

Informe RSA

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1. Estructura del main()

```
int main(){  
rsa_bloques Elle(1024);
```

string message = "The idea of an asymmetric public-private key cryptosystem is attributed to Whitfield Diffie and Martin Hellman, who published this concept in 1976. They also introduced digital signatures and attempted to apply number theory. Their formulation used a shared-secret-key created from exponentiation of some number, modulo a prime number. However, they left open the problem of realizing a one-way function, possibly because the difficulty of factoring was not well-studied at the time.[4] Ron Rivest, Adi Shamir, and Leonard Adleman at the Massachusetts Institute of Technology, made several attempts over the course of a year to create a one-way function that was hard to invert. Rivest and Shamir, as computer scientists, proposed many potential functions, while Adleman, as a mathematician, was responsible for finding their weaknesses. They tried many approaches including knapsack-based and permutation polynomials. For a time, they thought what they wanted to achieve was impossible due to contradictory requirements.[5] In April 1977, they spent Passover at the house of a student and drank a good deal of Manischewitz wine before returning to their homes at around midnight.[6] Rivest, unable to sleep, lay on the couch with a math textbook and started thinking about their one-way function. He spent the rest of the night formalizing his idea, and he had much of the paper ready by daybreak. The algorithm is now known as RSA – the initials of their surnames in same order as their paper.[7] Clifford Cocks, an English mathematician working for the British intelligence agency Government Communications Headquarters (GCHQ), described an equivalent system in an internal document in 1973.[8] However, given the relatively expensive computers needed to implement it at the time, it was considered to be mostly a curiosity and, as far as is publicly known, was never deployed. His discovery, however, was not revealed until 1997 due to its top-secret classification. Kid-RSA (KRSA) is a simplified public-key cipher published in 1997, designed for educational purposes. Some people feel that learning Kid-RSA gives insight into RSA and other public-key ciphers, analogous to simplified DES.[9][10][11][12][13] A patent describing the RSA algorithm was granted to MIT on 20 September 1983 U.S. Patent 4,405,829 Cryptographic communications system and method. From DWPIs abstract of the patent The system includes a communications channel coupled to at least one terminal having an encoding device and to at least one terminal having a decoding device. A message-to-be-transferred is enciphered to ciphertext at the encoding terminal by encoding the message as a number M in a predetermined set. That number is then raised to a first predetermined power (associated with the intended receiver) and finally computed. The remainder or residue, C, is... computed when the exponentiated number is divided by the product of two predetermined prime numbers (associated with the intended receiver). A detailed description of the algorithm was published in August 1977, in Scientific Americans Mathematical Games column.[7] This preceded the patents filing date of December 1977. Consequently, the patent had no legal standing outside the United States. Had Cocks's work been publicly known, a patent in the United States would not have been legal either. When the patent was issued, terms of patent were 17 years. The patent was about to expire, on 21 September 2000, when RSA Security released the

