binomial, data = train)
##
  Coefficients:
                     (Intercept)
                                                              age
                      -2.592e+02
                                                       -5.202e-04
##
                  jobblue-collar
                                                 jobentrepreneur
##
##
                      -2.230e-01
                                                       -1.544e-01
                    jobhousemaid
                                                   jobmanagement
                                                       -3.910e-02
##
                      -1.330e-01
##
                      jobretired
                                                jobself-employed
                       1.840e-01
                                                       -1.270e-01
##
                                                       jobstudent
##
                     jobservices
##
                      -1.110e-01
                                                        1.575e-01
##
                   jobtechnician
                                                   jobunemployed
##
                      -3.973e-03
                                                       -1.252e-01
##
                      jobunknown
                                                  maritalmarried
##
                      -2.090e-01
                                                        3.441e-02
##
                                                  maritalunknown
                   maritalsingle
##
                       4.207e-02
                                                        1.514e-01
##
               educationbasic.6y
                                               educationbasic.9y
##
                      -1.325e-02
                                                       -1.003e-02
                                             educationilliterate
##
           educationhigh.school
                       3.500e-02
                                                        1.484e+00
   {\tt education professional.course}
                                     educationuniversity.degree
##
##
                       4.533e-02
                                                        1.207e-01
##
                educationunknown
                                                  defaultunknown
                       1.078e-01
                                                       -3.288e-01
##
                                                  housingunknown
##
                      defaultyes
                                                       -6.708e-02
##
                      -7.295e+00
##
                      housingyes
                                                     loanunknown
##
                      -1.777e-02
##
                         loanyes
                                                contacttelephone
                                                      -7.356e-01
##
                      -8.333e-02
##
                        monthaug
                                                         monthdec
##
                       7.636e-01
                                                        4.606e-01
##
                        monthjul
                                                        monthjun
                       5.486e-02
                                                       -5.818e-01
##
##
                        monthmar
                                                         monthmay
                       1.992e+00
                                                       -4.789e-01
##
##
                        monthnov
                                                        monthoct
                      -5.174e-01
                                                        1.576e-01
##
```

```
##
                                                  day_of_weekmon
                        monthsep
                       4.115e-01
##
                                                      -1.396e-01
                                                  day_of_weektue
##
                  day of weekthu
##
                       2.131e-02
                                                       8.368e-02
                  day_of_weekwed
##
                                                        duration
                       1.997e-01
                                                       4.651e-03
##
                                                           pdays
##
                        campaign
##
                      -3.827e-02
                                                      -1.272e-03
##
                        previous
                                            poutcomenonexistent
##
                      -1.137e-01
                                                       3.566e-01
##
                poutcomesuccess
                                                    emp.var.rate
##
                       6.784e-01
                                                      -1.777e+00
##
                                                   cons.conf.idx
                  cons.price.idx
                                                       3.016e-02
##
                       2.340e+00
##
                       euribor3m
                                                     nr.employed
##
                       2.543e-01
                                                       7.329e-03
##
## Degrees of Freedom: 28830 Total (i.e. Null); 28778 Residual
## Null Deviance:
                         20360
## Residual Deviance: 12010
                                  AIC: 12110
```

In order to see how accurate our model is, we need to set up a confusion matrix. We use the test data that was separate from the training model in order to simulate some form of real world implementation and feed it into the predict.glm() function.

```
glm_prob <- predict.glm(glm_model, test, type = "response")</pre>
## Warning in predict.lm(object, newdata, se.fit, scale = 1, type = if (type == :
## prediction from a rank-deficient fit may be misleading
glm predict<- rep("no", nrow(test))</pre>
glm_predict[glm_prob>.5] <- "yes"</pre>
table(pred=glm_predict, true = test$y)
##
##
  pred
             no
                  yes
##
         10705
                  793
     no
           274
                  585
     yes
mean(glm_predict == test$y)
```

[1] 0.9136522

The Logistic Regression model works fairly well for the test data, with 91.3% accuracy. This is a model that works well with the data that was randomized and set once, for training and testing purposes. However, we must use K-Fold Cross Validation in order to test the model's ability to predict outside data not used in the process of creating this model.

Logistic Regression with K-Fold Cross Validation

We will use the caret library to implement cross validation. Below, we will again create a training and testing set for the data. However, this time the K-Fold Cross Validation will randomly select portions of the training data 10 times.

