

# Robot Exploration with Fast Frontier Detection: Theory and Experiments

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Thesis Defense



# Exploration

- Robot Exploration: a fundamental problem in mobile robotics
- Variety of applications:
  - Search and Rescue [Kitano et al., 1999]
  - Planetary Exploration [Apostolopoulos et al., 2001]
  - Surveillance [Hougen et al., 2000]



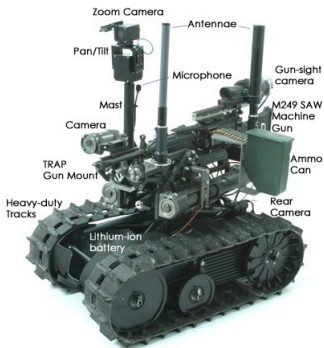
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# Frontier-Based Exploration

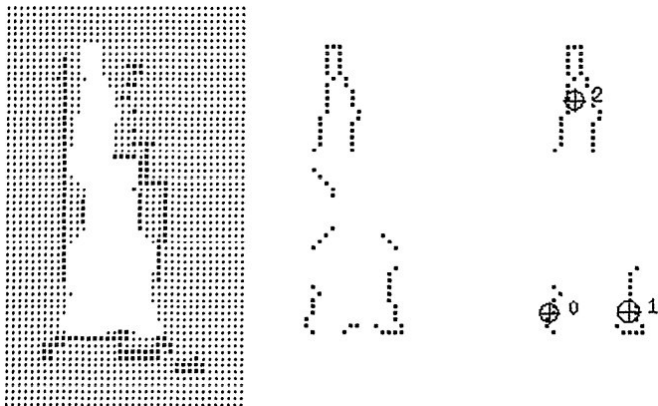
- The most common approach to exploration is based on *frontiers*
- *Frontier*: separates known regions from unknown regions
  - Set of *unknown* points
  - Each has at least one *open-space* neighbor
- By moving towards frontiers, robots keep discovering new regions
- Yamauchi was the first to show a frontier-based strategy
  - [Yamauchi, 1997, 1998]
- His work preceeded many others
  - [Burgard et al., 2005, Lau, 2003, Sawhney et al., 2009]



# Frontier-Based Exploration

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**Figure:** Image taken from [Yamauchi, 1998]: evidence grid, frontier points, extraction of different frontiers (from left to right).

# Outline

- Previous methods for computing frontiers: Slow!
  - searches the entire map with every call
- Two approaches for frontier detection: *WFD*, *FFD*
  - *WFD*: explores only known regions
  - *FFD*: explores only border of known regions
- Theoretical analysis (correctness, complexity)
- Incremental versions of *WFD*: *WFD-INC*, *WFD-IP*
- Results: improvement of 1-2 orders of magnitude over *SOTA*





# Existing Frontier Detection is Slow

- Frontier detection algorithms rely on computer vision methods
  - e.g. edge detection and region extraction
- They have to process the entire map data with every execution
- Existing frontier detection methods take  $\sim 10\text{--}30$  seconds to run
  - Even on powerful computers
  - Exploring a large area forces the robot to wait in its spot
  - Frontier detection is called only when the robot arrives at its target

## Result

Efficient frontier detection can shorten the exploration time



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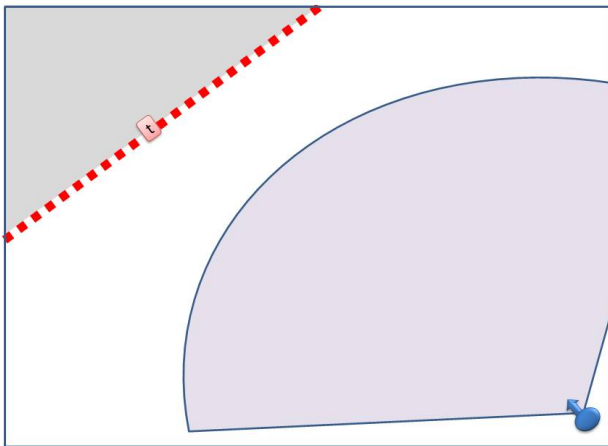
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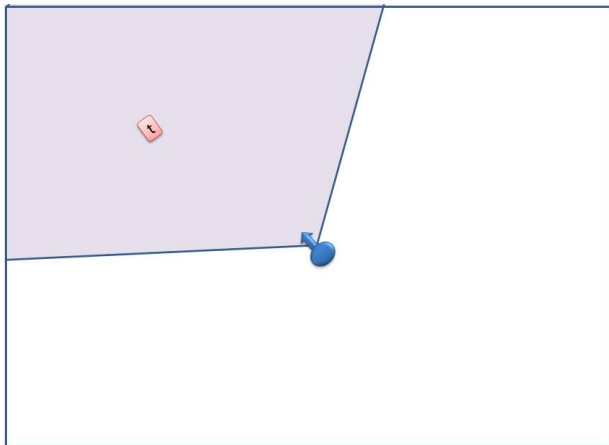
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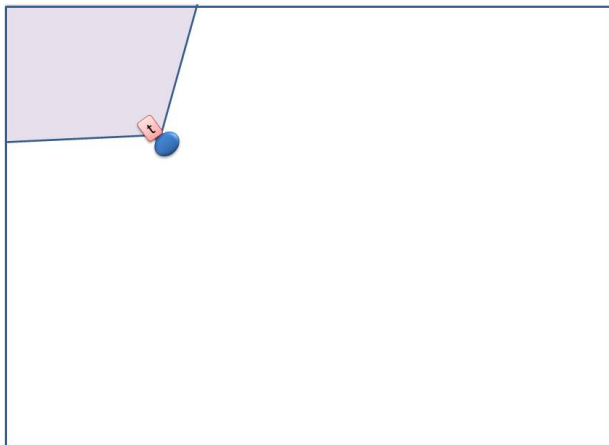
# Single-Robot Example