algorithm to the public domain, on 6 September 2000.[14] There are a number of attacks against plain RSA as described below. When encrypting with low encryption exponents (e.g., $e = 3$) and small values of the m , (i.e., $m < n^{1/e}$) the result of m^e is strictly less than the modulus n . In this case, ciphertexts can be decrypted easily by taking the e th root of the ciphertext over the integers. If the same clear text message is sent to e or more recipients in an encrypted way, and the receivers share the same exponent e , but different p , q , and therefore n , then it is easy to decrypt the original clear text message via the Chinese remainder theorem. Johan Håstad noticed that this attack is possible even if the cleartexts are not equal, but the attacker knows a linear relation between them.[22] This attack was later improved by Don Coppersmith (see Coppersmith's attack).[23] Because RSA encryption is a deterministic encryption algorithm (i.e., has no random component) an attacker can successfully launch a chosen plaintext attack against the cryptosystem, by encrypting likely plaintexts under the public key and test if they are equal to the ciphertext. A cryptosystem is called semantically secure if an attacker cannot distinguish two encryptions from each other, even if the attacker knows (or has chosen) the corresponding plaintexts. As described above, RSA without padding is not semantically secure.[24] RSA has the property that the product of two ciphertexts is equal to the encryption of the product of the respective plaintexts. That is $m_1 m_2^e \pmod{n}$. Because of this multiplicative property a chosen-ciphertext attack is possible. E.g., an attacker who wants to know the decryption of a ciphertext $c = m^e \pmod{n}$ may ask the holder of the private key d to decrypt an unsuspecting-looking ciphertext $c' = r^e c \pmod{n}$ for some value r chosen by the attacker. Because of the multiplicative property c' is the encryption of $mr \pmod{n}$. Hence, if the attacker is successful with the attack, they will learn $mr \pmod{n}$ from which they can derive the message m by multiplying mr with the modular inverse of r modulo n . [citation needed] Given the private exponent d one can efficiently factor the modulus $n = pq$. And given factorization of the modulus $n = pq$, one can obtain any private key (d, n) generated against a public key (e, n) . [15] To avoid these problems, practical RSA implementations typically embed some form of structured, randomized padding into the value m before encrypting it. This padding ensures that m does not fall into the range of insecure plaintexts, and that a given message, once padded, will encrypt to one of a large number of different possible ciphertexts. Standards such as PKCS1 have been carefully designed to securely pad messages prior to RSA encryption. Because these schemes pad the plaintext m with some number of additional bits, the size of the un-padded message M must be somewhat smaller. RSA padding schemes must be carefully designed so as to prevent sophisticated attacks that may be facilitated by a predictable message structure. Early versions of the PKCS1 standard (up to version 1.5) used a construction that appears to make RSA semantically secure. However, at Crypto 1998, Bleichenbacher showed that this version is vulnerable to a practical adaptive chosen ciphertext attack. Furthermore, at Eurocrypt 2000, Coron et al.[25] showed that for some types of messages, this padding does not provide a high enough level of security. Later versions of the standard include Optimal Asymmetric Encryption Padding (OAEP), which prevents these attacks. As such, OAEP should be used in any new application, and PKCS1 v1.5 padding should be replaced wherever possible. The PKCS1 standard also incorporates processing schemes designed to provide additional security for RSA signatures, e.g. the Probabilistic Signature Scheme for RSA (RSA-PSS). Secure padding schemes such as RSA-PSS are as essential for the security of message signing as they are for message encryption. Two USA patents on PSS were granted (USPTO 6266771 and USPTO 70360140); however, these patents expired on 24 July 2009 and 25 April 2010, respectively. Use of PSS no longer seems to be encumbered by patents.[original research] Note that using different RSA key-pairs for encryption and signing is potentially more secure.[26]";

```
cout << "\nmessage: " << message << endl;
ZZ n;
ZZ e;
cout << "\nn: "; cin >> n;
cout << "\ne: "; cin >> e;

cout << "\nmensaje cifrado" << endl;
cout << Elle.encrypt(Elle.dividirBloques(message),n,e) << endl;
```

```
string firma = "Cledy Becerra, 71666666, 11-333-1111";
cout << "\nfirma: \n" << endl;
cout << Elle.sign_encrypt(firma,n,e);
```

```
/*string message =
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8760997766929993295123184390860480823644329656940979911860918947182824769930053562
5210901697950300611563999494279098669625352630883895284076394212895323814714556807
6992367944029018547464932414628843179588958088519628948333089297891094710225091820
1172898433827507402794810689426726617211542897780459542267628307298999861544354457
7108870214559672594945582955906351040354426013574942127371237185878276121379144029
9417792513962880202726327544058990807884871136657965847594284983975972518363508589
7147143102008936398341539810045877012243040080552986250008757577643711986320479317
3906271023007297687515426437502455486892740273605886650280334721687663098106657479
3201396079105280448978225007142675659676090952401166156192762058676863349381051705
4301164195917985268434799501486383755577723597721950719791800581683611588936334765
8385339637837023208818060143429242502362550954776616591843135098247066190158474795
2153423916872344375641603766972834312179049040611160209093197898132950854183653001
9119873096060761023463689715645176680343302772610251742799944016803026455934621906
7240694697187357348627784198313506452113113253421393470444999891789180408898611540
3780434311950357656787764852420748204913306594841919774528186310074650041911140958
2004677828199192922314607237007742031764178371838082393569045205321492201380881782
4519231623673246743481883945343004857732094154811800318581908811726260098825407473
0685489980043709520662450406196004407737118730998156418876361965060647187938244801
0838573103947025904805600341281274836590172125624107399103454285353587092410655695
4550630883185774183163293897930334035099213825110705239552276005051940545633369305
9424601894323299920562098043657864989517685084192520140115744690794968493713722662
7678260772057135051442435037045621661826828560589632952600904660998256395760050804
2036595609231175140351241896447680554741359893239069670477590181301929717579755471
0255903345883978921704509725942884441245410952436632602704933155023825251904296457
0060557214920658995519278612341056639440267671705105854239969899970113180667788376
8436372765140174571578232399037004857441511555842741840811265915962363233893562197
6508177543944576986503224805851014013059103091144093863830417353139695186205757298
7344745529698112205735650766931917417560562925910566301326768711115732730240384522
2106340723540770127109054532811497983971609150975822296508132068661821103765239779
1550913501805518053866451396879941495712888855534086713741921405427824114255892768
3720882708658233026834379453555158668692552849096698203402596780541731193503359229
9655810685697101630893110669511651313389857179278900163451260454639093646004485423
2189543902411265107725237068771892798571647019598800541803284940785035333331470941
4794667351158987353386776573290567239065709230637745804705789036115229996878264601
3083978062";

