§1 GB\_ECON INTRODUCTION 1

Important: Before reading GB\_ECON, please read or at least skim the programs for GB\_GRAPH and GB\_IO.

1. Introduction. This GraphBase module contains the *econ* subroutine, which creates a family of directed graphs related to the flow of money between industries. An example of the use of this procedure can be found in the demo program ECON\_ORDER.

```
⟨gb_econ.h 1⟩ ≡
extern Graph *econ();
See also section 5.
```

2. The subroutine call econ(n, omit, threshold, seed) constructs a directed graph based on the information in econ.dat. Each vertex of the graph corresponds to one of 81 sectors of the U.S. economy. The data values come from the year 1985; they were derived from tables published in Survey of Current Business 70 (1990), 41–56.

If omit = threshold = 0, the directed graph is a "circulation"; that is, each arc has an associated flow value, and the sum of arc flows leaving each vertex is equal to the sum of arc flows entering. This sum is called the "total commodity output" for the sector in question. The flow in an arc from sector j to sector k is the amount of the commodity made by sector j that was used by sector k, rounded to millions of dollars at producers' prices. For example, the total commodity output of the sector called Apparel is 54031, meaning that the total cost of making all kinds of apparel in 1985 was about 54 billion dollars. There is an arc from Apparel to itself with a flow of 9259, meaning that 9.259 billion dollars' worth of apparel went from one group within the apparel industry to another. There also is an arc of flow 44 from Apparel to Household furniture, indicating that some 44 million dollars' worth of apparel went into the making of household furniture. By looking at all arcs that leave the Apparel vertex, you can see where all that new apparel went; by looking at all arcs that enter Apparel, you can see what ingredients the apparel industry needed to make it.

One vertex, called Users, represents people like you and me, the non-industrial end users of everything. The arc from Apparel to Users has flow 42172; this is the "total final demand" for apparel, the amount that didn't flow into other sectors of the economy before it reached people like us. The arc from Users to Apparel has flow 19409, which is called the "value added" by users; it represents wages and salaries paid to support the manufacturing process. The sum of total final demand over all sectors, which also equals the sum of value added over all sectors, is conventionally called the Gross National Product (GNP). In 1985 the GNP was 3999362, nearly 4 trillion dollars, according to econ.dat. (The sum of all arc flows coming out of all vertices was 7198680; this sum overestimates the total economic activity, because it counts some items more than once—statistics are recorded whenever an item passes a statistics gatherer. Economists try to adjust the data so that they avoid double-counting as much as possible.)

Speaking of economists, there is another special vertex called Adjustments, included by economists so that GNP is measured more accurately. This vertex takes account of such things as changes in the value of inventories, and imported materials that cannot be obtained within the U.S., as well as work done for the government and for foreign concerns. In 1985, these adjustments accounted for about 11% of the GNP.

Incidentally, some of the "total final demand" arcs are negative. For example, the arc from Petroleum and natural gas production to Users has flow -27032. This might seem strange at first, but it makes sense when imports are considered, because crude oil and natural gas go more to other industries than to end users. Total final demand does not mean total user demand.

#define flow a.I /\* utility field a specifies the flow in an arc \*/

2 INTRODUCTION GB\_ECON §3

3. If omit = 1, the Users vertex is omitted from the digraph; in particular, this will eliminate all arcs of negative flow. If omit = 2, the Adjustments vertex is also omitted, thereby leaving 79 sectors with arcs showing inter-industry flow. (The graph is no longer a "circulation," of course, when omit > 0.) If Users and Adjustments are not omitted, Users is the last vertex of the graph, and Adjustments is next-to-last.

If threshold = 0, the digraph has an arc for every nonzero flow. But if threshold > 0, the digraph becomes more sparse; there is then an arc from j to k if and only if the amount of commodity j used by sector k exceeds threshold/65536 times the total input of sector k. (The total input figure always includes value added, even if omit > 0.) Thus the arcs go to each sector from that sector's main suppliers. When n = 79, omit = 2, and threshold = 0, the digraph has 4602 arcs out of a possible  $79 \times 79 = 6241$ . Raising threshold to 1 decreases the number of arcs to 4473; raising it to 6000 leaves only 72 arcs. The total field in each arc is 1.

The constructed graph will have  $\min(n, 81 - omit)$  vertices. If n is less than 81 - omit, the n vertices will be selected by repeatedly combining related sectors. For example, two of the 81 original sectors are called 'Paper products, except containers' and 'Paperboard containers and boxes'; these might be combined into a sector called 'Paper products'. There is a binary tree with 79 leaves, which describes a fixed hierarchical breakdown of the 79 non-special sectors. This tree is pruned, if necessary, by replacing pairs of leaves by their parent node, which becomes a new leaf; pruning continues until just n leaves remain. Although pruning is a bottom-up process, its effect can also be obtained from the top down if we imagine "growing" the tree, starting out with a whole economy as a single sector and repeatedly subdividing a sector into two parts. For example, if omit = 2 and n = 2, the two sectors will be called Goods and Services. If n = 3, Goods might be subdivided into Natural Resources and Manufacturing; or Services might be subdivided into Indirect Services and Direct Services.

