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Problem Statement

Create a Linear Regression Model using Python/R to predict home prices using Boston Housing Dataset (https://www.kaggle.com/c/boston-housing). The Boston Housing dataset contains information about various houses in Boston through different parameters. There are 506 samples and 14 feature variables in this dataset.

The objective is to predict the value of prices of the house using the given features.

```
In [24]:
           # Import necessary libraries
           import numpy as np
           import pandas as pd
           # For plotting graphs
           import matplotlib.pyplot as plt
           import seaborn as sns
In [25]:
           # Load the data
           from sklearn.datasets import load_boston
           loaded_data = load_boston()
           # Convert the result into dataframe
           raw_data = pd.DataFrame(loaded_data.data, columns=loaded_data.feature_names)
In [26]:
           # .head() can be used to print the first 5 entries in the dataset
           raw_data.head()
              CRIM
                     ZN INDUS CHAS
                                       NOX
                                              RM AGE
                                                          DIS RAD
                                                                     TAX PTRATIO
                                                                                       B LSTA
Out[26]:
          0 0.00632 18.0
                           2.31
                                   0.0 0.538
                                             6.575
                                                  65.2 4.0900
                                                                1.0
                                                                    296.0
                                                                              15.3 396.90
                                                                                            4.98
          1 0.02731
                     0.0
                           7.07
                                   0.0 0.469
                                             6.421
                                                  78.9 4.9671
                                                                2.0 242.0
                                                                              17.8 396.90
                                                                                            9.14
                           7.07
                                                                2.0 242.0
          2 0.02729
                     0.0
                                   0.0 0.469
                                            7.185
                                                   61.1 4.9671
                                                                              17.8 392.83
                                                                                            4.00
            0.03237
                                   0.0 0.458 6.998
                                                   45.8 6.0622
                                                                3.0 222.0
                                                                              18.7 394.63
                     0.0
                           2.18
                                                                                            2.94
            0.06905
                     0.0
                           2.18
                                   0.0 0.458 7.147
                                                   54.2 6.0622
                                                                3.0 222.0
                                                                              18.7 396.90
                                                                                            5.30
          About the Data
In [28]:
```

```
print("The shape of the data is: ", raw_data.shape)
print("Thus, the number of columns/attributes are: ", raw_data.shape[1])
```

The shape of the data is: (506, 13)
Thus, the number of columns/attributes are: 1

There are 13 attributes for each house that are considered.

CRIM - per capita crime rate by town

ZN - proportion of residential land zoned for lots over 25,000 sq.ft.

INDUS - proportion of non-retail business acres per town.

CHAS - Charles River dummy variable (1 if tract bounds river; 0 otherwise)

NOX - nitric oxides concentration (parts per 10 million)

RM - average number of rooms per dwelling

AGE - proportion of owner-occupied units built prior to 1940

DIS - weighted distances to five Boston employment centres

RAD - index of accessibility to radial highways

TAX - full-value property-tax rate per 10,000 Dollars

PTRATIO - pupil-teacher ratio by town

B - 1000(Bk - 0.63)^2 where Bk is the proportion of blacks by town

LSTAT - % lower status of the population

Note: MEDV - Median value of owner-occupied homes in \$1000's

This is the target value (Price of the house)

Data Preprocessing

Out[9]:

```
In [8]:
         # First, let us get the target values loaded into a Series
         target_array = loaded_data.target
         # Convert numpy array into pandas series
         target_data = pd.Series(target_array, name='target')
         target_data.head()
             24.0
Out[8]:
             21.6
        1
             34.7
             33.4
             36.2
        Name: target, dtype: float64
In [9]:
         # Using .describe() to get Statistical Summary
         raw data.describe()
```

	CRIM	ZN	INDUS	CHAS	NOX	RM	AGE	
count	506.000000	506.000000	506.000000	506.000000	506.000000	506.000000	506.000000	506.0
mean	3.613524	11.363636	11.136779	0.069170	0.554695	6.284634	68.574901	3.7
std	8.601545	23.322453	6.860353	0.253994	0.115878	0.702617	28.148861	2.1
min	0.006320	0.000000	0.460000	0.000000	0.385000	3.561000	2.900000	1.1
25%	0.082045	0.000000	5.190000	0.000000	0.449000	5.885500	45.025000	2.1
50%	0.256510	0.000000	9.690000	0.000000	0.538000	6.208500	77.500000	3.2
75%	3.677083	12.500000	18.100000	0.000000	0.624000	6.623500	94.075000	5.1
max	88.976200	100.000000	27.740000	1.000000	0.871000	8.780000	100.000000	12.1
4								•