```
bank = read.csv("bank-additional-full.csv", sep = ";")
#Install caret function
library(caret)
```

```
## Loading required package: lattice
require(dplyr)
## Loading required package: dplyr
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:data.table':
##
##
       between, first, last
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
       intersect, setdiff, setequal, union
#Partition Data: Create index matrix of selected values
set.seed(1)
# Create index matrix
bank = na.omit(bank)
# data preparation
bank <- bank %% mutate(marital = ifelse(as.character(marital) =="married", 1, 0))
bank <- bank %>% mutate(housing = ifelse(as.character(housing) =="yes", 1, 0))
bank <- bank %>% mutate(loan = ifelse(as.character(loan) =="yes", 1, 0))
bank <- bank %>% mutate(y = ifelse(as.character(y) =="yes", 1, 0))
bank$job <- as.numeric(factor(bank$job, levels = as.character(unique(bank$job))))
bank$education <- as.numeric(factor(bank$education, levels = as.character(unique(bank$education))))
bank$default <- as.numeric(factor(bank$default, levels = as.character(unique(bank$default))))
bank$contact <- as.numeric(factor(bank$contact, levels = as.character(unique(bank$contact))))</pre>
bank$month <- as.numeric(factor(bank$month, levels = as.character(unique(bank$month))))
bank$day_of_week <- as.numeric(factor(bank$day_of_week, levels = as.character(unique(bank$day_of_week))
bank$poutcome <- as.numeric(factor(bank$poutcome, levels = as.character(unique(bank$poutcome))))</pre>
#Don't want list, we get a matrix.
index <- createDataPartition(bank$y, p = .7, list = FALSE, times = 1)</pre>
#Convert Dataframe bank to actual df
bank <- as.data.frame(bank)</pre>
# create train dataframe and test dataframe
train_df <- bank[index,]</pre>
test_df <- bank[-index,]</pre>
#Relabel values of y to factor (1 = yes, 0 = no), because Logistic Regression needs factors for the out
train_df$y[train_df$y == 1] <- "yes"</pre>
train_df$y[train_df$y == 0] <- "no"</pre>
test_df\$y[test_df\$y == 1] \leftarrow "yes"
test_df$y[test_df$y == 0] <- "no"</pre>
#Convert outcome variable to type factor with function as.factor()
```

After the cross validation is done, we need to see how well our improved model performs on test data. We use the predict() function to store the predictions generated by our model in predictions.

```
#Predict outcome using trained model with test data.
predictions <- predict(model1, newdata = test_df)</pre>
```

Now, we use the confusionMatrix() function from the caret package to generate our accuracy.

```
confusionMatrix(data = predictions, test_df$y)
```

```
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                 no
                      yes
##
             10696
                      833
          no
##
                282
                      545
          yes
##
##
                  Accuracy: 0.9098
                    95% CI: (0.9046, 0.9148)
##
##
       No Information Rate: 0.8885
       P-Value [Acc > NIR] : 5.554e-15
##
##
##
                     Kappa: 0.4482
##
    Mcnemar's Test P-Value : < 2.2e-16
##
##
               Sensitivity: 0.9743
##
##
               Specificity: 0.3955
##
            Pos Pred Value: 0.9277
##
            Neg Pred Value: 0.6590
##
                Prevalence: 0.8885
##
            Detection Rate: 0.8657
##
      Detection Prevalence: 0.9331
##
         Balanced Accuracy: 0.6849
##
##
          'Positive' Class : no
##
```

As we can see, the Logisitic Regression Model with and without cross validation has ~90-91% accuracy, but we need to add some form of bias because this model is overfit to this certain dataset. If we wanted to generalize this data to other banks in Portugal, we would need to compensate for the overfittness of this model to this dataset.

This is where Lasso Regularization comes in.

Lasso Regularization

Lasso Regularization for Logistic Regression is done by minimizing this Cost Function:

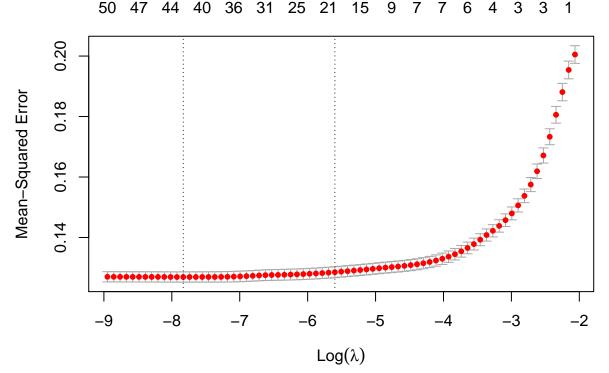
$$J(\Theta) = \frac{1}{m} \sum_{i=1}^{m} [-y^{i} log(h_{\Theta}(x^{i})) - (1-y^{i}) log(1 - (h_{\Theta}(x^{i})))] + \frac{\lambda}{2m} \sum_{j=1}^{n} |\Theta_{j}|$$

First, we build a matrix for all the features of the dataset, which we'll call x, and a vector for the response variable, we'll call y, which consists of 1's and 0's for Yes and No.