If seed = 0, the binary tree is pruned in such a way that the n resulting sectors are as equal as possible with respect to total input and output, while respecting the tree structure. If seed > 0, the pruning is carried out at random, in such a way that all n-leaf subtrees of the original tree are obtained with approximately equal probability (depending on seed in a machine-independent fashion). Any seed value from 1 to  $2^{31} - 1 = 2147483647$  is permissible.

As usual in GraphBase routines, you can set n = 0 to get the default situation where n has its maximum value. For example, either econ(0,0,0,0) or econ(81,0,0,0) produces the full graph; econ(0,2,0,0) or econ(79,2,0,0) produces the full graph except for the two special vertices.

```
#define MAX_N 81 /* maximum number of vertices in constructed graph */#define NORM_N MAX_N - 2 /* the number of normal SIC sectors */#define ADJ_SEC MAX_N - 1 /* code number for the Adjustments sector */
```

4. The U.S. Bureau of Economic Analysis and the U.S. Bureau of the Census have assigned code numbers 1–79 to the individual sectors for which statistics are given in econ.dat. These sector numbers are traditionally called Standard Industrial Classification (SIC) codes. If for some reason you want to know the SIC codes for all sectors represented by vertex v of a graph generated by econ, you can access them via a list of Arc nodes starting at the utility field  $v \rightarrow SIC\_codes$ . This list is linked by next fields in the usual way, and each SIC code appears in the len field; the tip field is unused.

The special vertex Adjustments is given code number 80; it is actually a composite of six different SIC categories, numbered 80–86 in their published tables.

For example, if n = 80 and omit = 1, each list will have length 1. Hence  $v \neg SIC\_codes \neg next$  will equal  $\Lambda$  for each v, and  $v \neg SIC\_codes \neg len$  will be v's SIC code, a number between 1 and 80.

The special vertex Users has no SIC code; it is the only vertex whose SIC\_codes field will be null in the graph returned by econ.

```
#define SIC\_codes\ z.A /* utility field z leads to the SIC codes for a vertex */
```

§5 GB\_ECON INTRODUCTION 3

**5.** The total output of each sector, which also equals the total input of that sector, is placed in utility field  $sector\_total$  of the corresponding vertex.

```
#define sector\_total\ y.I\ /* utility field y holds the total flow in and out */ \langle \mbox{gb\_econ.h } 1 \rangle + \equiv #define flow\ a.I\ /* definitions of utility fields in the header file */ #define SIC\_codes\ z.A #define sector\_total\ y.I
```

6. If the econ routine encounters a problem, it returns  $\Lambda$  (NULL), after putting a nonzero number into the external variable  $panic\_code$ . This code number identifies the type of failure. Otherwise econ returns a pointer to the newly created graph, which will be represented with the data structures explained in GB\_GRAPH. (The external variable  $panic\_code$  is itself defined in GB\_GRAPH.)

```
#define panic(c) { panic\_code = c; gb\_trouble\_code = 0; return \Lambda; }
```

7. The C file gb\_econ.c has the following overall shape:

```
/* we will use the GB_IO routines for input */
#include "gb_io.h"
#include "gb_flip.h"
                             /* we will use the GB_FLIP routines for random numbers */
#include "gb_graph.h"
                              /* and of course we'll use the GB_GRAPH data structures */
  \langle Preprocessor definitions \rangle
  (Type declarations 11)
  (Private variables 12)
  Graph *econ(n, omit, threshold, seed)
                            /* number of vertices desired */
       unsigned long n;
       unsigned long omit; /* number of special vertices to omit */
       unsigned long threshold; /* minimum per-64K-age in arcs leading in */
                     /* random number seed */
  { \langle Local variables 8 \rangle
    gb\_init\_rand(seed);
    init_area(working_storage);
     (Check the parameters and adjust them for defaults 9);
     \langle Set up a graph with n vertices 10\rangle;
     Read econ.dat and note the binary tree structure 14);
     \langle Determine the n sectors to use in the graph 17\rangle;
     \langle Put \text{ the appropriate arcs into the graph } 25 \rangle;
    if (gb\_close() \neq 0) panic(late\_data\_fault);
                                                    /* something's wrong with "econ.dat"; see io_errors */
    gb\_free (working\_storage);
    if (gb\_trouble\_code) {
       gb\_recycle(new\_graph);
       panic(alloc_fault);
                            /* oops, we ran out of memory somewhere back there */
    return new_graph;
8. \langle \text{Local variables } 8 \rangle \equiv
  Graph *new\_graph; /* the graph constructed by econ */
  register long j, k; /* all-purpose indices */
  Area working_storage; /* tables needed while econ does its thinking */
See also section 13.
```

This code is used in section 7.

