

Subset Sum (medium)

We'll cover the following ^

- Problem Statement
- *
 - Example 1:
 - Example 2:
 - Example 3:
- Try it yourself
- Basic Solution
- Bottom-up Dynamic Programming
 - Code
 - Time and Space complexity
- Challenge

Problem Statement

Given a set of positive numbers, determine if a subset exists whose sum is equal to a given number 'S'.

Example 1:

```
Input: {1, 2, 3, 7}, S=6
Output: True
The given set has a subset whose sum is '6': {1, 2, 3}
```

Example 2:





```
Input: {1, 2, 7, 1, 5}, S=10
Output: True
The given set has a subset whose sum is '10': {1, 2, 7}
```

Example 3:

```
Input: {1, 3, 4, 8}, S=6
Output: False
The given set does not have any subset whose sum is equal to '6'.
```

Try it yourself

Try solving this question here:

 Java	 Python3	 C++	 JS
--	---	---	--

```
1 def can_partition(num, sum):
2     # TODO: Write your code here
3     return False
4
5
6 def main():
7     print("Can partition: " + str(can_partition([1, 2, 3, 7], 6)))
8     print("Can partition: " + str(can_partition([1, 2, 7, 1, 5], 10)))
9     print("Can partition: " + str(can_partition([1, 3, 4, 8], 6)))
10
11
12 main()
13
14
```

Run

Save

Reset



Basic Solution

This problem follows the **0/1 Knapsack pattern** and is quite similar to [Equal Subset Sum Partition](#). A basic brute-force solution could be to try all subsets of the given numbers to see if any set has a sum equal to 'S'.

So our brute-force algorithm will look like:

```
1 for each number 'i'
2   create a new set which INCLUDES number 'i' if it does not exceed 'S', and recursively
3   process the remaining numbers
4   create a new set WITHOUT number 'i', and recursively process the remaining numbers
5 return true if any of the above two sets has a sum equal to 'S', otherwise return false
```

Since this problem is quite similar to [Equal Subset Sum Partition](#), let's jump directly to the bottom-up dynamic programming solution.

Bottom-up Dynamic Programming

We'll try to find if we can make all possible sums with every subset to populate the array `dp[TotalNumbers][S+1]`.

For every possible sum 's' (where $0 \leq s \leq S$), we have two options:

1. Exclude the number. In this case, we will see if we can get the sum 's' from the subset excluding this number => `dp[index-1][s]`
2. Include the number if its value is not more than 's'. In this case, we will see if we can find a subset to get the remaining sum => `dp[index-1][s-num[index]]`

If either of the above two scenarios returns true, we can find a subset with a sum equal to 's'.

Let's draw this visually, with the example input {1, 2, 3, 7}, and start with our base case of size zero:

num\sum	0	1	2	3	4	5	6
1	T						
{1, 2}	T						
{1, 2, 3}	T						
{1, 2, 3, 7}	T						

'0' sum can always be found through an empty set

1 of 10

num\sum	0	1	2	3	4	5	6
1	T	T	F	F	F	F	F
{1, 2}	T						
{1, 2, 3}	T						
{1, 2, 3, 7}	T						

With only one number, we can form a subset only when the required sum is equal to that number

2 of 10

num/sum	0	1	2	3	4	5	6
1	T	T	F	F	F	F	F
{1, 2}	T	T					
{1,2,3}	T						
{1,2,3,7}	T						

sum: 1, index:1=> (dp[index-1][sum] , as the 'sum' is less than the number at index '1' (i.e., 1 < 2)

3 of 10

num/sum	0	1	2	3	4	5	6
1	T	T	F	F	F	F	F
{1, 2}	T	T	T				
{1,2,3}	T						
{1,2,3,7}	T						

sum: 2, index:1=> (dp[index-1][sum] || dp[index-1][sum-2])

4 of 10

num/sum	0	1	2	3	4	5	6
1	T	T	F	F	F	F	F
{1, 2}	T	T	T	T			
{1,2,3}	T						
{1,2,3,7}	T						

sum: 3, index:1=> (dp[index-1][sum] || dp[index-1][sum-2])

5 of 10

num/sum	0	1	2	3	4	5	6
1	T	T	F	F	F	F	F
{1, 2}	T	T	T	T	F	F	F
{1,2,3}	T						
{1,2,3,7}	T						

sum: 4-6 index:1=> (dp[index-1][sum] || dp[index-1][sum-2])