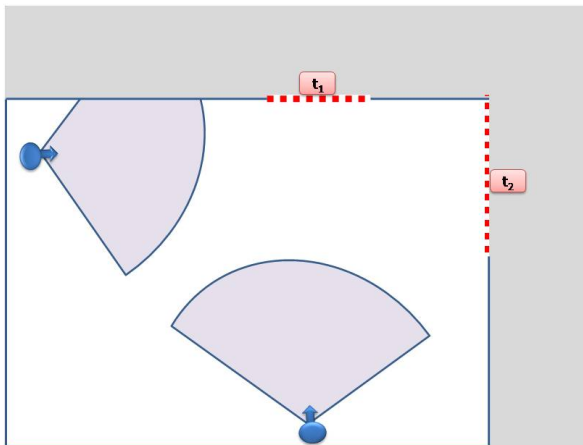
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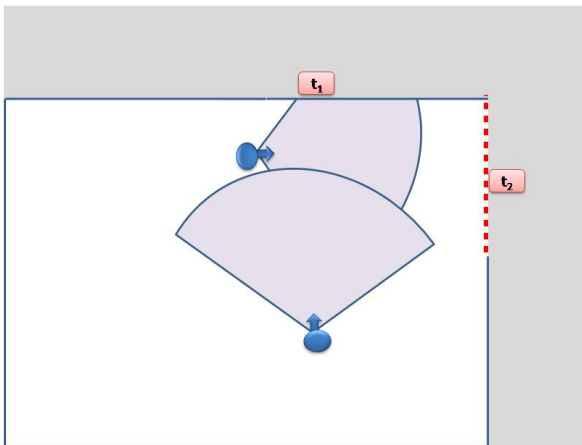
# Single-Robot Example



# Multi-Robot Example



# Multi-Robot Example





# Simultaneous Localization and Mapping Methods

- Builds a map of an unknown environment while navigating
- Robots do not utilize any *a priori* knowledge of the environment
- *SLAM* is a concept, not an algorithm
- *Extended Kalman Filter*
  - Beliefs are represented by moments
  - Markov assumptions are hold and the posteriors are Gaussian
  - Only one map that is composed from observed landmarks
- *Particle Filter*
  - Also known as *sequential Monte Carlo method*
  - Online version of *Markov Chain Monte Carlo (MCMC)* methods
  - State: set of variables (e.g map of explored area, robot position)
  - Each particle is an instance of the system state at a certain time



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# WFD: Wavefront Frontier Detector

- Breadth-first search approach for frontier detection
- *WFD* avoids searching unknown regions
- *WFD* scans only known regions



# WFD Outline

- 1 Enqueue current robot position
- 2 Perform Breadth-First Search
  - scan only open-space points that were not previously scanned
- 3 For every dequeued point, check if it is a frontier point
  - If True: extract the frontier by using another Breadth-First Search



# WFD Conclusions

- Ensures that only known regions are actually scanned
- Frontier points are adjacent to open space points
  - All relevant frontiers will be found when *WFD* finishes
  - Connectivity of frontier points ensures complete frontier extraction
  - The algorithm does not have to scan the entire grid each time
- *WFD* still searches frontiers in all known space



# FFD: Fast Frontier Detector

- Insights:
  - New frontiers are never contained within known regions
  - New frontiers are never wholly within unknown regions
- Hence, scanning all known regions is definitely unnecessary
  - and not time-efficient
- *FFD* avoids searching both known and unknown regions
  - Only processes new laser readings



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# FFD Outline

- 1 Sorting
- 2 Contour
- 3 Detecting New Frontiers
- 4 Maintaining Previously Detected Frontiers

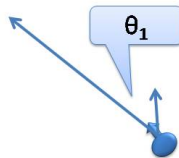


# Sorting

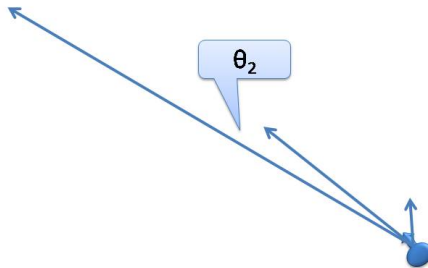
- Most laser sensors return readings that are already sorted
  - Points that are sorted according to polar angle
  - The robot as center
- However, if this is not the case, we can sort them efficiently

