

Adversarial ML

A black and white illustration of a dandelion seed head. The seed head is a large, spherical cluster of many small seeds, each with a long, thin stem. The seeds are arranged in a radial pattern, creating a dense, textured appearance. Several seeds are shown floating away from the main head, scattered across the upper left portion of the image. The background is a solid light gray, and a dark gray horizontal band runs across the middle of the image, behind the title text.

常見名詞 Part.1

• 常見名詞 •

Threat Model	Adversarial Falsification	False Negative(FN) (Adversarial example)	FGSM、L-BFGS、DeepFool、Uni. perturbations、C&W
		False Positive(FP) (Fooling example)	
	Adversary's Knowledge	White-Box	FGSM、L-BFGS、DeepFool、Uni. perturbations、C&W
		Black-Box	
	Adversarial Specificity	Targeted	L-BFGS、C&W
		Non-Targeted	FGSM、DeepFool、Uni. perturbations
	Attack Frequency	One-time	FGSM
		Iterative	L-BFGS、DeepFool、Uni. perturbations、C&W

• 常見名詞 •

Perturbation	Perturbation Scope	Individual	FGSM、L-BFGS、DeepFool、C&W
		Universal	Uni. perturbations
	Perturbation Limitation	Optimized	L-BFGS、DeepFool、Uni. perturbations、C&W
		Constraint	
		None	FGSM
	Perturbation Measurement (ℓ_p)	p=0	C&W
		p=1	
		p=2	L-BFGS、Uni. perturbations、DeepFool、C&W
		p= ∞	FGSM、DeepFool、Uni. perturbations、C&W

A black and white illustration of a dandelion seed head. The seed head is a large, spherical cluster of many small seeds, each with a long, thin stem. The seeds are arranged in a radial pattern, creating a dense, textured appearance. A few seeds are shown floating away from the main head, indicating they have been blown by the wind. The background is a solid dark gray, which makes the white lines of the dandelion stand out. The overall style is minimalist and artistic.

攻撃 Part.2

• Box-Constrained L-BFGS •

$$\min_{\boldsymbol{\rho}} \quad c|\boldsymbol{\rho}| + \mathcal{L}(\mathbf{I}_c + \boldsymbol{\rho}, \ell) \quad s.t. \quad \mathbf{I}_c + \boldsymbol{\rho} \in [0, 1]^m$$

- 第一篇提出「Adversarial Example」概念
- Results in the exact solution for a classifier that has a convex loss function.
- Make us understand better the input-to-output mapping represented by the trained network.

DeepFool

- To find a **minimal norm** adversarial perturbation for a given image in an **iterative** manner
- How: 推到分類器的邊界