4 INTRODUCTION GB\_ECON §9

 $\S11$  GB\_ECON THE ECONOMIC TREE 5

11. The economic tree. As we read in the data, we construct a sequential list of nodes, each of which represents either a micro-sector of the economy (one of the basic SIC sectors) or a macro-sector (which is the union of two subnodes). In more technical terms, the nodes form an extended binary tree, whose external nodes correspond to micro-sectors and whose internal nodes correspond to macro-sectors. The nodes of the tree appear in preorder. Subsequently we will do a variety of operations on this binary tree, proceeding either top-down (from the beginning of the list to the end) or bottom-up (from the end to the beginning).

Each node is a rather large record, because we will store a complete vector of sector output data in each node.

```
⟨Type declarations 11⟩ ≡
typedef struct node_struct { /* records for micro- and macro-sectors */
struct node_struct *rchild; /* pointer to right child of macro-sector */
char title [44]; /* "Sector_name" */
long table [MAX_N + 1]; /* outputs from this sector */
unsigned long total; /* total input to this sector (= total output) */
long thresh; /* flow must exceed thresh in arcs to this sector */
long SIC; /* SIC code number; initially zero in macro-sectors */
long tag; /* 1 if this node will be a vertex in the graph */
struct node_struct *link; /* next smallest unexplored sector */
Arc *SIC_list; /* first item on list of SIC codes */
} node;
This code is used in section 7.
```

 $\langle \text{Private variables } 12 \rangle \equiv$ 

This code is used in section 7.

12. When we read the given data in preorder, we'll need a stack to remember what nodes still need to have their *rchild* pointer filled in. (There is a no need for an *lchild* pointer, because the left child always follows its parent immediately in preorder.)

```
static node *stack[NORM_N + NORM_N];
  static node **stack_ptr;
                                 /* current position in stack */
  static node *node_block;
                                /* array of nodes, specifies the tree in preorder */
  static node *node\_index[MAX_N + 1]; /* which node has a given SIC code */
See also section 26.
This code is used in section 7.
13. \langle \text{Local variables } 8 \rangle + \equiv
  register node *p,*pl,*pr;
                                   /* current node and its children */
  register node *q; /* register for list manipulation */
14. \langle \text{Read econ.dat} \text{ and note the binary tree structure } 14 \rangle \equiv
  node\_block = gb\_typed\_alloc(2 * MAX_N - 3, node, working\_storage);
  if (qb\_trouble\_code) panic(no\_room + 1);
                                               /* no room to copy the data */
  if (gb\_open("econ.dat") \neq 0) panic(early\_data\_fault);
       /* couldn't open "econ.dat" using GraphBase conventions */
  Read and store the sector names and SIC numbers 15);
  for (k = 1; k \leq MAX_N; k++) (Read and store the output coefficients for sector k = 16);
```

6 THE ECONOMIC TREE GB\_ECON §15

15. The first part of econ.dat specifies the nodes of the binary tree in preorder. Each line contains a node name followed by a colon, and the colon is followed by the SIC number if that node is a leaf.

The tree is uniquely specified in this way, because of the nature of preorder. (Think of Polish prefix notation, in which a formula like '+x+xx' means '+(x,+(x,x))'; the parentheses in Polish notation are redundant.)

The two special sector names don't appear in the file; we manufacture them ourselves.

The program here is careful not to clobber itself in the presence of arbitrarily garbled data.

```
\langle Read and store the sector names and SIC numbers 15\rangle \equiv
  stack_ptr = stack;
  for (p = node\_block; p < node\_block + NORM_N + NORM_N - 1; p++)  { register long c;
    qb\_string(p \rightarrow title, ':');
    if (strlen(p \rightarrow title) > 43) panic(syntax_error);
                                                        /* sector name too long */
    if (gb\_char() \neq ":") panic(syntax\_error + 1);
                                                        /* missing colon */
    p \rightarrow SIC = c = gb\_number(10);
    if (c \equiv 0)
                  /* macro-sector */
       *stack_ptr ++ = p;
                            /* left child is p + 1, we'll know rehild later */
    else { /* micro-sector; p+1 will be somebody's right child */
       node\_index[c] = p;
       \textbf{if} \ (stack\_ptr > stack) \ (*--stack\_ptr) \neg rchild = p+1;
    if (gb\_char() \neq '\n') panic(syntax_error + 2); /* garbage on the line */
    gb\_newline();
  if (stack\_ptr \neq stack) panic(syntax\_error + 3); /* tree malformed */
  for (k = NORM_N; k; k--)
    if (node\_index[k] \equiv 0) panic(syntax\_error + 4); /* SIC code not mentioned in the tree */
  strcpy(p \rightarrow title, "Adjustments"); p \rightarrow SIC = ADJ_SEC; node\_index[ADJ_SEC] = p;
  strcpy((p+1) \neg title, "Users"); node\_index[MAX_N] = p+1;
```

This code is used in section 14.

