

# Domain Knowledge Driven 3D Dose Prediction Using Moment-Based Loss Function

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#### **PURPOSE**

To introduce a novel moment-based loss function for predicting 3D dose distribution for the challenging conventional lung IMRT plans. The moment-based loss function is convex and differentiable and can easily incorporate clinical dose volume histogram (DVH) domain knowledge in any deep learning framework without computational overhead

#### MATERIAL & METHODS

We used a large dataset of 360 (240 for training, 50 for validation and 70 for testing) challenging conventional lung patients with 2Gy x 30 fractions to train the deep learning (DL) model using clinically treated plans at our institution.

We trained a UNet like CNN architecture using computed tomography (CT), planning target volume (PTV) and organ-at-risk contours (OAR) as input to infer corresponding voxel-wise 3D dose distribution. We evaluated three different loss functions: 1) Mean Absolute Error (MAE) Loss 2) MAE Loss + DVH Loss (*D. Nguyen et. Al*) 3) MAE Loss + Moments Loss.

Moment of a structure *s* is given by,

$$M_p(s) = \left(\frac{1}{|V(s)|} \sum_{j \in V(s)} d_j^p\right)^{\frac{1}{p}}$$

where,  $M_p$  is the  $p^{th}$  moment of the structure, V(s) are the voxels belonging to the structure s and d is the dose And the moment loss used in this study is given by,

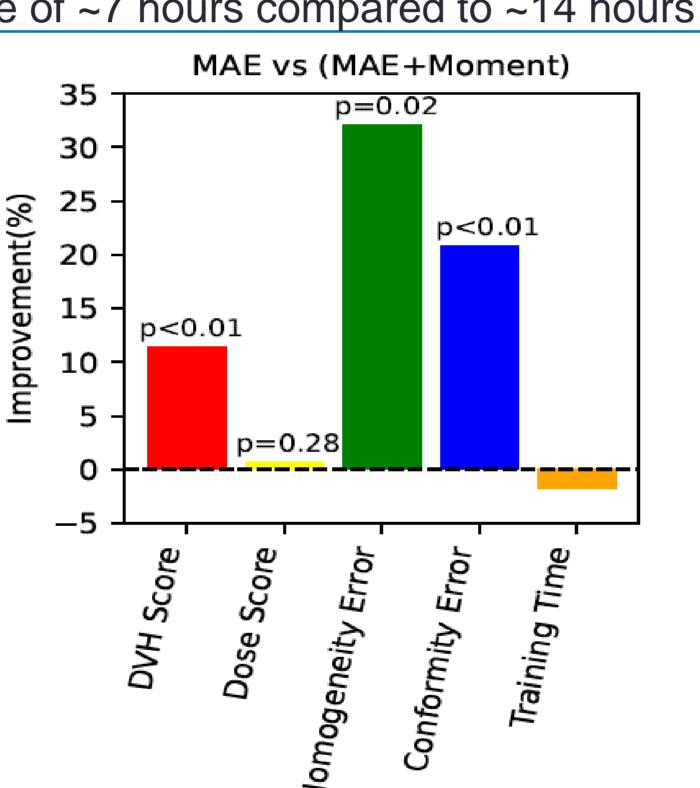
Moment loss = 
$$w \sum ||M_p(s) - \overline{M_p}(s)||_2^2$$

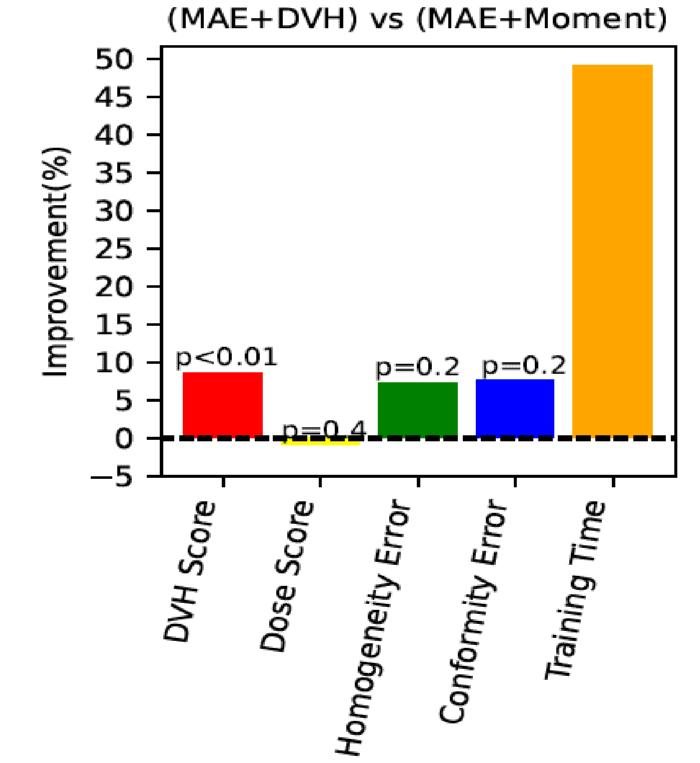
where, w is the weight for  $p^{th}$  moment of the structure  $M_p(s)$  is the actual moment and  $\overline{M_p}(s)$  is the predicted moment for structure s.

The quality of the predictions was compared using different DVH metrics as well as dose-score and DVH-score, recently introduced by the *AAPM knowledge-based planning grand challenge*.

#### RESULTS

Model with MAE + Moment loss function outperformed the MAE and MAE+DVH loss by 11.45% and 8.85% respectively. Dose score remains same for all the loss functions for a given model. (MAE+Moment) loss outperformed MAE loss with 32% and 20.84% improvement in homogeneity and conformity error respectively. (MAE+Moment) loss outperformed (MAE+DVH) loss with 7.23% and 7.58% improvement in homogeneity and conformity error, respectively. Model with MAE+Moment loss also converged twice as fast as MAE+DVH loss, with training time of ~7 hours compared to ~14 hours for MAE+DVH Loss.

