

# Normalization

1. Relation R has eight attributes ABCDEFGH. Fields of R contain only atomic values.  $F = \{CH \rightarrow G, A \rightarrow BC, B \rightarrow CFH, E \rightarrow A, F \rightarrow EG\}$  is a set of functional dependencies (FDs) so that  $F^+$  is exactly the set of FDs that hold for R. How many candidate keys does the relation R have?

2. Consider the relation scheme  $R = \{E, F, G, H, I, J, K, L, M, N\}$  and the set of functional dependencies  $\{\{E, F\} \rightarrow \{G\}, \{F\} \rightarrow \{I, J\}, \{E, H\} \rightarrow \{K, L\}, K \rightarrow \{M\}, L \rightarrow \{N\}$  on  $R$ . What is the key for  $R$ ?

3. Suppose you are given a relation  $R=\{A,B,C,D,E\}$  with the following functional dependencies : $\{CE \rightarrow D, D \rightarrow B, C \rightarrow A\}$ .
- a. Find all candidate keys.
  - b. Identify the normal form that  $R$  satisfies.

4. You are given the following set of functional dependencies for a relation  $R(A,B,C,D,E,F)$ .

$\{ABC \rightarrow D, ABD \rightarrow E, CD \rightarrow F, CDF \rightarrow B, BF \rightarrow D\}$

a. What are the keys of this relation?

b. Is this relation in 3NF? Is it 2NF ? Explain your answers.

5. The best normal form of relation scheme  $R(A, B, C, D)$  along with the set of functional dependencies  $F = \{AB \rightarrow C, AB \rightarrow D, C \rightarrow A, D \rightarrow B\}$  is

## Solutions

1.  $A^+$  is ABCDEFGH which is all attributes except D.  $B^+$  is also ABCDEFGH which is all attributes except D.  $E^+$  is also ABCDEFGH which is all attributes except D.  $F^+$  is also ABCDEFGH which is all attributes except D. So there are total 4 candidate keys AD, BD, ED and FD

2.  $\{EF\}^+ = \{EFGIJ\}$

$\{EFH\}^+ = \{EFGHIJKLMN\} = R$  (Candidate Key)

$\{EFHKL\}^+ = \{EFGHIJKLMN\} = R$  But it is not minimal key  
and for candidate key it should be minimal Super Key.



3. a.) Key - CE

b.) The relation is in 1NF

4. a. Keys {ABC,ACD}

b. It is not in 3NF .Counterexample  $ABD \rightarrow E$  and ABD is not a superkey and E is not prime attribute.

It is not in 2NF.  $CD \rightarrow F$  (partial dependency)

5. The relation is in 3NF.