Breast Ultra-Sound image segmentation: an optimization approach based on super-pixels and high-level descriptors

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ABSTRACT

This document shows the desired format and appearance of a manuscript prepared for the Proceedings of the SPIE. It contains general formatting instructions and hints about how to use LaTeX. The LaTeX source file that produced this document, `article.tex` (Version 3.3), provides a template, used in conjunction with `spie.cls` (Version 3.3).

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1. INTRODUCTION

Breast cancer is the second most common cancer (1.4 million cases per year, 10.9% of diagnosed cancers) after lung cancer, followed by colorectal, stomach, prostate and liver cancers.[1] In terms of mortality, breast cancer is the fifth most common cause of cancer death. However, it is ranked as the leading cause of cancer death among females in both western countries and economically developing countries.[2]

Due to reasons further detailed in the final manuscript, there is a growing interest in the medical community to incorporate Ultra-Sound (US) screening as part of the standard procedure of breast cancer screening.[3] This encourages the development of Computer Aided Diagnose (CAD) systems applied to BUS images.

Figure 1 offers a compact, brief and visual idea of breast's structure, their render in a 2D BUS image, and which markers are recommended to study in order to produce a diagnosis.[3] All these markers either describe the lesion's delineation, or describe the relation between the lesion and the surrounding tissue, which also requires a delineation of the lesion to differentiate between the two. [*]

When radiologists read an image to produce a diagnosis by analysing the markers, there is no need for an explicit delineation of the tissues or lesions present in the image since this is intrinsic to the reading process. However, developing accurate segmentation methodologies breast lesions and structures is crucial for developing CAD systems.

This article proposes a highly modular and flexible framework for segmenting lesions and tissues present in BUS images. The proposal takes advantage of an energy-based strategy to perform segmentations based on discrete optimization using super-pixels and a set of novel features analogous to the elements present in fig. 1.

2. SEGMENTATION METHODOLOGY DESCRIPTION

Optimization methodologies offer a standardized manner to approach segmentation by minimizing an application-driven cost function.[5] Figure 2 illustrates a generic representation of the segmentation strategy here adopted to delineate breast tissues or lesions in US images. The overall segmentation can be seen as a three steps strategy: (1) a mapping or encoding of the image into a discrete set of elements $\mathcal{S}$, (2) the optimization stage which is formulated as *metric labelling* problem, and (3) re-mapping the labels obtained from the previous stage to produce the final delineation.

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[*]More details regarding the visual cues used by radiologist would be present in the final manuscript as a building block for feature extraction

