## ICPC cheat sheet

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```
// AUXILIARY
bool cmp(int u, int v) {
   return st[u] < st[v];</pre>
}
void auxiliary() {
   sort(all.begin(), all.end(), cmp);
   for (int i = 0; i < k - 1; i++)
       all.push_back(lca(all[i], all[i + 1]));
   sort(all.begin(), all.end(), cmp);
   all.resize(unique(all.begin(), all.end()) - all.begin());
   stack <int> s;
   for (int u: all) {
       while (s.size() && (st[s.top()] > st[u] || en[s.top()] <= st[u]))</pre>
           s.pop();
       if (s.size())
           tree[s.top()].push back(\{u, h[u] - h[s.top()]\});
       s.push(u);
   }
}
// 2-SAT ([a | b] & [a | !b] & ... & [c | !a])
void add_edge(int u, int v) {
   adj[u].push back(v);
   rev adj[v].push back(u);
}
void add_clause(int u, int v) {
   add_edge(u ^ 1, v);
   add edge(v ^ 1, u);
}
void dfs(int u, vector <int> *g, vector <int> &vec, int c = 1) {
   vis[u] = c;
   for (int v: g[u])
       if (vis[v] == 0)
           dfs(v, g, vec, c);
   vec.push_back(u);
}
void kosaraju() {
   for (int u = 0; u < n << 1; u++)
       if (vis[u] == 0)
           dfs(u, adj, ord);
   reverse(ord.begin(), ord.end());
   memset(vis, 0, sizeof vis);
```

```
int cnt = 0;
   for (int u: ord)
       if (vis[u] == 0) {
           comp.clear();
           dfs(u, rev_adj, comp, ++cnt);
           for (int v: comp) {
               if (vis[v] == vis[v ^ 1]) {
                   cout << "Impossible" << endl;</pre>
                   exit(0);
               }
               if (v & 1 == 1 && vis[v ^ 1] == 0)
                   ans.push_back(v >> 1);
           }
       }
}
// EULER
int deg[N];
vector <int> adj[N], tour;
void add_edge(int u, int v) {
   adj[u].push_back(v);
   deg[u]++;
   deg[v]--;
}
void euler(int u) {
   while (adj[u].size()) {
       int v = adj[u].back();
       adj[u].pop_back();
       euler(v);
   }
   tour.push_back(u);
}
void make_graph() {
   cin >> n >> m;
   while (m--) {
       int u, v;
       cin >> u >> v;
       add_edge(--u, --v);
   }
}
```

```
void find_euler_tour() {
   int x1 = -1, x2 = -1;
   for (int u = 0; u < N; u++)</pre>
       if (x1 == -1 && deg[u] == 1)
           x1 = u;
       else if (x2 == -1 && deg[u] == -1)
           x2 = u;
       else if (deg[u] != 0)
           return cout << "NO" << endl, 0;</pre>
   for (int u = 0; u < N; u++)</pre>
       if (adj[u].size() && (u == x1 || x1 == -1)) {
           euler(u);
           break;
       }
   for (int u = 0; u < N; u++)</pre>
       if (adj[u].size())
           return cout << "NO" << endl, 0;</pre>
   reverse(tour.begin(), tour.end());
   for (int x: tour)
       cout << x + 1 << ' ';
}
// CUT VERTEX
void dfs(int v,int parent){
   dp[v]=h[v];
   mark[v]=true;
   int num=0;
   for(int u: adj[v]) {
       if(!mark[u]){
           h[u]=h[v]+1;
           dfs(u,v);
           if(v!=1 && dp[u]>=h[v])is[v]=true;
           dp[v]=min(dp[v],dp[u]);
           num++;
       }
       else{
           if(u!=parent){
                dp[v]=min(dp[v],h[u]);
           }
       }
   }
```