```
x <- model.matrix(y~., train)
y<- ifelse(train$y == "yes", 1,0)</pre>
```

In Lasso Regularization, there is a tuning parameter called Lambda in which we need to find the minimal value of, through cross validation. The minimum lambda will give us the most parsimonious model, but it will also generate a model which generally overfits. So we will pick the lambda which falls one standard error away from the minimum value in order to choose the simplest model without overfitting.

```
#Cross Validation for lambda parameter
cv.out <- cv.glmnet(x,y,alpha=1, family="binomial", type.measure = "mse")
#Show log plot
plot(cv.out)</pre>
```



```
#Minimum lambda
lambda_min <- cv.out$lambda.min
#Lambda value that gives simplest model but also lies within one standard error of the optimal value of
lambda_1se <- cv.out$lambda.1se</pre>
```

From this graph, we see that the lambda value between -8 and -7 will give us the most minimal model, but one standard error away from that value will give us the lambda value near -5, which will give us the minimal

```
model with the least overfitting.
```

```
lambda_min
```

[1] 0.0003969794

#Lambda value that gives simplest model but also lies within one standard error of the optimal value of lambda_1se

[1] 0.003702243

```
#Show coefficients of lassomodel
coef(cv.out, s = lambda_1se)
```

```
## 55 x 1 sparse Matrix of class "dgCMatrix"
## (Intercept)
                               46.3112124489
## (Intercept)
## age
## jobblue-collar
                              -0.1211438092
## jobentrepreneur
## jobhousemaid
## jobmanagement
                              0.0937744287
## jobretired
## jobself-employed
## jobservices
                                0.0950202311
## jobstudent
## jobtechnician
## jobunemployed
## jobunknown
## maritalmarried
## maritalsingle
## maritalunknown
## educationbasic.6y
## educationbasic.9y
## educationhigh.school
## educationilliterate
## educationprofessional.course .
## educationuniversity.degree 0.0167761111
## educationunknown
## defaultunknown
                               -0.1761173523
## defaultyes
## housingunknown
## housingyes
## loanunknown
## loanyes
## contacttelephone
                      -0.1618307419
## monthaug
## monthdec
## monthjul
## monthjun
                               0.0517527751
## monthmar
                               1.0229018486
                              -0.8062421344
## monthmay
## monthnov
                              -0.2427831094
## monthoct
                               -0.0338662302
## monthsep
```

```
## day_of_weekmon
                                 -0.0492829737
## day_of_weekthu
## day_of_weektue
## day_of_weekwed
                                  0.0221837727
## duration
                                  0.0042790778
## campaign
## pdays
                                 -0.0009976067
## previous
## poutcomenonexistent
                                  0.1642595712
## poutcomesuccess
                                  0.6431301954
## emp.var.rate
                                 -0.1796682179
## cons.price.idx
## cons.conf.idx
                                  0.0098710133
## euribor3m
## nr.employed
                                 -0.0094368591
```

From the list of coefficients for the lasso model, we see that it selected 12 features that were the most significant on the model.

We now use our test data to see how accurate our model is.

```
x_test <- model.matrix(y~., test)</pre>
lasso_prob <- predict(cv.out, newx = x_test, s = lambda_1se, type = "response")</pre>
lasso_predict<- rep("no", nrow(test))</pre>
lasso_predict[lasso_prob>.5]<- "yes"</pre>
#confusion matrix
table(pred= lasso_predict, true = test$y)
##
## pred
             no
                  yes
##
         10728
                  868
     no
##
                  510
     yes
            251
mean(lasso_predict == test$y)
```

[1] 0.909444

As we see, the accuracy of this model has decreased because we introduced some bias with the Lasso Regularization method. In order for this model to be applied to other data sets, we will sacrifice accuracy for the sake of not overfitting the model.

Random Forest

Another method we can use on this data is the Random Forest Method.

Using Random Forest gives us a vast amount of decision trees in which a model is made from the culmination of them. Using the ranodmForest library package, we can create the model in R. We first subset our data just like we previously did for the Logistic Regression model, with 70% of the data lumped into a Training Set, and 30% of our data lumped into the Test set.

