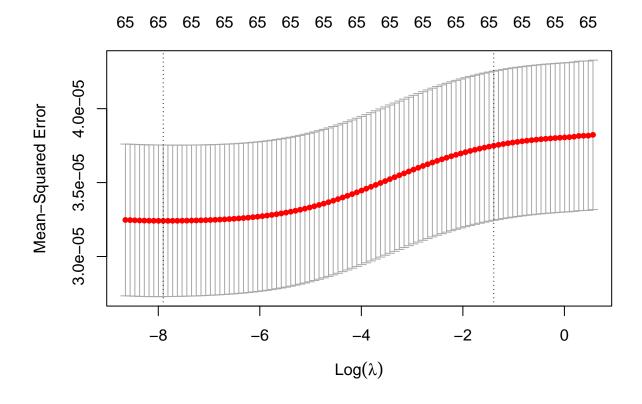
```
# install.packages("scales")
                                      # dependency of plot_glmnet
source("functions/plot_glmnet.R")
theft_train = read_csv("../data/clean/theft_train.csv")
## Rows: 1836 Columns: 69
## -- Column specification ------
## Delimiter: ","
## chr (2): county, state
## dbl (67): fips, pertrump, permale, med_age, nevermarried, widowed, fromdifst...
## i Use `spec()` to retrieve the full column specification for this data.
## i Specify the column types or set `show_col_types = FALSE` to quiet this message.
theft_test = read_csv("../data/clean/theft_test.csv")
## Rows: 457 Columns: 69
## -- Column specification --------
## Delimiter: ","
## chr (2): county, state
## dbl (67): fips, pertrump, permale, med_age, nevermarried, widowed, fromdifst...
## i Use `spec()` to retrieve the full column specification for this data.
## i Specify the column types or set `show_col_types = FALSE` to quiet this message.
```

Regression Based Methods

Ridge

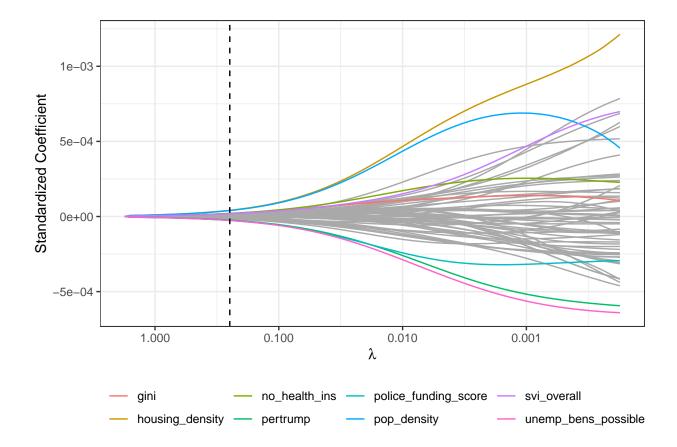
```
plot(ridge_fit)
```



plot_glmnet(ridge_fit, theft_train, features_to_plot = 8)

Table 1: Standardized coefficients for features in the Ridge model based on the one-standard-error rule.

Feature	Coefficient
housing_density pop_density no_health_ins gini svi_overall	4.110e-05 3.977e-05 2.090e-05 1.931e-05 1.887e-05
pct_child_in_pov lessthan_hs PopChangeRate1819	1.877e-05 1.665e-05 1.491e-05



lasso

```
set.seed(471) # set seed before cross-validation for reproducibility
lasso_fit = cv.glmnet(theftrate ~. -state -county -fips , alpha = 1, nfolds = 10, data = theft_train)
```

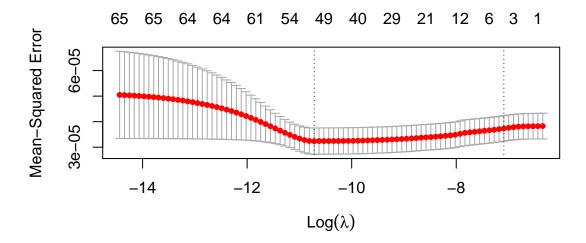


Figure 1: This is the CV plot for the 10-fold cross-validated lasso regression model on the training data.