```
if(v==1 && num>1)
       is[v]=true;
}
// CUT EDGE
void dfs(int v,int parent,int index){
   dp[v]=h[v];
   mark[v]=true;
   for(int i=0;i<adj[v].size();i++){</pre>
       int u=adj[v][i].first;
       int ind=adj[v][i].second;
       if(!mark[u]){
           h[u]=h[v]+1;
           dfs(u,v,ind);
           dp[v]=min(dp[v],dp[u]);
       }
       else{
           if(u!=parent){
               dp[v]=min(dp[v],h[u]);
           }
       }
   }
   if(v!=1){
       if(dp[v]==h[v])
           is[index]=true;
   }
}
// ordered set
#include <ext/pb ds/assoc container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
typedef tree<pair <int, int>,
   null_type,
   less<pair <int, int>>,
   rb_tree_tag,
   tree order statistics node update> ordered set;
```

```
struct multi_ordered_set {
   ordered set os;
   unordered_map <int, int> cnt;
   void insert(int x) {
       os.insert({x, cnt[x]});
       cnt[x]++;
   void erase(int x) {
       if (cnt[x]) {
           cnt[x]--;
           os.erase({x, cnt[x]});
       }
   }
   int find_by_order(int x) { // meqdare x om ro mi de (0 base)
       return os.find by order(x)->first;
   }
   int order of key(int x) { // mige adade x avalin ja koja ast (0 base)
       return os.order of key(\{x, 0\});
   int size() {
       return os.size();
   }
};
// SEGMENT 2D
const int N = 750 + 4;
struct node{
   int x;
};
struct seg2d{
   int n, m;
   node arr[N][N];
   node seg[4 * N][4 * N];
   node emp;
   node merge(node a, node b){
       node rt;
       rt.x = max(a.x, b.x);
       return rt;
   }
```

```
void buildy(int idx, int lx, int rx, int idy, int ly, int ry){
    if(ry - ly == 1){
        if (rx - lx == 1)
            seg[idx][idy] = arr[lx][ly];
        else
            seg[idx][idy] = merge(seg[2 * idx][idy], seg[2 * idx + 1][idy]);
    }else {
        int mid = (ly + ry) / 2;
        buildy(idx, lx, rx, 2 * idy, ly, mid);
        buildy(idx, lx, rx, 2 * idy + 1, mid, ry);
        seg[idx][idy] = merge(seg[idx][2 * idy], seg[idx][2 * idy + 1]);
    }
}
void buildx(int idx, int lx, int rx){
    if(rx - lx != 1){
        int mid = (1x + rx) / 2;
        buildx(2 * idx, lx, mid);
        buildx(2 * idx + 1, mid, rx);
    buildy(idx, 1x, rx, 1, 1, m + 1);
}
node gety(int idx, int idy, int ly, int ry, int st, int en) {
    if (st >= en)
        return emp;
    if (ly == st && ry == en)
        return seg[idx][idy];
    int mid = (ly + ry) / 2;
    return merge(gety(idx, 2 * idy, ly, mid, st, min(en, mid))
            , gety(idx, 2 * idy + 1, mid, ry, max(st, mid), en));
}
node getx(int idx, int lx, int rx, int stx, int enx, int sty, int eny) {
    if (stx >= enx)
        return emp;
    if (lx == stx && rx == enx)
        return gety(idx, 1, 1, m + 1, sty, eny);
    int mid = (1x + rx) / 2;
    return merge(getx(2 * idx, lx, mid, stx, min(enx, mid), sty, eny)
            , getx(2 * idx + 1, mid, rx, max(stx, mid), enx, sty, eny));
}
```

```
void updatey(int idx, int lx, int rx, int idy, int ly, int ry, int x, int y,
int new val) {
       if (ry - ly == 1) {
           if (rx - lx == 1){
               node X;
               X.x = new val;
               seg[idx][idy] = X;
           }
           else
               seg[idx][idy] = merge(seg[2 * idx][idy], seg[2 * idx + 1][idy]);
       } else {
           int mid = (ly + ry) / 2;
           if (y < mid)
               updatey(idx, lx, rx, 2 * idy, ly, mid, x, y, new_val);
           else
               updatey(idx, lx, rx, 2 * idy + 1, mid, ry, x, y, new val);
           seg[idx][idy] = merge(seg[idx][2 * idy], seg[idx][2 * idy + 1]);
       }
   }
   void updatex(int idx, int lx, int rx, int x, int y, int new_val) {
       if (rx - 1x > 1) {
           int mid = (lx + rx) / 2;
           if (x < mid)
               updatex(2 * idx, lx, mid, x, y, new_val);
           else
               updatex(2 * idx + 1, mid, rx, x, y, new val);
       updatey(idx, lx, rx, 1, 1, m + 1, x, y, new val);
   }
};
// 0 base suffix array O(nlg)
vector<int> sort cyclic shifts(string const& s) {
   int n = s.size();
   const int alphabet = 256;
   vector<int> p(n), c(n), cnt(max(alphabet, n), 0);
   for (int i = 0; i < n; i++)</pre>
       cnt[s[i]]++;
   for (int i = 1; i < alphabet; i++)</pre>
       cnt[i] += cnt[i-1];
```

