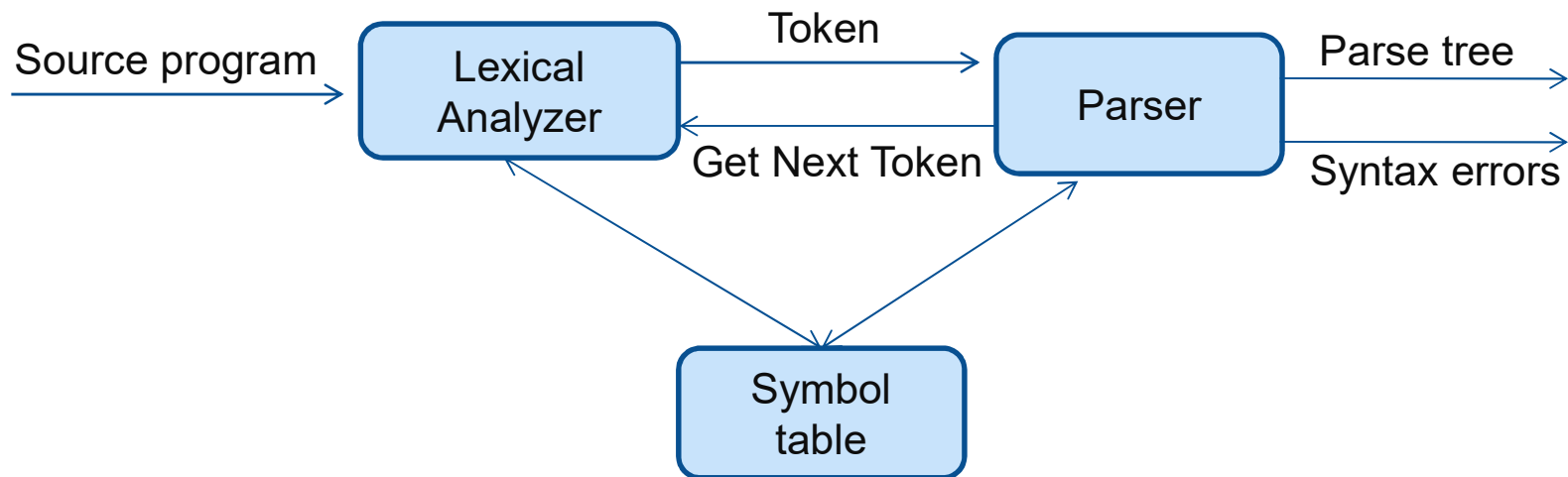


# **Syntax Analysis**

## **(Part-1)**

## Role of Parser

- The parser obtains a string of tokens from the lexical analyzer and verifies that the string can be generated by the grammar for the source language to form a ***parse tree***.
- The parser provides report for any ***syntax errors*** in an intelligible fashion. It should also recover from commonly occurring errors so that it can continue processing the remainder of its input.



# Error Handling

- The programmers frequently write incorrect programs, and a good compiler should assist the programmer in identifying and locating errors.
- The programs can contain errors at many different levels. For example, errors can be:
  - **lexical**, such as misspelling an identifier, keyword, or operator
  - **syntactic**, such as an arithmetic expression with unbalanced parentheses
  - **semantic**, such as an operator applied to an incompatible operand
  - **logical**, such as an infinitely recursive call
- Often ***much of the error detection*** and recovery in a compiler is centered around the syntax analysis phase.
- One reason for this is that ***many errors are syntactic in nature*** or are exposed when the stream of tokens coming from the lexical analyzer disobeys the grammatical rules.

# Context-free Grammars

A context free grammar (grammar for short) consists of terminals, non-terminals, a start symbol, and productions.

- Terminals are the basic symbols from which strings are formed. The word "**token**" is a synonym for "**terminal**" when we are talking about grammars for programming languages. Each of the keywords **if**, **then** and **else** is a terminal.
- **Non-terminals** are syntactic variables that denote sets of strings. The non-terminals define sets of strings that help to define the language generated by the grammar.
- In a grammar, one non-terminal is distinguished as the **start symbol**. And the set of strings it denotes is the language defined by the grammar.
- The **productions** of a grammar specify the manner in which the terminals and non-terminals can be combined to form strings. Each production consists of a non-terminal, followed by an arrow (sometimes the symbol  $:=$  is used), followed by a string of non-terminals and terminals.

## Grammar for Arithmetic Expression

**expr -> expr op expr**

**expr -> ( expr )**

**expr -> - expr**

**expr -> id**

**op -> +**

**op -> -**

**op -> \***

**op -> /**

In this grammar, the terminal symbols are **id + - / ( )**  
and the non-terminal symbols are **expr** and **op**.  
**expr** is the start symbol.

# Derivation Tree/ Parse Tree

- The sequence of intermediary strings generated to expand the start symbol of the grammar to a desired string of terminals is called a **derivation**.
- The derivation can be represented by a tree is called **parse tree**.

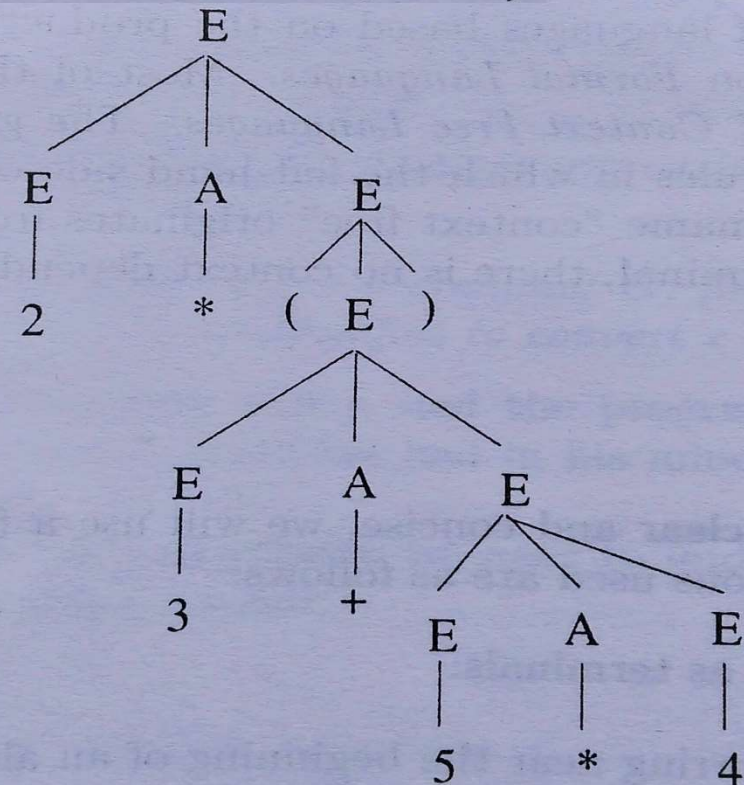
$E \rightarrow E A E \mid ( E ) \mid - E \mid \text{id}$

$A \rightarrow + \mid - \mid * \mid /$

## Derivation for “2\*(3+5\*4)”

$E \rightarrow EAE \rightarrow 2AE \rightarrow 2^*E$   
 $\rightarrow 2^*(E) \rightarrow 2^*(EAE)$   
 $\rightarrow 2^*(3AE) \rightarrow 2^*(3+E)$   
 $\rightarrow 2^*(3+EAE) \rightarrow 2^*(3+5AE)$   
 $\rightarrow 2^*(3+5^*E) \rightarrow 2^*(3+5^*4)$

Parse tree for “2\*(3+5\*4)”



# Leftmost and Rightmost Derivations

- The derivation in which the leftmost nonterminal is always replaced at each step is called ***leftmost derivation***.
- The derivation in which the rightmost nonterminal is always replaced at each step is called ***rightmost derivation***.
- In leftmost derivation, the intermediate strings are called ***left sentential forms***.
- In rightmost derivation, the intermediate strings are called ***right sentential forms***.
- The rightmost derivation is also called ***canonical representation***.