[▶ Sorting in details](#)

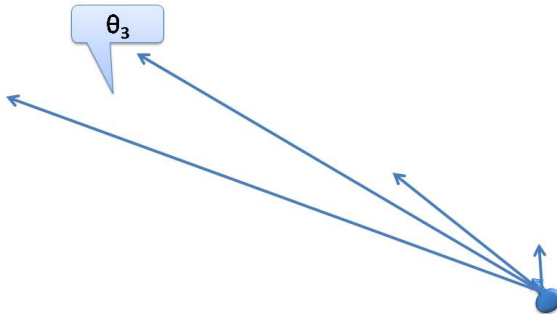
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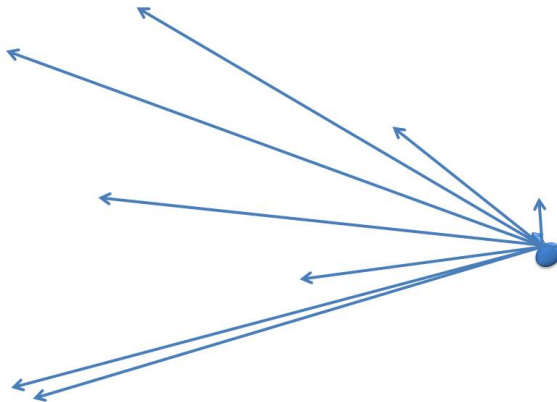
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# Sorting



# Contour

- **Input:** sorted set of points
- **Output:** a contour that is built from the laser readings set
  - The line that connects each two adjacent points from the set
- Calculate the points that lie between each adjacent laser readings
- The desired contour contains all the points mentioned above





# Contour

## Problem

We need the algorithm to be fast and robust against rounding errors

## Solution

We use *Bresenham's line algorithm* [Bresenham, 1965]



# Contour

## Problem

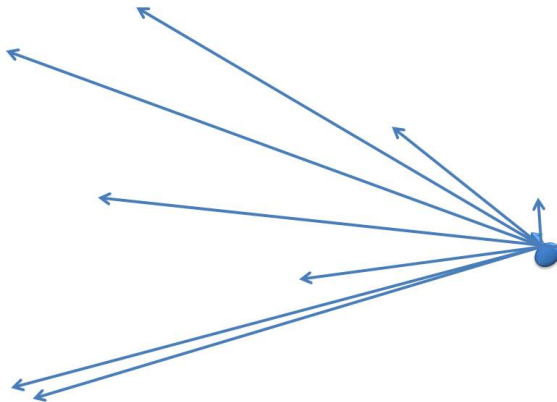
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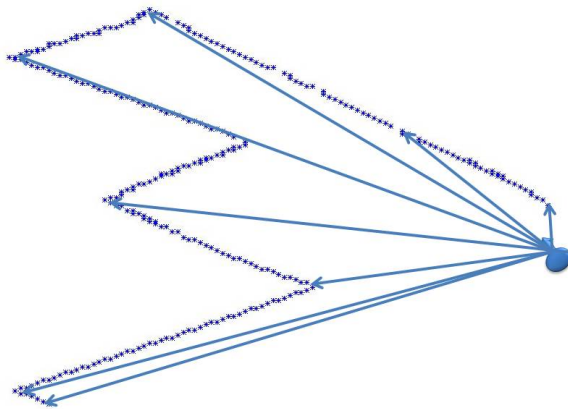
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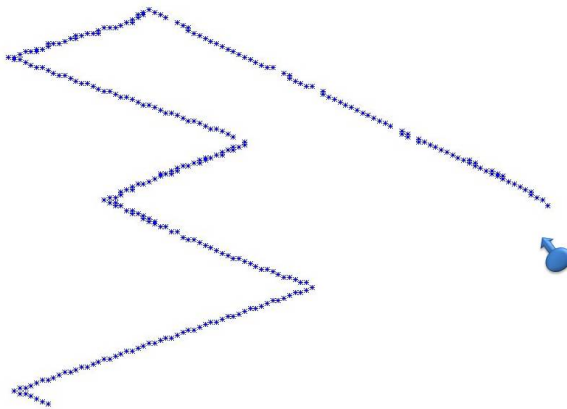
# Contour



# Contour



## Contour



# Detecting New Frontiers

- We scan the calculated contour from previous step
- Each point is compared with its (already scanned) predecessor
- Four possible cases:
  - Scanned point is not a frontier cell
  - Scanned point is a frontier cell but its predecessor is not
  - Both scanned point and its predecessor are frontier points
  - Scanned point is not a frontier cell but its predecessor is