```
for (int i = 0; i < n; i++)</pre>
       p[--cnt[s[i]]] = i;
   c[p[0]] = 0;
   int classes = 1;
   for (int i = 1; i < n; i++) {
       if (s[p[i]] != s[p[i-1]])
           classes++;
       c[p[i]] = classes - 1;
   }
   vector<int> pn(n), cn(n);
   for (int h = 0; (1 << h) < n; ++h) {
       for (int i = 0; i < n; i++) {</pre>
           pn[i] = p[i] - (1 << h);
           if (pn[i] < 0)
                pn[i] += n;
       }
       fill(cnt.begin(), cnt.begin() + classes, 0);
       for (int i = 0; i < n; i++)</pre>
           cnt[c[pn[i]]]++;
       for (int i = 1; i < classes; i++)</pre>
           cnt[i] += cnt[i-1];
       for (int i = n-1; i >= 0; i--)
           p[--cnt[c[pn[i]]]] = pn[i];
       cn[p[0]] = 0;
       classes = 1;
       for (int i = 1; i < n; i++) {</pre>
           pair<int, int> cur = {c[p[i]], c[(p[i] + (1 << h)) % n]};
           pair<int, int> prev = {c[p[i-1]], c[(p[i-1] + (1 << h)) % n]};</pre>
           if (cur != prev)
               ++classes;
           cn[p[i]] = classes - 1;
       }
       c.swap(cn);
   }
   return p;
}
vector<int> suffix array construction(string s) {
   s += "$";
   vector<int> sorted shifts = sort cyclic shifts(s);
   sorted shifts.erase(sorted shifts.begin());
   return sorted shifts;
}
```

```
// FFT
using cd = complex<double>;
const double PI = acos(-1);
void fft(vector<cd> & a, bool invert) {
   int n = a.size();
   for (int i = 1, j = 0; i < n; i++) {
       int bit = n >> 1;
       for (; j & bit; bit >>= 1)
           j ^= bit;
       j ^= bit;
       if (i < j)
           swap(a[i], a[j]);
   }
   for (int len = 2; len <= n; len <<= 1) {</pre>
       double ang = 2 * PI / len * (invert ? -1 : 1);
       cd wlen(cos(ang), sin(ang));
       for (int i = 0; i < n; i += len) {</pre>
           cd w(1);
           for (int j = 0; j < len / 2; j++) {
               cd u = a[i+j], v = a[i+j+len/2] * w;
               a[i+j] = u + v;
               a[i+j+len/2] = u - v;
               w *= wlen;
           }
       }
   }
   if (invert) {
       for (cd & x : a)
           x /= n;
   }
}
vector<int> multiply(vector<int> const& a, vector<int> const& b) {
   vector<cd> fa(a.begin(), a.end()), fb(b.begin(), b.end());
   int n = 1;
   while (n < a.size() + b.size())</pre>
       n <<= 1;
   fa.resize(n);
   fb.resize(n);
```

```
fft(fa, false);
   fft(fb, false);
   for (int i = 0; i < n; i++)</pre>
       fa[i] *= fb[i];
   fft(fa, true);
   vector<int> result(n);
   for (int i = 0; i < n; i++)</pre>
       result[i] = round(fa[i].real());
   return result;
// NTT mode = 988244353
const int md = 998244353;
int w[24], wi[24], inv2;
inline int mkey(int a,int b){
   int rt=a + b;
   if(rt >= md)
       rt-=md;
   return rt;
}
int pw(int a, int b){
   int rt = 1;
   while(b > 0){
       if(b & 1)
           rt = 1LL * rt * a % md;
       b /= 2;
       a = 1LL * a * a % md;
   }
   return rt;
}
void pre(){
   w[23] = 31;
   FORR(i, 22, 0)
       w[i] = 1LL * w[i + 1] * w[i + 1] % md;
   FOR(i, 0, 23)
       wi[i] = pw(w[i], md - 2);
   inv2 = pw(2, md - 2);
void fft(vector<int> &a, bool invert){
   int n = SZ(a);
```

