Mason Weiss

ELEC 576 - Introduction to Deep Learning

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Due: September 18, 2024

Assignment 0

Task 1:

\$ conda info

```
active environment : base
       active env location : /Users/mason/opt/anaconda3
                shell level : 1
          user config file : /Users/mason/.condarc
4
    populated config files : /Users/mason/.condarc
5
              conda version: 24.7.1
6
       conda-build version: 24.7.1
            python version: 3.9.19.final.0
                     solver : libmamba (default)
          virtual packages : __archspec=1=cannonlake
10
                              __conda=24.7.1=0
11
                              __osx=10.16=0
12
                              __unix=0=0
13
          base environment : /Users/mason/opt/anaconda3 (writable)
14
         conda av data dir : /Users/mason/opt/anaconda3/etc/conda
15
     conda av metadata url : None
16
              channel URLs: https://repo.anaconda.com/pkgs/main/osx-64
17
                              https://repo.anaconda.com/pkgs/main/noarch
18
                              https://repo.anaconda.com/pkgs/r/osx-64
19
                              https://repo.anaconda.com/pkgs/r/noarch
20
             package cache : /Users/mason/opt/anaconda3/pkgs
21
                              /Users/mason/.conda/pkgs
22
          envs directories : /Users/mason/opt/anaconda3/envs
23
                              /Users/mason/.conda/envs
                   platform : osx-64
25
                 user-agent: conda/24.7.1 requests/2.32.3 CPython/3.9.19
26
                 \rightarrow Darwin/22.3.0 OSX/10.16 solver/libmamba
                    conda-libmamba-solver/24.7.0 libmambapy/1.5.8 aau/0.4.4 c/. s/.
                    e/.
                    UID:GID: 501:20
27
                netrc file : None
              offline mode : False
```