[1] "The value of lambda based on the one-standard-error rule: 0.000834"

In Figure @ref(fig:lasso-cv-plot), we have the CV plot for a 10-fold cross-validated lasso regression model to the training data. (We can also note that corresponding to the right vertical dashed line on the plot (on the log scale), the value of lambda selected according to the one-standard-error rule is about 0.009.)

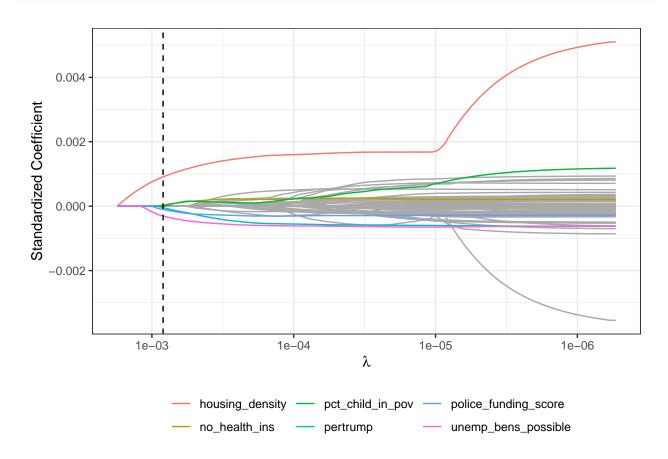
ii. How many features (excluding the intercept) are selected if lambda is chosen according to the one-standard-error rule?

[1] "The number of features (excluding intercept) selected (1se): 6"

Table 2: Standardized coefficients for features in the Lasso model based on the one-standard-error rule.

Feature	Coefficient
housing_density	0.00091026
no_health_ins	0.00003732
$\operatorname{pct_child_in_pov}$	0.00000162
pertrump	-0.00004780
police_funding_score	-0.00010290
$unemp_bens_possible$	-0.00030893

plot_glmnet(lasso_fit, theft_train)



Elastic net

Next, let's run an elastic net regression. We can do this via the cva.glmnet() function:

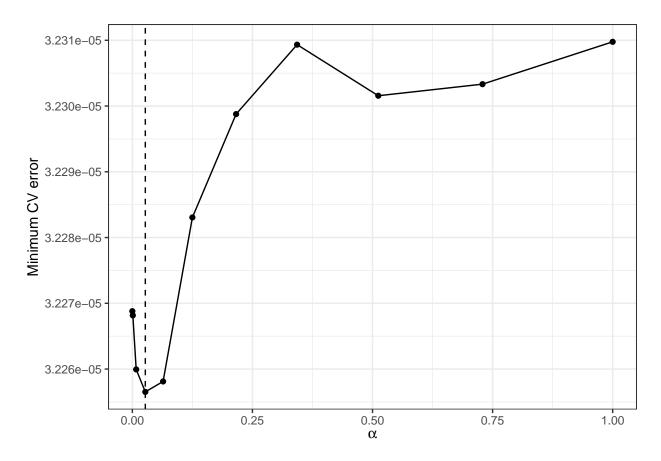
The following are the values of alpha that were used:

```
elnet_fit$alpha
```

```
## [1] 0.000 0.001 0.008 0.027 0.064 0.125 0.216 0.343 0.512 0.729 1.000
```

We can plot the minimum CV error for each value of alpha using the helper function plot_cva_glmnet() from plot_glmnet.R:

```
plot_cva_glmnet(elnet_fit)
```



We can then extract the cv.glmnet fit object based on the optimal alpha using extract_best_elnet from plot_glmnet.R:

```
elnet_fit_best = extract_best_elnet(elnet_fit)
```

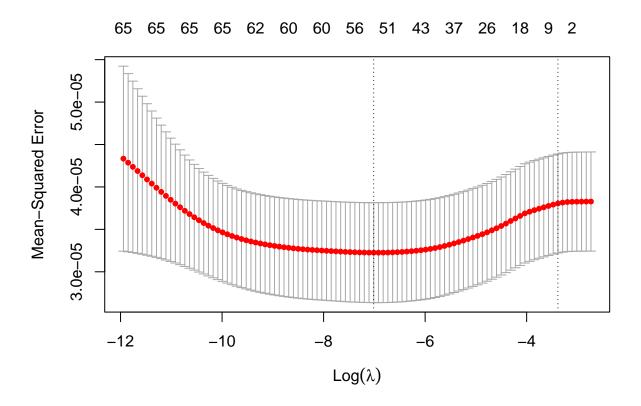
The elnet_fit_best object is a usual glmnet fit object, with an additional field called alpha specifying which value of alpha was used:

elnet_fit_best\$alpha

[1] 0.027

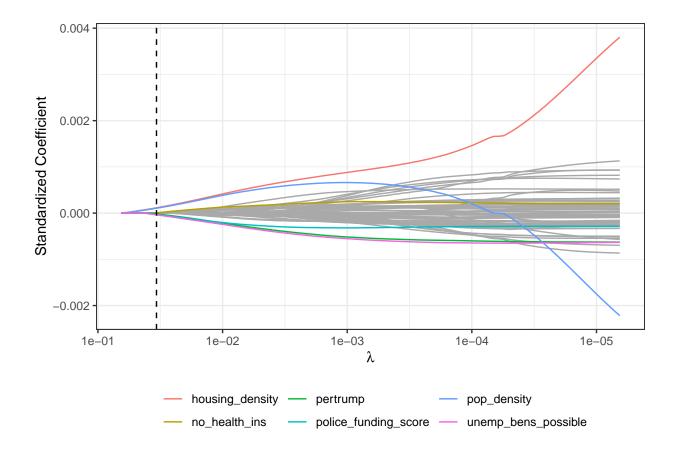
We can make a CV plot to select lambda as usual:

plot(elnet_fit_best)



And we can make a trace plot for this optimal value of alpha:

plot_glmnet(elnet_fit_best, theft_train)

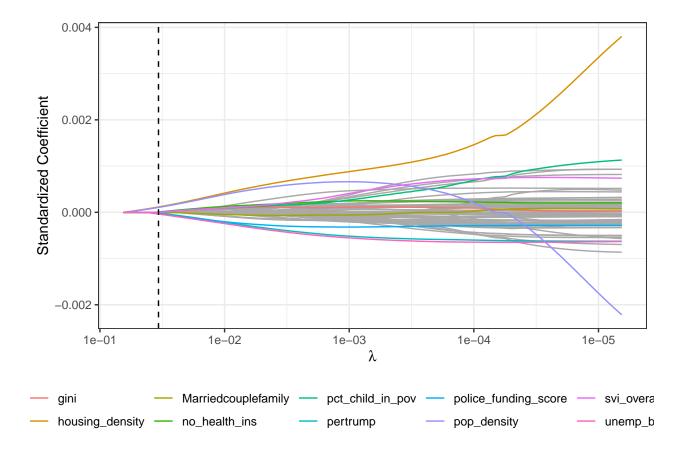


This is too many features to highlight, so let's choose a smaller number:

```
plot_glmnet(elnet_fit_best, theft_train, features_to_plot = 10)
```

Table 3: Standardized coefficients for features in the Lasso model based on the one-standard-error rule.

Feature	Coefficient
housing_density	0.00011531
pop_density	0.00010536
no_health_ins	0.00000646
pertrump	-0.00001689
police_funding_score	-0.00002962
$unemp_bens_possible$	-0.00003749

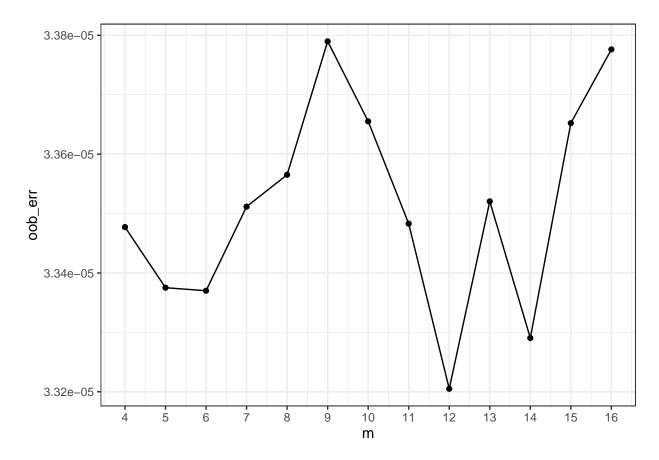


Tree based methods

random forest

```
set.seed(471) # set seed for reproducibility

mvalues = seq(4,16, by = 1)
oob_errors = numeric(length(mvalues))
ntree = 500
for(idx in 1:length(mvalues)){
    m = mvalues[idx]
    rf_fit = randomForest(theftrate ~. -fips -state - county, mtry = m, data = theft_train)
    oob_errors[idx] = rf_fit$mse[ntree]
}
tibble(m = mvalues, oob_err = oob_errors) %>%
    ggplot(aes(x = m, y = oob_err)) +
    geom_line() + geom_point() +
    scale_x_continuous(breaks = mvalues) +
    theme_bw()
```