```
if(n == 1)
       return;
   vector<int> a0(n / 2), a1(n / 2);
   FOR(i, 0, n / 2 - 1){
       a0[i] = a[2 * i];
       a1[i] = a[2 * i + 1];
   fft(a0, invert);
   fft(a1, invert);
   int W = 1;
   int wn = w[__builtin_ctz(n)];
   if(invert)
       wn = wi[__builtin_ctz(n)];
   FOR(i, 0, n / 2 - 1){
       a[i] = mkey(a0[i], (1LL * W * a1[i] % md));
       a[i + n / 2] = mkey(a0[i], (md - (1LL * W * a1[i] % md)));
       if(invert){
           a[i] = 1LL * a[i] * inv2 % md;
           a[i + n / 2] = 1LL * a[i + n / 2] * inv2 % md;
       }
       W = 1LL * wn * W % md;
  }
}
vector<int> mul(vector<int> a, vector<int> b){
   vector<int> fa(all(a)), fb(all(b));
   int n=1;
  while(n<SZ(a)+SZ(b)) n *= 2;</pre>
   fa.resize(n);
   fb.resize(n);
   fft(fa,0);
   fft(fb,0);
   FOR(i, 0, n - 1)
       fa[i] = 1LL * fa[i] * fb[i] % md;
   fft(fa, 1);
   vector<int> res(n);
   FOR(i, 0, n - 1){
       res[i] = fa[i];
   }
   return res;
}
```

```
// mcmf
11 n, m, N=0, M=0;
struct edge {
   11 u, v, cost, cap;
   edge () {}
   edge(int u1, int v1, int cost1, int cap1){
       u = u1;
       v = v1;
       cost = cost1;
       cap = cap1;
   }
};
edge ed[MXE];
vector<int> adj[MX];
// edges from left to right
void add edge(int u, int v, int cap, int cost=0) {
   ed[M] = edge(u, v, cost, cap);
   adj[u].pb(M++);
   ed[M] = edge(v, u, -cost, 0);
   adj[v].pb(M++);
}
// used spfa
pii cheapest_flow(int source, int sink) {
   int d[MX] = {}, p[MX] = {};
   bool inQ[MX] = \{\};
   queue<int> q;
   FOR(i, 1, N+2) d[i] = inf;
   d[source] = 0;
   int u = source;
   inQ[u] = true;
   q.push(u);
   while(!q.empty()) {
       u = q.front();
       q.pop();
       inQ[u] = false;
       for(int i:adj[u]) if(ed[i].cap) {
           int v = ed[i].v;
           if(d[v] > d[u] + ed[i].cost) {
               d[v] = d[u] + ed[i].cost;
               p[v] = i;
               if(!inQ[v]) q.push(v);
```

```
}
       }
   }
   u = sink;
   pii ans = pii(0, 0);
   if(d[u] == inf) return ans;
   while(u != source) {
       int i=p[u];
       ed[i].cap --;
       ed[i^1].cap ++;
       ans.S += ed[i].cost;
       u = ed[i].u;
   }
   ans.F = 1;
   return ans;
}
// returns (max flow, min cost);
pii mcmf(int source, int sink) {
   pii fc; // fc : (flow, cost)
   pii ans = pii(0, 0);
   do {
       fc = cheapest_flow(source, sink);
       ans.F += fc.F;
       ans.S += fc.S;
   } while(fc.F > 0);
   return ans;
// build graph in main using add edge, don't forget to check N, MX, source,
sink
// min-cut & max-flow
// e[u][v] represents the remaining capacity of the uv edge in that direction
// Look out for MX!
11 N, n, m, e[MX][MX], flow[MX][MX];
bool mark f[MX];
void add_edge(int u, int v, ll cap) {
   e[u][v] += cap;
}
void push_flow(int u, int v, ll f) {
   flow[u][v] += f;
   flow[v][u] -= f;
```