(a) Breast structure

(b) Breast structure location when USscreening

(c) Breast lesion characteristics in US screening influencing clinical management[4]
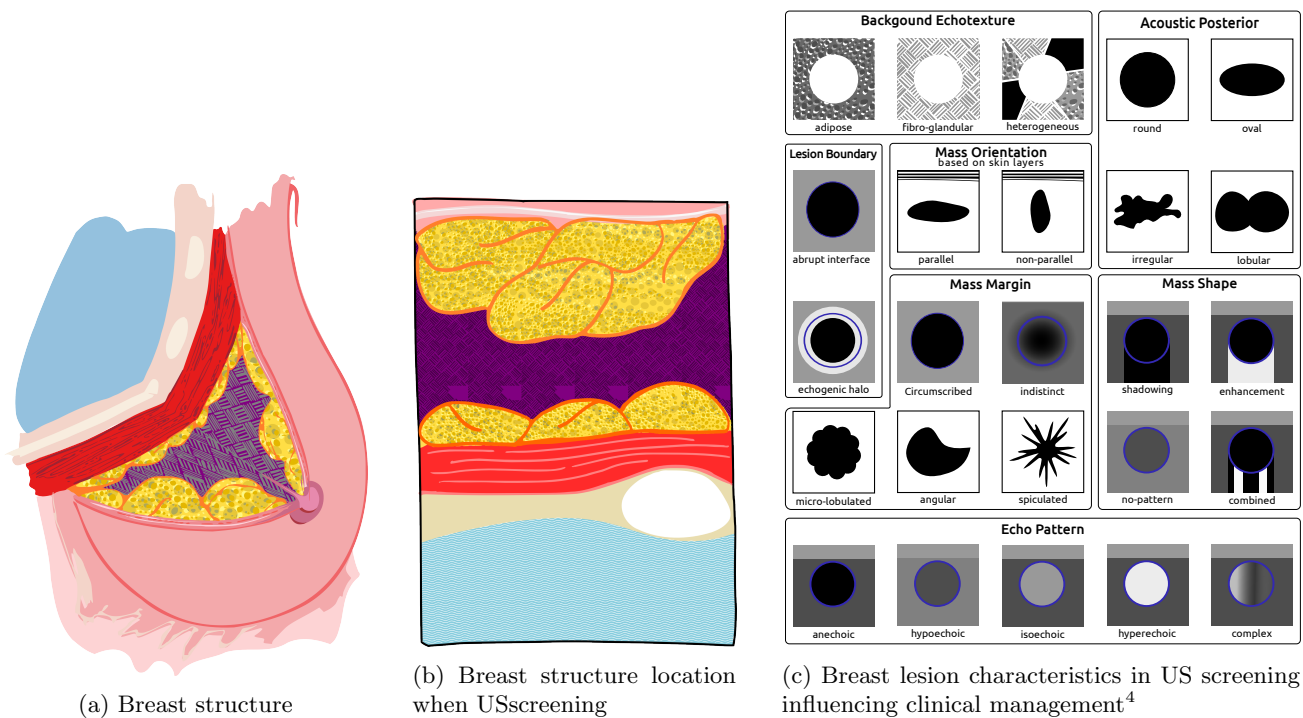
Figure 1: Visual reference of breast structures and visual cues used for standard BUS image assessment and diagnosis.

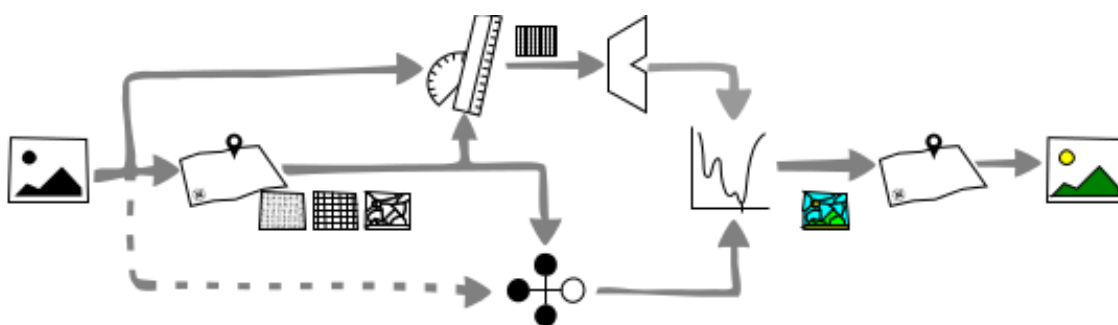Figure 2: Conceptual block representation of the segmentation methodology