A quick-and-dirty way to tune a random forest is to try out a few different values of mtry:

```
rf_5 = randomForest(theftrate ~. -fips -state - county, mtry = 5, data = theft_train)
rf_6 = randomForest(theftrate ~. -fips -state - county, mtry = 6, data = theft_train)
```

```
rf_12 = randomForest(theftrate ~. -fips -state - county, mtry = 12, data = theft_train)
rf_14 = randomForest(theftrate ~. -fips -state - county, mtry = 14, data = theft_train)
```

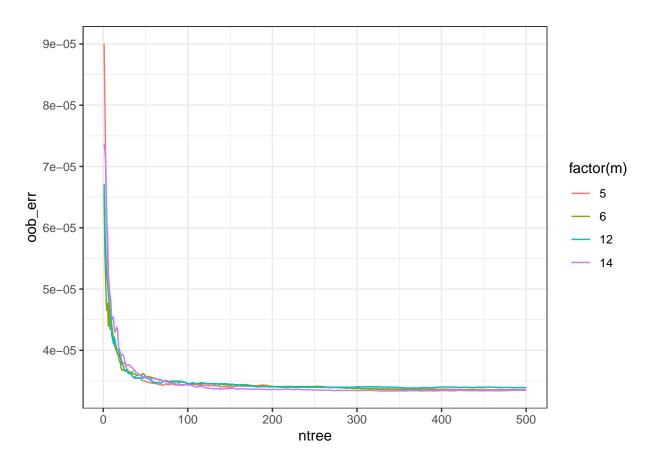
We can extract the OOB errors from each of these objects by using the mse field:

```
oob_errors2 = bind_rows(
  tibble(ntree = 1:500, oob_err = rf_5$mse, m = 5),
  tibble(ntree = 1:500, oob_err = rf_6$mse, m = 6),
  tibble(ntree = 1:500, oob_err = rf_12$mse, m = 12),
  tibble(ntree = 1:500, oob_err = rf_14$mse, m = 14),
)
oob_errors2
```

```
## # A tibble: 2,000 x 3
##
     ntree oob err
##
     <int>
               <dbl> <dbl>
##
   1
         1 0.0000900
         2 0.0000801
## 2
                         5
         3 0.0000682
                         5
## 3
## 4
         4 0.0000610
                         5
## 5
         5 0.0000595
                         5
         6 0.0000531
                         5
## 6
## 7
         7 0.0000504
                         5
         8 0.0000490
                         5
## 8
## 9
         9 0.0000481
                         5
## 10
        10 0.0000441
                         5
## # ... with 1,990 more rows
```

We can then plot these as follows:

```
oob_errors2 %>%
  ggplot(aes(x = ntree, y = oob_err, colour = factor(m))) +
  geom_line() + theme_bw()
```



```
set.seed(471) # set seed for reproducibility
rf_12 = randomForest(theftrate ~ .-fips -state -county, mtry = 12, data = theft_train, importance = TRU.
```