Task 2: Run all of Python commands in the table "Linear Algebra Equivalents" in Numpy for MATLAB Users.

```
(base) mason@masons-mbp ~ % ipython
   Python 3.9.19 (main, May 6 2024, 14:46:57)
   Type 'copyright', 'credits' or 'license' for more information
   IPython 8.15.0 -- An enhanced Interactive Python. Type '?' for help.
   In [1]: import numpy as np
   In [2]: import scipy.linalg
   In [3]: a =
    \rightarrow np.array([[1,2,3,4],[5,6,7,8],[9,10,11,12],[13,14,15,16],[17,18,19,20]])
   In [4]: np.ndim(a)
   Out[4]: 2
   In [5]: a.ndim
10
   Out[5]: 2
11
12
   In [6]: np.size(a)
13
   Out[6]: 20
14
   In [7]: a.size
   Out[7]: 20
17
18
   In [8]: np.shape(a)
19
   Out[8]: (5, 4)
20
^{21}
   In [9]: a.shape
   Out[9]: (5, 4)
23
24
   In [10]: n = 2
25
26
   In [11]: a.shape[n-1]
27
   Out[11]: 4
28
   In [12]: np.array([[1., 2., 3.], [4., 5., 6.]])
   Out[12]:
   array([[1., 2., 3.],
32
           [4., 5., 6.]])
33
34
   In [13]: b = a*-1
35
   In [14]: c = a*2
37
   In [15]: d = a*-3
```

```
40
   In [16]: np.block([[a, b], [c, d]])
41
   Out [16]:
42
                             4, -1, -2, -3, -4].
   array([[
             1,
                   2,
                        3,
43
                             8, -5,
                                      -6, -7,
           5,
                   6,
                        7,
44
                       11, 12, -9, -10, -11, -12],
           10,
             9,
45
           [ 13,
                  14,
                       15,
                            16, -13, -14, -15, -16],
                            20, -17, -18, -19, -20],
           [ 17,
                  18,
                       19.
47
                             8, -3, -6, -9, -12],
                   4,
                       6,
           [ 2,
48
                       14, 16, -15, -18, -21, -24],
           [ 10,
                  12,
49
           [ 18,
                  20,
                       22, 24, -27, -30, -33, -36],
50
                            32, -39, -42, -45, -48],
                  28,
                       30.
           [ 26,
51
           [ 34,
                  36,
                       38, 40, -51, -54, -57, -60]])
52
   In [17]: from numpy.random import default_rng
54
55
   In [18]: rng = default_rng(42)
56
57
   In [19]: a = rng.random((23, 11))
58
59
   In [20]: a[-1]
60
   Out [20]:
61
   array([0.23264074, 0.53076959, 0.60601582, 0.86773895, 0.60310716,
62
           0.41257157, 0.37418404, 0.42588209, 0.65193103, 0.86749063,
63
           0.45389688])
64
65
   In [21]: a[1, 4]
66
   Out[21]: 0.2272387217847769
67
   In [22]: a[1]
   Out[22]:
70
   array([0.92676499, 0.64386512, 0.82276161, 0.4434142, 0.22723872,
71
           0.55458479, 0.06381726, 0.82763117, 0.6316644, 0.75808774,
72
           0.35452597])
73
74
   In [23]: a[1, :]
75
   Out [23]:
   array([0.92676499, 0.64386512, 0.82276161, 0.4434142, 0.22723872,
77
           0.55458479, 0.06381726, 0.82763117, 0.6316644, 0.75808774,
78
           0.35452597])
79
80
   In [24]: a[:5]
81
   Out [24]:
82
   array([[0.77395605, 0.43887844, 0.85859792, 0.69736803, 0.09417735,
            0.97562235, 0.7611397, 0.78606431, 0.12811363, 0.45038594,
84
            0.37079802],
85
           [0.92676499, 0.64386512, 0.82276161, 0.4434142, 0.22723872,
86
```

```
0.55458479, 0.06381726, 0.82763117, 0.6316644, 0.75808774,
87
            0.35452597],
88
           [0.97069802, 0.89312112, 0.7783835, 0.19463871, 0.466721
89
            0.04380377, 0.15428949, 0.68304895, 0.74476216, 0.96750973,
90
            0.32582536],
91
           [0.37045971, 0.46955581, 0.18947136, 0.12992151, 0.47570493,
92
            0.22690935, 0.66981399, 0.43715192, 0.8326782, 0.7002651,
93
            0.31236664],
94
           [0.8322598, 0.80476436, 0.38747838, 0.2883281, 0.6824955,
95
            0.13975248, 0.1999082, 0.00736227, 0.78692438, 0.66485086,
96
            0.70516538]])
97
98
    In [25]: a[0:5, :]
99
    Out [25]:
100
    array([[0.77395605, 0.43887844, 0.85859792, 0.69736803, 0.09417735,
101
            0.97562235, 0.7611397, 0.78606431, 0.12811363, 0.45038594,
102
            0.37079802],
103
           [0.92676499, 0.64386512, 0.82276161, 0.4434142, 0.22723872,
104
            0.55458479, 0.06381726, 0.82763117, 0.6316644, 0.75808774,
105
            0.35452597],
106
           [0.97069802, 0.89312112, 0.7783835, 0.19463871, 0.466721
107
            0.04380377, 0.15428949, 0.68304895, 0.74476216, 0.96750973,
108
            0.32582536],
109
           [0.37045971, 0.46955581, 0.18947136, 0.12992151, 0.47570493,
110
            0.22690935, 0.66981399, 0.43715192, 0.8326782, 0.7002651,
111
            0.31236664],
112
           [0.8322598 , 0.80476436, 0.38747838, 0.2883281 , 0.6824955 ,
113
            0.13975248, 0.1999082, 0.00736227, 0.78692438, 0.66485086,
114
            0.70516538]])
115
116
    In [26]: a[0:5]
117
    Out[26]:
118
    array([[0.77395605, 0.43887844, 0.85859792, 0.69736803, 0.09417735,
119
            0.97562235, 0.7611397, 0.78606431, 0.12811363, 0.45038594,
120
            0.37079802],
121
           [0.92676499, 0.64386512, 0.82276161, 0.4434142, 0.22723872,
122
            0.55458479, 0.06381726, 0.82763117, 0.6316644, 0.75808774,
123
            0.35452597],
124
           [0.97069802, 0.89312112, 0.7783835, 0.19463871, 0.466721
125
            0.04380377, 0.15428949, 0.68304895, 0.74476216, 0.96750973,
126
127
           [0.37045971, 0.46955581, 0.18947136, 0.12992151, 0.47570493,
128
            0.22690935, 0.66981399, 0.43715192, 0.8326782, 0.7002651,
129
            0.31236664],
130
           [0.8322598 , 0.80476436 , 0.38747838 , 0.2883281 , 0.6824955 ,
131
            0.13975248, 0.1999082, 0.00736227, 0.78692438, 0.66485086,
132
            0.70516538]])
133
```

```
134
    In [27]: a[-5:]
135
    Out [27]:
136
