

Solution Review: Problem Challenge 3

We'll cover the following

- Count of Structurally Unique Binary Search Trees (hard)
- Solution
- Code
 - Time complexity
 - Space complexity
- Memoized version

Count of Structurally Unique Binary Search Trees (hard)

Given a number 'n', write a function to return the count of structurally unique Binary Search Trees (BST) that can store values 1 to 'n'.

Example 1:

```
Input: 2
Output: 2
Explanation: As we saw in the previous problem, there are 2 unique BSTs storing numbers from 1-2.
```

Example 2:

```
Input: 3
Output: 5
Explanation: There will be 5 unique BSTs that can store numbers from 1 to 3.
```

Solution

This problem is similar to [Structurally Unique Binary Search Trees](#). Following a similar approach, we can iterate from 1 to 'n' and consider each number as the root of a tree and make two recursive calls to count the number of left and right sub-trees.

Code

Here is what our algorithm will look like:

Java Python3 C++ JS

```
1
2 class TreeNode:
3     def __init__(self, val):
4         self.val = val
5         self.left = None
6         self.right = None
7
8
9 def count_trees(n):
10     if n <= 1:
11         return 1
12     count = 0
13     for i in range(1, n+1):
14         # making 'i' root of the tree
15         countOfLeftSubtrees = count_trees(i - 1)
16         countOfRightSubtrees = count_trees(n - i)
17         count += (countOfLeftSubtrees * countOfRightSubtrees)
18
19     return count
```

```

20
21
22 def main():
23     print("Total trees: " + str(count_trees(2)))
24     print("Total trees: " + str(count_trees(3)))
25
26
27 main()
28
29
30
31

```

Run Save Reset

Time complexity

The time complexity of this algorithm will be exponential and will be similar to [Balanced Parentheses](#). Estimated time complexity will be $O(n * 2^n)$ but the actual time complexity ($O(4^n / \sqrt{n})$) is bounded by the [Catalan number](#) and is beyond the scope of a coding interview. See more details [here](#).

Space complexity

The space complexity of this algorithm will be exponential too, estimated $O(2^n)$ but the actual will be ($O(4^n / \sqrt{n})$).

Memoized version

Our algorithm has overlapping subproblems as our recursive call will be evaluating the same sub-expression multiple times. To resolve this, we can use memoization and store the intermediate results in a **HashMap**. In each function call, we can check our map to see if we have already evaluated this sub-expression before. Here is the memoized version of our algorithm, please see highlighted changes:

Java Python3 C++ JS

```

1 class TreeNode:
2     def __init__(self, val):
3         self.val = val
4         self.left = None
5         self.right = None
6
7
8 def count_trees(n):
9     return count_trees_rec({}, n)
10
11
12 def count_trees_rec(map, n):
13     if n in map:
14         return map[n]
15
16     if n <= 1:
17         return 1
18     count = 0
19     for i in range(1, n+1):
20         # making 'i' the root of the tree
21         countOfLeftSubtrees = count_trees_rec(map, i - 1)
22         countOfRightSubtrees = count_trees_rec(map, n - i)
23         count += (countOfLeftSubtrees * countOfRightSubtrees)
24
25     map[n] = count
26     return count
27
28
29 def main():
30     print("Total trees: " + str(count_trees(2)))
31     print("Total trees: " + str(count_trees(3)))
32
33
34 main()
35

```

Run Save Reset

The time complexity of the memoized algorithm will be $O(n^2)$, since we are iterating from '1' to 'n' and ensuring that each sub-problem is evaluated only once. The space complexity will be $O(n)$ for the

memoization map.

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