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# Maintenance: Motivation

- *FFD* gains its speed by only processing the laser readings
  - rather than entire regions of the map
- Previously detected frontiers are not updated during navigation
- Only the frontier that the robot is headed to

## Problem

*FFD* is able to detect only *new* frontiers in each execution

## Solution

Maintenance of frontiers which are not covered in the sensors range





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Maintenance of frontiers which are not covered in the sensors range



# Maintenance 1: Eliminating Previously Detected Frontiers

- Points which are no longer in frontiers have to be eliminated
- *Active Area*: blocking rectangle constructed from laser readings
- If a frontier is to be eliminated, it must lie inside the active area
  - it contains regions that are covered by the robot's sensors
- *FFD* scans each point that lies inside the *Active Area*
  - Checking if a point is previously belonged to a frontier is fast



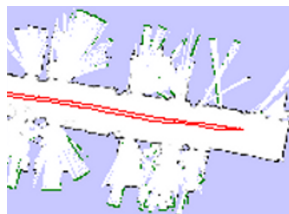
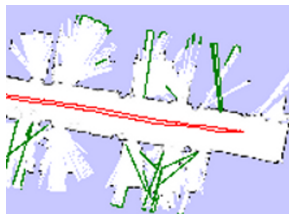
# Maintenance 2: Avoiding Re-detection of Same Frontier

## Problem

*FFD* might wrongly detect a new frontier in an already scanned area

## Solution

*FFD* distinguishes between laser readings in different time frames



# Maintenance: Summary

- *FFD* has to run in the background
  - In contrast to other approaches that are executed in a certain time
- *FFD* requires robustness against map orientation changes
  - caused by loop-closures



# FFD is Complete

## Lemma (1)

*Suppose  $f$  is a frontier point at time  $t$ , which was not a frontier point at any time  $s$ , where  $s < t$ .*

*Then FFD will mark  $f$  as a frontier given observation  $O_t$ .*



# FFD is Complete

## Proof.

- Towards a contradiction: *FFD* did not recognize  $f$  as a frontier
- $f$  cannot be located wholly within an *unknown* region
  - because it must have at least one *Open Space* neighbor
- $f$  cannot be located wholly within a *known*
  - since  $f$  is a valid frontier point and hence, its value is *Unknown*
- Therefore,  $f$  must be located on the contour itself.
- Detection Stage: *FFD* scans *all* contour points sequentially
  - and specifically searches for frontier points
- It follows that  $f$  would be detected, **contradicting** the assumption



# FFD is Complete

## Theorem (Completeness)

*Let  $f$  be a valid frontier point at time  $t$ .*

*Then FFD will mark  $f$  as a frontier point given the sequence of observations  $\langle O_0, \dots, O_t \rangle$ .*



# FFD is Complete

## Proof.

- **Case 1.  $f$  is a new frontier point at time  $t$ .**

Trivially, this case is handled directly by lemma 1.

- **Case 2.  $f$  was a new frontier point at time  $s$ , where  $s < t$ .**

- Let  $s$  be the earliest time in which  $f$  was a frontier.
- Based on lemma 1, it follows that it was detected at this time.
- $f$  must be a frontier point that is maintained by *FFD* at time  $t$ .
- $f$  can be eliminated only by the maintenance stage.
- $f$  is still a valid frontier and hence, was not covered by the sensors.
- Therefore,  $f$  will not be scanned and eliminated in time  $t$
- $\Rightarrow f$  remains classified as a frontier by *FFD*.

- In both cases *FFD* will recognize  $f$  to be a valid frontier at time  $t$ .





# FFD is Sound

## Theorem (Soundness)

*Let  $\hat{f}$  be an arbitrary point in the occupancy grid, which is not a frontier at time  $t$ .*

*Then FFD will not return  $\hat{f}$  as a frontier point, given the sequence of observations  $\langle O_0, \dots, O_t \rangle$ .*



# FFD is Sound

## Proof.

- $\hat{f}$  is not *Unknown* or all its neighbors are not *Open Space*
- **Case 1.  $\hat{f}$  is marked as a new frontier.**
  - FFD detects  $\hat{f}$  as a new frontier
  - $\hat{f}$  must be located on the contour *and* detected by Extraction stage
  - FFD specifically avoids detecting non-frontier points as frontiers
  - Case 1 is not possible
- **Case 2.  $\hat{f}$  is an old frontier but was not eliminated.**
  - $\hat{f}$  is located inside the active area and was not eliminated.
  - $\hat{f}$  is a point that was covered by the robot's sensors
  - Each point in the map keeps a frontier index (or NULL value)
  - FFD scans  $\hat{f}$  and finds out it has a not NULL frontier index
  - The Maintenance stage will eliminate  $\hat{f}$
  - Case 2 is not possible



# WFD Complexity

- WFD is based on Breadth-First Search (BFS) over the map.
- WFD scans all *Open Space* regions for frontier points.
- When a frontier point is found, another BFS is executed
  - in order to extract the frontier.
- BFS time complexity is linear in size of the search space.
- $\Rightarrow$  Linear in size of *area* and *perimeter* of *Open Space* regions