    array([[0.19643467, 0.31032367, 0.77740484, 0.97182643, 0.50074119,
137
            0.1438975, 0.01393629, 0.22965603, 0.13182222, 0.67765867,
138
            0.1218325 ],
139
           [0.50632993, 0.69426244, 0.58111661, 0.19977565, 0.80412453,
140
            0.71540713, 0.738984 , 0.13105775, 0.1237538 , 0.92756255,
141
            0.39757819],
142
            [0.30094869, 0.48858405, 0.66286421, 0.95562326, 0.28644623,
143
            0.92480843, 0.02485949, 0.55519804, 0.63397511, 0.1058974,
144
            0.1403396],
145
           [0.41911432, 0.96623191, 0.59604255, 0.93302322, 0.80436092,
146
            0.4673816, 0.78476345, 0.01783678, 0.109144, 0.82942861,
147
            0.79681709],
148
           [0.23264074, 0.53076959, 0.60601582, 0.86773895, 0.60310716,
149
            0.41257157, 0.37418404, 0.42588209, 0.65193103, 0.86749063,
150
            0.45389688]])
151
152
    In [28]: a[0:3, 4:9]
153
    Out [28]:
154
    array([[0.09417735, 0.97562235, 0.7611397, 0.78606431, 0.12811363],
155
           [0.22723872, 0.55458479, 0.06381726, 0.82763117, 0.6316644],
156
           [0.466721 , 0.04380377, 0.15428949, 0.68304895, 0.74476216]])
157
158
    In [29]: a[np.ix_([1, 3, 4], [0, 2])]
159
    Out [29]:
160
    array([[0.92676499, 0.82276161],
161
           [0.37045971, 0.18947136],
162
           [0.8322598 , 0.38747838]])
163
164
    In [30]: a[2:21:2,:]
165
    Out [30]:
166
    array([[0.97069802, 0.89312112, 0.7783835 , 0.19463871, 0.466721
167
            0.04380377, 0.15428949, 0.68304895, 0.74476216, 0.96750973,
168
            0.32582536],
169
            [0.8322598, 0.80476436, 0.38747838, 0.2883281, 0.6824955,
170
            0.13975248, 0.1999082, 0.00736227, 0.78692438, 0.66485086,
171
            0.70516538],
172
            [0.55920716, 0.3039501, 0.03081783, 0.43671739, 0.21458467,
173
            0.40852864, 0.85340307, 0.23393949, 0.05830274, 0.28138389,
174
            0.29359376],
175
           [0.16127178, 0.50104478, 0.1523121, 0.69632038, 0.44615628,
176
            0.38102123, 0.30151209, 0.63028259, 0.36181261, 0.08764992,
177
            0.1180059],
178
           [0.45577629, 0.20236336, 0.30595662, 0.57921957, 0.17677278,
179
            0.85661428, 0.75851953, 0.71946296, 0.43209304, 0.62730884,
180
```

```
0.58409797],
181
           [0.58106114, 0.3468698, 0.59091549, 0.02280387, 0.95855921,
182
            0.48230344, 0.78273523, 0.08273
                                              , 0.48665833, 0.49070699,
183
            0.93782645],
184
           [0.10857574, 0.67224009, 0.28123378, 0.65942263, 0.72699461,
185
            0.76864749, 0.10774095, 0.91601185, 0.23021399, 0.03741256,
            0.55485247],
187
           [0.43509706, 0.99237556, 0.89167727, 0.74860802, 0.89079249,
188
            0.89344664, 0.51885836, 0.31592905, 0.77201243, 0.66166126,
189
190
           [0.19643467, 0.31032367, 0.77740484, 0.97182643, 0.50074119,
191
            0.1438975, 0.01393629, 0.22965603, 0.13182222, 0.67765867,
192
            0.1218325],
193
           [0.30094869, 0.48858405, 0.66286421, 0.95562326, 0.28644623,
            0.92480843, 0.02485949, 0.55519804, 0.63397511, 0.1058974,
195
            0.1403396 ]])
196
197
    In [31]: a
198
    Out [31]:
199
    array([[0.77395605, 0.43887844, 0.85859792, 0.69736803, 0.09417735,
200
            0.97562235, 0.7611397, 0.78606431, 0.12811363, 0.45038594,
201
            0.37079802],
202
           [0.92676499, 0.64386512, 0.82276161, 0.4434142, 0.22723872,
203
            0.55458479, 0.06381726, 0.82763117, 0.6316644, 0.75808774,
204
            0.35452597],
205
           [0.97069802, 0.89312112, 0.7783835, 0.19463871, 0.466721
206
            0.04380377, 0.15428949, 0.68304895, 0.74476216, 0.96750973,
207
            0.32582536],
208
           [0.37045971, 0.46955581, 0.18947136, 0.12992151, 0.47570493,
            0.22690935, 0.66981399, 0.43715192, 0.8326782, 0.7002651,
210
            0.31236664],
211
           [0.8322598, 0.80476436, 0.38747838, 0.2883281, 0.6824955,
212
            0.13975248, 0.1999082, 0.00736227, 0.78692438, 0.66485086,
213
            0.70516538],
214
           [0.78072903, 0.45891578, 0.5687412, 0.139797, 0.11453007,
215
            0.66840296, 0.47109621, 0.56523611, 0.76499886, 0.63471832,
216
            0.5535794],
217
           [0.55920716, 0.3039501 , 0.03081783, 0.43671739, 0.21458467,
218
            0.40852864, 0.85340307, 0.23393949, 0.05830274, 0.28138389,
219
            0.29359376],
220
           [0.66191651, 0.55703215, 0.78389821, 0.66431354, 0.40638686,
221
            0.81402038, 0.16697292, 0.02271207, 0.09004786, 0.72235935,
222
            0.46187723],
223
           [0.16127178, 0.50104478, 0.1523121, 0.69632038, 0.44615628,
224
            0.38102123, 0.30151209, 0.63028259, 0.36181261, 0.08764992,
225
            0.1180059],
226
           [0.96189766, 0.90858069, 0.69970713, 0.26586996, 0.96917638,
227
```

```
0.7787509, 0.71689019, 0.4493615, 0.27224156, 0.09639096,
228
            0.9026024],
229
           [0.45577629, 0.20236336, 0.30595662, 0.57921957, 0.17677278,
230
            0.85661428, 0.75851953, 0.71946296, 0.43209304, 0.62730884,
231
            0.58409797],
232
           [0.6498466, 0.08444432, 0.4158074, 0.04161417, 0.49399082,
233
            0.32986121, 0.14452419, 0.10340297, 0.58764457, 0.17059297,
234
            0.92512012],
235
           [0.58106114, 0.3468698, 0.59091549, 0.02280387, 0.95855921,
236
            0.48230344, 0.78273523, 0.08273
                                              . 0.48665833, 0.49070699,
237
            0.93782645],
238
            [0.57172805, 0.4734894, 0.26697566, 0.331569, 0.5206724,
239
            0.43891146, 0.02161208, 0.82629192, 0.89616077, 0.14024909,
240
            0.55403614],
241
           [0.10857574, 0.67224009, 0.28123378, 0.65942263, 0.72699461,