For example

**expr -> expr op expr**

**expr -> ( expr )**

Leftmost derivation

**expr -> expr op expr  
-> ( expr ) op expr**

Rightmost derivation

**expr -> expr op expr  
-> expr op ( expr )**

# Ambiguous Grammar

- A grammar is said to be ambiguous if there exists more than one parse tree for the same sentence.
- An ambiguous grammar can have more than one leftmost and rightmost derivations.

**$E \rightarrow E + E \mid E - E \mid E * E \mid E / E \mid (E) \mid -E \mid id$**

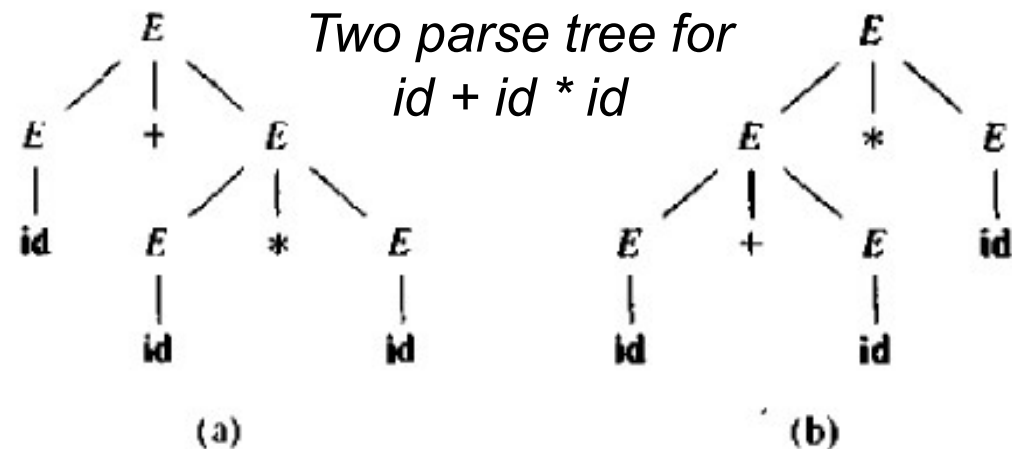
The sentence  **$id + id * id$**   
has the two distinct  
leftmost derivations.

Operator  $*$  having  
higher precedence  
than  $+$ .

Expression  $a+b*c$   
should be considered  
as  $a+(b*c)$  rather  
than as  $(a+b)*c$ .

$E \Rightarrow E + E$   
 $\Rightarrow id + E$   
 $\Rightarrow id + E * E$   
 $\Rightarrow id + id * E$   
 $\Rightarrow id + id * id$

$E \Rightarrow E * E$   
 $\Rightarrow E + E * E$   
 $\Rightarrow id + E * E$   
 $\Rightarrow id + id * E$   
 $\Rightarrow id + id * id$



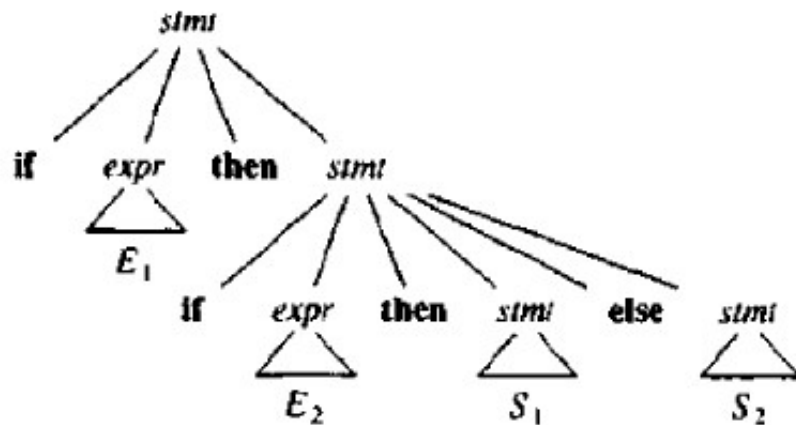


# Ambiguous Grammar

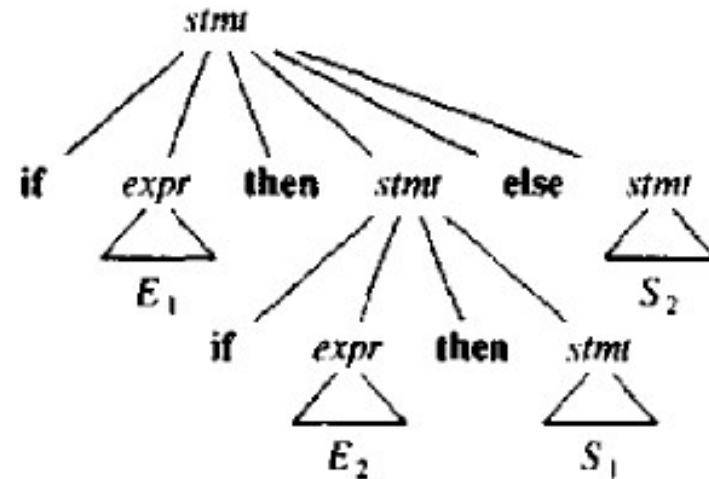
$stmt \rightarrow \text{if } expr \text{ then } stmt \mid \text{if } expr \text{ then } stmt \text{ else } stmt \mid \text{other}$

Here "other" stands for any other statement.

For example:  $\text{if } E_1 \text{ then if } E_2 \text{ then } S_1 \text{ else } S_2$



```
if E1 then
    if E2 then
        S1
    else
        S2
```



```
if E1 then
    if E2 then
        S1
else
    S2
```

# Eliminating Ambiguity

- In all programming languages with conditional statements of this form, the first parse tree is preferred.
- The general rule is "Match each else with the closest previous unmatched then."
- So, we can rewrite the grammar to eliminate ambiguity.

*stmt* -> *matched\_stmt* | *unmatched\_stmt*

*matched\_stmt* -> **if** *expr* **then** *matched\_stmt*  
**else** *matched\_stmt* | **other**

*unmatched\_stmt* -> **if** *expr* **then** *stmt* |  
**if** *expr* **then** *matched\_stmt* **else** *unmatched\_stmt*

**For example:** **if**  $E_1$  **then** **if**  $E_2$  **then**  $S_1$  **else**  $S_2$

*stmt* -> *unmatched\_stmt* -> **if** *expr* **then** *stmt* -> **if**  $E_1$  **then** *stmt*

-> **if**  $E_1$  **then** *matched\_stmt*

-> **if**  $E_1$  **then** **if** *expr* **then** *matched\_stmt* **else** *matched\_stmt*

-> **if**  $E_1$  **then** **if**  $E_2$  **then**  $S_1$  **else**  $S_2$

# Eliminating Ambiguity

- To resolve the ambiguity we can add a matching **endif** with an if statement. So the grammar should be

*stmt* -> **if** *expr* **then** *stmt* **endif** |  
          **if** *expr* **then** *stmt* **else** *stmt* **endif** | **other**

For example: **if**  $E_1$  **then** **if**  $E_2$  **then**  $S_1$  **else**  $S_2$  **endif** **endif**

