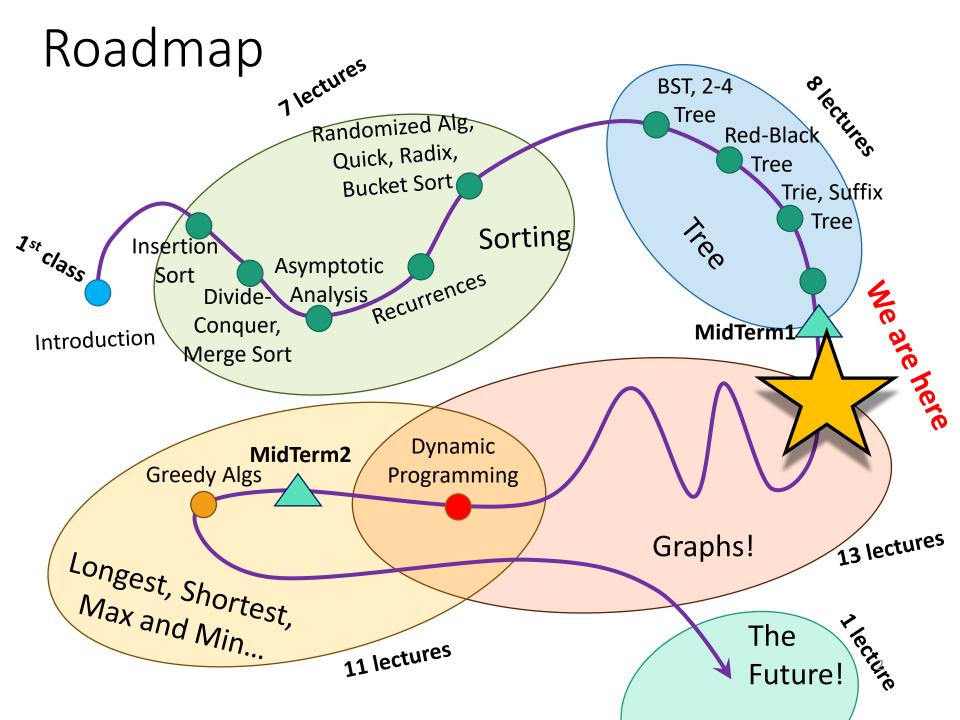
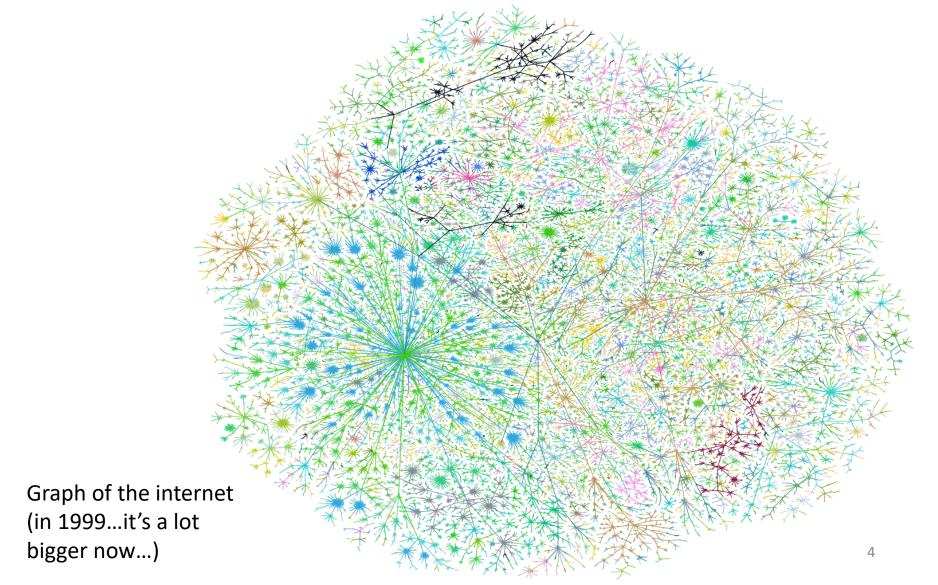
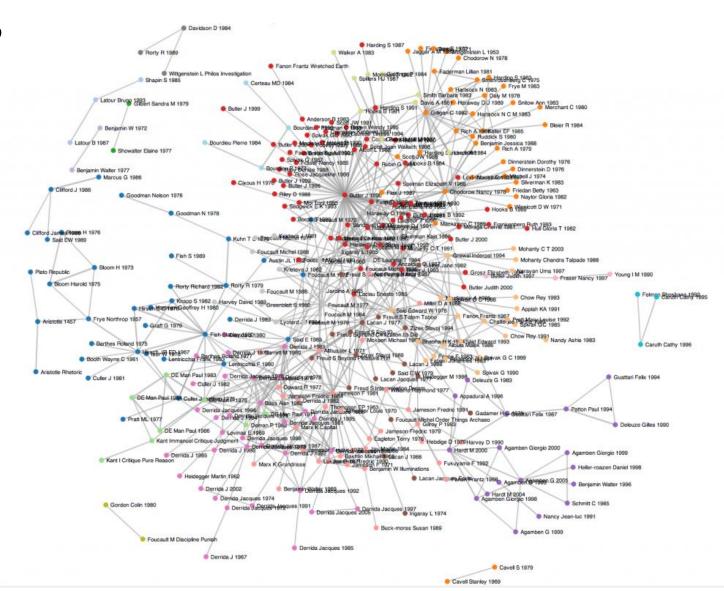
Advanced Data Structures and Algorithms