            0.76864749, 0.10774095, 0.91601185, 0.23021399, 0.03741256,
243
            0.55485247],
244
           [0.37092228, 0.82978974, 0.80825147, 0.31713889, 0.9528994,
245
            0.29091784, 0.51505713, 0.25596509, 0.93604357, 0.16460782,
246
            0.04491062],
247
           [0.43509706, 0.99237556, 0.89167727, 0.74860802, 0.89079249,
248
            0.89344664, 0.51885836, 0.31592905, 0.77201243, 0.66166126,
249
            0.37365773],
250
            [0.09446667, 0.74678961, 0.26246052, 0.93681315, 0.24097058,
251
            0.12275793, 0.83111267, 0.15328432, 0.17926831, 0.59938279,
252
            0.87456204].
253
           [0.19643467, 0.31032367, 0.77740484, 0.97182643, 0.50074119,
254
            0.1438975 , 0.01393629, 0.22965603, 0.13182222, 0.67765867,
255
            0.1218325 ],
           [0.50632993, 0.69426244, 0.58111661, 0.19977565, 0.80412453,
257
            0.71540713, 0.738984 , 0.13105775, 0.1237538 , 0.92756255,
258
            0.39757819],
259
           [0.30094869, 0.48858405, 0.66286421, 0.95562326, 0.28644623,
260
            0.92480843, 0.02485949, 0.55519804, 0.63397511, 0.1058974,
261
            0.1403396],
262
           [0.41911432, 0.96623191, 0.59604255, 0.93302322, 0.80436092,
263
            0.4673816, 0.78476345, 0.01783678, 0.109144, 0.82942861,
264
            0.79681709],
265
           [0.23264074, 0.53076959, 0.60601582, 0.86773895, 0.60310716,
266
            0.41257157, 0.37418404, 0.42588209, 0.65193103, 0.86749063,
267
            0.45389688]])
268
269
    In [32]: a =
270
    \rightarrow np.array([[1,2,3,4],[5,6,7,8],[9,10,11,12],[13,14,15,16],[17,18,19,20]])
271
    In [33]: a[::2, :]
    Out [33]:
273
```

```
array([[ 1, 2, 3, 4],
274
            [ 9, 10, 11, 12],
275
            [17, 18, 19, 20]])
276
277
    In [34]: a[::-1,:]
278
    Out [34]:
279
    array([[17, 18, 19, 20],
280
            [13, 14, 15, 16],
281
            [ 9, 10, 11, 12],
282
            [5, 6, 7, 8],
283
            [ 1,
                  2,
                      3,
                           4]])
284
285
    In [35]: a[np.r_[:len(a),0]]
286
    Out [35]:
287
    array([[ 1, 2,
                      3,
                           4],
288
            [5, 6, 7, 8],
289
            [ 9, 10, 11, 12],
290
            [13, 14, 15, 16],
291
            [17, 18, 19, 20],
292
            [1, 2, 3, 4]])
293
294
    In [36]: a.transpose()
295
    Out[36]:
296
    array([[ 1, 5, 9, 13, 17],
297
            [ 2,
                  6, 10, 14, 18],
298
            [3, 7, 11, 15, 19],
299
            [4, 8, 12, 16, 20]])
300
301
    In [37]: a.T
302
    Out[37]:
303
    array([[ 1,
                  5, 9, 13, 17],
304
            [ 2,
                  6, 10, 14, 18],
305
                 7, 11, 15, 19],
            [3,
306
                 8, 12, 16, 20]])
            [ 4,
307
308
    In [38]: a.conj().transpose()
309
    Out [38]:
310
    array([[ 1, 5, 9, 13, 17],
311
            [ 2,
                  6, 10, 14, 18],
312
            [3, 7, 11, 15, 19],
313
            [4, 8, 12, 16, 20]])
314
315
    In [39]: a.conj().T
316
    Out[39]:
317
    array([[ 1, 5, 9, 13, 17],
318
            [ 2,
                  6, 10, 14, 18],
319
            [3, 7, 11, 15, 19],
320
```

```
[4, 8, 12, 16, 20]])
321
322
    In [40]: b = a.T
323
324
    In [41]: a @ b
325
    Out [41]:
326
    array([[ 30,
                     70,
                          110,
                                 150,
                                       190],
327
            [ 70,
                    174,
                           278,
                                 382,
                                        486],
328
            [ 110,
                   278,
                           446,
                                 614,
                                        782],
329
                                 846, 1078],
            [ 150, 382,
                           614.
330
            [ 190, 486,
                          782, 1078, 1374]])
331
332
    In [42]: b = 3
333
334
    In [43]: a * b
335
    Out [43]:
336
    array([[ 3, 6, 9, 12],
337
            [15, 18, 21, 24],
338
            [27, 30, 33, 36],
339
            [39, 42, 45, 48],
340
            [51, 54, 57, 60]])
341
342
    In [44]: a/b
343
    Out [44]:
344
    array([[0.33333333, 0.66666667, 1. , 1.33333333],
345
            [1.66666667, 2.
                                    , 2.33333333, 2.66666667],
346
                     , 3.33333333, 3.66666667, 4.
347
            [4.33333333, 4.66666667, 5.
                                                 , 5.33333333],
348
                              , 6.33333333, 6.66666667]])
            [5.66666667, 6.
349
350
    In [45]: a**3
351
    Out [45]:
352
    array([[
               1,
                      8,
                            27,
                                  64],
353
            [ 125, 216, 343, 512],
354
            [729, 1000, 1331, 1728],
355
            [2197, 2744, 3375, 4096],
356
            [4913, 5832, 6859, 8000]])
357
358
    In [46]: (a > 0.5)
359
    Out [46]:
360
    array([[ True,
                     True,
                             True,
                                     True],
361
            [ True,
                     True,
                             True,
                                     True],
362
                             True,
            [ True,
                     True,
                                     True],
363
            [ True,
                     True,
                             True,
                                     True],
364
                             True,
            [ True,
                     True,
                                     True]])
365
366
    In [47]: np.nonzero(a > 0.5)
367
```

```
Out [47]:
368
    (array([0, 0, 0, 0, 1, 1, 1, 1, 2, 2, 2, 2, 3, 3, 3, 3, 4, 4, 4, 4]),
369