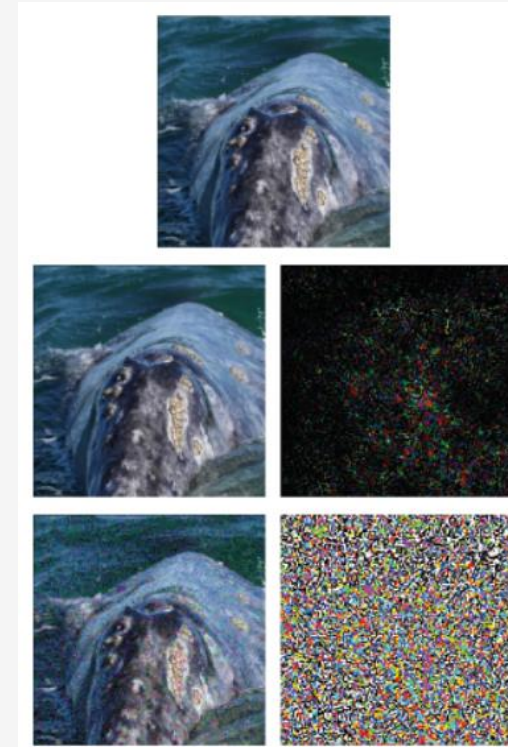
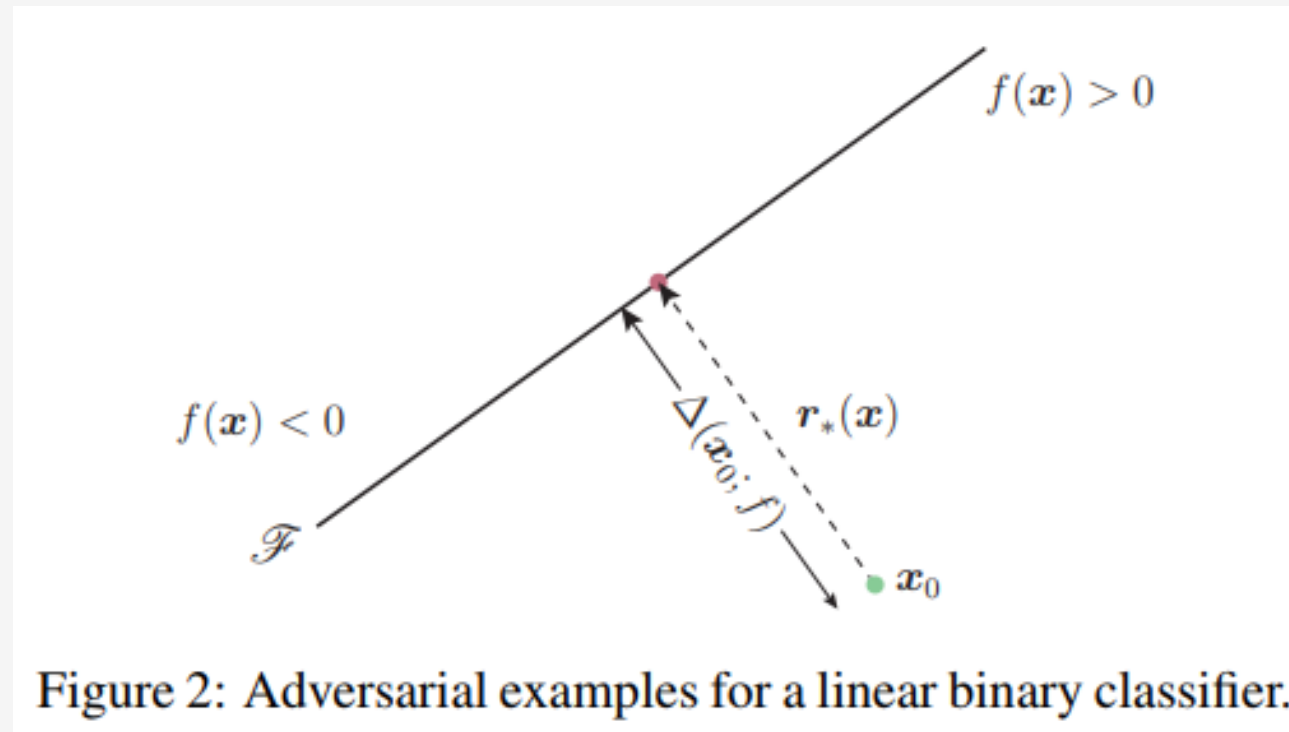


Figure 1: An example of adversarial perturbations. First row: the original image x that is classified as $\hat{k}(x)$ ="whale". Second row: the image $x + r$ classified as $\hat{k}(x + r)$ ="turtle" and the corresponding perturbation r computed by DeepFool. Third row: the image classified as "turtle" and the corresponding perturbation computed by the fast gradient sign method [4]. DeepFool leads to a smaller perturbation.

S.-M. Moosavi-Dezfooli, A. Fawzi, and P. Frossard, "Deepfool: a simple and accurate method to fool deep neural networks," in Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition (CVPR), 2016, pp. 2574–2582 [Online]. Available: <https://arxiv.org/abs/1511.04599>