```
cout << "\nmensaje: \n" << message << endl;
```

```
cout << "\nmensaje decifrado: " << endl;  
cout << Elle.decrypt(message) << endl;*/
```

```
/*ZZ n=
```

```
conv<ZZ>("853991922719896096503152601516856098693891821176223242685212919844208112  
8606266812965474423514260301370452733540760560658962552656301537875246168230782105
```

```

2579684275448776212306112922545681109178618798090130834664457261301431717909117641
4240666481797844358448664672963675776535072548378114898923212457412662294522440252
7862321175537556593241910726554277889051590319896721594908297650416866781267903004
4230054587815089927460923550663681303107337679126994703508166888754057212216526773
3614789006301134608595826246786118625402728175031177671563655976662151785830751312
8592910977571611257319190630187290454598957622902171");

```

```
ZZ e=
```

```

conv<ZZ>("835557209532937823961444966612144536310933339452294518435136096991532776
2283885135927417629864524571641058079948221737692176994591249324455944905035840775
2924921797079034310359090205882622610610193614608737352128716359413459308157267751
487567975401279393207985294366538400151500759751517041559305331773327601");

```

```
string firma =
```

```

"013370792928678654627281398596604959279025247936896396384234606374010519952712755
3880389242335140489950994729070620566667513397358600117079279076501143160853099267
0089855600095241556849467581874898147176415592241961980255278976254715788516636912
5974093955115194216885896318925781867239739737195823540084845729975065931512990538
4982950609042953615233430146803237145852544881166617002059490265334080334979593578
4479344646774651717143767801055750055643232155635333642258199267581851043903510834
8606123094867694614303214940971635340718730123916177129401058378745407978509592864
2197697265753154592998833084746036004352484302598941690137816474219242302085339122
6584586519410935060137709999884902563272543231836792533276251231318515286872040095
3929212369614154249979818023143892227214082829168331025547808944724431251785124073
2444922392761730906454202881917678055140942103094107336344693056132712409426444003
6213516235540573042448226494173995242666764649604000765555773914019338675257165506
8332145397932430996507881357625323177857702250273048339487478211592172568543394528
5307548286657766056719992392127917328754581122544879466770546154778594201881939057
6152287954303694403703734163510782747879787141284277511066686239924568348907301233
27564";

```

```
cout << "\nfirma: \n" << firma << endl;
```

```
cout << "\nfirma: " << endl;
```

```
cout << Elle.remove_sign(firma,n,e);*/
```

```
return 0;
```

```
}
```

2. Generación de claves

o Generación de números aleatorios

// En esta función accedemos a la arquitectura del computador donde en la variable processInfo guardamos los procesos:

```

void random::fillWithMemoryInfo() {
    DWORD aProcesses[1024], cbNeeded, cProcesses;
    if (EnumProcesses(aProcesses, sizeof(aProcesses), &cbNeeded)) { //obtiene los
        procesos en aProcesses
        cProcesses = cbNeeded / sizeof(DWORD);
    }
}

```

//Calcula cuántos procesos fueron retornados.