Note: MEDV attribute, which was mentioned earlier, is represented by target_data

```
# Check if there are any null values in the dataset
print("Number of Null values in each attribute is:")
print(raw_data.isna().sum())
print("\nNumber of Null values in target is: ", target_data.isna().sum())
```

Number of Null values in each attribute is:

```
CRIM
ΖN
INDUS
CHAS
NOX
            0
RM
AGE
DIS
RAD
TAX
            0
PTRATIO
            0
LSTAT
dtype: int64
```

Number of Null values in target is: 0

```
# Create a copy of raw data which will also store the target values
complete_data = raw_data.copy()

complete_data['target'] = target_data

complete_data.head()
```

Out[11]:		CRIM	ZN	INDUS	CHAS	NOX	RM	AGE	DIS	RAD	TAX	PTRATIO	В	LSTA
	0	0.00632	18.0	2.31	0.0	0.538	6.575	65.2	4.0900	1.0	296.0	15.3	396.90	4.98
	1	0.02731	0.0	7.07	0.0	0.469	6.421	78.9	4.9671	2.0	242.0	17.8	396.90	9.14
	2	0.02729	0.0	7.07	0.0	0.469	7.185	61.1	4.9671	2.0	242.0	17.8	392.83	4.00
	3	0.03237	0.0	2.18	0.0	0.458	6.998	45.8	6.0622	3.0	222.0	18.7	394.63	2.94
	4	0.06905	0.0	2.18	0.0	0.458	7.147	54.2	6.0622	3.0	222.0	18.7	396.90	5.3
	4													•

Visualization

First, we will try to guess how a change in each individual attribute will affect the target value (i.e, the price of the house).

We will use +ve to indicate that a rise in the value of the attribute will contribute to a rise in price of the house. Similarly, we will assign -ve for all the attributes which have a negative impact on the house price.

Crim - (-ve) An increase in crime rate will obviously make the house as well as the neighbourhood less attractive

Zn - (+ve) Zoning will increase the cost of land, because land is reserved.

Indus - (-ve) More the industrial area, worse are the living conditions.

Chas - (+ve) Riverside properties in general have a higher cost.

Nox - (-ve) Presence of Nox gases indicate the house is poorly ventilated.

Rm - (+ve) More the no. of rooms in a house, larger it's price

Age - (-ve) Older the houses, more the structural problems with them.

Dis - (+ve) Closer the house is to employment areas, higher it's price, because residents will save both time and money on commute.

Rad - (+ve) Larger the index, better accessibility to highways, more the cost of house.

Tax - Taxes are actually dependant on the property values, so not sure how these will affect house prices.

PTratio - (-ve) May indicate the quality of education in town

B - (-ve) Since there was a lot of discrimination against blacks in 1970s, we can expect that the

prices of houses to decrease if the proportion of blacks in town decrease.

Lstat - (-ve) Higher the lower status population, lower will be the price of the houses. Due to overall less paying capacity of the population.

Backing intuition with statistics: Pearson Correlation Coefficient

Pearson correlation coefficient or Pearson's correlation coefficient is defined in statistics as the measurement of the strength of the relationship between two variables and their association with each other.

```
In [12]: # Finding pearson coefficient for all attributes
    corr = complete_data.corr()

# Plot the data in the form of a heatmap
    plt.figure(figsize=(10, 10))

sns.heatmap(corr, annot=True, fmt='.2f', cbar=False, cmap="coolwarm", linewid
    plt.show()
```