DeepFool



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DeepFool

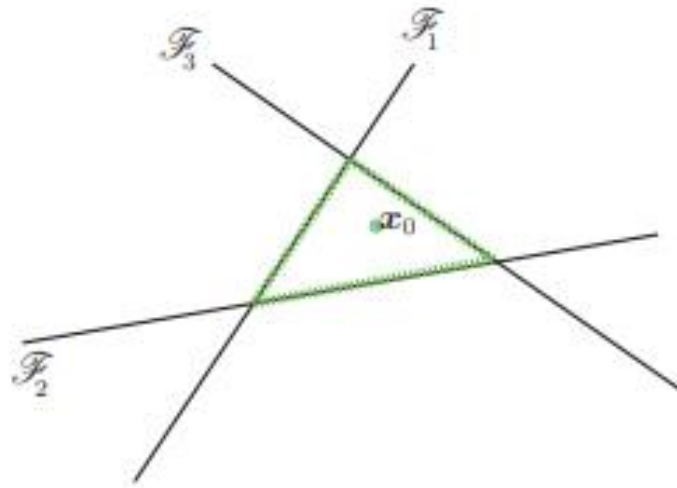


Figure 4: For x_0 belonging to class 4, let $\mathcal{F}_k = \{x : f_k(x) - f_4(x) = 0\}$. These hyperplanes are depicted in solid lines and the boundary of P is shown in green dotted line.

DeepFool

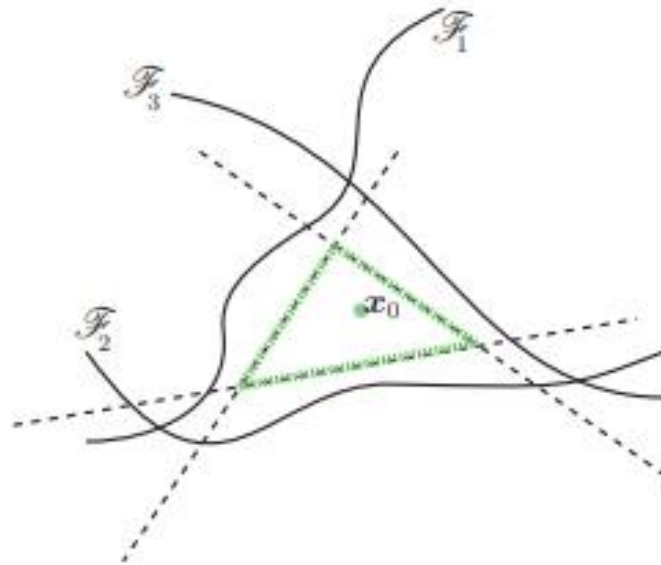


Figure 5: For x_0 belonging to class 4, let $\mathcal{F}_k = \{x : f_k(x) - f_4(x) = 0\}$. The linearized zero level sets are shown in dashed lines and the boundary of the polyhedron \tilde{P}_0 in green.

DeepFool

Algorithm 2 DeepFool: multi-class case

```
1: input: Image  $\mathbf{x}$ , classifier  $f$ .
2: output: Perturbation  $\hat{\mathbf{r}}$ .
3:
4: Initialize  $\mathbf{x}_0 \leftarrow \mathbf{x}$ ,  $i \leftarrow 0$ .
5: while  $\hat{k}(\mathbf{x}_i) = \hat{k}(\mathbf{x}_0)$  do
6:   for  $k \neq \hat{k}(\mathbf{x}_0)$  do
7:      $\mathbf{w}'_k \leftarrow \nabla f_k(\mathbf{x}_i) - \nabla f_{\hat{k}(\mathbf{x}_0)}(\mathbf{x}_i)$ 
8:      $f'_k \leftarrow f_k(\mathbf{x}_i) - f_{\hat{k}(\mathbf{x}_0)}(\mathbf{x}_i)$ 
9:   end for
10:   $\hat{l} \leftarrow \arg \min_{k \neq \hat{k}(\mathbf{x}_0)} \frac{|f'_k|}{\|\mathbf{w}'_k\|_2}$ 
11:   $\mathbf{r}_i \leftarrow \frac{|f'_i|}{\|\mathbf{w}'_i\|_2} \mathbf{w}'_i$ 
12:   $\mathbf{x}_{i+1} \leftarrow \mathbf{x}_i + \mathbf{r}_i$ 
13:   $i \leftarrow i + 1$ 
14: end while
15: return  $\hat{\mathbf{r}} = \sum_i \mathbf{r}_i$ 
```