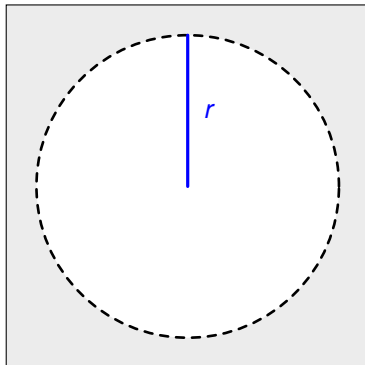
$$\mathcal{O} \left( \underbrace{\mathcal{S}(\text{open-space})}_{\text{area}} + \underbrace{\mathcal{P}(\text{open-space})}_{\text{perimeter}} \right)$$



# WFD Best Case

## Best Case

The perimeter of the *open-space* regions is minimal relatively to the area of the *open-space* regions



# WFD Best Case

- Notation:
  - $S_{open} :=$  the area of the shape
  - $P_{opt} :=$  the perimeter of the shape
- The best case holds:

$$S_{open} = 4\pi r^2$$

$$P_{opt} = 2\pi r$$



# WFD Worst Case

## Worst Case

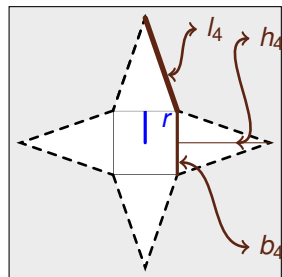
- Maximize the length of the perimeter
  - while **keeping** the total area of the *open-space* regions.
- Use a polygon as an approximation to a circle.
- The level of accuracy is determined by  $k$ , the number of vertices.



# WFD Worst Case

Notation (for a given  $k$  vertices):

- $S_k :=$  the area of the shape.
  - $S_k = S_{open}$  (area remains the same)
- $P_k :=$  the perimeter of the shape.
- $b_k :=$  the base of the inner *open-space* polygon.
- $h_k :=$  the height of an outer triangle
- $l_k :=$  the length of an outer triangle side.



## WFD

# WFD Worst Case

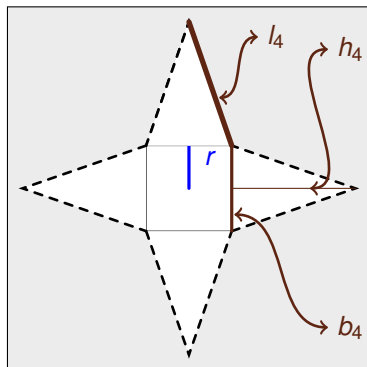


Figure:  $k = 4$



## WFD

# WFD Worst Case

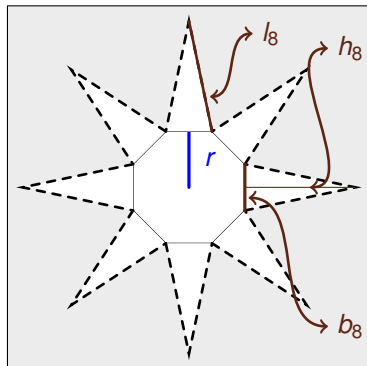


Figure:  $k = 8$

## WFD

# WFD Worst Case

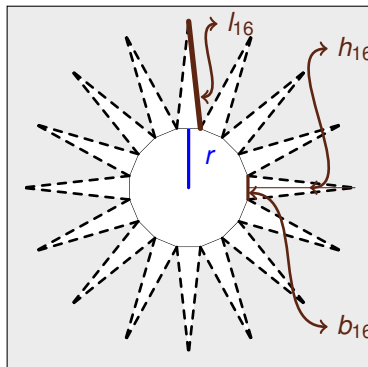


Figure:  $k = 16$

# WFD Worst Case

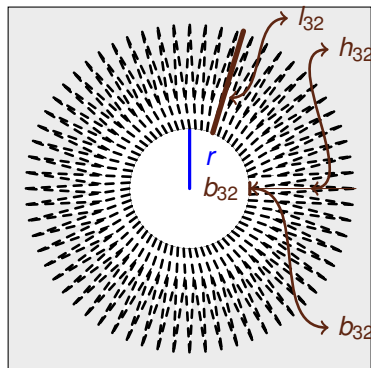


Figure:  $k = 32$

# WFD Worst Case

- The *open-space* regions are equal:

$$S_k = S_{open}$$

$$\underbrace{k \cdot \frac{r \cdot b_k}{2}}_{\text{inner polygon}} + \underbrace{k \cdot \frac{h_k \cdot b_k}{2}}_{\text{outer triangles}} = 4\pi r^2$$

