```
1 #%%
  2 # Importing libraries
  3 import matplotlib.pyplot as plt
  4 import numpy as np
  5 import matplotlib as mpl
  7 mpl.rcParams["figure.dpi"] = 100
  8 #%%
  9 # all diameters are in nm
10 S_g = 1.7 # standard deviation of the lognormal distribution
11 N = 1000 # number of particles in the distribution (cm^-3)
12 D_pg = 200 # geometric mean diameter (nm)
13
14 Dp = np.geomspace(1e-8, 1e-6, 1000)*1e9 # convert to nm
15 dN_dDp = N/(np.sqrt(2*np.pi)*np.log(S_g)*Dp)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_
       ))**2/(2*(np.log(S_g))**2))
16
17 dN_dlogDp = dN_dDp*Dp*np.log(10)
18 \ dN_dlnDp = dN_dDp*Dp
19 #%%
20 # Creating subplots
21 fig, axs = plt.subplots(3, 1, figsize=(10, 8))
22
23 # First plot
24 axs[0].plot(Dp, dN_dDp)
25 axs[0].set_xscale('log')
26 axs[0].set_xlabel('Dp (nm)')
27 axs[0].set_ylabel('dN/dDp (cm^-3)')
28 axs[0].legend(['dN/dDp'])
29
30 # Second plot
31 axs[1].plot(Dp, dN_dlnDp)
32 axs[1].set_xscale('log')
33 axs[1].set_xlabel('Dp (nm)')
34 axs[1].set_ylabel('dN/dlnDp')
35 axs[1].legend(['dN/dlnDp'])
36
37 # Third plot
38 axs[2].plot(Dp, dN_dlogDp)
39 axs[2].set_xscale('log')
40 axs[2].set_xlabel('Dp (nm)')
41 axs[2].set_ylabel('dN/dlogDp')
42 axs[2].legend(['dN/dlogDp'])
44 plt.savefig('1-2.png', bbox_inches='tight')
45 plt.show()
46 #%%
47 \text{ bin_number} = 40
48 bins_lower = np.geomspace(1e-9, 10.3e-6, bin_number + 1) #
49 bins_upper = bins_lower[1:]
50 bins_lower = bins_lower[:-1]
51 bins_mid = np.sqrt(bins_lower * bins_upper) # geometric mean
52 for i in range(bin_number):
```

```
print(i, bins_lower[i], bins_upper[i], bins_mid[i])
  54 #%%
 55 # all diameters are in nm
 56 S_g = 1.7 # standard deviation of the lognormal distribution
 57 N = 1000 \# number of particles in the distribution (cm^-3)
 58 D_pg = 200e-9 # geometric mean diameter (nm)
 59
  60 Dp = bins_mid
 61 dN_dDp = N/(np.sqrt(2*np.pi)*np.log(S_g)*Dp)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_pg)*np.exp(-(np.log(Dp/D_
        ))**2/(2*(np.log(S_q))**2))
 62 N = dN_dDp * (bins_upper - bins_lower)
 63 #%%
  64 # Creating histogram of N
 65 plt.bar(bins_mid*1e9, N, width=(bins_upper - bins_lower)*1e9, align='
       center', edgecolor='black')
 66 plt.xscale('log')
 67 # plt.yscale('log')
 68 plt.xlabel('Dp (nm)')
  69 plt.ylabel('N (cm^-3)')
 70 plt.suptitle('Histogram of N in each bin')
  71 #save the plot
 72 plt.savefig('1-3.png', bbox_inches='tight')
 74
 75 #
 76 #%%
 77 # Creating a gamma distribution of droplet sizes
  78 # Total number of drops in gamma distribution is N_d = 100 cm^-3
 79 # The mean diameter is D_pg = 20 \text{ um} = 20000 \text{ nm}
 80 # Dp_meαn_2 = 20000 # nm
 81 \# gamma = 1
 82 # Beta = 2
 83
 84 N_2 = 100 \# cm^{-3} (total number of droplets)
 85 rp_mean_2 = 20e-6 # m (mean diameter of droplets)
 86 Dp_2 = np.geomspace(1e-6, 1e-3, 1000) # convert to nm
 87 B_2 = 3 / rp_mean_2 \# r_mean = 3/B_2
  88 A_2 = N_2 * B_2**3 / 2 # N_2 = 2 * A_2 / B_2**3
  89 dN2_dr = A_2 * ((Dp_2 / 2 )**2) * np.exp( -B_2 * (Dp_2 / 2) ) #
       dN2_dr = A_2 * r^2 * exp(-B_2 * r)
 90 dN2_dDp = dN2_dr / 2 # dN2_dDp = dN2_dr / 2
  91 dN2_dlnDp = dN2_dDp * Dp_2
 92 dN2_dlogDp = dN2_dDp * Dp_2 * np.log(10)
 93 #%%
 94 # Creating subplots
 95 fig, axs = plt.subplots(3, 1, figsize=(10, 8))
 97 # First plot
 98 axs[0].plot(Dp_2*1e9, dN2_dDp) # convert to nm
 99 axs[0].set_xscale('log')
100 axs[0].set_xlabel('Dp (nm)')
101 axs[0].set_ylabel('dN/dDp (cm^-3)')
102 axs[0].legend(['dN/dDp'])
```

```
103
104 # Second plot
105 axs[1].plot(Dp_2*1e9, dN2_dlnDp) # convert to nm
106 axs[1].set_xscale('log')
107 axs[1].set_xlabel('Dp (nm)')
108 axs[1].set_ylabel('dN/dlnDp')
109 axs[1].legend(['dN/dlnDp'])
110
111 # Third plot
112 axs[2].plot(Dp_2*1e9, dN2_dlogDp) # convert to nm
113 axs[2].set_xscale('log')
114 axs[2].set_xlabel('Dp (nm)')
115 axs[2].set_ylabel('dN/dlogDp')
116 axs[2].legend(['dN/dlogDp'])
117 plt.savefig('1-2.png', bbox_inches='tight')
118 plt.show()
```