     array([0, 1, 2, 3, 0, 1, 2, 3, 0, 1, 2, 3, 0, 1, 2, 3, 0, 1, 2, 3]))
370
371
    In [48]: v = np.array([1, 0, 0, 1])
372
373
    In [49]: a[:,np.nonzero(v > 0.5)[0]]
374
    Out [49]:
375
    array([[ 1, 4],
376
            [5,8],
377
            [9, 12],
378
            [13, 16],
379
            [17, 20]])
380
381
    In [50]: a[:, v.T > 0.5]
382
    Out [50]:
383
    array([[ 1, 4],
384
            [5, 8],
385
            [9, 12],
386
            [13, 16],
387
            [17, 20]])
388
389
    In [51]: a = a/10
390
391
    In [52]: a[a < 0.5] = 0
392
393
    In [53]: a
394
    Out [53]:
395
    array([[0., 0., 0., 0.],
396
            [0.5, 0.6, 0.7, 0.8],
397
            [0.9, 1., 1.1, 1.2],
398
            [1.3, 1.4, 1.5, 1.6],
399
            [1.7, 1.8, 1.9, 2.]])
400
401
    In [54]: a =
402
        np.array([[1,2,3,4],[5,6,7,8],[9,10,11,12],[13,14,15,16],[17,18,19,20]])
403
    In [55]: a = a/10
404
405
    In [56]: a * (a > 0.5)
406
    Out [56]:
407
    array([[0., 0., 0., 0.],
408
            [0., 0.6, 0.7, 0.8],
409
            [0.9, 1., 1.1, 1.2],
410
            [1.3, 1.4, 1.5, 1.6],
411
            [1.7, 1.8, 1.9, 2.]])
412
413
```

```
In [57]: a[:] = 3
414
415
    In [58]: a
416
    Out [58]:
417
    array([[3., 3., 3., 3.],
418
           [3., 3., 3., 3.],
419
           [3., 3., 3., 3.],
420
           [3., 3., 3., 3.],
421
           [3., 3., 3., 3.]])
422
423
    In [59]: x =
424
    - np.array([[1,2,3,4],[5,6,7,8],[9,10,11,12],[13,14,15,16],[17,18,19,20]])
425
    In [60]: y = x.copy()
426
427
    In [61]: y
428
    Out [61]:
429
    array([[ 1, 2, 3, 4],
430
           [5, 6,
                     7, 8],
431
           [ 9, 10, 11, 12],
432
           [13, 14, 15, 16],
433
           [17, 18, 19, 20]])
434
435
    In [62]: y = x[1, :].copy()
436
437
    In [63]: y
438
    Out[63]: array([5, 6, 7, 8])
439
440
    In [64]: y = x.flatten()
441
442
    In [65]: y
443
    Out [65]:
444
    array([ 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17,
445
           18, 19, 20])
446
447
    In [66]: np.arange(1., 11.)
448
    Out[66]: array([1., 2., 3., 4., 5., 6., 7., 8., 9., 10.])
449
450
    In [67]: np.r_[1.:11.]
451
    Out[67]: array([ 1., 2.,
                                3., 4., 5., 6., 7., 8., 9., 10.])
452
453
    In [68]: np.r_[1:10:10j]
454
    Out[68]: array([ 1., 2., 3., 4., 5., 6., 7., 8., 9., 10.])
455
456
    In [69]: np.arange(10.)
457
    Out[69]: array([0., 1., 2., 3., 4., 5., 6., 7., 8., 9.])
458
459
```

```
In [70]: np.r_[:10.]
460
    Out[70]: array([0., 1., 2., 3., 4., 5., 6., 7., 8., 9.])
461
462
    In [71]: np.r_[:9:10j]
463
    Out[71]: array([0., 1., 2., 3., 4., 5., 6., 7., 8., 9.])
464
465
    In [72]: np.arange(1.,11.)[:, np.newaxis]
466
    Out [72]:
467
    array([[ 1.],
468
            [2.],
469
            [ 3.],
470
            [ 4.],
471
            [5.],
472
            [ 6.],
473
            [7.],
474
            [8.],
475
            [ 9.],
476
            [10.]])
477
478
    In [73]: np.zeros((3, 4))
479
    Out[73]:
480
    array([[0., 0., 0., 0.],
481
            [0., 0., 0., 0.],
482
            [0., 0., 0., 0.]])
483
484
    In [74]: np.zeros((3, 4, 5))
485
    Out [74]:
486
    array([[[0., 0., 0., 0., 0.],
487
             [0., 0., 0., 0., 0.]
488
             [0., 0., 0., 0., 0.]
489
             [0., 0., 0., 0., 0.]
490
491
            [[0., 0., 0., 0., 0.],
492
             [0., 0., 0., 0., 0.]
493
             [0., 0., 0., 0., 0.],
494
             [0., 0., 0., 0., 0.]
495
496
            [[0., 0., 0., 0., 0.],
497
             [0., 0., 0., 0., 0.]
498
             [0., 0., 0., 0., 0.]
499
             [0., 0., 0., 0., 0.]]
500
501
    In [75]: np.ones((3, 4))
502
    Out [75]:
503
    array([[1., 1., 1., 1.],
504
            [1., 1., 1., 1.],
505
            [1., 1., 1., 1.]])
506
```

```
507
    In [76]: np.eye(3)
508
    Out [76]:
509
    array([[1., 0., 0.],
510
            [0., 1., 0.],
511
            [0., 0., 1.]])
512
513
    In [77]: a = np.array([[3,2],[2,1]])
514
515
    In [78]: np.diag(a)
516
    Out[78]: array([3, 1])
517
518
    In [79]: np.diag(v, 0)
519
    Out [79]:
520
    array([[1, 0, 0, 0],
521
            [0, 0, 0, 0],
522
            [0, 0, 0, 0],
523
            [0, 0, 0, 1]])
524
525
    In [80]: rng = default_rng(42)
526
527
    In [81]: rng.random((3, 4))
528
    Out[81]:
529
    array([[0.77395605, 0.43887844, 0.85859792, 0.69736803],
530
            [0.09417735, 0.97562235, 0.7611397, 0.78606431],
531
            [0.12811363, 0.45038594, 0.37079802, 0.92676499]])
532
533
    In [82]: np.linspace(1,3,4)
534
    Out[82]: array([1.
                                 , 1.66666667, 2.333333333, 3.
                                                                         ])
535
536
    In [83]: np.mgrid[0:9.,0:6.]
537
    Out [83]:
538
    array([[[0., 0., 0., 0., 0., 0.],
539
             [1., 1., 1., 1., 1., 1.]
540
             [2., 2., 2., 2., 2., 2.],
541
             [3., 3., 3., 3., 3., 3.]
542
             [4., 4., 4., 4., 4., 4., 4.]
543
             [5., 5., 5., 5., 5., 5.]
544
             [6., 6., 6., 6., 6., 6.]
545
             [7., 7., 7., 7., 7., 7.],
546
             [8., 8., 8., 8., 8., 8.]
547
548
            [[0., 1., 2., 3., 4., 5.],
549
             [0., 1., 2., 3., 4., 5.],
550
             [0., 1., 2., 3., 4., 5.],
551
             [0., 1., 2., 3., 4., 5.],
552
             [0., 1., 2., 3., 4., 5.],
553
```

```
[0., 1., 2., 3., 4., 5.],
554
              [0., 1., 2., 3., 4., 5.],
555
              [0., 1., 2., 3., 4., 5.],
556
              [0., 1., 2., 3., 4., 5.]])
557
558
    In [84]: np.meshgrid([1,2,4],[2,4,5])
559
    Out[84]:
560
    [array([[1, 2, 4],
561
              [1, 2, 4],
562
              [1, 2, 4]]),
563
     array([[2, 2, 2],
564
              [4, 4, 4],
565
              [5, 5, 5]])]
566
567
    In [85]: np.ix_([1,2,4],[2,4,5])
568
    Out[85]:
569