- We can express  $b_k$  by:

$$b_k = 2r \cdot \tan \frac{\pi}{k}$$

- $\Rightarrow h_k$  can be expressed by:

$$h_k = \frac{8\pi r^2}{k \cdot b_k} - r$$



# WFD Worst Case

- Each outside triangle edge can be expressed by:

$$l_k = \sqrt{(h_k)^2 + \left(\frac{b_k}{2}\right)^2}$$

- The length of the polygon perimeter equals to:

$$P_k = 2k \cdot l_k$$

- We would like to express  $P_k$  as a function of  $S_{open}$ :

$$P_k = \sqrt{\left(\frac{2 \cdot S_{open}}{r \cdot \tan \frac{\pi}{k}}\right)^2 - 8 \frac{k \cdot S_{open}}{\tan \frac{\pi}{k}} + 4 \frac{k^2 \cdot r^2}{\cos^2 \frac{\pi}{k}}}$$



# WFD Worst Case

- Since  $k \leq S_{open}$ ,  $P_k$  can be bounded by:

$$P_k \leq \sqrt{\left(\frac{2 \cdot S_{open}}{r \cdot \tan \frac{\pi}{S_{open}}}\right)^2 - 8 \frac{S_{open}^2}{\tan \frac{\pi}{S_{open}}} + 2 \cdot S_{open}^2 \cdot r^2}$$

- $\Rightarrow$  Run-time complexity of *WFD* in terms of *open-space* area:

$$\mathcal{O}\left(S_{open} + \sqrt{\left(\frac{S_{open}}{r \cdot \tan \frac{\pi}{S_{open}}}\right)^2 - \frac{S_{open}^2}{\tan \frac{\pi}{S_{open}}} + S_{open}^2 \cdot r^2}\right)$$



# FFD Complexity

- It may seem that *FFD*'s complexity is contained within *WFD*
  - since *FFD* searches only inside the active area (*open-space*)
- It is not true since *FFD* has to persistently run in the background
- We analyse the complexity of each stage separately



# FFD Complexity - Sorting Stage

- *FFD* performs polar-sorting of laser readings.
- Cross-product instead of actually calculating angle and radius
  - which are relatively very time-consuming calculations
- Cross-product calculation is performed in a constant time
- Sorting is performed in time of  $\mathcal{O}(n \log n)$ .
- $l_r :=$  the number of laser readings received in each measurement
- Total complexity of this stage is:

$$\mathcal{O}(l_r \log l_r) \cdot \mathcal{O}(1) = \mathcal{O}(l_r \log l_r)$$





# FFD Complexity - Contour Stage

- Scans each two adjacent points from the polar-sorted readings.
- *FFD* connects each two adjacent points by a line
  - by calling *Bresenham's line algorithm*, linear time complexity
- $d_{p_i, p_j} :=$  euclidean distance between points  $p_i$  and  $p_j$
- $c^{(t)} :=$  the length of the contour in time  $t$
- Total complexity of this stage is:

$$\mathcal{O}\left(\sum_{p_i \in I_r} d_{p_{i-1}, p_i}\right) = \mathcal{O}\left(c^{(t)}\right)$$

# FFD Complexity - Detection Stage

- Scans the contour extracts new frontiers (if available any)
- Each found new detected frontier is added into a list
- All actions are performed in a constant time
- Total complexity of this stage is:

$$\underbrace{\mathcal{O}(1)}_{\text{special case}} + \underbrace{\mathcal{O}(c^{(t)}) \cdot \mathcal{O}(1)}_{\text{general case}} = \mathcal{O}(c^{(t)})$$

# FFD Complexity - Maintenance Stage (1)

Elimination of previous frontiers:

- Scans each point that lies inside the active area
- Checks if it was previously belonged to a frontier
- $A^{(t)}$  := the bounding rectangle (the active area) in time  $t$
- $f_{max}^{(t)}$  := length of the longest frontier the frontier database in time  $t$
- $n_f^{(t)}$  := number of frontiers in the frontier database in time  $t$
- Total complexity of this stage is:

$$O \left( \underbrace{A^{(t)}}_{\text{scanning active area}} \cdot \left( \underbrace{f_{max}^{(t)}}_{\text{find frontier point}} + \underbrace{\log n_f^{(t)}}_{\text{get frontier from DB}} \right) \right)$$



## FFD Complexity - Maintenance Stage (2)

Adding new frontiers:

- Scans each frontier point within all new detected frontiers
- $n_{new}^{(t)}$  := number of new frontiers that were found in time  $t$
- Checks if new frontier point belongs to previously detected frontier
- The check is performed in a constant time
- All other actions are performed in a constant time
- Total complexity of this stage is:

$$\mathcal{O} \left( \underbrace{n_{new}^{(t)}}_{\text{scan frontiers}} \cdot \left( \underbrace{f_{max}^{(t)}}_{\text{scan all points in frontier}} + \underbrace{\log n_f^{(t)}}_{\text{get frontier from DB}} \right) \right)$$



# FFD Complexity - Combining All Stages

- We join all previous stages and get:

$$\mathcal{O}\left(l_r \log l_r + c^{(t)} + \left(A^{(t)} + n_{new}^{(t)}\right) \cdot \left(f_{max}^{(t)} + \log n_f^{(t)}\right)\right)$$

