ALGEBRA

1. $\left(sec^2 - 1\right)\left(cos^2 - 1\right)$ is equal to:

    (a) -1

    (b) 1

    (c) 0

    (d) 2

2. The roots of the equation

$$x^2 + 3x - 10 = 0 \tag{1}$$

    are:

    (a) $(2, -5)$

    (b) $(-2, 5)$

    (c) $(2, 5)$

    (d) $(-2, -5)$

3. What is the area of a semi-circle of diameter $'d'$?

    (a) $\frac{1}{16}\pi d^2$

    (b) $\frac{1}{4}\pi d^2$

    (c) $\frac{1}{8}\pi d^2$

    (d) $\frac{1}{2}\pi d^2$

4. If a fair coin is tossed twice,find the probability of getting 'atmost one head'.

5. Prove that

$$\frac{\sin A - 2\sin^3 A}{2\cos^3 A - \cos A} = \tan A \tag{2}$$

6. Prove that

$$\sec A \, (1 - \sin A) \, (\sec A + \tan A) = 1. \tag{3}$$

7. Governing council of a local public development authority of Dehradun decided to build an adventurous playground on the top of a hill, which will have adequate space for parking.
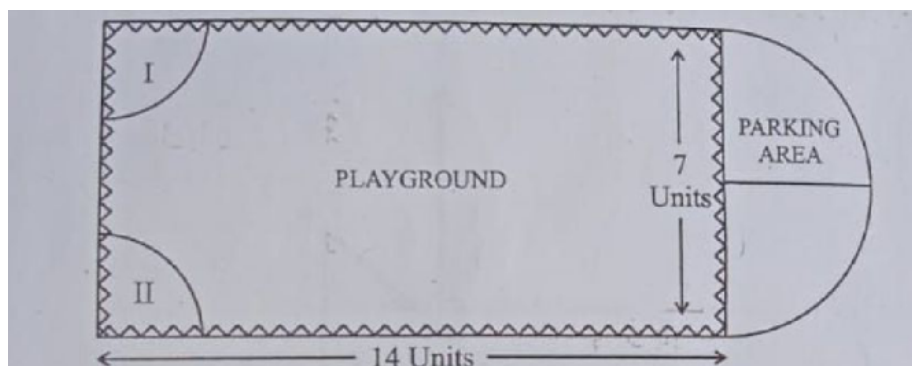

Figure 1: fig

After survey, it was decided to build rectangular playground, with a semi-circular area allotted for parking at one end of the playground. The length and breadth of the rectangular playground are 14 units and 7 units, respectively. There are two quadrants of radius 2 units on one side for special seats.

Based on the above information, answer the following questions:

(a) What is the total perimeter of the parking area?

(b) What is the total area of parking and the two quadrants?

(c) What is the ratio of area of playground to the area of parking area?

(d) Find the cost of fencing the playground and parking area at the rate of ₹ 2 per unit.

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