```

        for (int i = 100; i < cProcesses; i++){
            HANDLE hProcess = OpenProcess(PROCESS_QUERY_INFORMATION |
PROCESS_VM_READ, FALSE, aProcesses[i]);
            if (NULL != hProcess){
                PROCESS_MEMORY_COUNTERS pmc;
                if (GetProcessMemoryInfo(hProcess, &pmc, sizeof(pmc))) {

processInfo+=(to_string(pmc.PageFaultCount)+to_string(pmc.WorkingSetSize)+

to_string(pmc.QuotaPagedPoolUsage)+to_string(pmc.QuotaNonPagedPoolUsage)+to
_string(pmc.PeakPagefileUsage));
                }
            }
            CloseHandle(hProcess);
        }
    }
}
//Generamos nuestra semilla
vector<int> random::generateSeed(){
    if((processInfo.size()<contador+15)||processInfo.empty()){
        processInfo.clear();
        fillWithMemoryInfo();
        contador=0;
    }
    vector<int> k;
    for(int i=0, j=contador; i<5; i++, j+=3){
        int n=stoi(processInfo.substr(j,3));
        while(n>255) n>>=1;
        while(n<128) n<<=1;
        k.push_back(n);
    }
    contador+=15;
    return k;
}

vector<bool> random::RC4(vector<int> semilla){
    vector<int> Or;
    //permite que S solo pertenezca a este scope
    vector<int> S;
    for(int i=0; i<256; i++) S.push_back(i);
    //permite que k solo exista en este scope, optimiza memoria
    vector<int> K;
    for(int i=0, k=0; i<=51; i++)
        for(int j=0; j<5; j++, k++)
            K.push_back(semilla[j]);
    for(int i=0, f=0; i<256; i++){
        f=modint(f+S[i]+K[i], 256);
        swap(S[i], S[f]);
    }
    for(int i=0, f=0, k=0; k<8; k++){
        i=modint(i + 1, 256);
        f=modint(f+S.at(i), 256);
        swap(S.at(i), S.at(f));
        Or.push_back(S.at(modint(S.at(i) + S.at(f), 256)))/t
    }
}

```

```

    }
}
vector<bool> out;
for(int i=0;i<8;i++){
    bitset<8> aux(Or[i]);
    for(int j=0;j<8;j++)
        out.push_back(aux[j]);
}
return out;
}

```

```

void izqRotate(vector<bool> &vec, int times){
    //Rota times veces el vector llevando el primero al ultimo y borrando los primeros
    vec.insert(vec.end(),vec.begin(),vec.begin()+times); //Agrega al final del vector
    times elementos del inicio del vector
    vec.erase(vec.begin(),vec.begin()+times); //borra los primeros times valores.
}

```

//Arrays que tienen maximo como número máximo 64 y son al azar

//PC_1 tiene 56 números y PC_2 tiene 48

int

PC_1[]={56,48,40,32,24,16,8,0,57,49,41,33,25,17,9,1,58,50,42,34,26,18,10,2,59,51,43,35,62,54,46,38,30,22,14,6,61,53,45,37,29,21,13,5,60,52,44,36,28,20,12,4,27,19,11,3};

int

PC_2[]={13,16,10,23,0,4,2,27,14,5,20,9,22,18,11,3,25,7,15,6,26,19,12,1,40,51,30,36,46,54,29,39,50,44,32,47,43,48,38,55,33,52,45,41,49,35,28,31};

int rotaciones[]={1,1,2,2,2,2,2,2,1,2,2,2,2,2,2,1,1,1,2,2,2,2}; //propia del DES

//PC elección permutada

//Hacemos uso de la generación de claves de DES

//Donde teóricamente se usan 56 bits de la clave

//Teóricamente son 64 bits del PC_1 pero por paridad que no la necesitamos usamos sólo 56 bits

//Teóricamente se usan 48 bits de la subclave para PC_2