*stmt* -> **if** *expr* **then** *stmt* **endif** -> **if**  $E_1$  **then** *stmt* **endif**  
          -> **if**  $E_1$  **then** **if** *expr* **then** *stmt* **else** *stmt* **endif** **endif**  
          -> **if**  $E_1$  **then** **if**  $E_2$  **then**  $S_1$  **else**  $S_2$  **endif** **endif**

For example: **if**  $E_1$  **then** **if**  $E_2$  **then**  $S_1$  **endif** **else**  $S_2$  **endif**

*stmt* -> **if** *expr* **then** *stmt* **else** *stmt* **endif**  
          -> **if**  $E_1$  **then** *stmt* **else** *stmt* **endif**  
          -> **if**  $E_1$  **then** **if** *expr* **then** *stmt* **endif** **else** *stmt* **endif**  
          -> **if**  $E_1$  **then** **if**  $E_2$  **then**  $S_1$  **endif** **else**  $S_2$  **endif**

# Left Recursion

- A grammar is left recursive if it has a nonterminal  $A$  such that there is a derivation  $A \rightarrow A\alpha$  for some string  $\alpha$ .
- Top-down parsing methods cannot handle left-recursive grammars, so a transformation that eliminates left recursion is needed.

## Elimination of Immediate Left Recursion

- The left-recursive pair of productions  $A \rightarrow A\alpha \mid \beta$  could be replaced by the non-left-recursive productions as follows:

$$A \rightarrow \beta A'$$

$$A' \rightarrow \alpha A' \mid \epsilon$$

Thus, the rule  $A \rightarrow A\alpha_1 \mid A\alpha_2 \mid \dots \mid A\alpha_m \mid \beta_1 \mid \beta_2 \mid \dots \mid \beta_n$  can be modified as,

$$A \rightarrow \beta_1 A' \mid \beta_2 A' \mid \dots \mid \beta_n A'$$

$$A' \rightarrow \alpha_1 A' \mid \alpha_2 A' \mid \dots \mid \alpha_m A' \mid \epsilon$$

# Elimination of Left Recursion

Eliminate Immediate Left Recursion from the following grammar:

$E \rightarrow E + T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow (E) \mid \text{id}$

Solution:

$E \rightarrow T E'$

$E' \rightarrow + T E' \mid \epsilon$

$T \rightarrow F T'$

$T' \rightarrow * F T' \mid \epsilon$

$F \rightarrow (E) \mid \text{id}$

# Elimination of Left Recursion

For example, consider the grammar,  $S \rightarrow Aa, A \rightarrow Sb \mid c$

Here, S is left recursive, because  $S \rightarrow Aa \rightarrow Sba$ . This form of general recursion can be eliminated with the following algorithm.

## Algorithm for elimination of left recursion

1. Arrange non terminals in some order, say  $A_1, A_2, \dots, A_m$ .
2. For  $i = 1$  to  $m$  do  
    For  $j = 1$  to  $i-1$  do  
        For each set of productions  $A_i \rightarrow A_j \gamma$  and  $A_j \rightarrow \delta_1 \mid \delta_2 \mid \dots \mid \delta_k$   
        Replace  $A_i \rightarrow A_j \gamma$  by  $A_i \rightarrow \delta_1 \gamma \mid \delta_2 \gamma \mid \dots \mid \delta_k \gamma$
3. Eliminate immediate left recursion from all productions

-----  
So, for the grammar  $S \rightarrow Aa, A \rightarrow Sb \mid c$

**Step 1:** Order of non-terminals are S, A.

**Step 2:** For  $i=1$ ,  $S \rightarrow Aa$  (there is no immediate left recursion)

For  $i=2$ ,  $A \rightarrow Sb \mid c$  is modified as,  $A \rightarrow Aab \mid c$

**Step 3:** Finally,  $S \rightarrow Aa, A \rightarrow cA', A' \rightarrow abA' \mid \epsilon$

# Elimination of Left Recursion

**Assignment No. 3: Eliminate Left Recursion of the following grammars.**

**a)  $A \rightarrow Ac \mid Aad \mid bd \mid \epsilon$**

**b)  $E \rightarrow E + E \mid E * E \mid (E) \mid id$**

# Left Factoring

- **Left factoring** is a grammar transformation that is useful for producing a grammar suitable for **predictive parsing**.
- The basic idea is that when it is not clear which of two alternative productions to use to expand a nonterminal  $A$ , we may be able to rewrite the  $A$ -productions to defer the decision until we have seen enough of the input to make the right choice.
- For example, if we have the two productions
$$stmt \rightarrow \text{if expr then stmt else stmt} \mid \text{if expr then stmt}$$
- On seeing the input token **if**, we cannot immediately tell which production to choose to expand  $stmt$ . Only after **then**, if token **else** is found, we can decide the first rule to be used.
- This necessitates backtracking if token **else** is absent in the input stream, that is, it is an if-then statement. To **eliminate** this problem, the grammar is **left-factored** to take out the common portion separately as follows:
$$stmt \rightarrow \text{if expr then stmt else-clause}$$
$$else\_clause \rightarrow \text{else stmt} \mid \epsilon$$



# Algorithm for Left Factoring

- *Input:* Grammar  $G$ .
- *Output:* An equivalent left-factored grammar.
- *Method:* For each nonterminal  $A$  find the longest prefix  $\alpha$  common to two or more of its alternatives. If  $\alpha \neq \epsilon$ , i.e., there is a nontrivial common prefix, replace all the  $A$  productions  $A \rightarrow \alpha\beta_1 \mid \alpha\beta_2 \mid \dots \mid \alpha\beta_n \mid \gamma$  where  $\gamma$  represents all alternatives that do not begin with  $\alpha$  by

$$A \rightarrow \alpha A' \mid \gamma$$

$$A' \rightarrow \beta_1 \mid \beta_2 \mid \dots \mid \beta_n$$

Here  $A'$  is a new nonterminal. Repeatedly apply this transformation until no two alternatives for a nonterminal have a common prefix.

For example:  $S \rightarrow iEtS \mid iEtSeS \mid a$

$$E \rightarrow b$$

After Left Factoring:

$$S \rightarrow iEtSS' \mid a$$

$$S' \rightarrow eS \mid \epsilon$$

$$E \rightarrow b$$

# Top-Down Parsing

- Top-down parsers get the name from the fact that they try to find a derivation of the input stream from the start symbol of the grammar.
- Equivalently, it can be viewed as an attempt to construct the parse tree rooted at the start symbol of the grammar for the input stream. There are two main approaches for top-down parsing.
  - **Recursive descent parsing**
  - **Predictive parsing**

## Recursive Descent Parsing

- Top-down parsing can be viewed as an attempt to find a leftmost derivation for an input string.
- It can be viewed as an attempt to construct a parse tree for the input starting from the root and creating the nodes of the parse tree in preorder.
- A general form of top-down parsing, called recursive descent, that may involve backtracking, that is, making repeated scans of the input.
- However, backtracking parsers are not seen frequently due to inefficiency.

# Recursive Descent Parsing

**Example:** Consider the grammar

**$S \rightarrow abA, \quad A \rightarrow cd \mid c \mid \epsilon$**

For the input stream **ab**:

- The parser starts by constructing a parse tree representing  $S \rightarrow abA$  as shown in Fig. (a).
- The tree is expanded with the production  $A \rightarrow cd$  as shown in Fig. (b).
- Since it does not match the string **ab**, the parser backtracks and then, tries the alternative  $A \rightarrow c$  as shown in Fig. (c). However, the parse tree does not match the string **ab**.
- So, the parser backtracks and tries out the alternative  $A \rightarrow \epsilon$  as shown in Fig. (d). This time it finds a match. Thus, the parsing is complete and successful.