Graphs

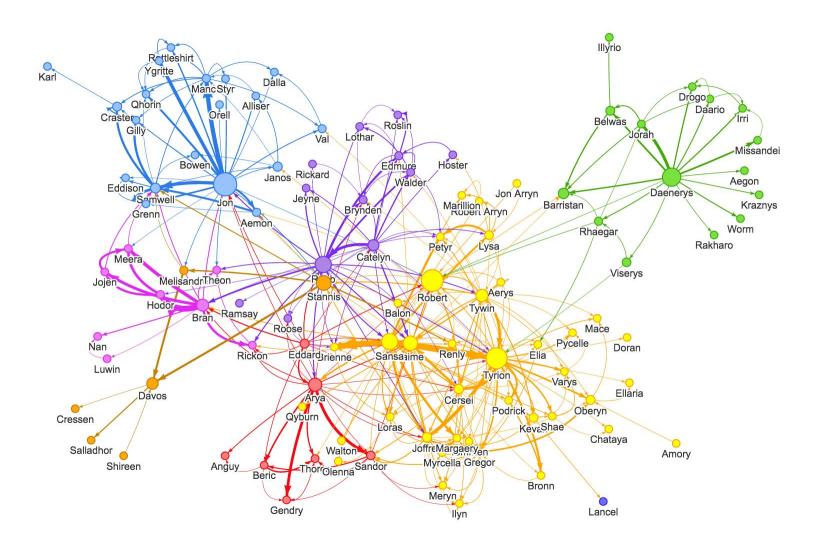






Citation graph of literary theory academic papers

Game of Thrones Character Interaction Network



AIR INDIA route map अंतरदेशीय Domestic Jammes Jammes धर्मशाला Dharamsala अमृतसर कुरूर Amnitsan Kullu • एअर इंडिया / Air India पण्डीगढ़ Chambrid ्र एअर इंडिया एक्सप्रेस / Air India Express Dehradun Pantnagar पासीघाट गुवाहाटी लखनऊ वागडोगरा 🐞 Jodhpur नोरखपुर Gorakhpur शिलांग 🛊 शिलाधर उदयपुर Udaipu वा राणसी राजकोट Ahmedabad इंदोप Indore आईजोल अवसपुर labalpur संची Ranchi भोपाल जामन्यर 💣 वडोदश कोलकाता Jamnagar