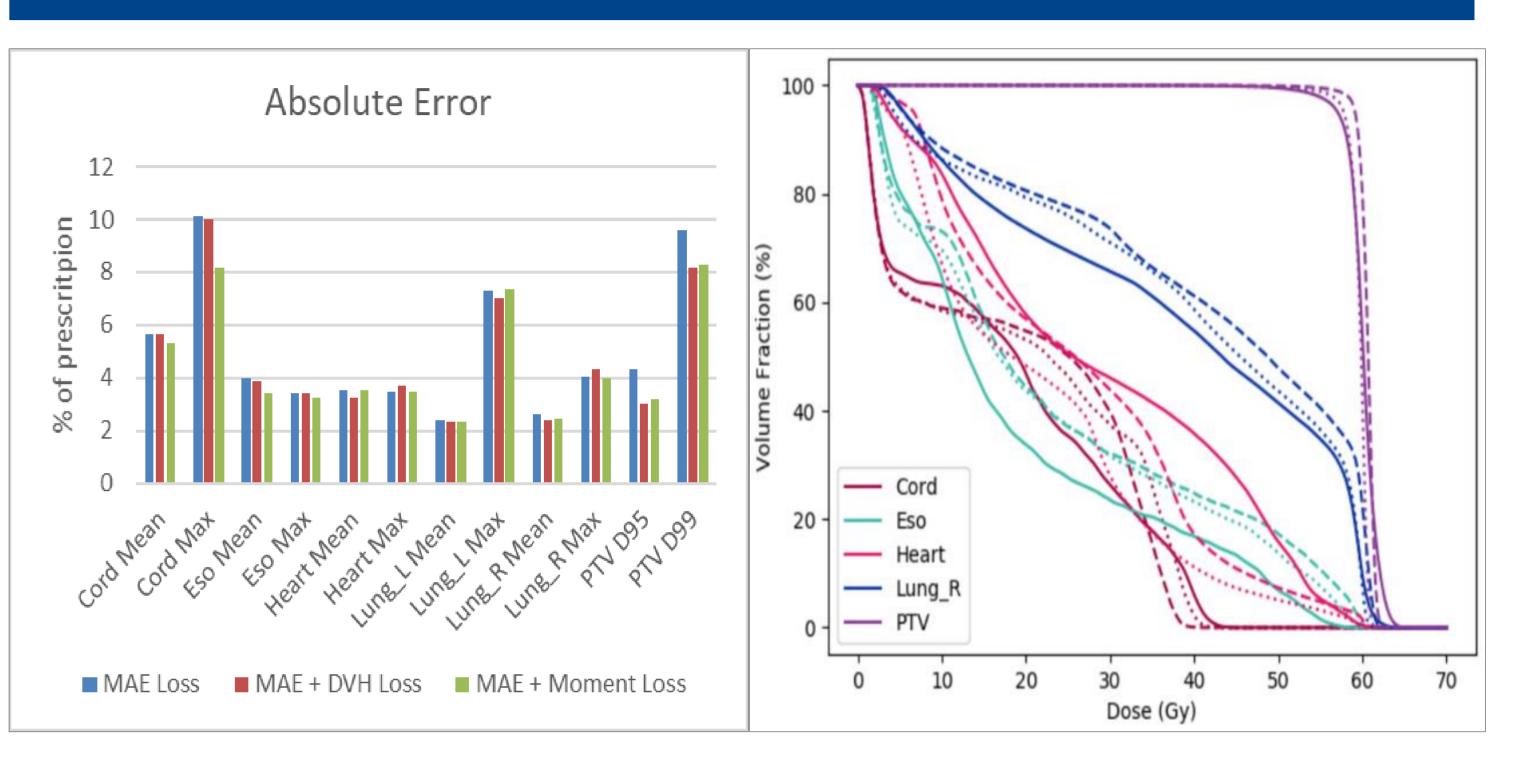




**Figure 1** Comparison of different metrics for (a) MAE vs (MAE + Moment) and (b) (MAE+ DVH) vs (MAE + Moment) losses.

Figure 2 on the left shows the dose prediction error (in percentage of prescription) for different OARs and target volume. Critical OARs like cord, esophagus showed substantial improvement in max/ mean absolute dose error using MAE + Moment loss compared to other two. PTV D95 and D99 showed marginal improvement in the dose prediction quality compared to MAE loss. Figure 2 on right show the DVH comparison for different loss function with the same model. The DVH for the predicted dose using MAE + Moment loss (indicated in dot) is more like the actual dose compared to the DVH for MAE + DVH loss (indicated in dash)

#### RESULTS CONTINUED



**Figure 2 Left-** Absolute error comparison for different loss type **Right-** DVH comparison for i) actual dose(solid) ii) predicted dose using MAE + DVH loss (dash) iii) predicted dose using MAE + Moment loss (Dot)

## CONCLUSION

DVH metrics are widely accepted evaluation criteria in the clinic. However, incorporating them into the 3D dose prediction model is challenging due to their non-convexity and non-differentiability. Moments provide a mathematically rigorous and computationally efficient way to incorporate DVH information in any deep learning architecture.

#### REFERENCES

**D. Nguyen et al.** Incorporating human and learned domain knowledge into training deep neural networks: A differentiable dose-volume histogram and adversarial inspired framework for generating Pareto optimal dose distributions in radiation therapy, Medical Physics 47, 837–849 (2020)

### **ACKNOWLEDGEMENTS**

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