Universal adversarial perturbations

- To find a **single perturbation** which is able to fool a network on “any” image with high confidence
- How: 漸進的推進到分類的邊界

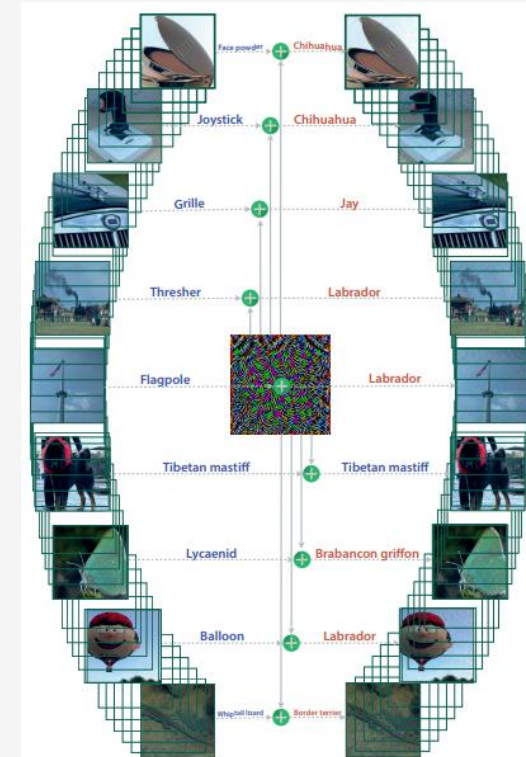


Figure 1: When added to a natural image, a universal perturbation image causes the image to be misclassified by the deep neural network with high probability. *Left images:* Original natural images. The labels are shown on top of each arrow. *Central image:* Universal perturbation. *Right images:* Perturbed images. The estimated labels of the perturbed images are shown on top of each arrow.

S.-M. Moosavi-Dezfooli, A. Fawzi, O. Fawzi, and P. Frossard, “Universal adversarial perturbations,” in Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition (CVPR), 2017. [Online]. Available: <https://arxiv.org/abs/1610.08401>