D

विजयवाडां

मन

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Puducherry

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हेदनाबाद

आरंगाबाद

वेगलुर

• मैसूर Mysore

INDIAN OCEAN

कोयम्बत्र

Graphs

बार मानवित्र विजयर है तथा किसी देश या प्रदेश की वैधानिक स्थिति ज्ञावन सरहब या गीनाओं के गीनानिकारन को संबंध में प्रकारक अववार एसके प्राचीनकों के किसी मत को अभिन्यका नहीं करता है।

This map is for illustrative purposes and does not imply the expression of any opinion on the part of the publisher or their sponsors concerning the legal status of any country or ferritory or concerning the delimitation of frontiers or boundaries.

भवनेश्वर

विशाखापटनम

Bhabaneshwar

BAY OF

BENGAL

पोर्ट क्लेयर

Andaman and Nicobar Islands(India)

Map not to scale. Cartographers tik roaps.

Lakshadweep (India)

нтантих Bhaynagai

मृंबई Mumba

मॅगलंडर

कोझीकोड Kozhkode

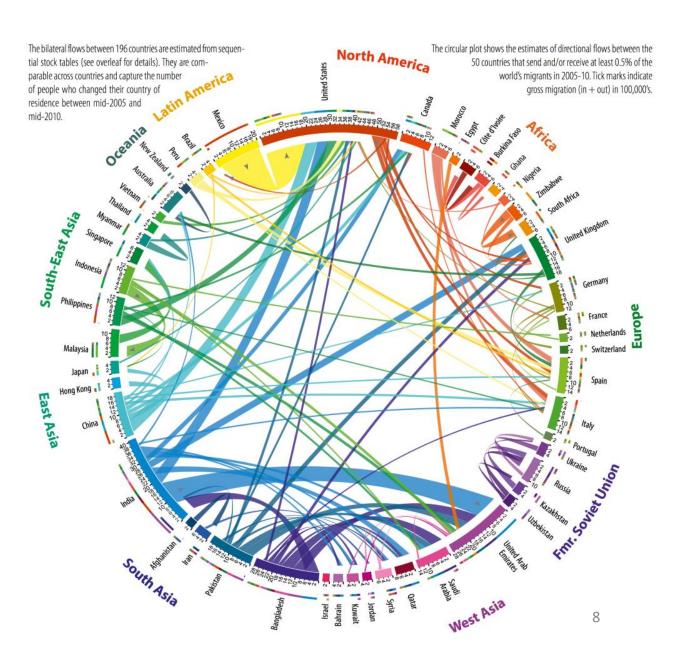
तिरुवनन्तपुरम Thiruvananthapuram

अगति

ARABIAN

SEA

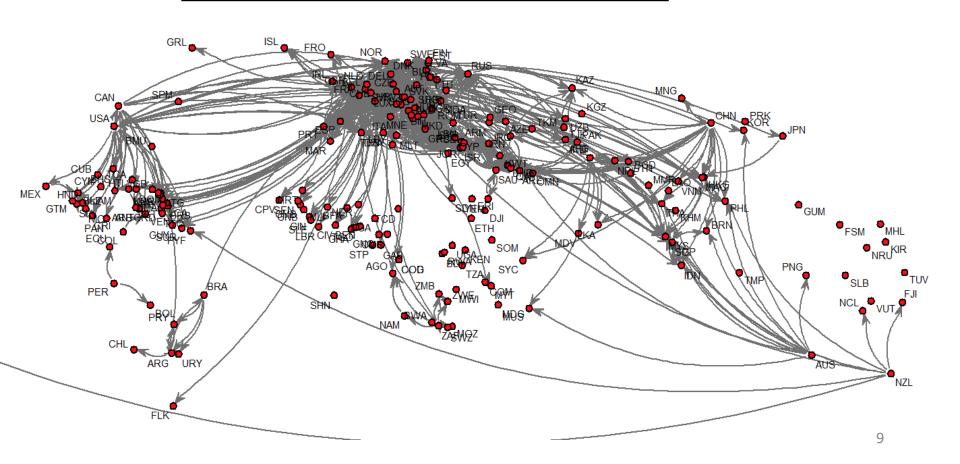
Immigration flows

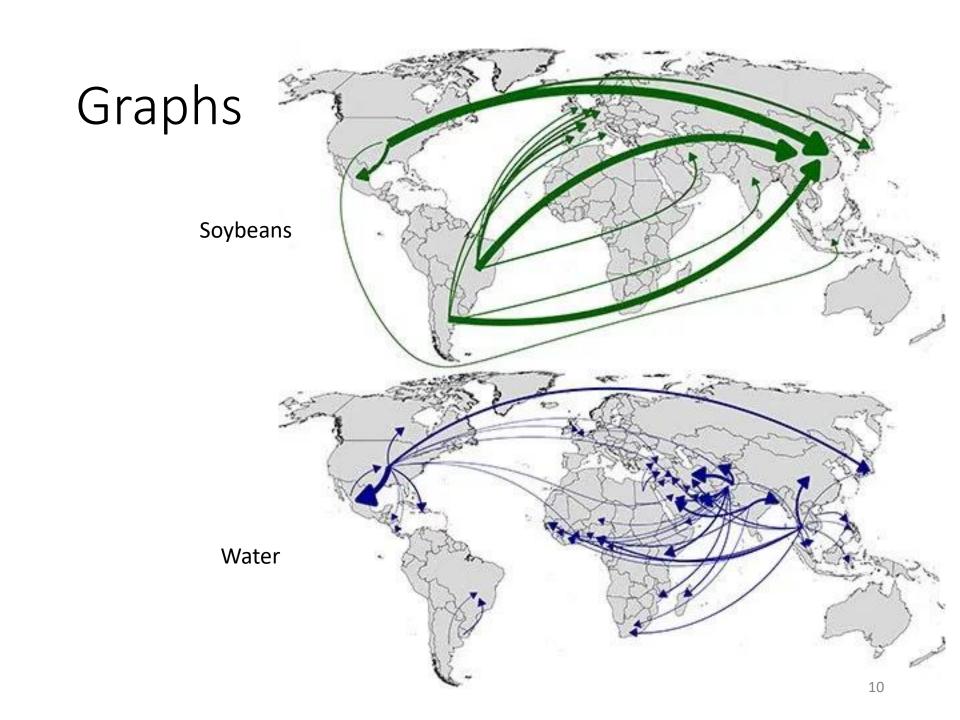


Potato trade

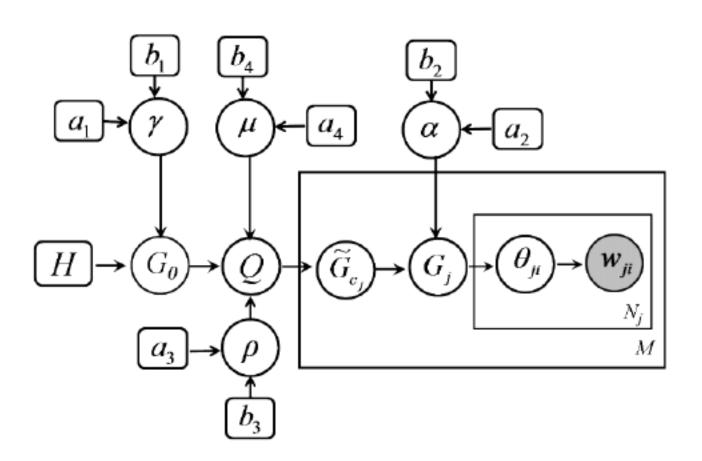
Graphs