```
e[u][v]-=f;
   e[v][u]+=f;
}
11 dfs(int u, 11 in f, 11 min w, int sink){
   if(u==sink) return in_f;
   mark f[u] = true;
   for(int v=1; v<=N; v++) if(!mark_f[v] and e[u][v]>=min_w){
       11 f = dfs(v, min(in f, e[u][v]), min w, sink);
       if(f) {
           push flow(u, v, f);
           return f;
       }
   }
   return 0;
}
int main(){
   cin>>n;
   N = 2*n+2;
   FOR(i, 1, n){
       string s;
       cin>>s;
       FOR(j, 0, n-1) if(s[j] != '.'){
           add_edge(i, j+n+1, inf);
       }
   }
   int source = 2*n+1;
   int sink = 2*n+2;
   FOR(i, 1, n) {
       add_edge(source, i, 1);
   FOR(i, n+1, 2*n) {
       add_edge(i, sink, 1);
   }
   11 max flow = 0;
   // LOGW is the log of max edge capacity
   11 i = 111<<<LOGW; while(i>0){
       FOR(u, 1, N) mark_f[u] = false;
       11 f = dfs(source, infl, i, sink);
       max flow+= f;
       if(f==0) i>>=1;
   }
```

```
cout<<max flow<<'\n';</pre>
   //iterate all existing edges:
   FOR(u, 1, N) FOR(v, 1, N) if(flow[u][v])
       // condition for an edge to be in min cut
       if(mark_f[u] and !mark_f[v])
           cout<<u<<' '<<v<<'\n';</pre>
}
  in bipartite graphs:
  min\ edge\ cover\ =\ n\ -\ max\ matching
  min\ vertex\ cover = n - max\ independent\ set
*/
// Convex Hull
struct Line {
   double a, b, x left;
   Line(double a, double b): a(a), b(b), x_left(-1e18) {};
   double get_y(double x) {
       return a * x + b;
   }
   bool operator < (double x) const {</pre>
       return x left < x;</pre>
   }
};
double inter_x(Line 11, Line 12) {
   return (l1.b - l2.b) / (l2.a - l1.a);
}
struct Convex_Hull {
   deque <Line> dq;
   enum Type {front, back} type;
   vector <pair <Type, vector <Line>>> rem;
   void pop_back() {
       dq.pop back();
   void push_back(Line 1) {
       1.x left = -1e18;
       if (dq.size())
           1.x left = inter x(1, dq.back());
       dq.push back(1);
   }
```

```
void add_back_line(Line 1) {
       rem.push_back({back, {}});
       while (dq.size() >= 2 && dq.back().x_left >= inter_x(dq.back(), 1)) {
           rem.back().second.push_back(dq.back());
           pop back();
       }
       push back(1);
   }
   void pop_front() {
       dq.pop_front();
       dq[0].x_left = -1e18;
   }
   void push_front(Line 1) {
       if (dq.size())
           dq[0].x left = inter x(1, dq[0]);
       1.x left = -1e18;
       dq.push front(1);
   }
   void add front line(Line 1) {
       rem.push_back({front, {}});
       while (dq.size() \ge 2 \&\& dq[1].x_left <= inter_x(dq[0], 1)) {
           rem.back().second.push back(dq[0]);
           pop front();
       push front(1);
   }
  void undo() {
       if (rem.back().first == front)
           pop front();
       else
           pop back();
       reverse(rem.back().second.begin(), rem.back().second.end());
       for (auto 1: rem.back().second)
           rem.back().first == front? push_front(1): push_back(1);
       rem.pop back();
   double get_max(double x) {
       auto best line = lower bound(dq.begin(), dq.end(), x) - 1;
       return best_line->get_y(x);
   }
};
```