rf_12\$importance

```
%IncMSE IncNodePurity
##
## pertrump
                                3.268471e-06 0.0021423476
## permale
                                5.791992e-07 0.0010647745
## med_age
                                4.448595e-07 0.0007421022
## nevermarried
                                3.311118e-07 0.0008855598
## widowed
                                1.486440e-07 0.0006215402
## fromdifstate
                                2.251692e-07 0.0006548981
## fromabroad
                                5.055631e-08 0.0004622736
## divorced
                                1.220735e-06 0.0009135617
## foodstamp
                                4.599561e-07 0.0007782685
## Marriedcouplefamily
                                9.882575e-07 0.0006096238
                                2.859487e-07 0.0010440935
## single_mom
## inschool
                                7.440281e-07 0.0007791918
## inundergrad
                                1.607562e-07 0.0006266991
## ingradprofesh
                                4.481941e-07 0.0007847604
## lessthan_hs
                                1.285329e-06 0.0019144692
## bachplus
                                2.514062e-06 0.0024429584
## med_income
                                7.520443e-07 0.0006356728
## gini
                                1.705314e-07 0.0006974698
## singledad
                                7.064211e-08 0.0004742167
```

```
## withkids
                                8.160782e-07 0.0013242636
## med 2bed
                                9.932610e-07 0.0007409655
## foreignborn
                                7.705772e-07 0.0005623356
                                7.912557e-07 0.0005909172
## unemployed_rate
## employed rate
                                1.167479e-06 0.0007045857
## no health ins
                                1.617277e-06 0.0018726872
## dis5to17
                                3.538471e-07 0.0006403859
## dis18to34
                               -2.418496e-08 0.0006541598
## dis35to64
                                9.246326e-07 0.0008900862
## pop_density
                                1.667041e-06 0.0019541441
## housing_density
                                1.625485e-06 0.0024304063
## pct_all_in_pov
                                7.094815e-07 0.0011744358
## police_violence_score
                                1.915837e-07 0.0007978518
## police_accountability_score
                                4.150848e-07 0.0006533829
## approach_to_policing_score
                                3.089152e-07 0.0007761506
## police_funding_score
                                6.074883e-07 0.0017992451
## mean_hha_score
                                2.057019e-07 0.0002055870
## svi overall
                                1.842966e-06 0.0008742754
## res_seg_nonwhite_white
                                4.743153e-07 0.0008105365
## pct child in pov
                                1.605542e-06 0.0012193034
## sev_hou_cost_burden
                                3.016869e-07 0.0007918913
## sev_hou_prob
                                8.478450e-07 0.0010582980
## poor_fair_health
                                4.343328e-07 0.0016873722
## spend per capita
                                2.621906e-06 0.0010974209
## unemp_bens_possible
                                2.569956e-06 0.0025678906
## saversperhouses
                                5.221259e-07 0.0007441583
## ForeignBornEuropePct
                                5.306777e-07 0.0007536977
## ForeignBornMexPct
                                1.845339e-07 0.0005367608
## ForeignBornCaribPct
                                4.486352e-07 0.0006101083
## ForeignBornCentralSouthAmPct
                                2.041437e-07 0.0005759721
                                8.934119e-07 0.0007867626
## ForeignBornAsiaPct
## ForeignBornAfricaPct
                                2.130971e-07 0.0005704192
## AvgHHSize
                                8.468149e-07 0.0007666426
## PopChangeRate1819
                                5.920033e-07 0.0010119685
                                8.031597e-07 0.0006855051
## NonEnglishHHNum
## PctEmpChange1920
                                5.079400e-07 0.0007690777
## PctEmpConstruction
                                4.281844e-07 0.0026076394
## PctEmpMining
                                3.037590e-07 0.0007866685
## PctEmpTrade
                                7.251240e-08 0.0006374936
## PctEmpTrans
                               -1.192790e-08 0.0008641203
## PctEmpInformation
                                4.914684e-07 0.0016163770
## PctEmpFIRE
                                3.280471e-07 0.0014551722
## Deep Pov Children
                                5.235189e-07 0.0005797682
## PerCapitaInc
                                1.156042e-06 0.0013849461
## Deep_Pov_All
                                4.015176e-07 0.0005207421
## incar_rate
                                1.186708e-07 0.0005256170
```

varImpPlot(rf_12, n.var = 10)

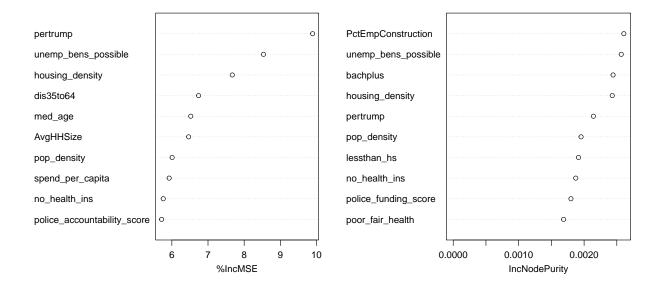


Figure 2: Variable Importance Plot for the optimal random forest model.