```

vector<bool> DES(int bits=1024){
    vector<bool> K; //para guardar todas las k
    {
        vector<bool> k=RC4(generateSeed()); //64 bools o bits
        int nBits=bits/48+1;
        vector<bool> c; vector<bool> d;
        for(int i=0;i<28;i++) c.push_back(k.at(PC_1[i])); //Añade cierta posición de k en c
        //entre las posiciones adquiridas esta los primeros 28 números de PC_1
        for(int i=28;i<56;i++) d.push_back(k.at(PC_1[i])); //Añade cierta posición de k en d
        //entre las posiciones adquiridas está de 28 a 56 números de PC_1
        for(int i=0;i<nBits;i++){
            izqRotate(c,rotaciones[i]);
            izqRotate(d,rotaciones[i]); //Rotara los vectores rotaciones[i] veces
            vector<bool> both(c.begin(),c.end()); //Vector duplicamos con los valores de c
            both.insert(both.end(),d.begin(),d.end()); //Agregamos todo el vector de d
            for(int i=0;i<48;i++) K.push_back(both.at(PC_2[i])); //Agregamos a k cierta
            //posición de both entre las posiciones 0-48 de Pc_2
        }
    }
}

```

```

K.resize(bits);//Modifica el k para quedar con cierto número de bits
K[0]=1; K[bits-1]=1;//Primer y ultimo valor de k sera 1
return K;
}

//Convierte un vector booleano a ZZ tomándolo como número binario
ZZ random::generate_random(int bits){
    return Random_Number(DES(bits));
}

```

o Generación de primos

```

bool Miller_Rabin(ZZ d, ZZ n){

    ZZ a; a=2;
    ZZ x = Power_mod(a, d, n);
    if (x == 1 || x == n-1)return true;
    while (d != n-1){

        x = modulo((x * x), n);
        d *= 2;
        if (x == 1)return false;
        if (x == n-1)return true;
    }

    return false;
}

bool isPrime(ZZ n){
    ZZ k; k=0;
    if (n <= 1 or n == 4)return false;
    if (n <= 3)return true;

    ZZ d = n - 1;
    while (even(d)){
        //d /= 2;
        d >>= 1;
        k++;
    }
    for (int i = 0; i < k+1; i++)
        if (!Miller_Rabin(d, n))
            return false;

    return true;
}

ZZ gen_prime(ZZ n){//Encuentra el primo más cercano a un número aleatorio
    ZZ a= modulo(n, ZZ(6));
    n-=a+ZZ(5); //para obtener la forma 6n+5
    //Los números primos tienen la forma de 6n+1 y 6n+5, no necesariamente todos los números obtenidos con esa
    if(isPrime(n)) return n;//Si es primo retorna ese valor
    else{//Caso contrario busca los siguientes números de la forma 6n+1 y 6n+5 hasta encontrar un primo
        while(true){

```

```

        n+=2;
        if(isPrime(n)) return n;
        n+=4;
        if(isPrime(n)) return n;
    }
}
}

```

o Inversa

```

//evalúa si mcd es 1
bool Existe_Inversa(ZZ x, ZZ y){
    if(even(x)&&even(y)) return 0;
    while(x!=0){
        while(even(x)) x=x>>1;
        while(even(y)) y=y>>1;
        ZZ t=valAbs((x-y))>>1;
        if(x>=y) x=t;
        else y=t;
    }
    return y==ZZ(1);
}
//Determina si es par o impar
bool even(ZZ a){
    ZZ r=(a>>1)<<1;
    if(r<0) r=ZZ(2)+r;
    return r==a;
}
//Convertir en positivo-Valor Absoluto
ZZ valAbs(ZZ a){
    if (a<0) return (a*-1);
    return a;
}

```

o Euclides extendido

//Implementamos para Algoritmo Binario del MCD y lo combinamos con el extendido de euclides para retornar un bool para saber si tiene inversa o no.

