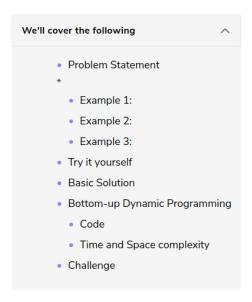
# Subset Sum (medium)



# Problem Statement #

Given a set of positive numbers, determine if a subset exists whose sum is equal to a given number 'S'.

### Example 1:

```
Input: {1, 2, 3, 7}, S=6
Output: True
The given set has a subset whose sum is '6': {1, 2, 3}
```

#### Example 2:

```
Input: {1, 2, 7, 1, 5}, S=10
Output: True
The given set has a subset whose sum is '10': {1, 2, 7}
```

### Example 3:

```
Input: {1, 3, 4, 8}, S=6
Output: False
The given set does not have any subset whose sum is equal to '6'.
```

## Try it yourself #

Try solving this question here:

```
Java  Python3  C++  Js JS

1  def can_partition(num, sum):
2  # TODO: Write your code here
3  return False

4

5
6  def main():
7  print("Can partition: " + str(can_partition([1, 2, 3, 7], 6)))
8  print("Can partition: " + str(can_partition([1, 2, 7, 1, 5], 10)))
9  print("Can partition: " + str(can_partition([1, 3, 4, 8], 6)))

10

11

12  main()

13

14
```



## Basic Solution #

This problem follows the **0/1 Knapsack pattern** and is quite similar to Equal Subset Sum Partition. A basic brute-force solution could be to try all subsets of the given numbers to see if any set has a sum equal to 'S'.

So our brute-force algorithm will look like:

```
for each number 'i'
create a new set which INCLUDES number 'i' if it does not exceed 'S', and recursively
process the remaining numbers
create a new set WITHOUT number 'i', and recursively process the remaining numbers
return true if any of the above two sets has a sum equal to 'S', otherwise return false
```

Since this problem is quite similar to Equal Subset Sum Partition, let's jump directly to the bottom-up dynamic programming solution.

# **Bottom-up Dynamic Programming**

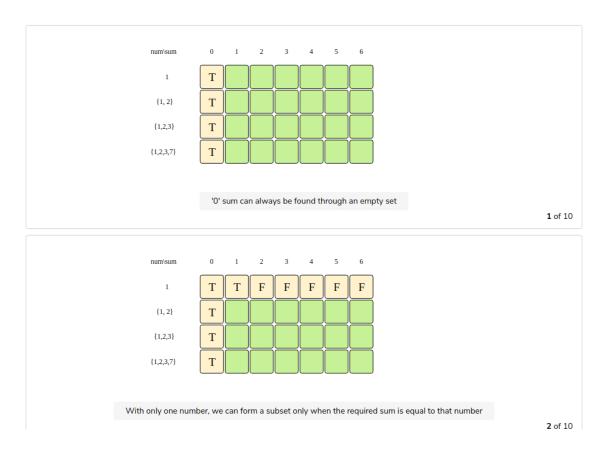
We'll try to find if we can make all possible sums with every subset to populate the array dp[TotalNumbers]
[S+1].

For every possible sum 's' (where 0 <= s <= S), we have two options:

- Exclude the number. In this case, we will see if we can get the sum 's' from the subset excluding this number => dp[index-1][s]
- 2. Include the number if its value is not more than 's'. In this case, we will see if we can find a subset to get the remaining sum => dp[index-1][s-num[index]]

If either of the above two scenarios returns true, we can find a subset with a sum equal to 's'.

Let's draw this visually, with the example input {1, 2, 3, 7}, and start with our base case of size zero:







### Code #

Here is the code for our bottom-up dynamic programming approach:

```
def can_partition(num, sum):

n = len(num)

dp = [[False for x in range(sum+1)] for y in range(n)]

# populate the sum = 0 columns, as we can always form '0' sum with an empty set

for i in range(0, n):

dp[i][0] = True

# with only one number, we can form a subset only when the required sum is

# equal to its value
for s in range(1, sum+1):

dp[0][s] = True if num[0] == s else False

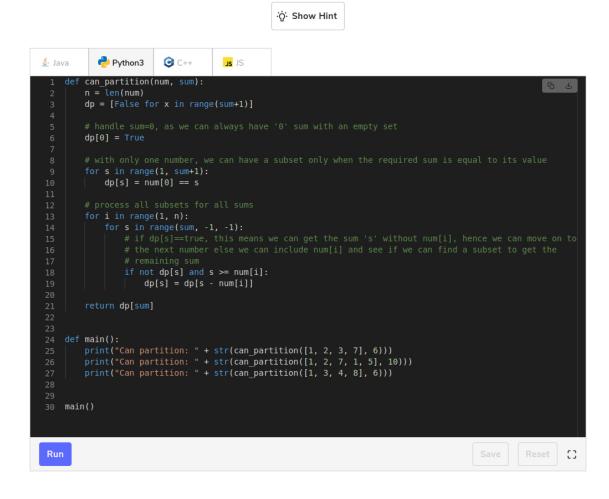
# process all subsets for all sums
for i in range(1, n):
```

## Time and Space complexity

The above solution has the time and space complexity of O(N\*S), where 'N' represents total numbers and 'S' is the required sum.

## Challenge #

Can we improve our bottom-up DP solution even further? Can you find an algorithm that has O(S) space complexity?



, Duck

Equal Subset Sum Partition (medium)

Minimum Subset Sum Difference (hard)



Propertian Issue Ask a Question