§16 GB\_ECON THE ECONOMIC TREE 7

16. The remaining part of econ.dat is an  $81 \times 80$  matrix in which the kth row contains the outputs of sector k to all sectors except Users. Each row consists of a blank line followed by 8 data lines; each data line contains 10 numbers separated by commas. Zeroes are represented by "" instead of by "0". For example, the data line

```
8490,2182,42,467,,,,,
```

follows the initial blank line; it means that sector 1 output 8490 million dollars to itself, \$2182M to sector 2,  $\dots$ , \$0M to sector 10.

```
 \left\{ \begin{array}{ll} \text{Read and store the output coefficients for sector } k \ 16 \right\rangle \equiv \\ \left\{ \begin{array}{ll} \text{register long } s = 0; & /* \text{ row sum } */ \\ \text{register long } x; & /* \text{ entry read from econ.dat } */ \\ \text{if } (gb\_char() \neq \text{`}\n') \ panic(syntax\_error + 5); & /* \text{ blank line missing between rows } */ \\ gb\_newline(); \\ p = node\_index[k]; \\ \text{for } (j = 1; \ j < \text{MAX\_N}; \ j++) \ \{ \\ p^{\rightarrow}table[j] = x = gb\_number(10); \ s += x; \\ node\_index[j] \neg total \ += x; \\ \text{if } ((j \% \ 10) \equiv 0) \ \{ \\ \text{if } (gb\_char() \neq \text{`}\n') \ panic(syntax\_error + 6); \ /* \ \text{out of synch in input file } */ \\ gb\_newline(); \\ \} \ \text{else if } (gb\_char() \neq \text{`},\text{`}) \ panic(syntax\_error + 7); \ /* \ \text{missing comma after entry } */ \\ \} \\ p^{\rightarrow}table[\text{MAX\_N}] = s; \ /* \ \text{sum of } table[1] \ \text{through } table[80] \ */ \\ \} \\ \end{array}
```

This code is used in section 14.

8 GROWING A SUBTREE GB\_ECON §17

17. Growing a subtree. Once all the data appears in  $node\_block$ , we want to extract from it and combine it as specified by parameters n, omit, and seed. This amalgamation process effectively prunes the tree; it can also be regarded as a procedure that grows a subtree of the full economic tree.

18. The chosen leaves of our subtree are identified by having their tag field set to 1.

```
 \begin{array}{l} \langle \, \text{Choose all sectors 18} \, \rangle \equiv \\ \quad \text{ for } (k = \texttt{NORM\_N}; \ k; \ k--) \ node\_index[k] \neg tag = 1; \\ \text{This code is used in section 17}. \end{array}
```

19. To grow the l-leaf subtree when seed = 0, we first pass over the tree bottom-up to compute the total input (and output) of each macro-sector; then we proceed from the top down to subdivide sectors in decreasing order of their total input. This process provides a good introduction to the bottom-up and top-down tree methods we will be using in several other parts of the program.

The *special* node is used here for two purposes: It is the head of a linked list of unexplored nodes, sorted by decreasing order of their *total* fields; and it appears at the end of that list, because special - total = 0.

```
 \left\{ \begin{array}{ll} \text{Grow a subtree with $l$ leaves by subdividing largest sectors first 19} \right\} \equiv \\ \left\{ \begin{array}{ll} \textbf{register node} *special = node\_index [\texttt{MAX\_N}]; & /* \text{ the Users node at the end of } node\_block */ \\ \textbf{for } (p = node\_index [\texttt{ADJ\_SEC}] - 1; & p \geq node\_block; & p - -) & /* \text{ bottom up } */ \\ \textbf{if } (p \neg rchild) & p \neg total = (p+1) \neg total + p \neg rchild \neg total; \\ special \neg link = node\_block; & node\_block \neg link = special; & /* \text{ start at the root } */ \\ k = 1; & /* & k \text{ is the number of nodes we have tagged or put onto the list } */ \\ \textbf{while } (k < l) & \langle \text{If the first node on the list is a leaf, delete it and tag it; otherwise replace it by its two children 20}; \\ \textbf{for } (p = special \neg link; & p \neq special; & p = p \neg link) & p \neg tag = 1; & /* \text{ tag everything on the list } */ \\ \end{array} \right\}
```

This code is used in section 17.

This code is used in section 19.

§21 GB\_ECON GROWING A SUBTREE 9

21. We can obtain a uniformly distributed l-leaf subtree of a given tree by choosing the root when l=1 or by using the following idea when l>1: Suppose the given tree T has subtrees  $T_0$  and  $T_1$ . Then it has T(l) subtrees with l leaves, where  $T(l)=\sum_k T_0(k)T_1(l-k)$ . We choose a random number r between 0 and T(l)-1, and we find the smallest m such that  $\sum_{k\leq m} T_0(k)T_1(l-k)>r$ . Then we proceed recursively to compute a random m-leaf subtree of  $T_0$  and a random (l-m)-leaf subtree of  $T_1$ .