6 of 10

num/sum	0	1	2	3	4	5	6
1	T	T	F	F	F	F	F
{1, 2}	T	T	T	T	F	F	F
{1,2,3}	T	T	T	T			
{1,2,3,7}	T						

sum: 1,2,3, index:2=> (dp[index-1][sum] || dp[index-1][sum-3])

7 of 10

num/sum	0	1	2	3	4	5	6
1	T	T	F	F	F	F	F
{1, 2}	T	T	T	T	F	F	F
{1,2,3}	T	T	T	T	T		
{1,2,3,7}	T						

sum: 4, index:2=> (dp[index-1][sum] || dp[index-1][sum-3])

8 of 10

num/sum	0	1	2	3	4	5	6
1	T	T	F	F	F	F	F
{1, 2}	T	T	T	T	F	F	F
{1,2,3}	T	T	T	T	T	T	T
{1,2,3,7}	T						

sum: 5, 6, index:2=> (dp[index-1][sum] || dp[index-1][sum-3])

9 of 10

num/sum	0	1	2	3	4	5	6
1	T	T	F	F	F	F	F
{1, 2}	T	T	T	T	F	F	F
{1,2,3}	T	T	T	T	T	T	T
{1,2,3,7}	T	T	T	T	T	T	T

sum: 1-6, index:3=> (dp[index-1][sum] || dp[index-1][sum-7])

10 of 10



Code

Here is the code for our bottom-up dynamic programming approach:

Java

Python3

C++

JS

```
1 def can_partition(num, sum):
2     n = len(num)
3     dp = [[False for x in range(sum+1)] for y in range(n)]
4
5     # populate the sum = 0 columns, as we can always form '0' sum with an empty set
6     for i in range(0, n):
7         dp[i][0] = True
8
9     # with only one number, we can form a subset only when the required sum is
10    # equal to its value
11    for s in range(1, sum+1):
12        dp[0][s] = True if num[0] == s else False
13
14    # process all subsets for all sums
15    for i in range(1, n):
```

```
16     for s in range(1, sum+1):
17         # if we can get the sum 's' without the number at index 'i'
18         if dp[i - 1][s]:
19             dp[i][s] = dp[i - 1][s]
20         elif s >= num[i]:
21             # else include the number and see if we can find a subset to get the remaining sum
22             dp[i][s] = dp[i - 1][s - num[i]]
23
24     # the bottom-right corner will have our answer.
25     return dp[n - 1][sum]
26
27
28 def main():
29     print("Can partition: " + str(can_partition([1, 2, 3, 7], 6)))
30     print("Can partition: " + str(can_partition([1, 2, 7, 1, 5], 10)))
31     print("Can partition: " + str(can_partition([1, 3, 4, 8], 6)))
32
33
34 main()
35
36
37
38
39
```

Run Save Reset

Time and Space complexity

The above solution has the time and space complexity of $O(N * S)$, where 'N' represents total numbers and 'S' is the required sum.

Challenge

Can we improve our bottom-up DP solution even further? Can you find an algorithm that has $O(S)$ space complexity?

Show Hint

Java Python3 C++ JS

```
1 def can_partition(num, sum):
2     n = len(num)
3     dp = [False for x in range(sum+1)]
4
5     # handle sum=0, as we can always have '0' sum with an empty set
6     dp[0] = True
7
8     # with only one number, we can have a subset only when the required sum is equal to its value
9     for s in range(1, sum+1):
10         dp[s] = num[0] == s
11
12     # process all subsets for all sums
13     for i in range(1, n):
14         for s in range(sum, -1, -1):
15             # if dp[s]==true, this means we can get the sum 's' without num[i], hence we can move on to
16             # the next number else we can include num[i] and see if we can find a subset to get the
17             # remaining sum
18             if not dp[s] and s >= num[i]:
19                 dp[s] = dp[s - num[i]]
20
21     return dp[sum]
22
23
24 def main():
25     print("Can partition: " + str(can_partition([1, 2, 3, 7], 6)))
26     print("Can partition: " + str(can_partition([1, 2, 7, 1, 5], 10)))
27     print("Can partition: " + str(can_partition([1, 3, 4, 8], 6)))
28
29
30 main()
```

Run Save Reset


✓ 100%

Equal Subset Sum Partition (medium)

100% ✓

Minimum Subset Sum Difference (hard)

✓ Completed

 Report an Issue  Ask a Question