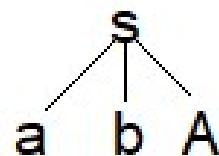


Fig. (a)

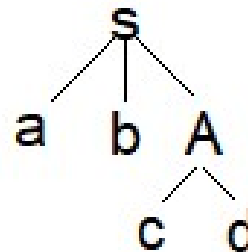


Fig. (b)

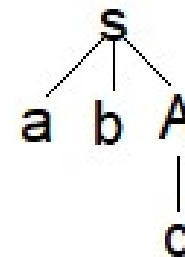


Fig. (c)

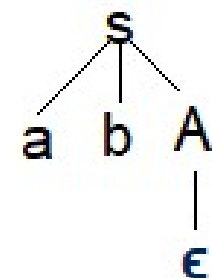


Fig. (d)

# Recursive Descent Parsing

- If the grammar is ***left-recursive***, a recursive descent parser ***may fall into an infinite loop*** even in the presence of backtracking.
- This happens because of the fact that for a left-recursive rule, the parser has to expand without consuming any further input symbol.
- A parser construction strategy, known as ***predictive parser*** is developed to create a recursive descent parser that ***does not need backtracking***.
- The ***predictive parser*** can be constructed in both ***recursive and non-recursive*** manner.

# Recursive Predictive Parsing

- In many cases, by carefully writing a grammar, eliminating left recursion from it, and left factoring the resulting grammar, we can obtain a grammar that can be parsed by a recursive-descent parser that needs no backtracking, i.e., a predictive parser.
- To construct a predictive parser, we must know, given the current input symbol  $a$  and the nonterminal  $A$  to be expanded, which one of the alternatives of production  $A \rightarrow \alpha_1 \mid \alpha_2 \mid \dots \mid \alpha_n$  is the unique alternative that derives a string beginning with  $a$ . That is, the proper alternative must be detectable by looking at only the first symbol it derives.
- Flow-of-control constructs in most programming languages, with their distinguishing keywords are usually detectable in this way.
- For example, if we have the productions  
 $stmt \rightarrow \text{if } expr \text{ then } stmt \text{ else } stmt \mid \text{while } expr \text{ do } stmt$   
then the keywords **if** and **while** tell us which alternative is the only one that could possibly succeed if we are to find a statement.

# Recursive Predictive Parsing

- **After left factoring**, the resultant rules can also be represented in the form of a set of transition diagrams. For this purpose we can **create a diagram for each nonterminal A**.
  1. Create an initial and final (return) state.
  2. For each production  $A \rightarrow X_1 X_2 \dots X_n$ , create a path from the initial state to the final state, with edge labeled  $X_1, X_2, \dots, X_n$ .
- The predictive parser begins in the start state **s** for the start symbol. If after some actions it moves to a state **t** with an edge label of terminal **a**, and if the next input symbol is **a**, then the parser moves the input cursor one position right and goes to state **t**.
- If the edge is labeled by a nonterminal **A**, the parser instead goes to the start state for **A**, without moving the input cursor. If it ever reaches the final state for **A**, it immediately goes to state **t**, in effect having "read" **A** from the input during the time it moved from state **s** to **t**.
- Finally, if there is an edge from **s** to **t** labeled **ε**, then from state **s** the parser immediately goes to state **t**, without advancing the input.

# Recursive Predictive Parsing

**For example:**     $\text{exp} \rightarrow \text{exp} + \text{term} \mid \text{term}$   
                       $\text{term} \rightarrow \text{term} * \text{factor} \mid \text{factor}$   
                       $\text{factor} \rightarrow ( \text{exp} ) \mid \text{id}$

After removal of left-recursion we get

$\text{exp} \rightarrow \text{term exp\_tail}$

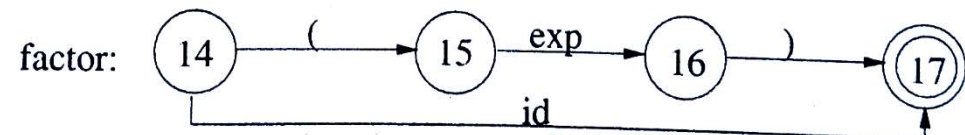
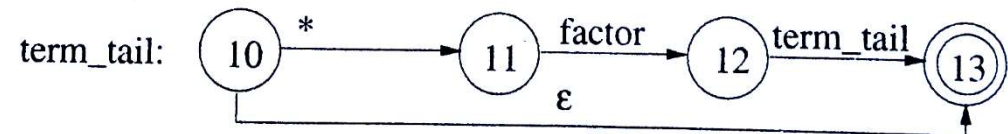
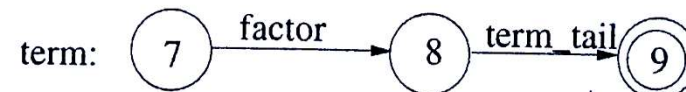
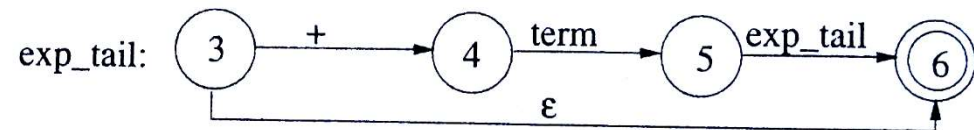
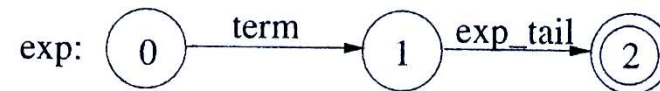
$\text{exp\_tail} \rightarrow + \text{term exp\_tail} \mid \epsilon$

$\text{term} \rightarrow \text{factor term\_tail}$

$\text{term\_tail} \rightarrow * \text{factor term\_tail} \mid \epsilon$

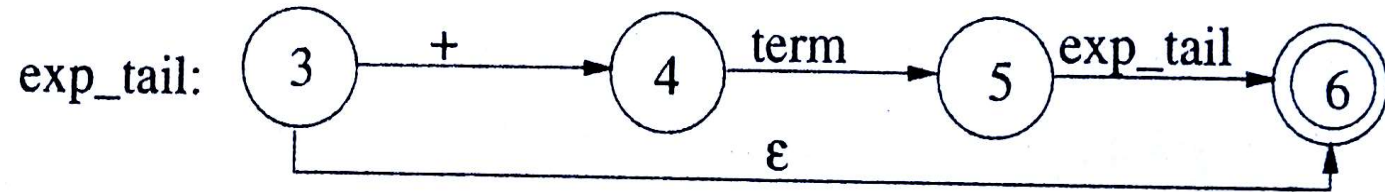
$\text{factor} \rightarrow ( \text{exp} ) \mid \text{id}$