- The above equation can be bounded to:

$$\mathcal{O}\left(c^{(t)} + \log n_f^{(t)}\right)$$

- *FFD* has to run in the background
  - $l_\omega :=$  frequency of the laser sensor
  - $t_m :=$  worst-case elapsed time between two following map-events
  - $P_n :=$  number of particles in the SLAM implementation

$$\mathcal{O}\left(P_n \cdot (t_m \cdot l_\omega) \cdot \left(c^{(t)} + \log n_f^{(t)}\right)\right)$$



# General Maintenance Concepts

- *WFD*: detects old and new frontiers within each execution
- *FFD*: is able to detect new frontiers only
  - and therefore has perform a background maintenance
- The maintenance algorithm can be applied to *WFD*
  - and to other frontier detection algorithms



# Incremental Wavefront Frontier Detector

- Abbreviation: *WFD-INC*
- Search domain contains only points that lie inside the active area
  - instead of searching the whole known regions for frontier points
- Key idea: the only region that contains changes is the active area
- If a map orientation was changed, then *WFD-INC* acts as *WFD*
- *WFD-INC* has to call the maintenance routine
  - since it does not search the whole map



# Incremental-Parallel Wavefront Frontier Detector

- Abbreviation: *WFD-IP*
- Robust against map orientation changes that happens too often
- Key idea: keep a separate instance of *WFD-INC* for each particle
- Execute *WFD-INC* according to each particle's map data
- Result: all *WFD-INC* instances keep frontier data between calls





# Experiment Design

- We have fully implemented *WFD*, *WFD-INC*, *WFD-IP* and *FFD*
- We compare all algorithms with a State-of-the-Art algorithm<sup>1</sup>
- Our system is based on *GMapping* SLAM implementation
  - [Grisetti et al., 2005, 2007]
- Two machines:
  - Intel Core 2 Duo T6600 CPU, 2.20GHz, 4GB RAM
  - Intel Pentium III Coppermine CPU, 800MHz, 1GB RAM
- We measured CPU-process time



<sup>1</sup>We thank Kai M. Wurm and Wolfram Burgard for providing us their own implementation

# Experiment Design

- All detection algorithms are executed when a map update occurs
- *FFD* is executed when a new laser reading is received
- We accumulate *FFD*'s time between calls to other algorithms
- Tested on data obtained from RADISH [Howard and Roy, 2003]

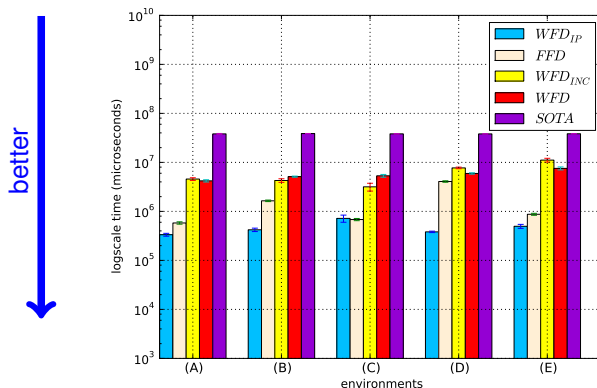


# Experiment Design



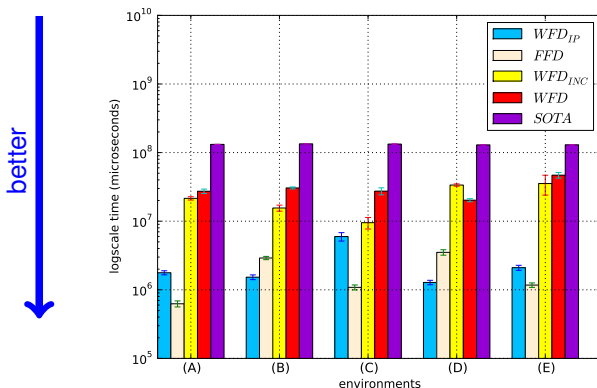
**Figure:** Example of a testing environment, University of Freiburg. Image was taken from RADISH, Howard and Roy [2003]

# Runtime Comparision (Core 2 Duo)



- Y axis: mean execution time (microseconds) on a *logaritimic scale*
- $WFD, WFD-INC$ : faster than  $SOTA$  by an order of magnitude
- $FFD, WFD-IP$ : faster than  $SOTA$  by two orders of magnitude

# Runtime Comparision (Coppermine)



- Y axis: mean execution time (microseconds) on a *logaritimic scale*
- $WFD, WFD_{INC}$ : faster than  $SOTA$  by an order of magnitude
- $FFD, WFD_{IP}$ : faster than  $SOTA$  by two orders of magnitude

# What Happend in Environment (D)?

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The mean run-time of *WFD* is not relatively slower than *FFD*

## Answer

- Environment (D) contains regions that contains small obstacles
- The obstacles enlarge the length of contour scanned by *FFD*
- As shown, the contour length affects the run-time complexity



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# Why is *WFD-INC* Sometimes Worse than *WFD*?