Universal adversarial perturbations

1. Goal

$$\hat{k}(x + v) \neq \hat{k}(x) \text{ for “most” } x \sim \mu.$$

1. Constraints

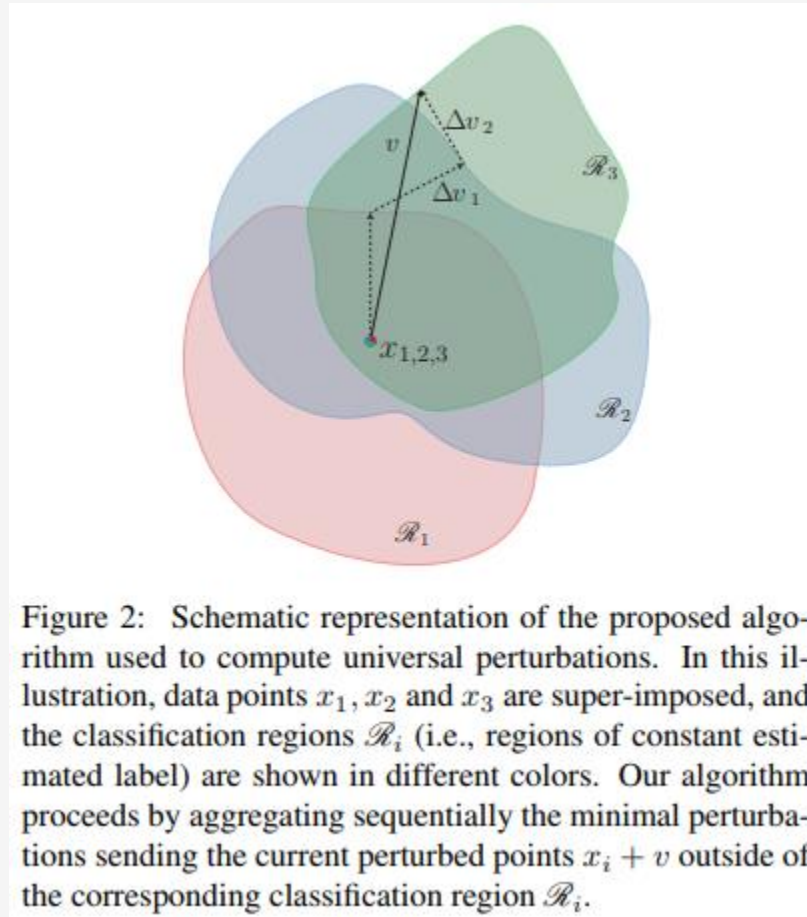
- 擾動不能過大

$$\|v\|_p \leq \xi,$$

- 成功率要夠高

$$\mathbb{P}_{x \sim \mu} \left(\hat{k}(x + v) \neq \hat{k}(x) \right) \geq 1 - \delta.$$

Universal adversarial perturbations



S.-M. Moosavi-Dezfooli, A. Fawzi, O. Fawzi, and P. Frossard, “Universal adversarial perturbations,” in Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition (CVPR), 2017. [Online]. Available: <https://arxiv.org/abs/1610.08401>

Universal adversarial perturbations

3. Algorithm

a. If v not best perturbation:

$$\Delta v_i \leftarrow \arg \min_r \|r\|_2 \text{ s.t. } \hat{k}(x_i + v + r) \neq \hat{k}(x_i).$$

b. To fit constraint-1:

$$\mathcal{P}_{p,\xi}(v) = \arg \min_{v'} \|v - v'\|_2 \text{ subject to } \|v'\|_p \leq \xi.$$

c. Update v :

$$v \leftarrow \mathcal{P}_{p,\xi}(v + \Delta v_i).$$

d. Stop when:

$$\text{Err}(X_v) := \frac{1}{m} \sum_{i=1}^m 1_{\hat{k}(x_i+v) \neq \hat{k}(x_i)} \geq 1 - \delta.$$

Universal adversarial perturbations

Algorithm 1 Computation of universal perturbations.

```
1: input: Data points  $X$ , classifier  $\hat{k}$ , desired  $\ell_p$  norm of  
   the perturbation  $\xi$ , desired accuracy on perturbed sam-  
   ples  $\delta$ .  
2: output: Universal perturbation vector  $v$ .  
3: Initialize  $v \leftarrow 0$ .  
4: while  $\text{Err}(X_v) \leq 1 - \delta$  do  
5:   for each datapoint  $x_i \in X$  do  
6:     if  $\hat{k}(x_i + v) = \hat{k}(x_i)$  then  
7:       Compute the minimal perturbation that  
       sends  $x_i + v$  to the decision boundary:  
  
       
$$\Delta v_i \leftarrow \arg \min_r \|r\|_2 \text{ s.t. } \hat{k}(x_i + v + r) \neq \hat{k}(x_i).$$
  
8:       Update the perturbation:  
  
       
$$v \leftarrow \mathcal{P}_{p,\xi}(v + \Delta v_i).$$
  
9:     end if  
10:   end for  
11: end while
```


CARLINI AND WAGNER ATTACKS (C&W)

- The objective function to change the label vector

$$f_1(x') = -\text{loss}_{F,t}(x') + 1$$

$$f_2(x') = (\max_{i \neq t} (F(x')_i) - F(x')_t)^+$$

$$f_3(x') = \text{softplus}(\max_{i \neq t} (F(x')_i) - F(x')_t) - \log(2)$$

$$f_4(x') = (0.5 - F(x')_t)^+$$

$$f_5(x') = -\log(2F(x')_t - 2)$$

$$f_6(x') = (\max_{i \neq t} (Z(x')_i) - Z(x')_t)^+$$

$$f_7(x') = \text{softplus}(\max_{i \neq t} (Z(x')_i) - Z(x')_t) - \log(2)$$

CARLINI AND WAGNER ATTACKS (C&W)

- An adversarial method to attack defensive distillation(防禦性蒸餾)
- 攻擊防禦性蒸餾模型實際上很簡單，不考慮這些其他的類向量值，**只考慮需要超過的類向量(目標類)和自身的類向量值即可**，甚至可以只關注增加自身的類向量

- Ex:

[-674.3225 , -371.59705 , -177.78831 , 562.87225 , -
1313.5781 , 998.18207 , -886.97107 , -511.58194 , -
126.719666, -43.129272]