## Transition Diagrams

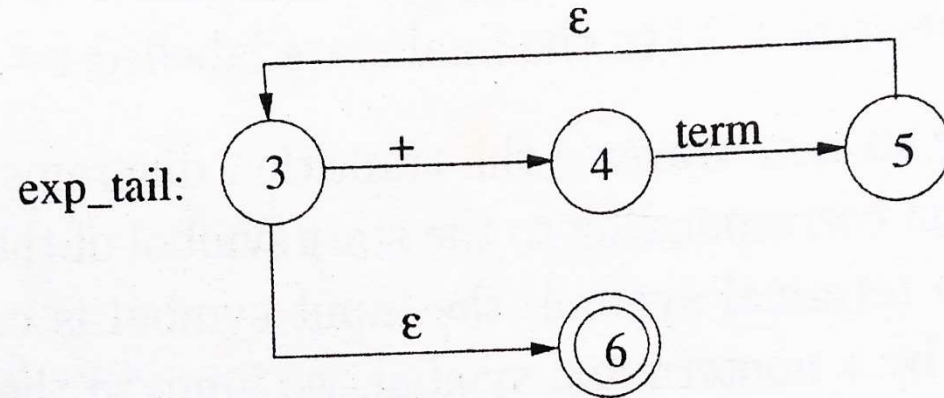


# Recursive Predictive Parsing

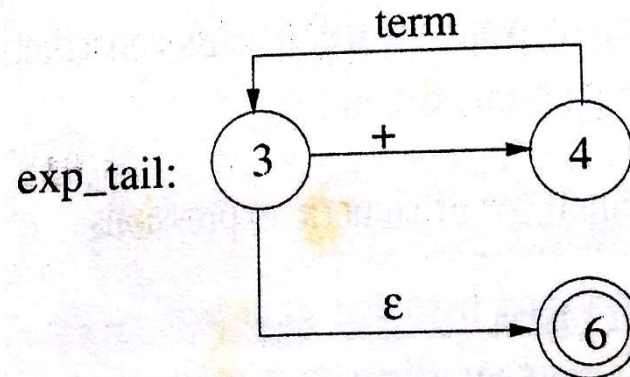
Simplification of diagrams may create a more compact and efficient parser.



First, we eliminate self-recursion in the `exp_tail` transition diagram, substituting an iterative model.

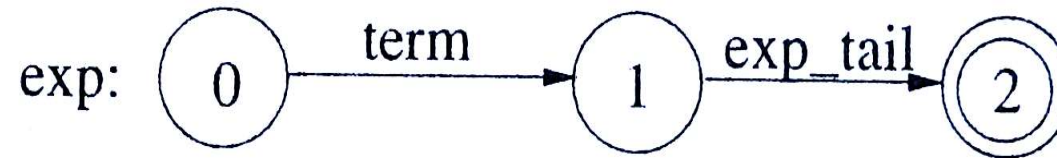


Further simplification by removing the redundant  $\epsilon$ -edge.

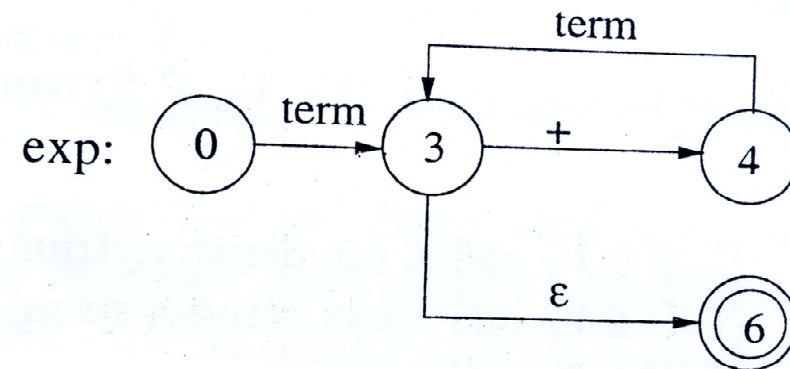




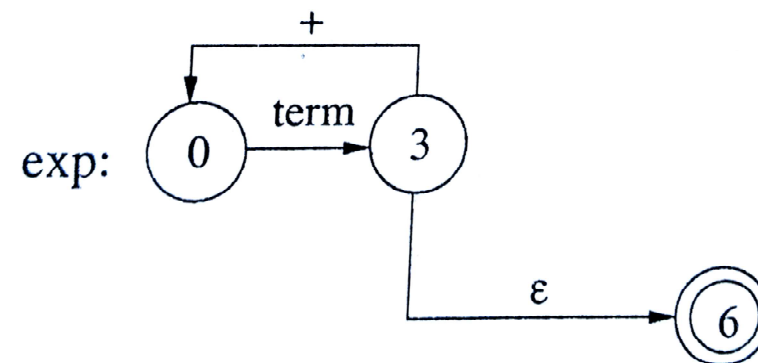
# Recursive Predictive Parsing



If we substitute the exp\_tail diagram in the exp one, replacing the exp\_tail edge from 1 to 2, we get