CRIM -	1.00	-0.20	0.41	-0.06	0.42	-0.22	0.35	-0.38	0.63	0.58	0.29	-0.39	0.46	-0.39
ZN -	-0.20	1.00	-0.53	-0.04	-0.52	0.31	-0.57	0.66	-0.31	-0.31	-0.39	0.18	-0.41	0.36
INDUS -	0.41	-0.53	1.00	0.06	0.76	-0.39	0.64	-0.71	0.60	0.72	0.38	-0.36	0.60	-0.48
CHAS -	-0.06	-0.04	0.06	1.00	0.09	0.09	0.09	-0.10	-0.01	-0.04	-0.12	0.05	-0.05	0.18
NOX -	0.42	-0.52	0.76	0.09	1.00	-0.30	0.73	-0.77	0.61	0.67	0.19	-0.38	0.59	-0.43
RM -	-0.22	0.31	-0.39	0.09	-0.30	1.00	-0.24	0.21	-0.21	-0.29	-0.36	0.13	-0.61	0.70
AGE -	0.35	-0.57	0.64	0.09	0.73	-0.24	1.00	-0.75	0.46	0.51	0.26	-0.27	0.60	-0.38
DIS -	-0.38	0.66	-0.71	-0.10	-0.77	0.21	-0.75	1.00	-0.49	-0.53	-0.23	0.29	-0.50	0.25
RAD -	0.63	-0.31	0.60	-0.01	0.61	-0.21	0.46	-0.49	1.00	0.91	0.46	-0.44	0.49	-0.38
TAX -	0.58	-0.31	0.72	-0.04	0.67	-0.29	0.51	-0.53	0.91	1.00	0.46	-0.44	0.54	-0.47
PTRATIO -	0.29	-0.39	0.38	-0.12	0.19	-0.36	0.26	-0.23	0.46	0.46	1.00	-0.18	0.37	-0.51
В -	-0.39	0.18	-0.36	0.05	-0.38	0.13	-0.27	0.29	-0.44	-0.44	-0.18	1.00	-0.37	0.33
LSTAT -	0.46	-0.41	0.60	-0.05	0.59	-0.61	0.60	-0.50	0.49	0.54	0.37	-0.37	1.00	-0.74
target -	-0.39	0.36	-0.48	0.18	-0.43	0.70	-0.38	0.25	-0.38	-0.47	-0.51	0.33	-0.74	1.00
	CRIM	ΖŃ	INDUS	CHAS	Nox	RМ	AĠE	DİS	RÅD	TÁX	PTRÁTIO	В	LSTAT	target

Understanding the Heatmap

The heatmap shows how each attribute is related to other attributes of housing, as well as the final housing price.

It must be noted that higher the magnitude of the coefficient, larger positive or negative impact the attribute will have. Darker the shade of color in heatmap, more it's magnitude.

Unexpected Observations

Almost all of the guesses we made on each attribute of housing came out to be correct. However,

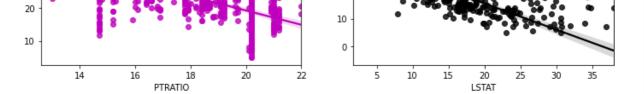
It is observed that:

30

- Contrary to what we believed, RAD (Accessibilty to highways) has a negative impact on price of the house. (Unable to justify why this is the case).
- Also, the proportion of blacks in the town seems to have a positive impact on price of the houses, a result we did not expect. This is something almost all the studies do not agree to. Studies have shown that housing discrimination still exists and there is a disparity in housing appraisals on the basis on race.
- Tax seems to have a negative impact on house prices. More the Tax lesser is the house price.

```
In [13]:
            # Now, let us plot all the attributes with a high coefficient
            plot_list = ['INDUS', 'NOX', 'RM', 'TAX', 'PTRATIO', 'LSTAT']
color_list = ['b', 'g', 'r', 'c', 'm', 'k']
            x_plot = complete_data.loc[:, plot_list]
            y_plot = complete_data['target']
            fig, axes = plt.subplots(3, 2, figsize=(12,12))
            axes_flatten = axes.flatten()
            index = 0
            for i in plot list:
                 sns.regplot(y=y_plot, x=x_plot[i], ax=axes_flatten[index], color=color_li
                 index += 1
             20
                                                              10
             10
                                            20
                                                                0.4
                                                                                                  0.8
                                  INDUS
             50
             40
             30
           target
             20
                                                              20
             10
                                                              10
                                  6
                                                  8
                                                                200
                                                                        300
                                                                                               600
                                                                                                       700
                                                                               400
                                                                                       500
                                                                                   TAX
                                   RM
             50
             40
```

target



Observations

The above graphs thus show a linear relationship between the attribute and price of the house (target)

