

1,

ab \ cd	00	01	11	10
00	1	0	0	0
01	1	0	0	1
11	1	1	0	1
10	1	1	0	0

$$\Rightarrow f_1 = \bar{a}\bar{b} + \bar{a}c + \bar{b}d$$

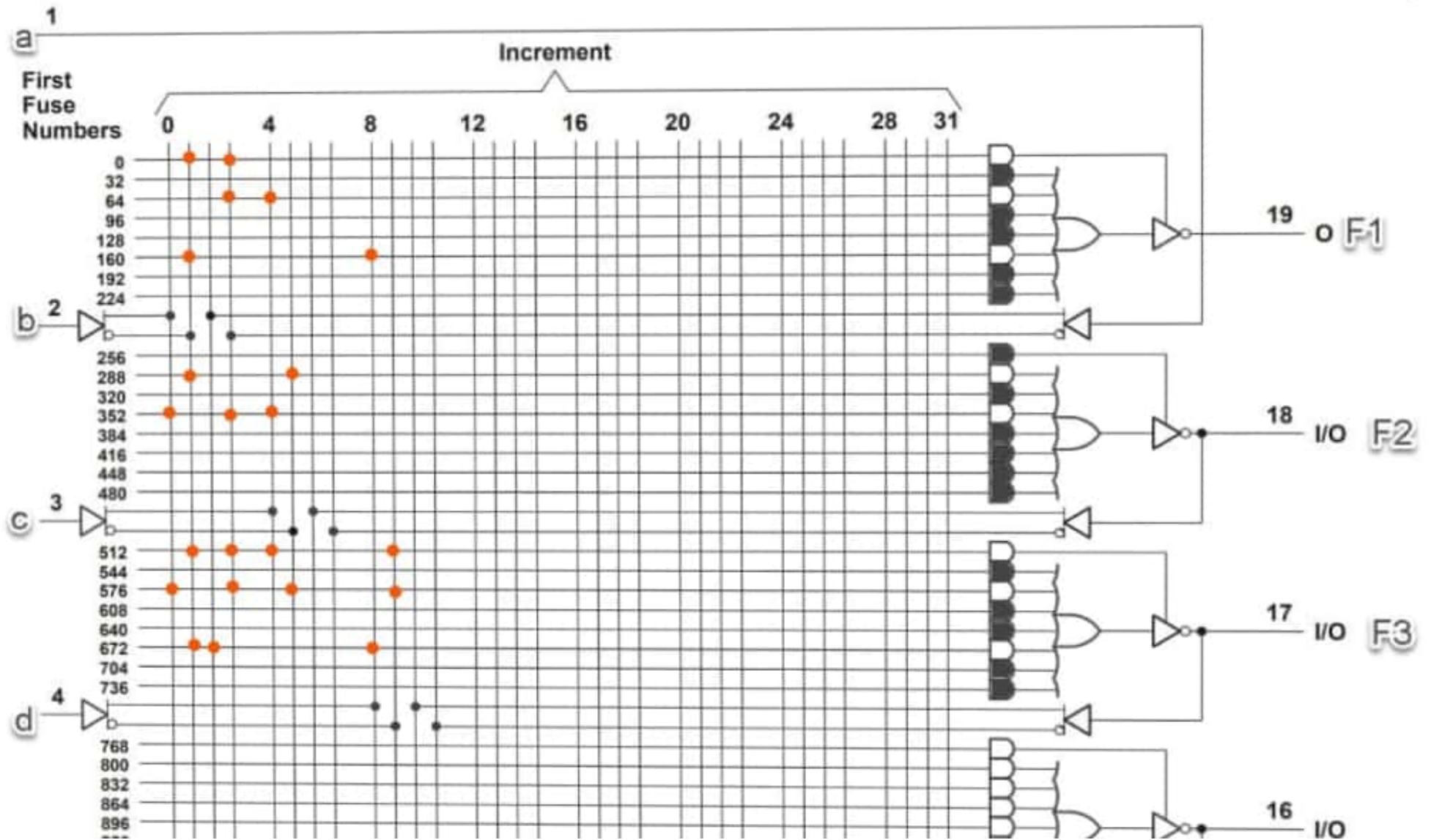
ab \ cd	00	01	11	10
00	1	0	0	1
01	1	0	0	1
11	0	1	0	0
10	0	1	0	0

$$f_2 = \bar{b}\bar{c} + \bar{a}bc$$

ab \ cd	00	01	11	10
00	0	1	0	0
01	0	0	0	1
11	0	0	0	1
10	1	0	0	0

$$f_3 = \bar{a}\bar{b}c\bar{d} + \bar{a}b\bar{c}\bar{d} + \bar{a}b\bar{d}$$

logic diagram (positive logic)



2)

