

## Inverse functions

A function  $f$  has an inverse  $f^{-1}$  if it is bijective because we can find a way of getting from the codomain back to the domain

The formula for converting Celcius to Fahrenheit is

$$F = \frac{9}{5}C + 32 \quad \text{this is a function}$$
$$f(x) = \frac{9}{5}x + 32$$

We have output (degrees Fahrenheit) in terms of input (degrees Celcius)

If we put the eq<sup>n</sup> so that it is Celcius in terms of Fahrenheit we have the inverse

$$F = \frac{9}{5}C + 32$$
$$\frac{9}{5}C = F - 32$$
$$C = \frac{5}{9}(F - 32) \quad \text{This is the inverse}$$

## Finding the inverse graphically

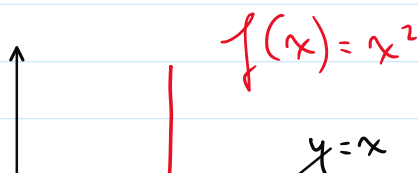
With the restriction that  $0 \leq x$   
for  $f(x) = x^2$ ,  $f(x)$  is bijective.

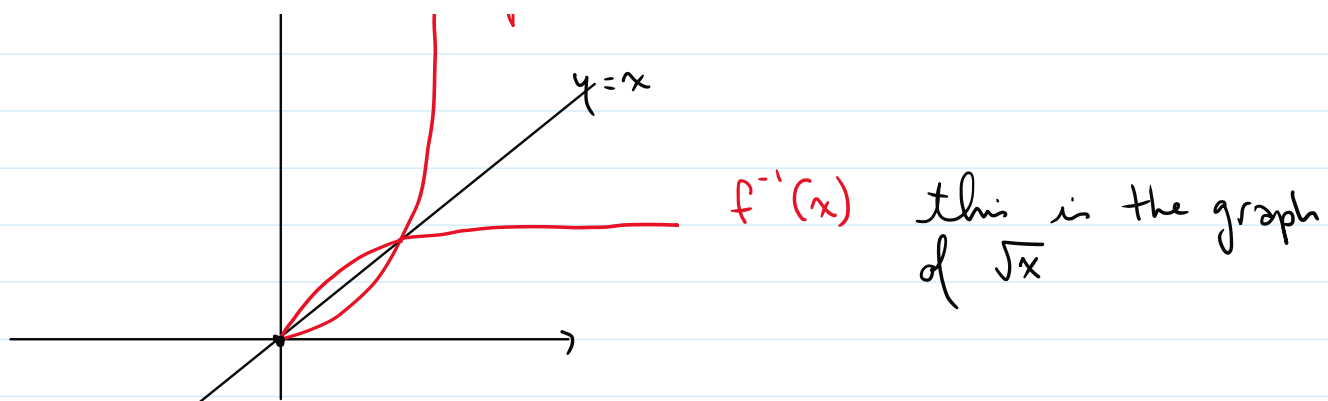
$$f(x) = y = x^2$$

$$\sqrt{y} = x$$

$x$  will be the positive square roots of  $y$

The graph of  $f(x) = x^2$ ,  $0 \leq x$  looks like this





So to find the inverse graphically you reflect your curve in the line  $y=x$

## Composition of functions

given two functions  $f(x), g(x)$

The composition  $f(g(x))$  is found by taking  $g(x)$  and then  $f(x)$

This is written  $(f \circ g)(x)$

$$\text{If } \begin{aligned} g(x) &= x^2 \\ f(x) &= x+1 \end{aligned}$$

$$f(g(x)) = (f \circ g)(x) = (x^2) + 1$$

$$\begin{aligned} \text{Similarly } (g \circ f)(x) &= g(f(x)) = \\ &= (x+1)^2 \end{aligned}$$