A difficulty arises when T(l) is  $2^{31}$  or more. But then we can replace  $T_0(k)$  and  $T_1(l-k)$  in the formulas

A difficulty arises when T(l) is  $2^{31}$  or more. But then we can replace  $T_0(k)$  and  $T_1(l-k)$  in the formulas above by  $\lceil T_0(k)/d_0 \rceil$  and  $\lceil T_1(k)/d_1 \rceil$ , respectively, where  $d_0$  and  $d_1$  are arbitrary constants; this yields smaller values T(l) that define approximately the same distribution of k.

The program here computes the T(l) values bottom-up, then grows a random tree top-down. If node p is not a leaf, its table[0] field will be set to the number of leaves below it; and its table[l] field will be set to T(l), for  $1 \le l \le table[0]$ .

The data in econ.dat is sufficiently simple that most of the T(l) values are less than  $2^{31}$ . We need to scale them down to avoid overflow only at the root node of the tree; this case is handled separately.

We set the tag field of a node equal to the number of leaves to be grown in the subtree rooted at that node. This convention is consistent with our previous stipulation that tag = 1 should characterize the nodes that are chosen to be vertices.

```
 \left\{ \begin{array}{l} \text{Grow a random subtree with $l$ leaves 21$} \right\} \equiv \left\{ \begin{array}{l} node\_block \neg tag = l; \\ \text{for } (p = node\_index[\texttt{ADJ\_SEC}] - 1; \ p > node\_block; \ p - -) \end{array} \right. / * \text{ bottom up, except root } * / \\ \text{if } (p \neg rchild) \left< \texttt{Compute the } T(l) \text{ values for subtree } p \text{ 22} \right> ; \\ \text{for } (p = node\_block; \ p < node\_index[\texttt{ADJ\_SEC}]; \ p + +) \end{array} \right. / * \text{ top down, from root } * / \\ \text{if } (p \neg tag > 1) \left\{ \\ l = p \neg tag; \\ pl = p + 1; \ pr = p \neg rchild; \\ \text{if } (pl \neg rchild \equiv \Lambda) \left\{ \\ pl \neg tag = 1; \ pr \neg tag = l - 1; \\ \} \text{ else if } (pr \neg rchild \equiv \Lambda) \left\{ \\ pl \neg tag = l - 1; \ pr \neg tag = 1; \\ \} \text{ else } \left< \text{Stochastically determine the number of leaves to grow in each of $p$'s children 24} \right> ; \\ \} \\ \right\}
```

This code is used in section 17.

 $GB_{-}ECON$  §22

```
Here we are essentially multiplying two generating functions. Suppose f(z) = \sum_{l} T(l)z^{l}; then we are
computing f_p(z) = z + f_{pl}(z) f_{pr}(z).
\langle Compute the T(l) values for subtree p \ 22 \rangle \equiv
      pl = p + 1; pr = p \rightarrow rchild;
                                                /* T(1) and T(2) are always 1 */
      p \rightarrow table[1] = p \rightarrow table[2] = 1;
      if (pl \neg rchild \equiv 0) { /* left child is a leaf */
         if (pr \neg rchild \equiv 0) p \neg table[0] = 2;
                                                          /* and so is the right child */
         else \{ /* no, it isn't */
            for (k = 2; k \le pr \rightarrow table[0]; k++) p \rightarrow table[1 + k] = pr \rightarrow table[k];
            p \rightarrow table[0] = pr \rightarrow table[0] + 1;
      } else if (pr \rightarrow rchild \equiv 0) { /* right child is a leaf */
         \textbf{for} \ (k=2; \ k \leq pl \neg table[0]; \ k++) \ p \neg table[1+k] = pl \neg table[k];
         p \rightarrow table[0] = pl \rightarrow table[0] + 1;
                      /* neither child is a leaf */
         \langle \text{Set } p\text{-}table[2], p\text{-}table[3], \dots \text{ to convolution of } pl \text{ and } pr \text{ table entries } 23 \rangle;
         p \rightarrow table[0] = pl \rightarrow table[0] + pr \rightarrow table[0];
This code is used in section 21.
23. \langle \text{Set } p \text{-} table[2], p \text{-} table[3], \dots \text{ to convolution of } pl \text{ and } pr \text{ table entries } 23 \rangle \equiv
   p \rightarrow table[2] = 0;
   for (j = pl \neg table[0]; j; j --) { register long t = pl \neg table[j];
      for (k = pr \rightarrow table[0]; k; k \rightarrow p \rightarrow table[j + k] += t * pr \rightarrow table[k];
This code is used in section 22.
24. (Stochastically determine the number of leaves to grow in each of p's children 24) \equiv
   { register long ss, rr;
      j = 0;
                    /* we will set j = 1 if scaling is necessary at the root */
      if (p \equiv node\_block) {
         ss = 0;
         if (l > 29 \land l < 67) {
                       /* more than 2^{31} possibilities exist */
            for (k = (l > pr \rightarrow table[0] ? l - pr \rightarrow table[0] : 1); k \leq pl \rightarrow table[0] \land k < l; k++)
               ss += ((pl - table[k] + *3ff) \gg 10) * pr - table[l - k]; /* scale with d_0 = 1024, d_1 = 1 */
         } else
            for (k = (l > pr \rightarrow table[0] ? l - pr \rightarrow table[0] : 1); k \leq pl \rightarrow table[0] \land k < l; k++)
               ss += pl \neg table[k] * pr \neg table[l - k];
      } else ss = p \rightarrow table[l];
      rr = gb\_unif\_rand(ss);
      if (j)
         for (ss = 0, k = (l > pr \neg table[0] ? l - pr \neg table[0] : 1); ss \le rr; k++)
            ss += ((pl \rightarrow table[k] + \#3ff) \gg 10) * pr \rightarrow table[l - k];
      else
         for (ss = 0, k = (l > pr \rightarrow table[0] ? l - pr \rightarrow table[0] : 1); ss \leq rr; k++)
            ss += pl \rightarrow table[k] * pr \rightarrow table[l-k];
      pl \rightarrow tag = k - 1; pr \rightarrow tag = l - k + 1;
This code is used in section 21.
```