	$\frac{xy}{2}$					
		00	01	11	10	
A	0	0	0	1	0	3 4
	1	1	1	0	1	

	$\frac{xy}{2}$					
		00	01	11	10	
\bar{A}	0	1	1	0	1	3
	1	0	0	1	0	

	$\frac{xy}{2}$					
		00	01	11	10	
B	0	1	0	1	0	2 4
	1	1	0	1	0	

	$\frac{xy}{2}$					
		00	01	11	10	
\bar{B}	0	0	1	0	1	2
	1	0	1	0	1	

	$\frac{xy}{2}$					
		00	01	11	10	
C	0	0	0	0	0	2 2
	1	0	1	0	1	

	$\frac{xy}{2}$					
		00	01	11	10	
\bar{C}	0	1	1	1	1	3
	1	1	0	1	0	

	$\frac{xy}{2}$					
		00	01	11	10	
D	0	0	1	0	1	4
	1	1	0	1	1	

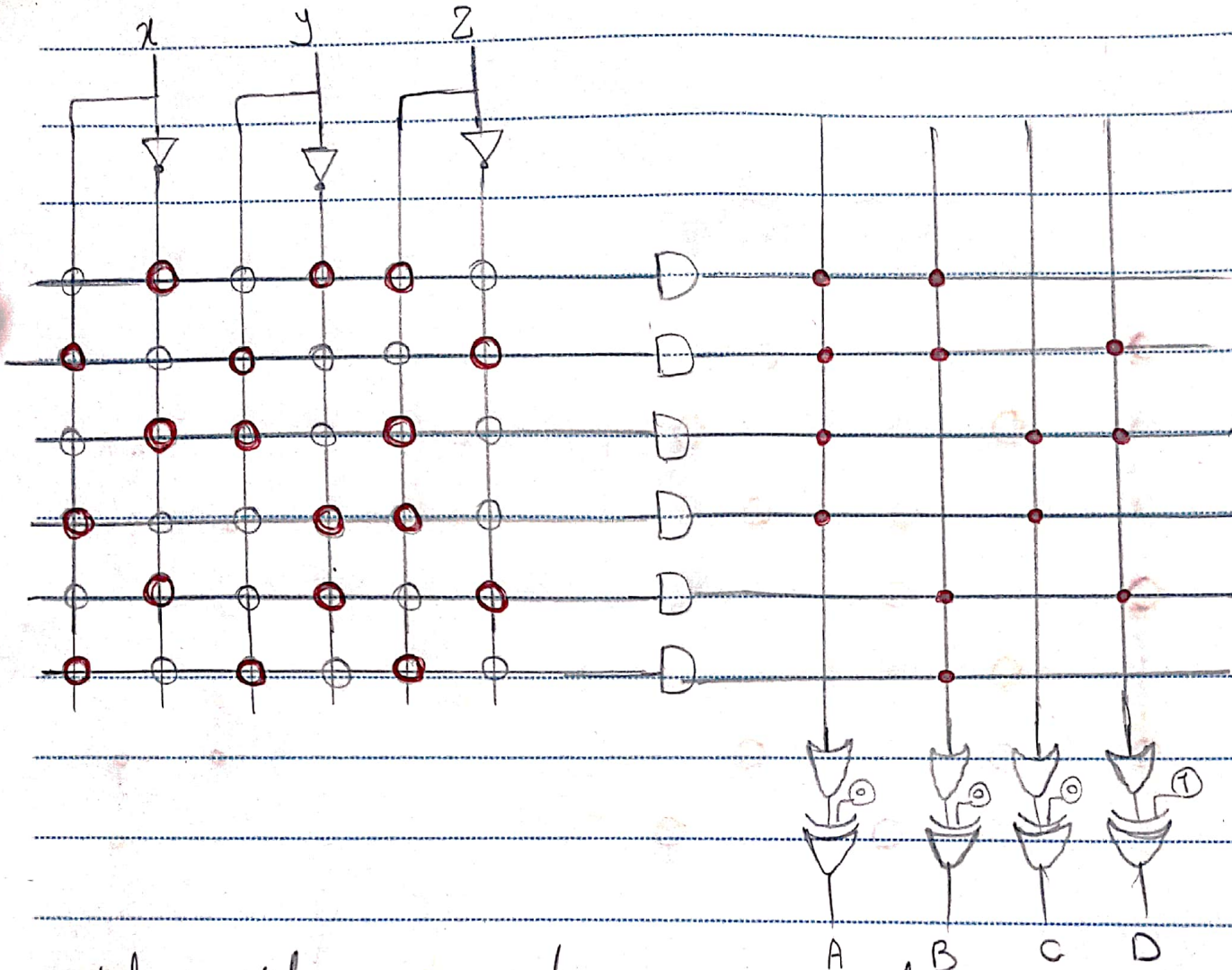
	$\frac{xy}{2}$					
		00	01	11	10	
\bar{D}	0	1	0	1	0	3 3
	1	0	1	0	0	

چون منیم تعداد product term ها را می خواهیم باید هر حالت بررسی شود تا بیشترین میج های اشتراک را بداییم. حالت مطلوب برای A, B, C, \bar{D} است که 6 میج داریم.

$$xy\bar{z} + \bar{x}\bar{y}z + \bar{x}yz + x\bar{y}z + \bar{x}\bar{y}\bar{z} + x\bar{y}z$$



$$xy\bar{z} + \bar{x}\bar{y}z + \bar{x}yz + x\bar{y}z + \bar{x}y\bar{z} + xyz$$



product terms	product terms No	inputs			outputs			
		x	y	z	A	B	C	\bar{D}
$xy\bar{z}$	①	1	1	0	1	1	-	1
$\bar{x}\bar{y}z$	②	0	0	1	1	1	-	-
$\bar{x}yz$	③	0	1	1	1	-	1	1
$x\bar{y}z$	④	1	0	1	1	-	1	-
$\bar{x}y\bar{z}$	⑤	0	0	0	-	1	-	1
xyz	⑥	1	1	1	-	1	-	-

3,

Q_n	T	Q_{n+1}	J	K
0	0	0	0	X
0	1	1	1	X
1	0	1	X	0
1	1	0	X	1

Q_n	Q_{n+1}	J	K
0	0	0	X
0	1	1	X
1	0	X	1
1	1	X	0

$J \backslash Q_n$	0	1
0	0	1
1	X	X

$J=T$

$K \backslash Q_n$	0	1
0	X	X
1	0	1

$K=T$