## What Happend?

- In the worst-case, *WFD-INC* should perform the same as *WFD*
- The run-time means of *WFD* and *WFD-INC* do not have a trend

## Hypothesis

- Certain environments have high frequency of particle change
- $\Rightarrow$  *WFD-INC* cleans its previous detected frontiers more often

Map	Changes	Executions	Percent (%)
(A)	56	110	50.91
(B)	52	287	18.12
(C)	25	160	15.62
(D)	193	429	44.99
(E)	73	340	21.47





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# What Happend to *WFD-IP* in Environments (A),(C),(E), Weak Machine?

- Strong machine: *WFD-IP* outperforms all other algorithms
- Weak machine: the situation is different in maps (A),(C),(E)
- Hypothesis (1) Memory:
  - Weak machine is equipped with less RAM than strong machine
  - *WFD-IP* holds a separate instance of *WFD-INC* for each particle
  - Hypothesis: strong machine runs each thread on a separate core
  - In our experiment, 30 instances of *WFD-INC*
- Hypothesis (2) CPU:
  - Weak machine is equipped a single CPU
  - GMapping runs two threads (Main thread and SLAM thread)
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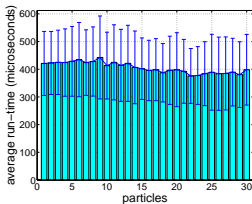


# Measuring Run-Time for Individual Particle

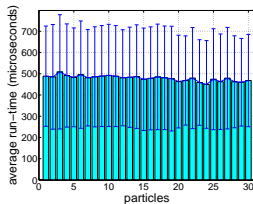
- We compare the run-time of individual particles in each map
- Each bar represents a specific particle
- Vertical axis: measures the run-time of *FFD* for the particle
- Error-bars: the standard deviation of each particle's run-time



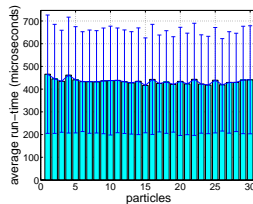
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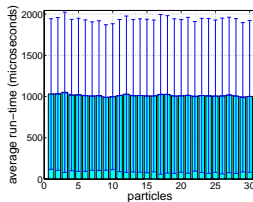
(a)



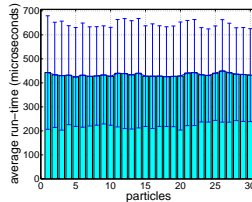
(b)



(c)



(d)



(e)



# FFD Performance According to Number of Particles

- *FFD* has to persistently run in the background
- Particle-filter systems: each particle has its own instance of *FFD*
- Hence, the overall run-time is increased
- We change the number of particles in different maps
- Each bar represents a run with a specific number of particles
- Vertical axis: mean run-time of *FFD* for the configuration
- Error-bars: standard deviation of each configuration run-time

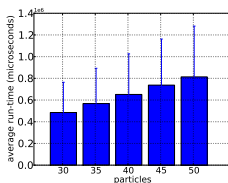


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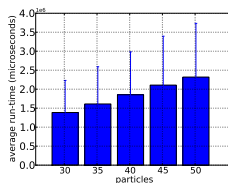
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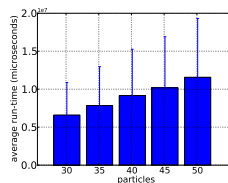
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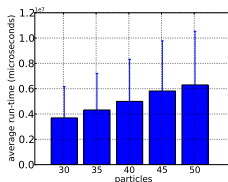
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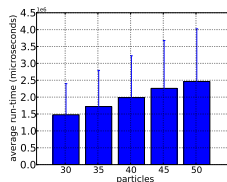
(b)



(c)



(d)



(e)

# Summary and Future Work

- Real-Time frontier detection on weak CPU's
- *WFD, FFD, WFD-INC, WFD-IP*: methods for frontier detection
  - significant reduction of calculation time
- Publications:
  - AAMAS 2012
  - ARMS workshop at AAMAS 2011
- Future work:
  - Address efficient methods for maintaining frontiers in *FFD*
  - Novel exploration policies based on real-time frontier-detection



# Sorting

- The first step sorts laser readings based on their angle
  - i.e based on the polar coordinates with the robot as the origin
- The naive method for converting Cartesian coordinates to polar coordinates is time-consuming
  - calling *atan2* and *sqrt*
- By using *Cross-Product* we can perform sorting much faster
  - $(p_1 - p_0) \times (p_2 - p_0) = (x_1 - x_0) \cdot (y_2 - y_0) - (x_2 - x_0) \cdot (y_1 - y_0)$
  - If the result is positive, then  $\overrightarrow{P_0P_1}$  is clockwise from  $\overrightarrow{P_0P_2}$ .
  - Else, it is counter-clockwise.
  - If result is 0, then the two vectors lie on the same line in the plane

► Back to FFD



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