```
//Convex Polygon
struct Point {
   long long x, y;
   bool type;
   Point() {}
   Point(long long x, long long y, bool type) : x(x), y(y), type(type) {}
   bool operator < (Point p) const {</pre>
       return x < p.x \mid | (x == p.x \&\& y < p.y);
   }
};
long long cross_product(Point 0, Point A, Point B) {
   return (A.x - 0.x) * (B.y - 0.y) - (A.y - 0.y) * (B.x - 0.x);
}
double shib(Point a, Point b) {
   return 1. * (a.y - b.y) / (a.x - b.x);
}
vector <Point> convex hull(vector <Point> points) {
   int n = points.size(), k = 0;
   sort(points.begin(), points.end());
   if (n <= 3)
       return points;
   vector <Point> ans(2 * n);
   for (int i = 0; i < n; ++i) {</pre>
       while (k \ge 2 \&\& cross product(ans[k - 2], ans[k - 1], points[i]) < 0)
           k--;
       ans[k++] = points[i];
   }
   for (int i = n - 1, t = k + 1; i > 0; --i) {
       while (k \ge t \&\& cross product(ans[k - 2], ans[k - 1], points[i - 1]) <
0)
           k--;
       ans[k++] = points[i - 1];
   ans.resize(k - 1);
   return ans;
}
//Dynamic convex hell
enum Type {line, query};
struct Line {
   double a, b, x left;
   Type type;
```

```
long long val;
   Line() : type(line) {}
   Line(long long a, long long b) : a(a), b(b), type(line), x_left(-1e18) {}
   Line(long long val) : val(val), type(query) {}
   long long get_y(long long x) const {
       return a * x + b;
   bool operator < (Line 1) const {</pre>
       if (1.type == line)
           return a < 1.a;</pre>
       return x left < 1.val;</pre>
   }
};
bool are parallel(Line 11, Line 12) {
   return 11.a == 12.a;
}
double inter x(Line 11, Line 12) {
   return are_parallel(11,12)? 1e18: 1.0 * (12.b - 11.b) / (11.a - 12.a);
}
struct Convex_Hull_Dynamic {
   set <Line> s;
  bool has_prev(set <Line>::iterator it) {
       return it != s.begin();
   bool has next(set <Line>::iterator it) {
       return it != s.end() && next(it) != s.end();
   bool irrelevant(Line 11, Line 12, Line 13) {
       return inter x(11, 13) \leftarrow x(11, 12);
   bool irrelevant(set<Line>::iterator it) {
       return has prev(it) && has next(it) && irrelevant(*prev(it), *it,
*next(it));
   }
   set <Line>::iterator update_left_border(set <Line>::iterator it) {
       if (has_prev(it) == false)
           return it;
       Line tmp(*it);
       tmp.x_left = inter_x(*it, *prev(it));
       it = s.erase(it);
       it = s.insert(it, tmp);
       return it;
   }
```

```
void add_line(Line 1) {
       auto it = s.lower bound(1);
       if (it != s.end() && are_parallel(*it, 1)) {
           if (it->b < 1.b)
               it = s.erase(it);
           else
               return;
       }
       it = s.insert(it, 1);
       if (irrelevant(it)) {
           s.erase(it);
           return;
       }
       while (has prev(it) && irrelevant(prev(it)))
           s.erase(prev(it));
       while (has next(it) && irrelevant(next(it)))
           s.erase(next(it));
       it = update left border(it);
       if (has_prev(it))
           update left_border(prev(it));
       if (has_next(it))
           update left border(next(it));
   }
   long long get_max(long long x) {
       auto best_line = --s.lower_bound(Line(x));
       return best line->get y(x);
   }
};
//Matrices
struct Matrix {
   int n, m;
   vector <vector <long long>> val;
  Matrix(int n, int m, int v = 0) : n(n), m(m) {
       for (int i = 0; i < n; i++) {</pre>
           val.push_back({});
           val.back().resize(m, 0);
           if (i < m)
               val[i][i] = v;
       }
   }
```

```
Matrix operator * (Matrix a) {
       Matrix res(n, a.m);
       for (int i = 0; i < n; i++)</pre>
           for (int j = 0; j < a.m; j++)</pre>
               for (int k = 0; k < m; k++)
                   res.val[i][j] += val[i][k] * a.val[k][j];
       return res;
   }
   Matrix operator ^ (int b) {
       if (b == 0)
           return Matrix(n, m, 1);
       auto tmp = *this ^ (b / 2);
       return tmp * tmp * (b % 2? *this: Matrix(n, m, 1));
   }
};
int r(int n) {
   return rand() % n + 1;
}
int main() {
   int c;
   cin >> c;
   srand(c);
   int n = r(10);
}
g++ myCode.cpp -std=c++17 -o myCode.out
g++ correctCode.cpp -std=c++17 -o correctCode.out
g++ generator.cpp -std=c++17 -o generator.out
ok=0;
for i in `seq 1 100`
do
```