Boosting

Model tuning (4 points)

i. (2 points) Fit boosted tree models with interaction depths 1, 2, and 3. For each, use a shrinkage factor of 0.1, 1000 trees, and 5-fold cross-validation.

Solution:

```
shrinkage = 0.1,
              cv.folds = 5,
              data = theft_train)
set.seed(471) # for reproducibility (DO NOT CHANGE)
# TODO: Fit random forest with interaction depth 3
gbm_3 = gbm(theftrate ~ . -fips -state -county,
              distribution = "gaussian",
              n.trees = 1000,
              interaction.depth = 3,
              shrinkage = 0.1,
              cv.folds = 5,
              data = theft_train)
ntrees = 1000
cv_errors = bind_rows(
 tibble(ntree = 1:ntrees, cv_err = gbm_1$cv.error, Depth = 1),
 tibble(ntree = 1:ntrees, cv_err = gbm_2$cv.error, Depth = 2),
 tibble(ntree = 1:ntrees, cv_err = gbm_3$cv.error, Depth = 3)
) %>% mutate(Depth = factor(Depth))
# plot CV errors
mins = cv_errors %% group_by(Depth) %>% summarise(min_err = min(cv_err))
gbm.perf(gbm_3, plot.it = FALSE)
## [1] 43
cv_errors %>%
  ggplot(aes(x = ntree, y = cv_err, colour = Depth)) +
  geom_line() + theme_bw() +
  geom_hline(aes(yintercept = min_err, color = Depth),
             data = mins, linetype = "dashed") +
  labs(y = "CV Error", x = "Trees") + scale_y_log10()
```



Figure 3: CV Error by Trees and Interaction Depth (with min error for each depth dashed)

Solution:

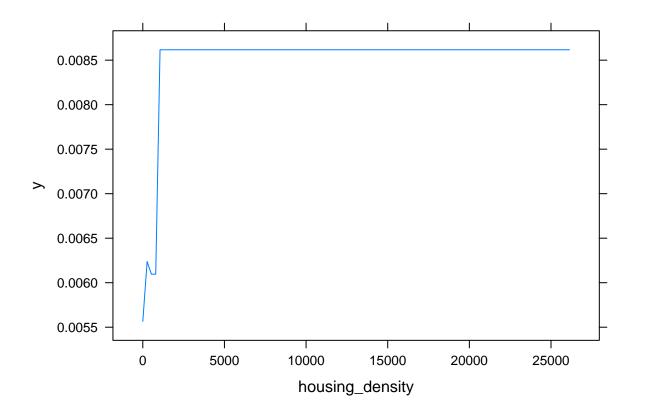
Table 4: These are the first ten rows of the relative influence table for the optimal boosting model above.

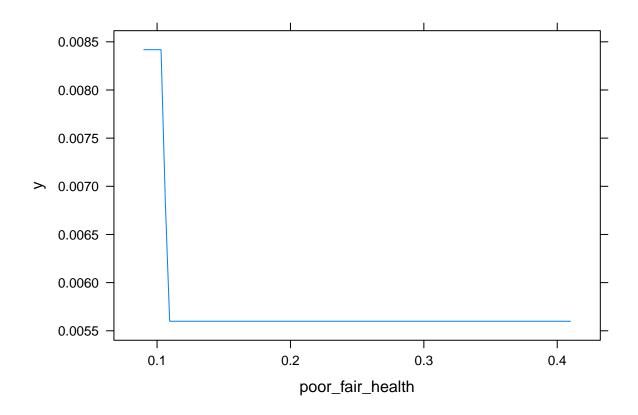
Variable	Relative influence
bachplus PctEmpFIRE unemp_bens_possible	22.800 9.707 9.269
housing_density pertrump poor fair health	4.708 4.603 3.635
pop_density police_funding_score withkids	3.632 3.370 3.279
dis35to64	3.241