```

ZZ inversa(ZZ r1, ZZ r2){
    ZZ s1=ZZ(1), s2=ZZ(0), b=ZZ(r2);
    if (Existe_Inversa(r1, r2)){
        while (r2>0){
            ZZ q=r1/r2;
            ZZ r=r1-q*r2;
            r1=r2;
            r2=r;
            ZZ s=s1-q*s2;
            s1=s2;
            s2=s;
        }
        if(s1<0) return s1+=b;
        return s1;
    }
}

```

```

    }
    else cout<<"No tiene inversa"<<endl;
    return ZZ(0);
}
//evalúa si mcd es 1
bool Existe_Inversa(ZZ x, ZZ y){
    if(even(x)&&even(y)) return 0;
    while(x!=0){
        while(even(x)) x=x>>1;
        while(even(y)) y=y>>1;
        ZZ t=valAbs((x-y))>>1;
        if(x>=y) x=t;
        else y=t;
    }
    return y==ZZ(1);
}
//Determina si es par o impar
bool even(ZZ a){
    ZZ r=(a>>1)<<1;
    if(r<0) r=ZZ(2)+r;
    return r==a;
}
//Convertir en positivo-Valor Absoluto
ZZ valAbs(ZZ a){
    if (a<0) return (a*-1);
    return a;
}

```

3. Formación de Bloques

o Llenar ceros

```

string rsa_bloques::completarCeros(string mensaje,ZZ Nr ){
    int digit =ZZtoStr(Nr).size()-1;
    int c = modint(mensaje.size(),digit);//las letras que no llegan a completar un
bloque
    string cero(digit-c,'0');///la cantidad de 0s que faltan
    return cero+mensaje;
}
int modint(int a,int n){
    int q=a/n;
    if(q<0) q--;
    return a-(n*q);
}

```

o ZZ a string

// Convertimos el número en string lo utilizamos en el cifrado y descifrado con y sin firma digital.

```

string rsa_bloques::ZZtoStr(ZZ z){
    stringstream ss;
    ss<<z;

```



```

    return ss.str();
}

```

o Dividir bloques

```

string rsa_bloques::dividirBloques(string mensaje){
    //Divide en bloques y completa para tener dígitos al igual que el número de dígitos mayor
    int digit=to_string(alfabeto.size()).size();//número de dígitos del alfabeto
    string str;
    {
        string cero(digit,'0');//string hecha de 0 para completar
        for(int i=0;i<mensaje.size();i++){
            size_t pos=alfabeto.find(mensaje.at(i));//size_t adquiere cualquier tipo de variable en los vectores
            int len=to_string(pos).size();//la longitud del número
            if(len<digit) str+=cero.substr(0,digit-len);//completa los 0
            str+=to_string(pos);
        }
    }
    digit=ZZtoStr(n).size()-1;
    while(modint(str.size(),digit)) str+="22";//Aquí completamos el mensaje con W para evitar espacios en blanco
    return str;
}

```

4. Exponenciación modular

```

ZZ Power_mod(ZZ base, ZZ exp, ZZ n){
    //Usamos exponenciación modular el documento
    //Exponenciación Modular Binaria
    ZZ salida(1);
    do{
        if(!even(exp))
            salida= modulo(salida * base, n);
        base= modulo(base * base, n);
        exp>>=1;
    }while(exp!=ZZ(0));
    return salida;
}
ZZ modulo(ZZ a, ZZ b){
    ZZ q= a / b;
    if(q<0) q--;
    return a-(b * q);
}

```

5. Función de cifrado

```

string rsa_bloques::encrypt(string mensaje, ZZ Nr, ZZ Er){
    int digit=ZZtoStr(Nr).size()-1;
    string out;

```

```

for(int i=0; i < mensaje.size(); i+=digit){
    ZZ p(conv<ZZ>(mensaje.substr(i, digit).c_str()));
    p=Power_mod(p,Er,Nr);
    string ceros((digit+1-ZZtoStr(p).size()),'0');
    out+=ceros+ZZtoStr(p);
}
return out;
}

```

6. Función de descifrado