World trade in fresh potatoes, flows over 0.1 m US\$ average 2005-2009

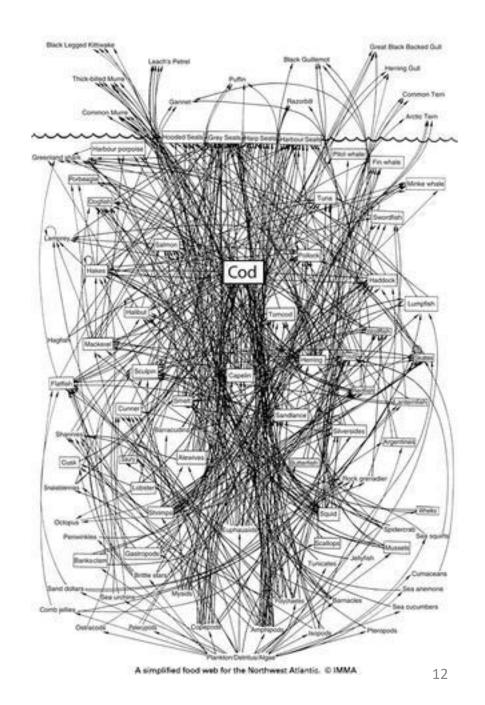




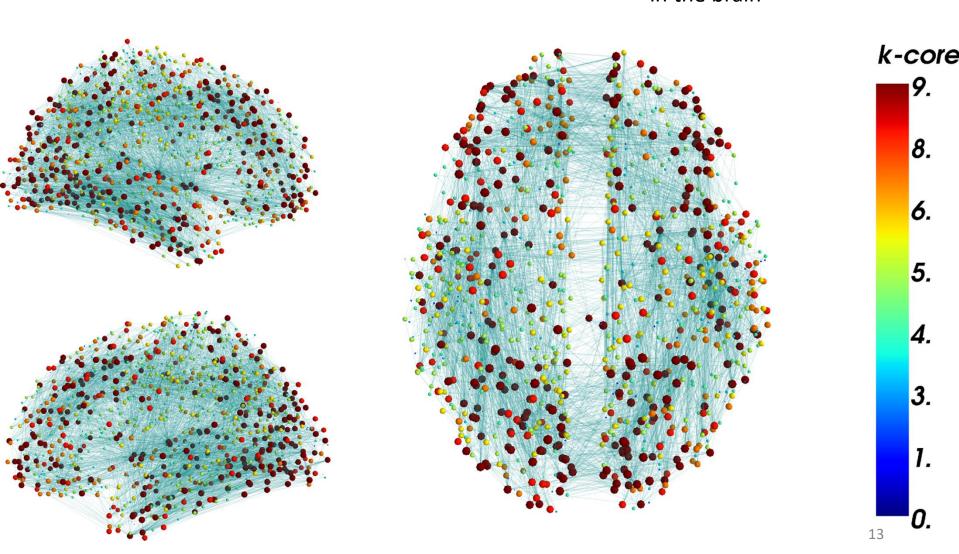
Graphical models



What eats what in the Atlantic ocean?



Neural connections in the brain



There are a lot of graphs.

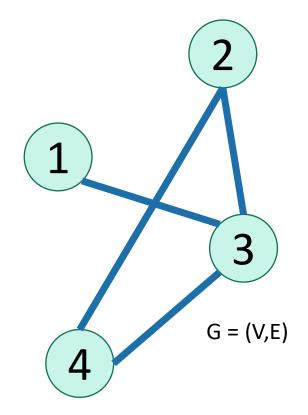
- We want to answer questions about them.
 - Efficient routing?
 - Community detection/clustering?
 - Signing up for classes without violating pre-requestions
 - How to distribute fish in tanks so that none of them will fight.
- This is what we'll do for the next several lectures.