(a) Problem definition

(b) Data term

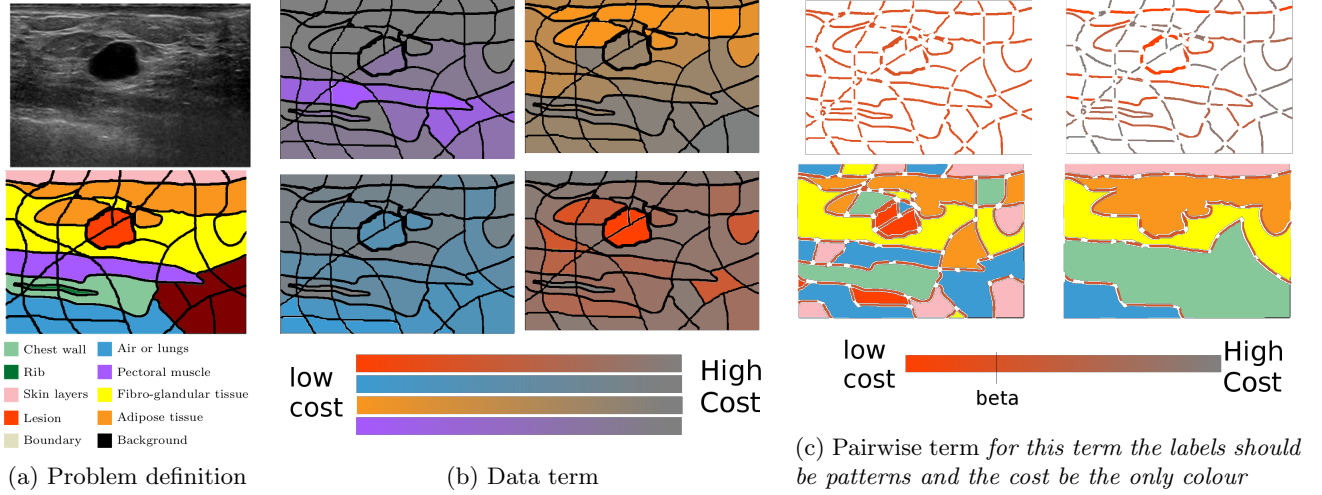(c) Pairwise term *for this term the labels should be patterns and the cost be the only colour*

Figure 3: Methodology terms interpretation

In order to formulate the segmentation like a metric labelling problem, the image is conceived as a discrete set of elements $\mathcal{S}$ that need to be labelled using a label l from the labelling set $\mathcal{L}$ (i.e. $l \in \{\text{lesion}, \overline{\text{lesion}}\}$ or $l \in \{\text{lungs}, \text{fat}, \cdots, \text{lesion}\}$). Let $\mathcal{W}$ be all the possible labelling configurations of the set $\mathcal{S}$ given $\mathcal{L}$; and, let $U(\cdot)$ be a cost function encoding how good is a labelling configuration $\omega \in \mathcal{W}$ based on the appearance of the elements in $\mathcal{S}$, their inner relation and some desig constraints. Then, the desired segmentation $\hat{\omega}$ corresponds to the labelling configuration that minimize this cost function, as described in eq. (1).

$$\hat{\omega} = \arg\min_{\omega} U(\omega) \tag{1}$$

The nature of $U(\cdot)$ and $\mathcal{W}$ dictates which minimization strategies should be applied to find ω sine not every strategy is suitable or desirable.

Equation (2) determines this cost function as the combination of two independent costs that need to be simultaneously minimized as a whole. The left hand side of the expression integrates the so called *data* term, while the right hand side integrates the *pairwise* term, which is also referred as the *smoothing* term. Both terms are shaped by $\mathcal{S}$ and evaluated in $\mathcal{W}$.

$$U(\omega) = \sum_{s \in s} D_s(\omega_s) + \sum_{s} \sum_{r \in \mathcal{N}_s} V_{s,r}(\omega_s, \omega_r) \tag{2}$$

Figure 3 illustrates the terms and elements relating the framework's outline, presented in fig. 2, with its formulation in eq. (2). The problem of delineating the tissues present in BUS image has been used here for this illustrative purposes.

In general, $\mathcal{S}$ can be any discrete set representing the image (i.e. pixels, overlapping or non overlapping windows, etc.). For this work $\mathcal{S}$ is chosen to be a super-pixels representation of the image,[6] though. Figure 3a shows a BUS image example and a its associated super-pixels representation $\mathcal{S}$ coloured according to the image's Ground Truth (GT).

Bear in mind that given an unseen BUS image, the ultimate goal is to represent the image as a set of super-pixels and infer the appropriated labelling for each of them. To do so using the strategy here proposed, it requires to define: a data term, a pairwise term, and a proper minimization methodology.