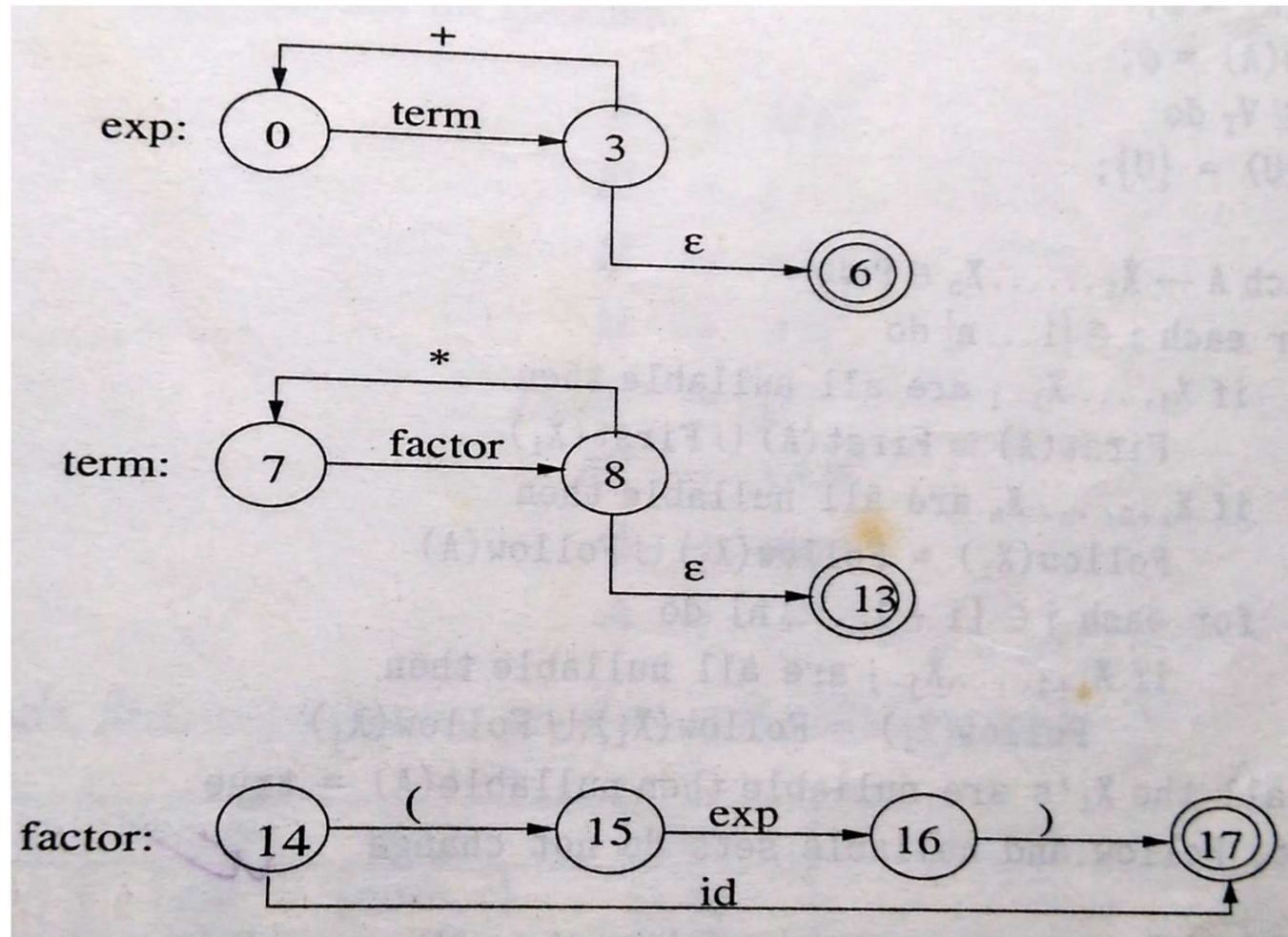
By further simplification we get



# Recursive Predictive Parsing

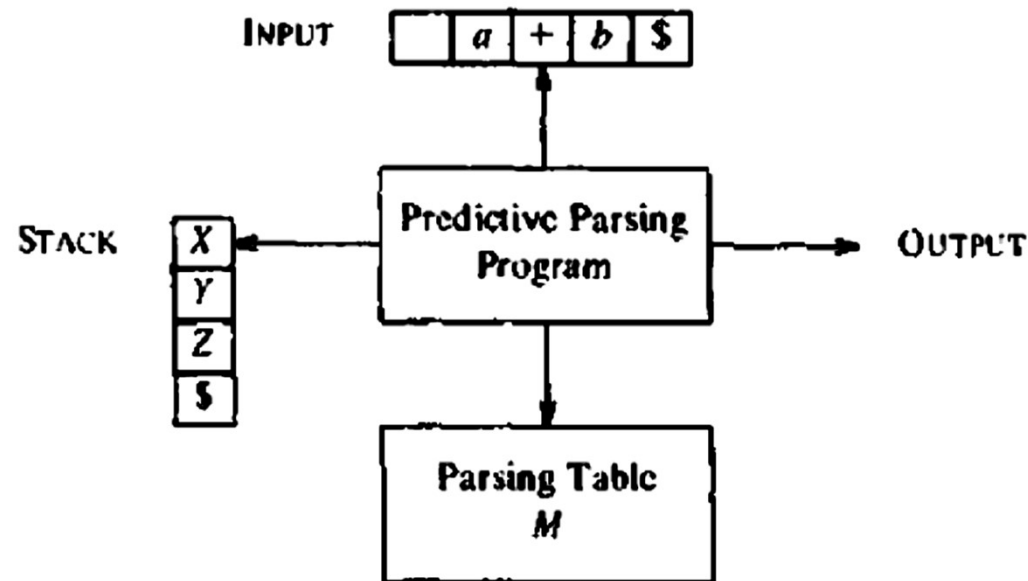
Applying the same approach to term and term\_tail, we get a reduced set of diagrams for arithmetic expressions as shown below.

## Final Set of Transition diagrams for expression grammar



# Non-Recursive Predictive Parsing- LL(k) Parsing

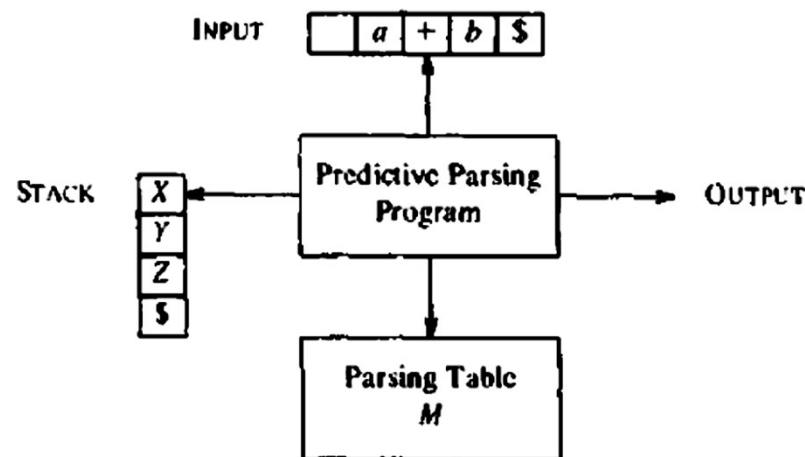
- It is possible to build a nonrecursive predictive parser by maintaining a stack explicitly, rather than implicitly via recursive calls. The key problem during predictive parsing is that of determining the production to be applied for a nonterminal. The nonrecursive parser looks up the production to be applied in a parsing table.



- This parser scan over the input stream using a prefix of tokens to identify the production applied. This parser is also called LL(k) parser, where *k* is the length of the prefix. “LL” stands for left-to-right scanning of the input stream and left-most derivation respectively.

# Non-Recursive Predictive Parsing- LL(k) Parsing

- A table-driven predictive parser has an input buffer, a stack, a parsing table, and an output stream.
- The input buffer contains the string to be parsed, followed by \$, a symbol used as a right endmarker to indicate the end of the input string.
- The stack contains a sequence of grammar symbols with \$ on the bottom, indicating the bottom of the stack.
- Initially, the stack contains the start symbol of the grammar on top of \$.
- The parsing table is a two dimensional array  $M[A, a]$ , where  $A$  is a nonterminal, and  $a$  is a terminal or the symbol \$.



# Non-Recursive Predictive Parsing- LL(k) Parsing

## Why FIRST and FOLLOW in Compiler Design?

- The need of backtracking is really a complex process to implement a parser.
- If the compiler would have come to know in advance, that what is the “**first** character of the string produced when a production rule is applied”, and comparing it to the current character or token in the input string, it can wisely take decision on which production rule to apply.

$S \rightarrow cAd$

$A \rightarrow bc|a$

And the input string is “cad”.

- After reading character ‘c’ in the input string and applying  $S \rightarrow cAd$ , next character in the input string is ‘a’, then it would directly use the production rule  $A \rightarrow a$ .

# Non-Recursive Predictive Parsing- LL(k) Parsing

## Why FIRST and FOLLOW in Compiler Design?

- The parser faces one more problem. Let us consider below grammar to understand this problem.

$A \rightarrow aBb$

$B \rightarrow c \mid \epsilon$

And suppose the input string is “ab” to parse.

- As the first character in the input is a, the parser applies the rule  $A \rightarrow aBb$ . Now the parser checks for the second character of the input string which is b, and the Non-Terminal to derive is B, but the parser can't get any string derivable from B that contains b as first character.
- But the Grammar does contain a production rule  $B \rightarrow \epsilon$ , if that is applied then B will vanish. But the parser can apply it only when it knows that the character that follows B in the production rule is same as the current character in the input.

# Non-Recursive Predictive Parsing- LL(k) Parsing

## Rules to Calculate First(X)

To compute First(X) for all grammar symbols X, apply the following rules:

1. If X is a terminal, then First(X) is {X}.
2. If  $X \rightarrow \epsilon$  is a production, then add  $\epsilon$  to First(X).
3. If X is nonterminal and  $X \rightarrow Y_1 Y_2 \dots Y_k$  is a production, then place a in First(X) if for some i, a is in First( $Y_i$ ), and  $\epsilon$  is in all of First( $Y_1$ ),  $\dots$ , First( $Y_{i-1}$ ); that is,  $Y_1 \dots Y_{i-1} \approx \epsilon$ . If  $\epsilon$  is in First( $Y_j$ ) for all  $j = 1, 2, \dots, k$ , then add  $\epsilon$  to First(X).