```

string rsa_bloques::decrypt(string mensaje){
    string salida;
    int digitN=ZZtoStr(n).size();
    int digit=digitN-1;
    for(int i=0;i<mensaje.size();i+=digitN){
        ZZ c(conv<ZZ>(mensaje.substr(i,digitN).c_str()));
        c=TRC(c);
        string ceros((digit-ZZtoStr(c).size()),'0');
        salida+=ceros+ZZtoStr(c);
    }
    digit=to_string(alfabeto.size()).size();
    string outLetters;
    for(int i=0;i<salida.size();i+=digit){
        outLetters+=alfabeto.at(stoi(salida.substr(i,digit)));
    }
    return outLetters;
}

```

7. Firma digital

- Cifrado:

```

string rsa_bloques::sign_encrypt(string mensajeL, ZZ Nr, ZZ Er){
    string aux = encryptD(mensajeL);
    return encrypt(completarCeros(aux, Nr), Nr, Er);
}

```

```

string rsa_bloques::encryptD(string mensajeL){
    string mensajeNo = dividirBloques(mensajeL);
    int digit=ZZtoStr(n).size()-1;
    string out;
    for(int i=0;i<mensajeNo.size();i+=digit){
        ZZ c(conv<ZZ>(mensajeNo.substr(i,digit).c_str()));
        c=TRC(c);//se realiza una segunda versión para optimizar con el TRC y mayor
velocidad
        string ceros((digit+1-ZZtoStr(c).size()),'0');

```

```

        out=out+ceros+ZZtoStr(c);
    }
    return out;
}

```

- Descifrado:

```

string rsa_bloques::remove_sign(string mensaje, ZZ Ne, ZZ Ee){
    return decryptE(mensaje, Ne, Ee);
}

```

```

string rsa_bloques::decryptE(string mensaje, ZZ Ne, ZZ Ee){
    string salida;
    int digitN=ZZtoStr(n).size();
    int digit=digitN-1;
    for(int i=0;i<mensaje.size();i+=digitN){
        ZZ c(conv<ZZ>(mensaje.substr(i,digitN).c_str()));
        c=TRC(c);
        string ceros((digit-ZZtoStr(c).size()),'0');
        salida+=ceros+ZZtoStr(c);
    }
    string mensajeNo = salida;
    int a= modint(mensajeNo.size(), ZZtoStr(Ne).size());
    mensajeNo = mensajeNo.substr(a);

    string salida2;
    digit=ZZtoStr(Ne).size()-1;
    digitN=digit+1;
    for(int i=0; i < mensajeNo.size(); i+=digitN){
        ZZ c(conv<ZZ>(mensajeNo.substr(i, digitN).c_str()));
        c=Power_mod(c,Ee,Ne);
        string ceros((digit-ZZtoStr(c).size()),'0');
        salida2+=ceros+ZZtoStr(c);
    }
    digit=to_string(alfabeto.size()).size();
    string outLetters;
    for(int i=0;i<salida2.size();i+=digit){
        outLetters+=alfabeto.at(stoi(salida2.substr(i,digit)));
    }
    return outLetters;
}

```

8. TRC

```

ZZ rsa_bloques::TRC(ZZ M){
    ZZ q1= inversa(modulo(q, p), p);
    ZZ a1= Power_mod(modulo(M, p), modulo(d, p - 1), p);
    ZZ q2= inversa(modulo(p, q), q);
    ZZ a2= Power_mod(modulo(M, q), modulo(d, q - 1), q);
    return modulo(modulo(a1 * q * q1, n) + modulo(a2 * p * q2, n), n);
}

```

```
ZZ Power_mod(ZZ base, ZZ exp, ZZ n){  
    //Usamos exponenciación modular el documento  
    //Exponenciación Modular Binaria  
    ZZ salida(1);  
    do{  
        if(!even(exp))  
            salida= modulo(salida * base, n);  
        base= modulo(base * base, n);  
        exp>>=1;  
    }while(exp!=ZZ(0));  
    return salida;  
}
```