Undirected Graphs

- Has vertices and edges
 - V is the set of vertices
 - E is the set of edges
 - Formally, a graph is G = (V,E)

Example

- $V = \{1,2,3,4\}$
- $E = \{ \{1,3\}, \{2,4\}, \{3,4\}, \{2,3\} \}$



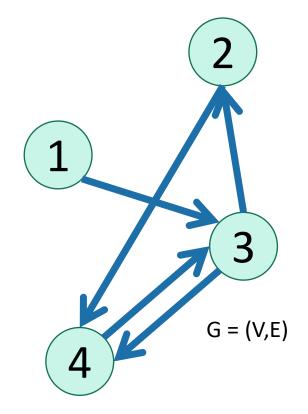
- The degree of vertex 4 is 2.
 - There are 2 edges coming out.
- Vertex 4's neighbors are 2 and 3

Directed Graphs

- Has vertices and edges
 - V is the set of vertices
 - E is the set of **DIRECTED** edges
 - Formally, a graph is G = (V,E)

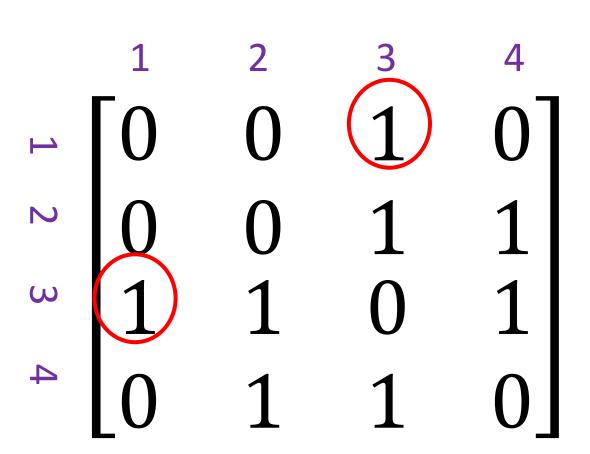
Example

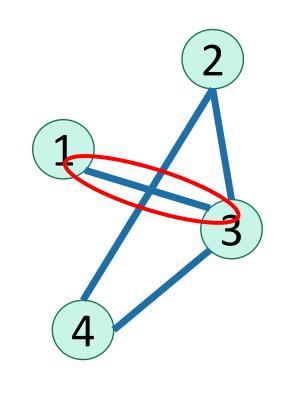
- $V = \{1,2,3,4\}$
- $E = \{ (1,3), (2,4), (3,4), (4,3), (3,2) \}$



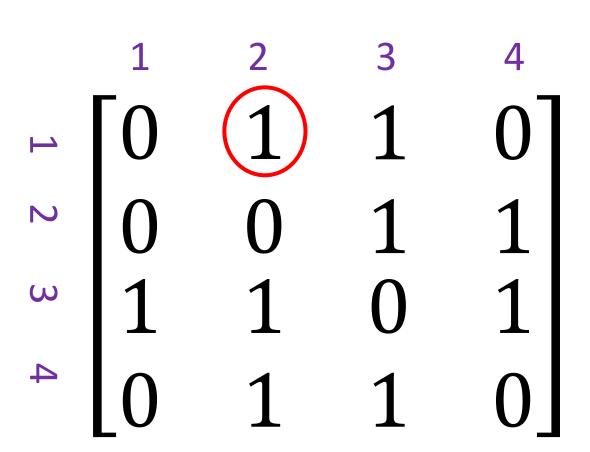
- The in-degree of vertex 4 is 2.
- The out-degree of vertex 4 is 1.
- Vertex 4's incoming neighbors are 2,3
- Vertex 4's outgoing neighbor is 3.