10

GROWING A SUBTREE

 $\S25$  GB.ECON ARCS 11

25. Arcs. In the general case, we have to combine some of the basic micro-sectors into macro-sectors by adding together the appropriate input/output coefficients. This is a bottom-up pruning process.

Suppose p is being formed as the union of pl and pr. Then the arcs leading out of p are obtained by summing the numbers on arcs leading out of pl and pr; the arcs leading into p are obtained by summing the numbers on arcs leading into pl and pr; the arcs from p to itself are obtained by summing the four numbers on arcs leading from pl or pr to pl or pr.

We maintain the  $node\_index$  table so that its non- $\Lambda$  entries contain all the currently active nodes. When pl and pr are being pruned in favor of p, node p inherits pl's place in  $node\_index$ ; pr's former place becomes  $\Lambda$ .

```
\langle \text{Put the appropriate arcs into the graph } 25 \rangle \equiv
   Prune the sectors that are used in macro-sectors, and form the lists of SIC sector codes 28;
    Make the special nodes invisible if they are omitted, visible otherwise 30);
    Compute individual thresholds for each chosen sector 27);
   { register Vertex *v = new\_graph\neg vertices + n;}
     for (k = MAX_N; k; k--)
        if ((p = node\_index[k]) \neq \Lambda) {
           vert\_index[k] = --v;
           v \rightarrow name = gb\_save\_string(p \rightarrow title);
           v \rightarrow SIC\_codes = p \rightarrow SIC\_list;
           v \rightarrow sector\_total = p \rightarrow total;
        } else vert\_index[k] = \Lambda;
     if (v \neq new\_qraph\_vertices) panic(impossible); /* bug in algorithm; this can't happen */
     for (j = MAX_N; j; j--)
        if ((p = node\_index[j]) \neq \Lambda) { register Vertex *u = vert\_index[j];
           for (k = MAX_N; k; k--)
              if ((v = vert\_index[k]) \neq \Lambda)
                 if (p \rightarrow table[k] \neq 0 \land p \rightarrow table[k] > node\_index[k] \rightarrow thresh) {
                    gb\_new\_arc(u, v, 1_L);
                    u \rightarrow arcs \rightarrow flow = p \rightarrow table[k];
        }
  }
This code is used in section 7.
```

26. ⟨Private variables 12⟩ +≡
static Vertex \*vert\_index[MAX\_N + 1]; /\* the vertex assigned to an SIC code \*/

**27.** The theory underlying this step is the following, for integers a, b, c, d with b, d > 0:

$$\frac{a}{b} > \frac{c}{d}$$
  $\iff$   $a > \left| \frac{b}{d} \right| c + \left| \frac{(b \mod d)c}{d} \right|.$ 

In our case, b=p-total and  $c=threshold \leq d=65536=2^{16}$ , hence the multiplications cannot overflow. (But they can come awfully darn close.)

```
 \begin{split} &\langle \text{Compute individual thresholds for each chosen sector 27} \rangle \equiv \\ & \textbf{for } (k = \texttt{MAX\_N}; \ k; \ k--) \\ & \textbf{if } ((p = node\_index[k]) \neq \Lambda) \ \{ \\ & \textbf{if } (threshold \equiv 0) \ p\text{-}thresh = -99999999; \\ & \textbf{else } p\text{-}thresh = ((p\text{-}total \gg 16) * threshold) + (((p\text{-}total \& \#ffff) * threshold) \gg 16); \\ & \} \end{split}
```

This code is used in section 25.