# Non-Recursive Predictive Parsing- LL(k) Parsing

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**Example:**

$E \rightarrow T E'$

$E' \rightarrow + T E' \mid \epsilon$

$T \rightarrow F T'$

$T' \rightarrow * F T' \mid \epsilon$

$F \rightarrow (E) \mid id$

$First(F) = \{First((E)), First(id)\}$

$First(T') = \{First(* F T'), \epsilon\}$

$First(T) = \{First(F)\}$

$First(E') = \{First(+ T E'), \epsilon\}$

$First(E) = \{First(T)\}$

	First
E	{(,id}
E'	{+,ε}
T	{(,id}
T'	{*,ε}
F	{(,id}



# Non-Recursive Predictive Parsing- LL(k) Parsing

## Rules to Calculate First(X)

To compute First(X) for all grammar symbols X, apply the following rules:

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Consider the grammar

$S \rightarrow aABe$      $A \rightarrow Abc \mid b$      $B \rightarrow d$

**Show the First sets for each nonterminal symbol.**

$\text{First}(B) = \{\text{First}(d)\} = \{d\}$

$\text{First}(A) = \{\text{First}(Abc), \text{First}(b)\} = \{\text{First}(A), b\} = \{b\}$

$\text{First}(S) = \{\text{First}(aABe)\} = \{a\}$

	First
S	{a}
A	{b}
B	{d}

# Non-Recursive Predictive Parsing- LL(k) Parsing

## Rules to Calculate First(X)

To compute First(X) for all grammar symbols X, apply the following rules:

1. If X is a terminal, then First(X) is {X}.
2. If  $X \rightarrow \epsilon$  is a production, then add  $\epsilon$  to First(X).
3. If X is nonterminal and  $X \rightarrow Y_1 Y_2 \dots Y_k$  is a production, then place a in First(X) if for some i, a is in First( $Y_i$ ), and  $\epsilon$  is in all of First( $Y_1$ ),  $\dots$  First( $Y_{i-1}$ ); that is,  $Y_1 \dots Y_{i-1} \approx \epsilon$ . If  $\epsilon$  is in First( $Y_j$ ) for all  $j = 1, 2, \dots, k$ , then add  $\epsilon$  to First(X).

Consider the grammar

$S \rightarrow A \mid B, A \rightarrow cA + b \mid a, B \rightarrow cB + a \mid b$

**Show the First sets for each nonterminal symbol.**

First(B)={c, b}

First(A)={c, a}

First(S) = {First(A), First(B)} = {a, b, c}

	First
S	{a,b,c}
A	{a, c}
B	{b, c}

# Non-Recursive Predictive Parsing- LL(k) Parsing

## Rules to Calculate First(X)

To compute First(X) for all grammar symbols X, apply the following rules:

1. If X is a terminal, then First(X) is {X}.
2. If  $X \rightarrow \epsilon$  is a production, then add  $\epsilon$  to First(X).
3. If X is nonterminal and  $X \rightarrow Y_1 Y_2 \dots Y_k$  is a production, then place a in First(X) if for some i, a is in First( $Y_i$ ), and  $\epsilon$  is in all of First( $Y_1$ ),  $\dots$  First( $Y_{i-1}$ ); that is,  $Y_1 \dots Y_{i-1} \approx \epsilon$ . If  $\epsilon$  is in First( $Y_j$ ) for all  $j = 1, 2, \dots, k$ , then add  $\epsilon$  to First(X).

Consider the grammar

$$\begin{aligned} S &\rightarrow iEaSS' \mid a \\ S' &\rightarrow eS \mid \epsilon \\ E &\rightarrow b \end{aligned}$$

Show the First sets for each nonterminal symbol.

	First
S	{i, a}
S'	{e, $\epsilon$ }
E	{b}

# Non-Recursive Predictive Parsing- LL(k) Parsing

## Rules to Calculate Follow(A)

To compute Follow(X) for all grammar symbols X, apply the following rules:

1. Place \$ in Follow(S), where S is the start symbol and \$ is the input right endmarker.
2. If there is a production,  $A \rightarrow \alpha B \beta$ , then everything in First( $\beta$ ) except for  $\epsilon$  is placed in Follow(B).
3. If there is a production,  $A \rightarrow \alpha B$ , or a production  $A \rightarrow \alpha B \beta$  where First( $\beta$ ) contains  $\epsilon$  (i.e.  $\beta \approx \epsilon$ ), then everything in Follow(A) is in Follow(B).

# Non-Recursive Predictive Parsing- LL(k) Parsing

## Rules to Calculate Follow(A)

To compute Follow(X) for all grammar symbols X, apply the following rules:

1. Place \$ in Follow(S), where S is the start symbol and \$ is the input right endmarker.
2. If there is a production,  $A \rightarrow \alpha B \beta$ , then everything in First( $\beta$ ) except for  $\epsilon$  is placed in Follow(B).
3. If there is a production,  $A \rightarrow \alpha B$ , or a production  $A \rightarrow \alpha B \beta$  where First( $\beta$ ) contains  $\epsilon$  (i.e.  $\beta \approx \epsilon$ ), then everything in Follow(A) is in Follow(B).

**Example:**

$E \rightarrow T E'$

$E' \rightarrow + T E' \mid \epsilon$

$T \rightarrow F T'$

$T' \rightarrow * F T' \mid \epsilon$

$F \rightarrow (E) \mid id$

$Follow(E) = \{\$, First( ) \}$

$Follow(E') = \{Follow(E)\}$

$Follow(T) = \{First(E'), Follow(E)\}$

$Follow(T') = \{Follow(T)\}$

$Follow(F) = \{First(T'), Follow(T)\}$

	First	Follow
E	{(,id}	{), \$}
E'	{+, $\epsilon$ }	{), \$}
T	{(,id}	{+, ), \$}
T'	{*, $\epsilon$ }	{+, ), \$}
F	{(,id}	{+, *, ), \$}

# Non-Recursive Predictive Parsing- LL(k) Parsing

## Rules to Calculate Follow(A)

To compute Follow(X) for all grammar symbols X, apply the following rules:

1. Place \$ in Follow(S), where S is the start symbol and \$ is the input right endmarker.
2. If there is a production,  $A \rightarrow \alpha B \beta$ , then everything in First( $\beta$ ) except for  $\epsilon$  is placed in Follow(B).
3. If there is a production,  $A \rightarrow \alpha B$ , or a production  $A \rightarrow \alpha B \beta$  where First( $\beta$ ) contains  $\epsilon$  (i.e.  $\beta \approx \epsilon$ ), then everything in Follow(A) is in Follow(B).

Consider the grammar  $S \rightarrow aABe$        $A \rightarrow Abc \mid b$        $B \rightarrow d$

**Show the First and Follow sets for each nonterminal symbol.**

Follow(S) = {\$}

Follow(A) = {First(B), First(b)} = {d, b}

Follow(B) = {First(e)} = { e }

	First	Follow
S	{a}	{ \$ }
A	{b}	{b, d}
B	{d}	{e}

# Non-Recursive Predictive Parsing- LL(k) Parsing

## Rules to Calculate Follow(A)

To compute Follow(X) for all grammar symbols X, apply the following rules:

1. Place \$ in Follow(S), where S is the start symbol and \$ is the input right endmarker.
2. If there is a production,  $A \rightarrow \alpha B \beta$ , then everything in First( $\beta$ ) except for  $\epsilon$  is placed in Follow(B).
3. If there is a production,  $A \rightarrow \alpha B$ , or a production  $A \rightarrow \alpha B \beta$  where First( $\beta$ ) contains  $\epsilon$  (i.e.  $\beta \approx \epsilon$ ), then everything in Follow(A) is in Follow(B).