2.1 Data term

Given a label configuration $\omega \in \mathcal{W}$, the data term penalizes the labelling of a particular image element or site ($\omega_s = l$) based on the data associated to s. In this manner $D_s(\omega_s = l_{\checkmark}) << D_s(\omega_s = l_{\times})$. To perceive the effect or behaviour of this data term, fig. 3b shows some labelling configurations ω' where all the sites share the same label, $\omega' \in \{\omega_s = l, \ \forall s \in \mathcal{S}\}$

Designing $D(\cdot)$ that accomplish the desired behaviour by defining an obscure heuristic, is rather complicated task to achieve out of the box. Therefore, an easier and cleaner approach is to take advantage of Machine Learning (ML) techniques to design this data cost in a systematic manner based on a training stage. The idea is to generate image or data model for each class from training samples, and let $D(\cdot)$ be a distance or goodness measure reflecting the likelihood for s to to belong to class l. Defining the data term in this manner allows for great flexibility while offering a systematic approach towards its design. $D(\cdot)$ is fully customizable through the features, through the construction of the model where several classifiers and training techniques can be applied; or through definition of the relation between the testing sample and the data models.

This type of data term is incorporated to our framework as represented at the upper side of the diagram in fig. 2. Each site s is treated as a sample and the features to describe it are extracted from the original image. For the work here reported, a Support Vector Machine (SVM) classifier is used to determine the data model during the training stage. During testing stage $D_s(\omega_s = l)$ corresponds to the distance between the testing sample and the model associated to l as the SVM classification reward.

Further discussion regarding the feature choices can be found in **??**, whereas other designing choices regarding ML are out of the scope for this work.

2.2 Pairwise or smoothing term

The pairwise term represents the cost of the assignation ω_s taking into account the labels of its neighbour sites, ω_r, $r \in \mathcal{N}_s$. This term models a Markov Random Fields (MRFs) or a Conditional Random Fields (CRFs). The typical form of this term, given in eq. (3), is called homogenization which acts as a regularization factor favouring configurations that have coherent labelling.

$$V_{s,r}(\omega_s, \omega_r) = \begin{cases} \beta, & \text{if } \omega_s \neq \omega_r \\ 0, & \text{otherwise} \end{cases} \tag{3}$$

Figure 3c offers a visual interpretation of this cost. If the resulting segmentation associated to the current labelling configuration ω has a boundary segment, this boundary brings a penalization β to the total cost $U(\omega)$. In this manner the regularization term can be seen as a post-processing or denoising stage since some sites will flip their labelling if the cost of producing and edge is larger than the cost of adopting the neighbour's label.

More sophisticated smoothing terms where boundaries have different penalization based not only on site relations in $\mathcal{S}$ but also based on image information would (see fig. 3c) be found in the final version of the document in **??**.

2.3 Searching the best labelling configuration

Once defined $U(\omega)$ so that the cost for a particular labelling configuration ω can be computed, the problem of finding $\hat{\omega}$ corresponding to the global minimum of the space $\mathcal{W}$ of all possible labelling configurations needs to be faced.

This problem falls into the category of NP-hard problems. More over, due to limitations in building $U(\cdot)$ such as noise, training policies, etc. there are no guarantees that the global minimum $\hat{\omega}$ corresponds to the true labelling.

Nevertheless, there is a large body of literature proposing methodologies to find suboptimal solutions to the problem trading-off between time of convergence and accuracy of the solution reached. Szeliski et al.[7] conducted an exhaustive review in terms of solution quality and runtime of the most common energy minimization

algorithms used in Computer Vision (CV), such as Iterated Conditional Modes (ICM), Simulate Anealing (SA) or Graph-Cuts (GC).

The minimization strategy used for this work is GC. This technique was initially introduced to solve CV applications by Boykov et al.[8] Soon after its introduction, it become the minimization technique of choice for CV problems. Since, when GC is applicable, it allows to rapidly find a strong local minima guaranteeing that no other minimum with with lower energy can be found.[9] GC is applicable if, and only if, the pairwise term favours coherent labelling configurations and penalizes labelling configurations where neighbours labels differs. Such is our case, given eq. (3).

3. FEATURE DESCRIPTION

Features description

ACKNOWLEDGMENTS

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