12 ARCS GB\_ECON §28

 $\langle$  Prune the sectors that are used in macro-sectors, and form the lists of SIC sector codes 28  $\rangle$ 

```
for (p = node\_index[ADJ\_SEC]; p \ge node\_block; p--) {
                                                                                         /* bottom up */
      if (p→SIC) {
                             /* original leaf */
          p \rightarrow SIC\_list = gb\_virgin\_arc();
          p \rightarrow SIC\_list \rightarrow len = p \rightarrow SIC;
      } else {
          pl = p + 1; pr = p \rightarrow rchild;
          if (p \rightarrow tag \equiv 0) p \rightarrow tag = pl \rightarrow tag + pr \rightarrow tag;
          if (p \rightarrow taq < 1) (Replace pl and pr by their union, p 29);
This code is used in section 25.
29. \langle Replace pl and pr by their union, p 29\rangle \equiv
   { register Arc *a = pl \neg SIC\_list;
      register long jj = pl \rightarrow SIC, kk = pr \rightarrow SIC;
      p \rightarrow SIC_list = a;
      while (a \rightarrow next) a = a \rightarrow next;
      a \neg next = pr \neg SIC\_list;
      for (k = MAX_N; k; k--)
          if ((q = node\_index[k]) \neq \Lambda) {
             if (q \neq pl \land q \neq pr) q \rightarrow table[jj] += q \rightarrow table[kk];
             p \rightarrow table[k] = pl \rightarrow table[k] + pr \rightarrow table[k];
      p \rightarrow total = pl \rightarrow total + pr \rightarrow total;
      p \rightarrow SIC = jj;
      p \rightarrow table[jj] += p \rightarrow table[kk];
      node\_index[jj] = p;
      node\_index[kk] = \Lambda;
This code is used in section 28.
```

**30.** If the Users vertex is not omitted, we need to compute each sector's total final demand, which is calculated so that the row sums and column sums of the input/output coefficients come out equal. We've already computed the column sum, p-total; we've also computed p-table[1] +  $\cdots$  + p-table[ADJ\_SEC], and put it into p-table[MAX\_N]. So now we want to replace p-table[MAX\_N] by p-total - p-table[MAX\_N]. As remarked earlier, this quantity might be negative.

In the special node p for the Users vertex, the preliminary processing has made  $p \rightarrow total = 0$ ; moreover,  $p \rightarrow table[\texttt{MAX\_N}]$  is the sum of value added, or GNP. We want to switch those fields.

We don't have to set the *tag* fields to 1 in the special nodes, because the remaining parts of the arcgeneration algorithm don't look at those fields.

```
 \begin{split} &\langle \, \text{Make the special nodes invisible if they are omitted, visible otherwise 30} \, \rangle \equiv \\ & \text{if } (\mathit{omit} \equiv 2) \ \mathit{node\_index} [\mathtt{ADJ\_SEC}] = \mathit{node\_index} [\mathtt{MAX\_N}] = \Lambda; \\ & \text{else if } (\mathit{omit} \equiv 1) \ \mathit{node\_index} [\mathtt{MAX\_N}] = \Lambda; \\ & \text{else } \{ \\ & \text{for } (k = \mathtt{ADJ\_SEC}; \ k; \ k--) \\ & \text{if } ((p = \mathit{node\_index}[k]) \neq \Lambda) \ \mathit{p-table} [\mathtt{MAX\_N}] = \mathit{p-total} - \mathit{p-table} [\mathtt{MAX\_N}]; \\ & p = \mathit{node\_index} [\mathtt{MAX\_N}]; \ /* \ \text{the special node } */ \\ & p - \mathit{total} = \mathit{p-table} [\mathtt{MAX\_N}]; \\ & p - \mathit{table} [\mathtt{MAX\_N}] = 0; \\ \} \end{split}
```

This code is used in section 25.

§31 GB.ECON INDEX 13

**31.** Index. As usual, we close with an index that shows where the identifiers of  $gb\_econ$  are defined and used.

a: <u>29</u>.  $\mathtt{ADJ\_SEC:} \quad \underline{3}, \ 15, \ 19, \ 21, \ 28, \ 30.$  $alloc\_fault$ : 7. **Arc**: 4, 11, 29. arcs: 25.Area: 8. c: 15.  $early\_data\_fault$ : 14. econ: 1, 2, 3, 4, 6, 7, 8. flow: 2, 3, 5, 11, 25.  $gb\_char$ : 15, 16.  $qb\_close$ : 7.  $gb\_free: 7.$  $gb\_init\_rand$ : 7.  $gb\_new\_arc$ : 25.  $gb\_new\_graph$ : 10.  $gb\_newline$ : 15, 16.  $gb\_number$ : 15, 16.  $gb\_open$ : 14.  $qb\_recycle$ : 7.  $gb\_save\_string$ : 25. $qb\_string$ : 15.  $gb\_trouble\_code$ : 6, 7, 14.  $gb\_typed\_alloc$ : 14.  $gb\_unif\_rand$ : 24.  $gb\_virgin\_arc$ : 28. Graph: 1, 7, 8. id: 10.impossible: 25.  $init\_area\colon \ \ 7.$  $io\_errors$ : 7. j:  $\underline{8}$ . jj: 29.*k*: <u>8</u>.  $kk: \underline{29}$ l: 17.  $late\_data\_fault$ : 7. len: 3, 4, 28.link: 11, 19, 20.MAX\_N: 3, 9, 11, 12, 14, 15, 16, 19, 25, 26, 27, 29, 30. n:  $\underline{7}$ . name: 25. $new\_graph$ : 7,  $\underline{8}$ , 10, 25.  $next{:}\quad 4,\ 29.$ *no\_room*: 10, 14. **node**: <u>11</u>, 12, 13, 14, 19. node\_block: 12, 14, 15, 17, 19, 21, 24, 28. node\_index: 12, 15, 16, 18, 19, 21, 25, 27, 28, 29, 30.