CARLINI AND WAGNER ATTACKS (C&W)

- Box Constraint

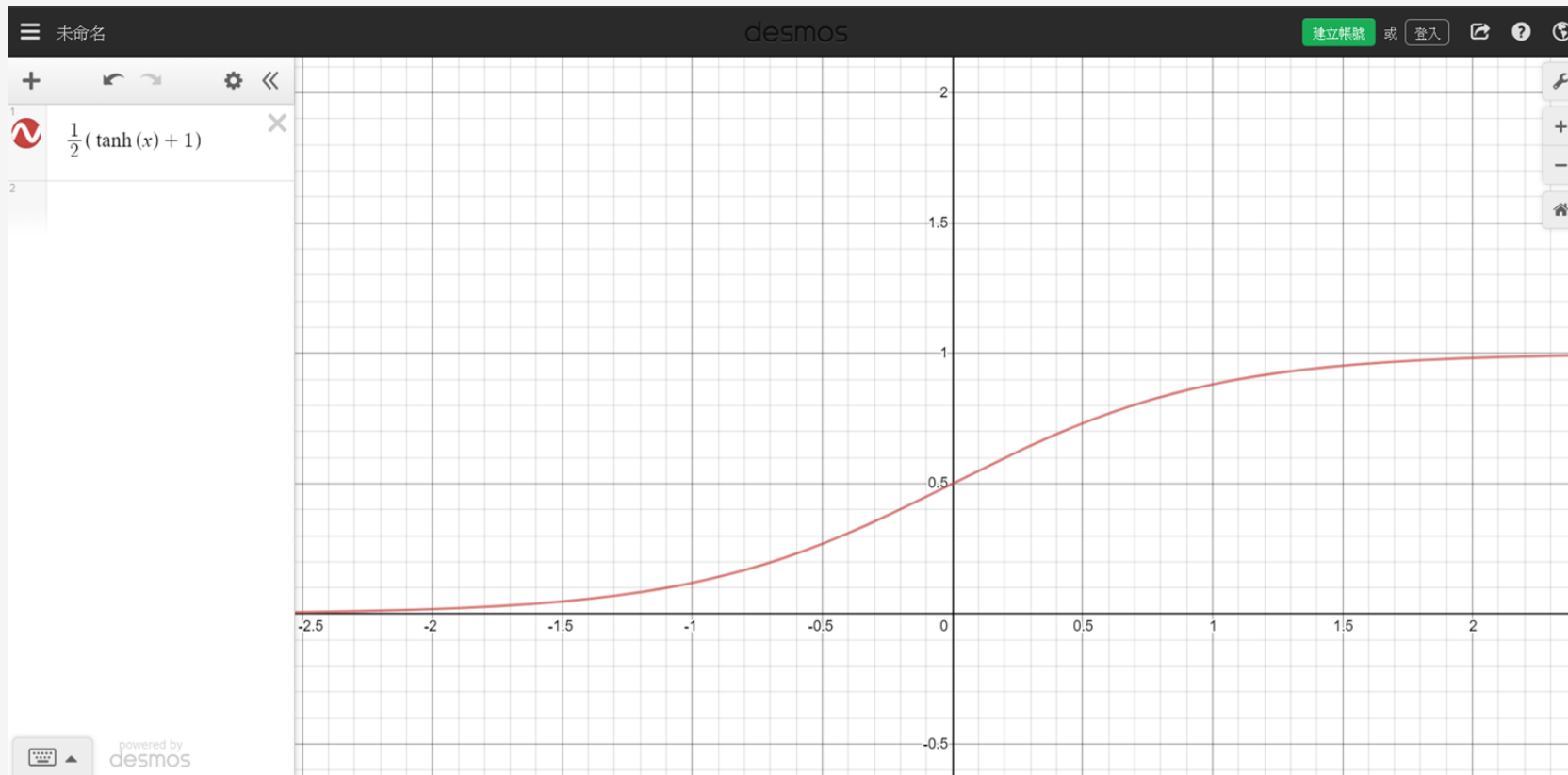
$$0 \leq x_i + \delta_i \leq 1$$

CARLINI AND WAGNER ATTACKS (C&W)