    (array([[1],
570
              [2],
571
              [4]]),
572
     array([[2, 4, 5]]))
573
574
    In [86]: m = 1
575
576
    In [87]: n = 2
577
578
    In [88]: np.tile(a, (m, n))
579
    Out[88]:
580
    array([[3, 2, 3, 2],
581
            [2, 1, 2, 1]])
583
    In [89]: b = np.array([[2, 3], [0,5]])
584
585
    In [90]: np.concatenate((a,b),1)
586
    Out [90]:
587
    array([[3, 2, 2, 3],
588
            [2, 1, 0, 5]])
589
590
    In [91]: np.hstack((a,b))
591
    Out [91]:
592
    array([[3, 2, 2, 3],
593
            [2, 1, 0, 5]])
594
595
    In [92]: np.column_stack((a,b))
596
    Out [92]:
597
    array([[3, 2, 2, 3],
598
            [2, 1, 0, 5]])
599
600
```

```
In [93]: np.c_[a,b]
601
    Out [93]:
602
    array([[3, 2, 2, 3],
603
            [2, 1, 0, 5]])
604
605
    In [94]: np.concatenate((a,b))
606
    Out [94]:
607
    array([[3, 2],
608
            [2, 1],
609
            [2, 3],
610
            [0, 5]])
611
612
    In [95]: np.vstack((a,b))
613
    Out [95]:
614
    array([[3, 2],
615
            [2, 1],
616
            [2, 3],
617
            [0, 5]])
618
619
    In [96]: np.r_[a,b]
620
    Out [96]:
621
    array([[3, 2],
622
            [2, 1],
623
            [2, 3],
624
            [0, 5]])
625
626
    In [97]: a.max()
627
    Out[97]: 3
628
629
    In [98]: np.nanmax(a)
630
    Out[98]: 3
631
632
    In [99]: a.max(0)
633
    Out[99]: array([3, 2])
634
635
    In [100]: a.max(1)
636
    Out[100]: array([3, 2])
637
638
    In [101]: np.maximum(a, b)
639
    Out[101]:
640
    array([[3, 3],
641
            [2, 5]])
642
643
    In [102]: v
644
    Out[102]: array([1, 0, 0, 1])
645
646
    In [103]: np.sqrt(v @ v)
647
```

```
Out[103]: 1.4142135623730951
648
649
    In [104]: np.linalg.norm(v)
650
    Out[104]: 1.4142135623730951
651
652
    In [105]: np.logical_and(a,b)
653
    Out[105]:
654
    array([[ True,
                      True],
655
            [False,
                      True]])
656
657
    In [106]: np.logical_or(a,b)
658
    Out[106]:
659
    array([[ True,
                      True],
660
            [ True,
                      True]])
661
662
    In [107]: a & b
663
    Out[107]:
664
    array([[2, 2],
665
            [0, 1]])
666
667
    In [108]: a | b
668
    Out[108]:
669
    array([[3, 3],
670
            [2, 5]])
671
672
    In [109]: np.linalg.inv(a)
673
    Out[109]:
674
    array([[-1., 2.],
675
            [ 2., -3.]])
676
677
    In [110]: np.linalg.pinv(a)
678
    Out [110]:
679
    array([[-1., 2.],
680
            [ 2., -3.]])
681
682
    In [111]: np.linalg.matrix_rank(a)
683
    Out[111]: 2
684
685
    In [112]: a
686
    Out[112]:
687
    array([[3, 2],
688
            [2, 1]])
689
690
    In [113]: b = np.array([[1],[1]])
691
692
    In [114]: np.linalg.solve(a, b)
693
    Out[114]:
694
```

```
array([[ 1.],
695
           [-1.]])
696
697
    In [115]: b = b.T
698
699
    In [116]: np.linalg.solve(a.T, b.T).T
700
    Out[116]: array([[ 1., -1.]])
701
702
    In [117]: a = np.array([[5,7,6,5],[7,10,8,7],[6,8,10,9],[5,7,9,10]])
703
704
    In [118]: U, S, Vh = np.linalg.svd(a)
705
706
    In [119]: U
707
    Out[119]:
708
    array([[-0.38026207, -0.39630556, -0.09330504, -0.83044375],
709
           [-0.52856785, -0.61486128, 0.30165233, 0.50156506],
710
           [-0.55195485, 0.27160104, -0.76031843, 0.2085536],
711
           [-0.52092478, 0.62539618, 0.56764067, -0.12369746]])
712
713
    In [120]: S
714
    Out[120]: array([3.02886853e+01, 3.85805746e+00, 8.43107150e-01, 1.01500484e-02])
715
716
    In [121]: Vh.T
717
    Out[121]:
718
    array([[-0.38026207, -0.39630556, -0.09330504, -0.83044375],
719
           [-0.52856785, -0.61486128, 0.30165233, 0.50156506],
720
           [-0.55195485, 0.27160104, -0.76031843, 0.2085536],
721
           [-0.52092478, 0.62539618, 0.56764067, -0.12369746]])
722
723
    In [122]: S**2
    Out[122]: array([9.17404460e+02, 1.48846073e+01, 7.10829666e-01, 1.03023482e-04])
725
726
    In [123]: Vh@Vh.T
727
    Out[123]: array([[ 1.00000000e+00, -7.05395086e-17, 4.76007668e-17,
728
            -1.07622236e-16],
729
           [-7.05395086e-17, 1.00000000e+00, 2.11109113e-16,
730
             2.12834394e-16],
731
           [ 4.76007668e-17, 2.11109113e-16, 1.00000000e+00,
732
            -1.38049606e-16],
733
           [-1.07622236e-16, 2.12834394e-16, -1.38049606e-16,
734
             1.00000000e+00]])
735
736
    In [124]: U@np.diag(S)@Vh
737
    Out [124]:
738
    array([[ 5., 7., 6., 5.],
739
           [7., 10., 8., 7.],
740
           [6., 8., 10., 9.],
741
```

```
[5., 7., 9., 10.]])
742
743
    In [125]: np.linalg.cholesky(a)
744
    Out [125]:
745
    array([[ 2.23606798e+00, 0.00000000e+00, 0.00000000e+00,
746
             0.00000000e+00],
747
           [ 3.13049517e+00, 4.47213595e-01, 0.00000000e+00,
748
             0.00000000e+00],
749
           [ 2.68328157e+00, -8.94427191e-01, 1.41421356e+00,
750
             0.00000000e+00].
751
           [ 2.23606798e+00, -6.32813837e-16, 2.12132034e+00,
752
             7.07106781e-01])
753
754
    In [126]: D,V = np.linalg.eig(a)
756
    In [127]: D
757
    Out[127]: array([3.02886853e+01, 3.85805746e+00, 1.01500484e-02, 8.43107150e-01])
758
759
    In [128]: V
760
    Out[128]:
761
    array([[-0.38026207, -0.39630556, -0.83044375, -0.09330504],
762
           [-0.52856785, -0.61486128, 0.50156506, 0.30165233],
763
           [-0.55195485, 0.27160104, 0.2085536, -0.76031843],
764
           [-0.52092478, 0.62539618, -0.12369746, 0.56764067]])
765
766
    In [129]: b = np.eye(4)
767
768
    In [130]: D,V = scipy.linalg.eig(a, b)
769
770
    In [131]: D
771
    Out[131]:
772
    array([3.02886853e+01+0.j, 3.85805746e+00+0.j, 1.01500484e-02+0.j,
773
           8.43107150e-01+0.j])
774
775
    In [132]: V
776
    Out [132]:
777
    array([[ 0.38026207, -0.39630556, 0.83044375, -0.09330504],
778