```
library(randomForest) # random forest methodology

## randomForest 4.6-14

## Type rfNews() to see new features/changes/bug fixes.

##
## Attaching package: 'randomForest'
```

```
## The following object is masked from 'package:dplyr':
##
## combine

## The following object is masked from 'package:ggplot2':
##
## margin

bank.data = na.omit(bank.data)
bank.data$y = as.factor(bank.data$y)
dataset.size = floor(nrow(bank.data)*0.70)
index <- sample(1:nrow(bank.data),size= dataset.size)
training <- bank.data[index,]
test <- bank.data[-index,]</pre>
```

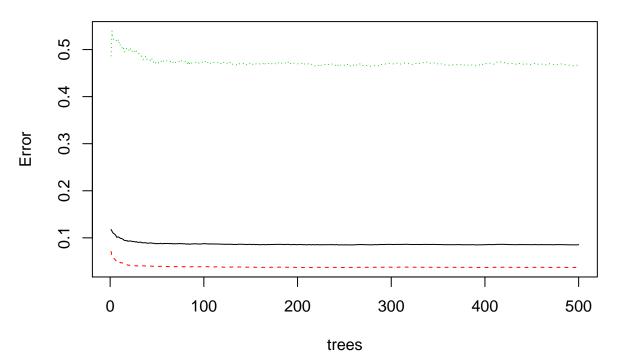
We then use the function "randomForest()" and train it with the previously created training set, which will create our random forest model to use for predictions.

```
rf <- randomForest(y~., data = training, importance = T)</pre>
```

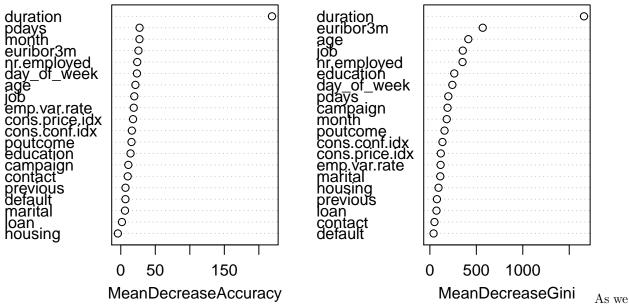
After this is made, we can plot to see how many trees are necessary for our model

```
plot(rf)
```

rf



This graph shows us that around 100-200 trees is where our model has minimum error Now, let's confirm the variables of importance for the dataset using the varImpPlot() function rf



can see, duration ranks number 1 most important variable in this dataset, which from eyeballing the data, we see the strong relationship between a phone calls duration and the result of a term deposit being made. This graph confirms this notion.

Now, let's see how accurate this model is after feeding the model our test data. We will use the caret package to create the confusion matrix.

```
library(caret)
rftest <- predict(rf, newdata = test)
confusionMatrix(data = rftest, test$y)</pre>
```

```
## Confusion Matrix and Statistics
##
##
             Reference
##
   Prediction
                  no
                       yes
                       708
##
              10587
          no
                       710
##
                 352
          yes
##
                   Accuracy : 0.9142
##
##
                     95% CI : (0.9091, 0.9191)
##
       No Information Rate: 0.8852
       P-Value [Acc > NIR] : < 2.2e-16
##
##
##
                      Kappa: 0.526
##
##
    Mcnemar's Test P-Value : < 2.2e-16
##
##
                Sensitivity: 0.9678
```

```
##
               Specificity: 0.5007
##
            Pos Pred Value : 0.9373
##
            Neg Pred Value: 0.6685
##
                Prevalence: 0.8852
            Detection Rate: 0.8568
##
##
     Detection Prevalence : 0.9141
         Balanced Accuracy: 0.7343
##
##
##
          'Positive' Class : no
##
```

From this confusion matrix, we can see that the accuracy was at 91.34%, and the Kappa value was at .52, which makes for a moderate model. This model gives us around the same accuracy as the logistic regression model.