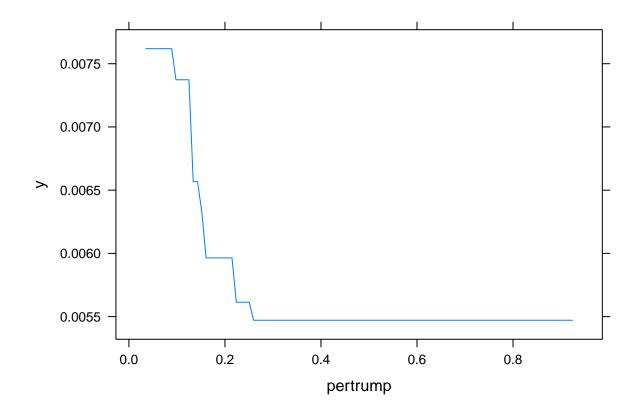
ii. (4 points) Produce partial dependence plots for the top three features based on relative influence.

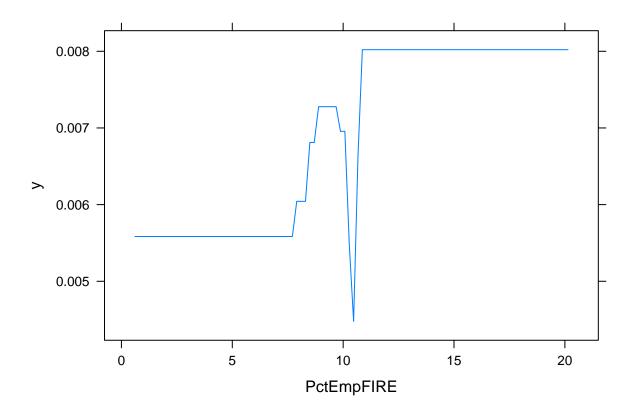
Comment on the nature of the relationship with the response and whether it makes sense.

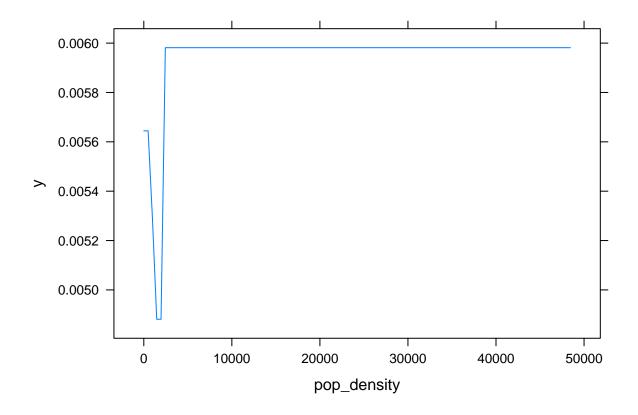
Solution:

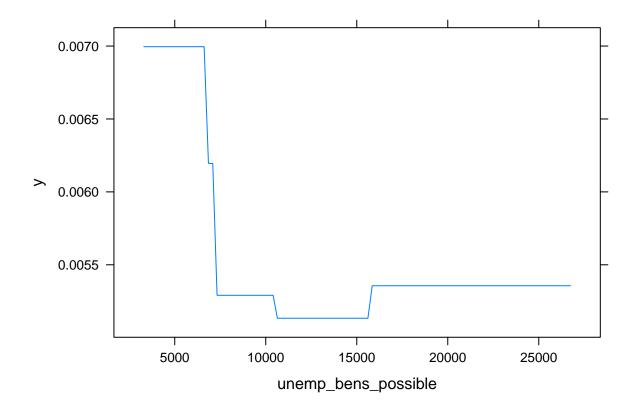


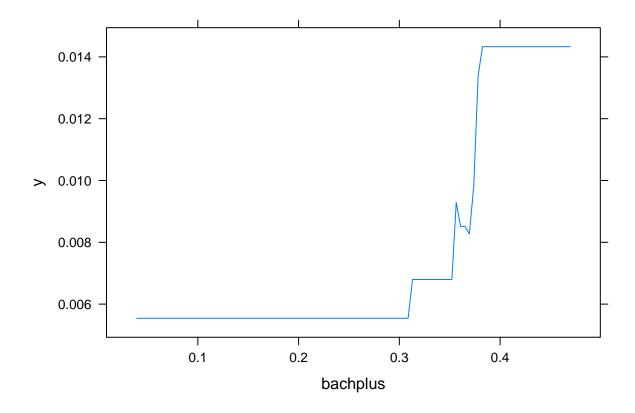


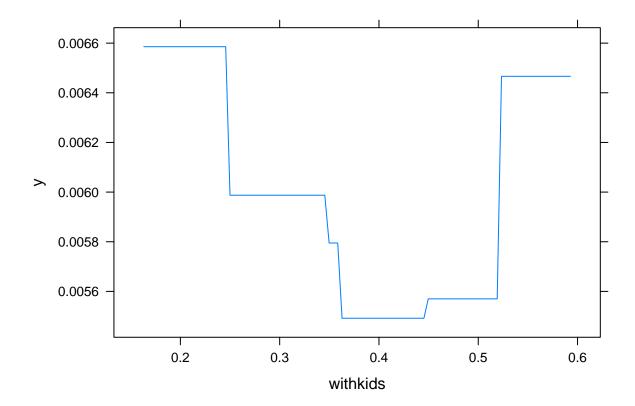




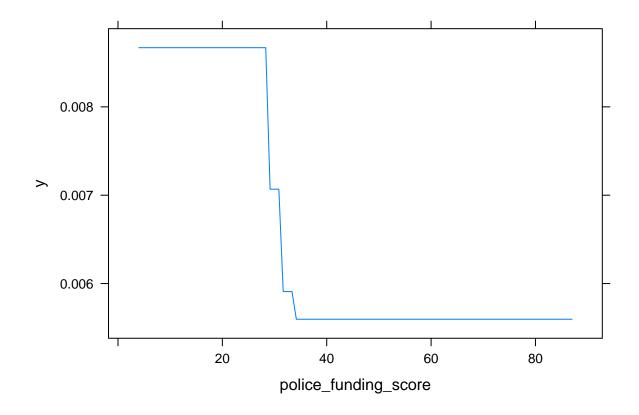








 $police_funding_score$



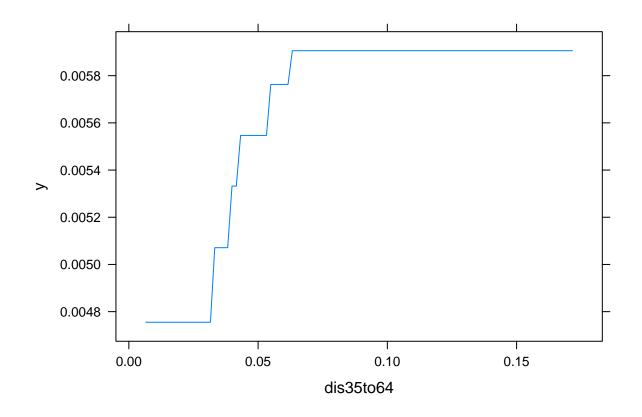


Table 5: Root-mean-squared prediction errors by model type, and intercept-only models.

Model	Test RMSE
Ridge	0.00641267
Lasso	0.00637219
Intercept-only	0.00645320
Elastic_Net	0.00644403
$Random_Forest$	0.00630238
Boosting	0.00630166

```
s = "lambda.1se") %>%
  as.numeric()
elnet_RMSE = sqrt(mean((elnet_predictions-theft_test$theftrate)^2))
# intercept-only prediction error
training_mean_response = mean(theft_test$theftrate)
constant_RMSE = sqrt(mean((training_mean_response-theft_test$theftrate)^2))
#RF
rf_predictions = predict(rf_12, newdata = theft_test)
rf_RMSE = sqrt(mean((rf_predictions-theft_test$theftrate)^2))
#Boosting
gbm_predictions = predict(gbm_3, n.trees = optimal_num_trees,
                          newdata = theft_test)
gbm_RMSE = sqrt(mean((gbm_predictions-theft_test$theftrate)^2))
# print nice table
tibble(Ridge = ridge_RMSE, Lasso = lasso_RMSE, `Intercept-only` = constant_RMSE,
       Elastic_Net = elnet_RMSE, Random_Forest = rf_RMSE, Boosting = gbm_RMSE) %>% pivot_longer(everyth
  kable(format = "latex", row.names = NA,
       booktabs = TRUE, digits = 8,
       caption = "Root-mean-squared prediction errors by model type,
      and intercept-only models.") %>%
kable_styling(position = "center")
```

mean(theft_test\$theftrate)

[1] 0.005804112