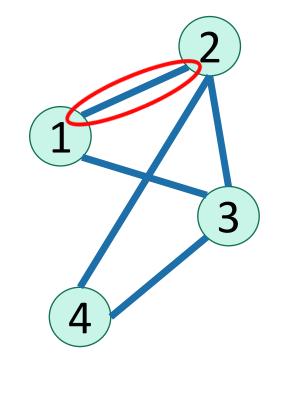
Option 1: adjacency matrix



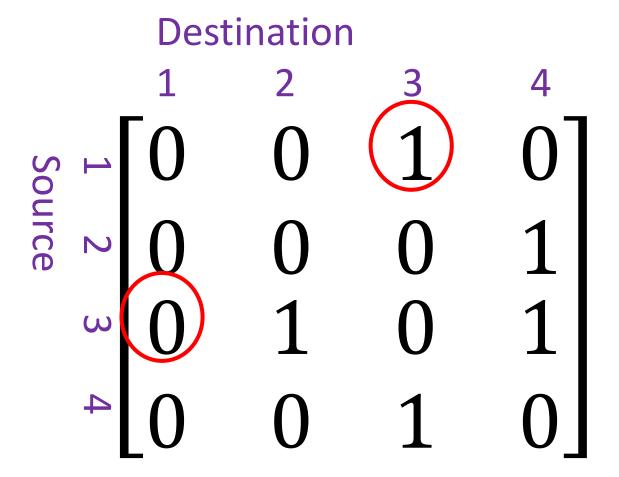


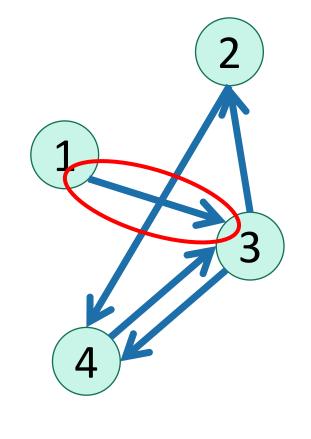
Option 1: adjacency matrix



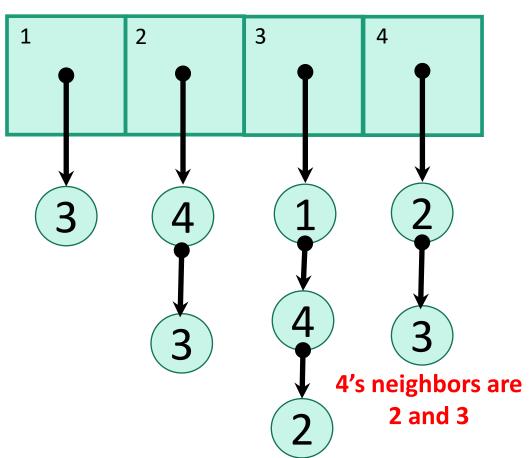


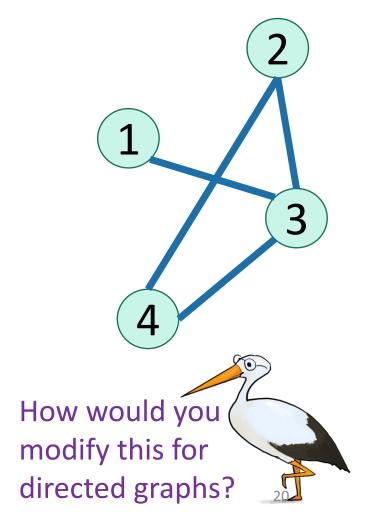
Option 1: adjacency matrix





Option 2: adjacency lists.



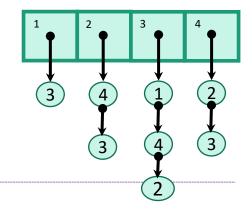


In either case

- Vertices can store other information
 - Attributes (name, IP address, ...)
 - helper info for algorithms that we will perform on the graph
- Want to be able to do the following operations:
 - Edge Membership: Is edge e in E?
 - Neighbor Query: What are the neighbors of vertex v?

Say there are n vertices	
and m edges.	

$$\begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 1 & 1 \\ 1 & 1 & 0 & 1 \\ 0 & 1 & 1 & 0 \end{bmatrix}$$



Edge membership

Is
$$e = \{v, w\}$$
 in E?

Neighbor query

Give me v's neighbors.

$$O(n^2)$$

$$O(n + m)$$

We'll assume this representation for the rest of the class