Creating the Model

```
In [14]:
          # Split the data into train and test
          from sklearn.model_selection import train_test_split
          # Separate the dependant and independant variables
          X = complete_data.drop('target', axis=1)
          y = complete data['target']
          # Store a copy of X for later use
          X_{copy} = X.copy()
          X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.3, rand
          # Scaling the data to improve model accuracy
          from sklearn.preprocessing import StandardScaler
          scaler = StandardScaler()
          X_train = pd.DataFrame(scaler.fit_transform(X_train), columns=X_train.columns
          X_test = pd.DataFrame(scaler.transform(X_test), columns=X_test.columns)
          # Get the X test data which is not scaled
           _, unscaled_X_test, _, _ = train_test_split(X_copy, y, test_size=0.3, random_
In [15]:
          print("Shape of X_train is: ", X_train.shape)
          print("Shape of X_test is: ", X_test.shape)
          print("Shape of y_train is: ", y_train.shape)
          print("Shape of y_test is: ", y_test.shape)
         Shape of X_{train} is: (354, 13)
         Shape of X_{\text{test}} is: (152, 13)
         Shape of y_{train} is: (354,)
         Shape of y_{test} is: (152,)
In [16]:
          # Linear Regression Model
          from sklearn.linear_model import LinearRegression
          model = LinearRegression()
In [17]:
          # Train the data
          model.fit(X train, y train)
         LinearRegression()
Out[17]:
In [18]:
          # Get the Prediction
          y preds = model.predict(X test)
```

Performance testing

```
In [20]: # Print out the different performance metrics for the model
    from sklearn.metrics import mean_squared_error, mean_absolute_error, r2_score

    mse = mean_squared_error(y_test, y_preds)
    mae = mean_absolute_error(y_test, y_preds)
    r2_score = r2_score(y_test, y_preds)

    print('For testing data:')
    print('Mean Squared Error is: ', mse)
    print('Mean absolute Error is: ', mae)
    print('R2 score is: ', r2_score)

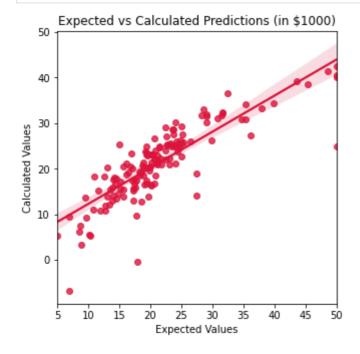
For testing data:
    Mean Squared Error is: 21.51744423117721
    Mean absolute Error is: 3.1627098714574053
    R2 score is: 0.7112260057484932
```

In [21]:

```
# Plotting predicted and target results
plt.figure(figsize=(5,5))

# Scatter Plot
sns.regplot(x=y_test, y=y_preds, color='crimson')

plt.title("Expected vs Calculated Predictions (in $1000)")
plt.xlabel("Expected Values")
plt.ylabel("Calculated Values")
plt.show()
```



In [22]:

```
# Print the coefficients of the regression model
np.set_printoptions(suppress=True)

coeff_dataframe = pd.DataFrame({'Attribute': X.columns, 'Regression Coefficie
coeff_dataframe
```

Out[22]:		Attribute	Regression Coefficient
	0	CRIM	-1.108346
	1	ZN	0.808440
	2	INDUS	0.343135

```
3
                  CHAS
                                     0.813864
            4
                   NOX
                                     -1.798043
            5
                                     2.913858
                   RM
            6
                   AGE
                                     -0.298939
            7
                   DIS
                                     -2.942511
            8
                   RAD
                                     2.094193
            9
                    TAX
                                     -1.447067
           10 PTRATIO
                                     -2.052322
           11
                      В
                                     1.023752
           12
                  LSTAT
                                     -3.885790
In [23]:
            # Add the Final Predictions in dataframe
            final_data = unscaled_X_test.copy()
            final_data['Target'] = y_test
final_data['Prediction'] = y_preds
```