           [0.52856785, -0.61486128, -0.50156506, 0.30165233],
779
           [0.55195485, 0.27160104, -0.2085536, -0.76031843],
780
           [ 0.52092478, 0.62539618, 0.12369746, 0.56764067]])
781
782
    In [133]: D,V = scipy.sparse.linalg.eigs(b, k=2)
783
784
    In [134]: D
785
    Out[134]: array([1.+0.j, 1.+0.j])
786
787
    In [135]: V
788
```

```
Out [135]:
789
    array([[-0.96312067+0.j, 0.33743833+0.j],
790
            [-0.08300551+0.j, -0.31645308+0.j],
791
            [ 0.01517654+0.j, 0.45922686+0.j],
792
            [-0.25549625+0.j, -0.7583558 +0.j]])
793
794
    In [136]: Q,R = np.linalg.qr(a)
795
796
    In [137]: Q
797
    Out[137]:
798
    array([[-0.43033148, -0.08439495, -0.36952858, -0.81923192],
799
            [-0.60246408, -0.57388564, -0.25706336, 0.49153915],
800
            [-0.51639778, 0.81019149, -0.12853168, 0.24576958],
801
            [-0.43033148, -0.08439495, 0.88365529, -0.16384638]])
802
803
    In [138]: R
804
    Out [138]:
805
    array([[-11.61895004, -16.18046376, -16.43866265, -15.31980079],
806
            Γ Ο.
                         , -0.43885373,
                                             2.2449056, 2.00859974],
807
            0.
                              0.
                                             2.39390251,
                                                           4.03268141],
808
            [ 0.
                              0.
                                             0.
                                                        , -0.08192319]])
809
810
    In [139]: Q@R
811
    Out[139]:
812
    array([[ 5., 7., 6., 5.],
813
            [7., 10., 8., 7.],
814
            [6., 8., 10., 9.],
815
            [5., 7., 9., 10.]])
816
    In [140]: P,L,U = scipy.linalg.lu(a)
818
819
    In [141]: P
820
    Out[141]:
821
    array([[0., 0., 0., 1.],
822
            [1., 0., 0., 0.],
823
            [0., 1., 0., 0.],
824
            [0., 0., 1., 0.]])
825
826
    In [142]: L
827
    Out [142]:
828
                         , 0.
    array([[ 1.
                                          0.
                                                        0.
                                                                   ],
829
                                                                  ],
            [ 0.85714286,
                           1.
                                          0.
                                                        0.
830
            [ 0.71428571, 0.25
                                         1.
                                                        0.
                                                                   ],
831
            [ 0.71428571, 0.25
                                       , -0.2
                                                        1.
                                                                  ]])
832
833
    In [143]: U
    Out[143]:
```

```
7.
    array([[ 7.
                                                                 ],
                        , 10.
                                        8.
836
           [ 0.
                        , -0.57142857, 3.14285714,
                                                      3.
                                                                 ],
837
                                        2.5
           [ 0.
                                                      4.25
                                                                 ],
                        , 0.
838
                        , 0.
           [ 0.
                                        0.
                                                      0.1
                                                                ]])
839
840
    In [144]: P@L@U
841
    Out[144]:
    array([[ 5., 7., 6., 5.],
843
           [7., 10., 8., 7.],
844
           [6., 8., 10., 9.],
845
           [5., 7., 9., 10.]])
846
847
    In [145]: scipy.sparse.linalg.cg(a,np.array([1,1,1,1]))
848
    Out[145]: (array([ 20., -12., -5., 3.]), 0)
850
    In [146]: np.fft.fft(a)
851
    Out [146]:
852
    array([[23.+0.j, -1.-2.j, -1.+0.j, -1.+2.j],
853
           [32.+0.j, -1.-3.j, -2.+0.j, -1.+3.j],
854
           [33.+0.j, -4.+1.j, -1.+0.j, -4.-1.j],
855
           [31.+0.j, -4.+3.j, -3.+0.j, -4.-3.j]
856
857
    In [147]: np.fft.ifft(a)
858
    Out[147]:
859
    array([[ 5.75+0.j , -0.25+0.5j , -0.25+0.j , -0.25-0.5j ],
860
           [8. +0.j, -0.25+0.75j, -0.5 +0.j, -0.25-0.75j],
861
           [8.25+0.j, -1. -0.25j, -0.25+0.j, -1. +0.25j],
862
           [7.75+0.j, -1. -0.75j, -0.75+0.j, -1. +0.75j]])
863
864
    In [148]: np.sort(a)
865
    Out[148]:
866
    array([[5, 5, 6, 7],
867
           [7, 7, 8, 10],
868
           [6, 8, 9, 10],
869
           [5, 7, 9, 10]])
870
871
    In [149]: np.sort(a, axis=1)
    Out[149]:
873
    array([[ 5, 5, 6, 7],
874
           [7, 7, 8, 10],
875
           [6, 8, 9, 10],
876
           [5, 7, 9, 10]])
877
878
    In [150]: I = np.argsort(a[:, 0])
879
880
    In [151]: b = a[I,:]
881
882
```

```
In [152]: b
883
    Out[152]:
884
    array([[5, 7, 6, 5],
885
           [5, 7, 9, 10],
886
           [6, 8, 10, 9],
887
           [7, 10, 8, 7]])
888
889
    In [153]: Z = np.array([[0,1],[1,1],[2,1],[3,1]])
890
891
    In [154]: y = np.array([-1, 0.2, 0.9, 2.1])
892
893
    In [155]: x = np.linalg.lstsq(Z, y,rcond=None)
894
895
    In [156]: x
896
    Out[156]: (array([ 1. , -0.95]), array([0.05]), 2, array([4.10003045,
897
    → 1.09075677]))
898
    In [157]: Z@x[0]
899
    Out[157]: array([-0.95, 0.05, 1.05, 2.05])
900
901
    In [158]: q=1
902
903
    In [159]: scipy.signal.resample(y, int(np.ceil(len(y)/q)))
904
    Out[159]: array([-1., 0.2, 0.9, 2.1])
905
906
    In [160]: np.unique(a)
907
    Out[160]: array([5, 6, 7, 8, 9, 10])
908
909
    In [161]: a = np.array([[[0], [1], [2]]])
910
911
    In [162]: a.squeeze()
912
    Out[162]: array([0, 1, 2])
```

