

# STA 674

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Regression Analysis And Design Of Experiments

Advanced Concepts – Lecture 3

Pseudoreplication



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## Pseudoreplication

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- Last time, talked about analysis of split plot designs and fixed versus random effects.
- This time, we're going to discuss a pitfall to avoid in study design: pseudoreplication.

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## Pseudoreplication

### Example – aerial spraying of crop types, revisited

- An agricultural scientist wants to compare the effects of two aerially sprayed insecticides on the yield of corn using a field that is 100 m wide by 75 m deep. She can only spray the insecticides in strips that are 25 m wide, so she proceeds as follows:
  1. She divides the field width-wise into 4 25-m. strips,
  2. she randomly assigns an insecticide to each strip,
  3. she plants corn in 3 25 m×25 m plots within each strip.
- After the corn is harvested compares the mean yield for the 2 insecticides using a two-sample t-test with 6 replicates of each insecticide.
- *Why is this not a split-plot design?* there's no second randomization of the corn...because it's all corn
- *What is the problem with the test she has used?* overstating the amount of information obtained...it's really just two observations of each insecticide (even though she 'split' each strip into threes)...pseudoreplicates



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## Pseudoreplication

### Pseudoreplication

- Pseudoreplication occurs when repeated observations are obtained from a single experimental unit and treated as if they were independent measurements.

### Problem

- Pseudoreplication artificially decreases the experimental error:
  - $p$ -values will be too small, over-expressing significance,
  - confidence intervals will be too narrow, over-stating precision.

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## Pseudoreplication

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### Example – fish fat

- A fisheries researcher wants to compare the accumulation of toxins by three species of fish. He places three fish from each species in 9 separate tanks and adds the same amount of toxin to each tank. At the end of the experiment he measures the amount of toxin from:
    - 3 samples of fat
    - from each of 3 fish
    - from each of the 3 species.
1. What are the experimental units? tanks
  2. How many replicates are there for each species?
  3. What type of variation do we need to estimate to test differences between species?



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## Pseudoreplication

- Extent of the Problem

Scrutiny of 176 experimental studies published between 1960 and the present revealed that Pseudoreplication occurred in 27% of them, or 48% of all such studies that applied inferential statistics. (Hurlbert, 1983)

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## Analysis of Balanced Data with Pseudoreplicates

Two equivalent approaches:

1. Model both levels of variation with a mixed effects model.
2. Average over the pseudoreplicates for each experimental unit and apply a fixed effects model

## Analysis of Unbalanced Data with Pseudoreplicates

Only one approach:

1. Model both levels of variation with a mixed effects model.



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## Analysis of Balanced Data with Pseudoreplicates

Approach #1: Model both levels of variation with a mixed effects model

```
PROC MIXED data=fish;  
CLASS species fish sample;  
MODEL fat=species / DDFM=satterth;  
RANDOM fish(species);  
LSMEANS species / CL;  
RUN;
```



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### Analysis of Balanced Data with Pseudoreplicates

Incorrect approach:

```
TITLE 'Fish Fat -- incorrect analysis';  
PROC GLM DATA=fish;  
CLASS species;  
MODEL fat=species;  
LSMEANS species / CL;  
RUN;
```