Consider the grammar  $S \rightarrow A \mid B$ ,  $A \rightarrow cA+b \mid a$ ,  $B \rightarrow cB + a \mid b$

**Show the First and Follow sets for each nonterminal symbol.**

First(B)={c, b}

First(A)={c, a}

First(S) = {First(A), First(B)} = {a, b, c}

Follow(S)={\$}

Follow(A)={Follow(S), +}

Follow(B)={Follow(S), +}

	First	Follow
S	{a,b,c}	{\$}
A	{a, c}	{+, \$}
B	{b, c}	{+, \$}

# Non-Recursive Predictive Parsing- LL(k) Parsing

## LL(1) Grammar

A grammar is an LL(1) if all productions conform to the following LL(1) conditions:

1. For each production  $A \rightarrow \alpha_1 \mid \alpha_2 \mid \dots \mid \alpha_n$ ,  $\text{First}(\alpha_i) \cap \text{First}(\alpha_j) = \Phi$ ,  $\forall i \neq j$
2. If nonterminal  $X$  can derive  $\epsilon$ , then  $\text{First}(X) \cap \text{Follow}(X) = \Phi$

Check the grammar  $S \rightarrow A \mid B$ ,  $A \rightarrow cA + b \mid a$ ,  $B \rightarrow cB + a \mid b$  is LL(1) or not.

$\text{First}(B) = \{c, b\}$

$\text{First}(A) = \{c, a\}$

$\text{First}(S) = \{\text{First}(A), \text{First}(B)\} = \{a, b, c\}$

$\text{Follow}(S) = \{\$ \}$

$\text{Follow}(A) = \{\text{Follow}(S), +\}$

$\text{Follow}(B) = \{\text{Follow}(S), +\}$

	First	Follow
S	{a, b, c}	{ \$ }
A	{a, c}	{ +, \$ }
B	{b, c}	{ +, \$ }

$\text{First}(A) \cap \text{First}(B) = \{c\}$   
So, this is not LL(1).



# Non-Recursive Predictive Parsing- LL(k) Parsing

## Assignment No. 04

Consider the grammar

$A \rightarrow BCx \mid y$

$B \rightarrow yA \mid \epsilon$

$C \rightarrow Ay \mid x$

Where  $\{A, B, C\}$  is the set of nonterminal symbols,  $A$  is the start symbol,  $(x, y)$  is the set of terminal symbols.

1. Show the First and Follow sets for each nonterminal symbol.
2. Check the grammar is in LL(1) or not.

# Non-Recursive Predictive Parsing- LL(k) Parsing

## Construction of Predictive Parsing Table

- For each production  $A \rightarrow \alpha$  of the grammar
  - For each terminal  $a$  in  $\text{First}(\alpha)$ , add  $A \rightarrow \alpha$  to  $M[A, a]$ .
  - If  $\epsilon$  is in  $\text{First}(\alpha)$ , add  $A \rightarrow \alpha$  to  $M[A, b]$  for each terminal  $b$  in  $\text{Follow}(A)$ .
  - If  $\epsilon$  is in  $\text{First}(\alpha)$  and  $\$$  is in  $\text{Follow}(A)$ , add  $A \rightarrow \alpha$  to  $M[A, \$]$ .
- Make each undefined entry of  $M$  be error.

	First	Follow
E	{(,id}	{), \$}
E'	{+,ε}	{), \$}
T	{(,id}	{+, ), \$}
T'	{*,ε}	{+, ), \$}
F	{(,id}	{+, *, ), \$}

$E \rightarrow TE'$      $E' \rightarrow +TE' \mid \epsilon$      $T \rightarrow FT'$      $T' \rightarrow *FT' \mid \epsilon$      $F \rightarrow (E) \mid id$

NONTER-MINAL	INPUT SYMBOL					
	id	+	*	(	)	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow id$			$F \rightarrow (E)$		

# Non-Recursive Predictive Parsing- LL(k) Parsing

## Construction of Predictive Table

$$S \rightarrow iEtSS' \mid a$$

$$S' \rightarrow eS \mid \epsilon$$

$$E \rightarrow b$$

$$\text{Follow}(S) = \{\$, \text{First}(S'), \text{Follow}(S')\}$$

$$\text{Follow}(S') = \{\text{Follow}(S)\}$$

$$\text{Follow}(E) = \{t\}$$

	First	Follow
S	{i, a}	{\$, e}
S'	{e, ε}	{\$, e}
E	{b}	{t}

NONTER- MINAL	INPUT SYMBOL					
	a	b	e	i	t	\$
S	$S \rightarrow a$			$S \rightarrow iEtSS'$		
S'			$S' \rightarrow \epsilon$ $S' \rightarrow eS$			$S' \rightarrow \epsilon$
E		$E \rightarrow b$				

# Non-Recursive Predictive Parsing- LL(k) Parsing

## Nonrecursive predictive parsing

Set  $ip$  to point to the first symbol of  $w\$$

### **Repeat**

Let  $X$  be the top stack symbol and  $a$  the symbol pointed to by  $ip$

**If**  $X$  is a terminal or  $\$$  **Then**

**If**  $X = a$  **Then**

pop  $X$  from the stack and advance  $ip$

**Else** parsing error

**Elseif**  $M[X, a] = X \rightarrow Y_1 Y_2 \dots Y_k$  **Then** /\*  $X$  is a nonterminal \*/

pop  $X$  from the stack and

push  $Y_k, Y_{k-1}, \dots, Y_1$  onto the stack, with  $Y_1$  on top;

output the production  $X \rightarrow Y_1, Y_2 \dots Y_k$

**Else** parsing error

**Until**  $X = \$$  /\* stack is empty \*/

# Non-Recursive Predictive Parsing- LL(k) Parsing

NONTER-MINAL	INPUT SYMBOL					
	id	+	*	(	)	\$
$E$	$E \rightarrow TE'$			$E \rightarrow TE'$		
$E'$		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
$T$	$T \rightarrow FT'$			$T \rightarrow FT'$		
$T'$		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
$F$	$F \rightarrow id$			$F \rightarrow (E)$		

id + id \* id



Set  $ip$  to point to the first symbol of  $w\$$

**Repeat**

Let  $X$  = top stack symbol and  $a$  is pointed by  $ip$

**If**  $X$  is a terminal or  $\$$  **Then**

**If**  $X = a$  **Then**

pop  $X$  from the stack and advance  $ip$

**Else** parsing error

**Elseif**  $M[X, a] = X \rightarrow Y_1 Y_2 \dots Y_k$  **Then**

pop  $X$  from the stack and

push  $Y_k, Y_{k-1}, \dots, Y_1$  onto the stack  $Y_1$  on top;

output the production  $X \rightarrow Y_1 Y_2 \dots Y_k$

**Else** parsing error

**Until**  $X = \$$  /\* stack is empty \*/

STACK	INPUT	OUTPUT
$\$E$	id + id * id\$	
$\$E'T$	id + id * id\$	$E \rightarrow TE'$
$\$E'T'F$	id + id * id\$	$T \rightarrow FT'$
$\$E'T'id$	id + id * id\$	$F \rightarrow id$
$\$E'T'$	+ id * id\$	
$\$E'$	+ id * id\$	$T' \rightarrow \epsilon$
$\$E'T +$	+ id * id\$	$E' \rightarrow +TE'$
$\$E'T$	id * id\$	
$\$E'T'F$	id * id\$	$T \rightarrow FT'$
$\$E'T'id$	id * id\$	$F \rightarrow id$
$\$E'T'$	* id\$	
$\$E'T'F*$	* id\$	$T' \rightarrow *FT'$
$\$E'T'F$	id\$	
$\$E'T'id$	id\$	$F \rightarrow id$
$\$E'T'$	\$	
$\$E'$	\$	$T' \rightarrow \epsilon$
$\$$	\$	$E' \rightarrow \epsilon$

THANK YOU