node\_struct: 11. NORM\_N: 3, 12, 15, 17, 18. omit: 2, 3, 4, 7, 9, 10, 17, 30. p: 13. panic: 6, 7, 10, 14, 15, 16, 25.  $panic\_code$ : 6. pl: 13, 20, 21, 22, 23, 24, 25, 28, 29.pr: 13, 20, 21, 22, 23, 24, 25, 28, 29.rchild: 11, 12, 15, 19, 20, 21, 22, 28.  $rr: \underline{24}.$ s: 16.  $sector\_total$ : 5, 25. seed: 2, 3, 7, 10, 17, 19. SIC: <u>11</u>, 15, 28, 29.  $SIC\_codes$ :  $\underline{4}$ ,  $\underline{5}$ , 25. SIC\_list: 11, 25, 28, 29. special: 19, 20.sprint f: 10. $ss: \underline{24}.$ stack: 12, 15.  $stack_ptr: \underline{12}, 15.$ strcpy: 10, 15. strlen: 15. $syntax\_error$ : 15, 16. t: 23. table: 11, 16, 21, 22, 23, 24, 25, 29, 30. tag: 11, 18, 19, 20, 21, 24, 28, 30. thresh:  $\underline{11}$ , 25, 27. threshold:  $2, 3, \underline{7}, 9, 10, 27.$ tip: 4. $title \colon \ \underline{11},\ 15,\ 25.$  $total \colon \ \underline{11}, \ 16, \ 19, \ 20, \ 25, \ 27, \ 29, \ 30.$ u:  $\underline{25}$ .  $util\_types$ : 10. v: 25.  $vert\_index$ : 25, 26. Vertex: 25, 26. vertices: 25.  $working\_storage$ : 7,  $\underline{8}$ , 14.  $x: \underline{16}.$ 

14 NAMES OF THE SECTIONS GB\_ECON

```
(Check the parameters and adjust them for defaults 9) Used in section 7.
Choose all sectors 18 \ Used in section 17.
Compute individual thresholds for each chosen sector 27 \ Used in section 25.
Compute the T(l) values for subtree p(22) Used in section 21.
Determine the n sectors to use in the graph 17 \rangle Used in section 7.
Grow a random subtree with l leaves 21 \ Used in section 17.
Grow a subtree with l leaves by subdividing largest sectors first 19 \rangle Used in section 17.
(If the first node on the list is a leaf, delete it and tag it; otherwise replace it by its two children 20) Used
(Local variables 8, 13) Used in section 7.
Make the special nodes invisible if they are omitted, visible otherwise 30 \> Used in section 25.
\langle Private variables 12, 26 \rangle Used in section 7.
(Prune the sectors that are used in macro-sectors, and form the lists of SIC sector codes 28) Used in
    section 25.
(Put the appropriate arcs into the graph 25) Used in section 7.
Read econ.dat and note the binary tree structure 14 \rangle Used in section 7.
 Read and store the output coefficients for sector k 16\rangle Used in section 14.
 Read and store the sector names and SIC numbers 15 \) Used in section 14.
Replace pl and pr by their union, p 29 \rangle Used in section 28.
Set up a graph with n vertices 10 \rangle Used in section 7.
Set p-table [2], p-table [3], ... to convolution of pl and pr table entries 23 \rangle Used in section 22.
Stochastically determine the number of leaves to grow in each of p's children 24 \rangle Used in section 21.
Type declarations 11 \rangle Used in section 7.
\langle gb\_econ.h 1, 5 \rangle
```

## $GB_{-}ECON$

	Section	ı Page
Introduction	1	1 1
The economic tree	13	1 5
Growing a subtree	17	7 8
Arcs	25	5 11
Index	31	1 13

## © 1993 Stanford University

This file may be freely copied and distributed, provided that no changes whatsoever are made. All users are asked to help keep the Stanford GraphBase files consistent and "uncorrupted," identical everywhere in the world. Changes are permissible only if the modified file is given a new name, different from the names of existing files in the Stanford GraphBase, and only if the modified file is clearly identified as not being part of that GraphBase. (The CWEB system has a "change file" facility by which users can easily make minor alterations without modifying the master source files in any way. Everybody is supposed to use change files instead of changing the files.) The author has tried his best to produce correct and useful programs, in order to help promote computer science research, but no warranty of any kind should be assumed.

Preliminary work on the Stanford Graph Base project was supported in part by National Science Foundation grant CCR-86-10181.