```
echo $i > tmp
   ./generator.out < tmp > test
   ./correctCode.out < test > correctRet
   ./myCode.out < test > myRet
   diff myRet correctRet > /dev/null
   if [ $? == 0 ]
   then
       ((ok++))
   else
       echo "Wrong answer on test $i"
       echo "Test"
       ./generator.out < tmp</pre>
       echo "Output"
       ./myCode.out < test</pre>
       echo "Answer"
       ./correctCode.out < test
       break
   fi
done
if [ $ok == 100 ]
then
   echo ACCEPTED
fi
// returns d = gcd(a,b); finds x,y such that d = ax + by
int extended_euclid(int a, int b, int &x, int &y) {
   int xx = y = 0;
   int yy = x = 1;
   while (b) {
       int q = a/b;
       int t = b; b = a%b; a = t;
       t = XX; XX = x-q*XX; x= t;
       t = yy; yy = y-q*yy; y = t;
   }
   return a;
}
```

$$aX + b = Y$$
,  $a'X + b' = Y -> x_0 = \frac{b-b'}{a'-a}$ 

تقاطع دو خط:

$$(x_0, y_0), aX + bY + c = 0 \rightarrow d = \frac{|ax_0 + by_0 + c|}{\sqrt{a^2 + b^2}}$$

فاصله نقطه از خط:

$$aX + bY + c = 0$$
 ,  $a'X + b'Y + c' = 0$   $-> d = \frac{|c-c'|}{\sqrt{a^2+b^2}}$  فاصله دو خط موازی:

$$tan(\alpha) = \left| \frac{a-a'}{1+aa'} \right|$$

زاویه بین دو خط با شیبهای a و a' برحسب رادیان:

$$\frac{1}{2}$$
. a. b.  $sin(\alpha)$ 

مساحت مثلث برحسب ۲ ضلع و زاویه بین:

$$\frac{1}{2} [x_A(y_B - y_C) + x_B(y_C - y_A) + x_C(y_A - y_B)]$$
 د مساحت مثلث برحسب ۳ راس آن:

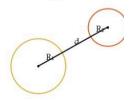


متخارج

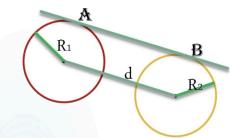




d= اختلاف شعاع ها



d>R1+RY d همان خط المركزين است.



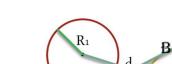
AB^Y=d^Y-(R1-RY)^Y

مماس مشترک داخلی

متداخل

d< اختلاف شعاع ها

مماس خارج



هم مرکز



d=0

d همان خط المركزين است.

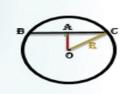
d=R1+RY

متقاطع



R1-RY<d<R1+RY d همان خط المركزين است.

 $AB^Y=d^Y-(R_1+R_Y)^Y$ 



$$BC = 2\sqrt{(R^2 - (OA)^2)}$$

```
struct query {
   int 1, r, id;
} q[N];
void add(int 1, int r) {
   while (1 < r) {
       //..
       1++;
   }
}
void remove(int 1, int r) {
   while (1 < r) {
       //..
       1++;
   }
}
int main() {
   ios_base::sync_with_stdio(0), cin.tie(0), cout.tie(0);
   sort(q, q + m, [] (query x, query y) {
       return x.1 / Sq != y.1 / Sq? x.1 < y.1: x.r < y.r;</pre>
   });
   int st = 0, en = 0;
   for (int i = 0; i < query; i++) {</pre>
       auto [l, r, id] = q[i];
       1 < st? add(1, st): remove(st, 1);</pre>
       r < en? remove(r, en): add(en, r);</pre>
       st = 1, en = r;
       res[id] = ans;
   }
}
```