Task 3: Run the following script in IPython and paste the figure created by the script into your report.

```
(base) mason@masons-mbp Desktop % ipython
   Python 3.9.19 (main, May 6 2024, 14:46:57)
   Type 'copyright', 'credits' or 'license' for more information
   IPython 8.15.0 -- An enhanced Interactive Python. Type '?' for help.
   In [1]: import matplotlib.pyplot as plt
   Matplotlib is building the font cache; this may take a moment.
   In [2]: plt.plot([1,2,3,4], [1,2,7,14])
4
   Out[2]: [<matplotlib.lines.Line2D at 0x7fd741fc6f40>]
6
   In [3]: plt.axis([0, 6, 0, 20])
   Out[3]: (0.0, 6.0, 0.0, 20.0)
   In [4]: plt.show()
10
   2024-09-08 17:18:45.301 python[20991:3560702] +[CATransaction synchronize] called
   \hookrightarrow within transaction
  2024-09-08 17:18:45.609 python[20991:3560702] +[CATransaction synchronize] called
    \hookrightarrow within transaction
```

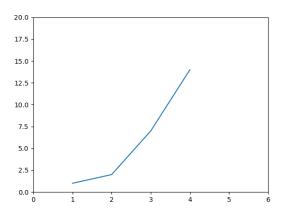


Figure 1: Output from Task 3

Task 4: Use Matplotlib to create a figure of your choice in IPython. Paste your code and figure into your report.

```
(base) mason@masons-mbp Desktop % ipython
   Python 3.9.19 (main, May 6 2024, 14:46:57)
   Type 'copyright', 'credits' or 'license' for more information
   IPython 8.15.0 -- An enhanced Interactive Python. Type '?' for help.
   In [1]: import numpy as np
   In [2]: import matplotlib.pyplot as plt
   In [3]: x = np.linspace(0,100,10001)
   In [4]: y = np.cos(x)*np.sqrt(x)
   In [5]: plt.plot(x, y, 'r-')
   Out[5]: [<matplotlib.lines.Line2D at 0x7fadd2bb5df0>]
10
11
   In [6]: plt.grid()
12
13
   In [7]: plt.show()
14
   2024-09-08 18:07:00.499 python[21981:3600780] +[CATransaction synchronize] called
   \hookrightarrow within transaction
   2024-09-08 18:07:00.823 python[21981:3600780] +[CATransaction synchronize] called
   \hookrightarrow within transaction
   2024-09-08 18:07:08.918 python[21981:3600780] +[CATransaction synchronize] called
   \hookrightarrow within transaction
   2024-09-08 18:07:09.789 python[21981:3600780] +[CATransaction synchronize] called
    \hookrightarrow within transaction
```

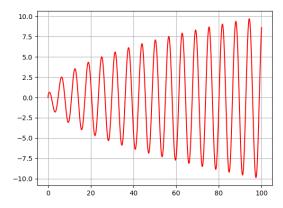


Figure 2: Output from Task 4

Task 5: Paste your VCS account into your report.

GitHub Account: https://github.com/masonweiss

Task 6: Start a new project in Pycharm. Commit and push your project to GitHub as a public project. Paste the link of your project in your report.

 ${\bf Repository~Link:~https://github.com/masonweiss/ELEC576}$