- To solve box constraints
 - a. 投影梯度下降法:對於具有複雜更新步驟的梯度下降方法（例如，具有動量的梯度下降），效果不佳
 - b. 裁剪梯度下降法:將裁剪直接放入了優化目標，但容易卡在平坦區域，x卡在邊界值動不了
 - c. 改變變量:用新的變量w代替原先的x(本篇作者的用法)

$$\delta_i = \frac{1}{2}(\tanh(w_i) + 1) - x_i.$$

CARLINI AND WAGNER ATTACKS (C&W)



CARLINI AND WAGNER ATTACKS (C&W)

- How: L2 attack
 - a. Chose the target label t
 - b. Our goal is to optimize:

$$\text{minimize } \left\| \frac{1}{2}(\tanh(w) + 1) - x \right\|_2^2 + c \cdot f\left(\frac{1}{2}(\tanh(w) + 1)\right)$$
$$f(x') = \max(\max\{Z(x')_i : i \neq t\} - Z(x')_t, -\kappa).$$

- a. by adjusting c : from 10^{-4} to 10^{10} ;
- b. by adjusting k : 錯誤分類發生的置信度

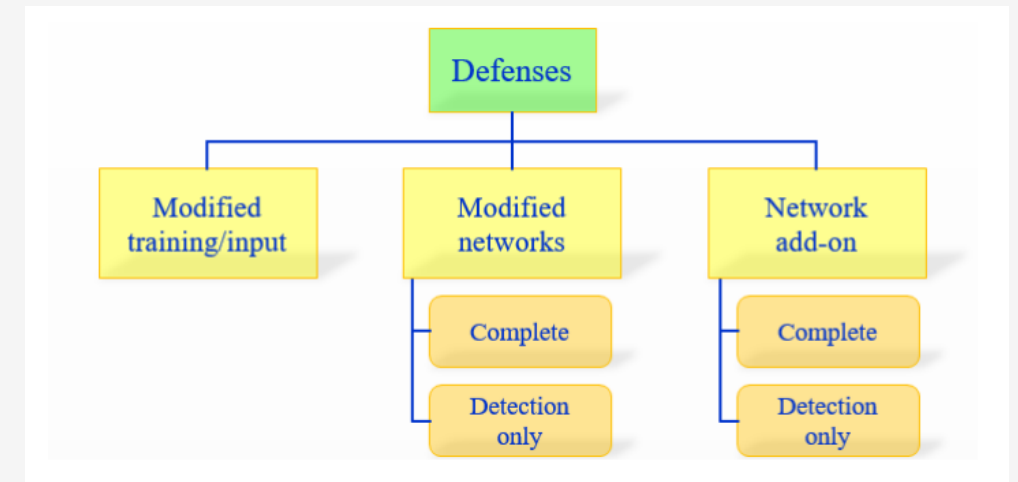
A black and white illustration of a dandelion seed head. The seed head is a large, spherical cluster of many small seeds, each with a long, thin stem. The seeds are arranged in a radial pattern, with the stems pointing outwards. Some seeds are shown in the process of being blown away, with their stems curved and the seeds floating in the air. The background is a solid dark grey, and the overall style is minimalist and artistic.

防禦 Part.2

架構

- 三種防禦方法

- a. Training時修改訓練集或testing時修改測試樣本
- b. 更改網路架構-training
- c. 外接其他網路-testing



- 兩種對抗程度

- a. Complete-能辨識回原本label
- b. Detection only-僅辨識是否為攻擊樣本並拒絕分類

Brute-Force Adversarial Training

- Modified Training/Input
- 使用adversarial training的方法，需要來自強大攻擊方法的樣本增加訓練集，使模型正規化，減少overfitting
- Virtual Adversarial Training
- 缺點：依舊能找出新漏洞

Virtual Adversarial Training(VAT)

- 目標函數
$$\frac{1}{N} \sum_{n=1}^N \log p(y^{(n)} | x^{(n)}, \theta) + \lambda \frac{1}{N} \sum_{n=1}^N LDS(x^{(n)}, \theta)$$

- 定義LDS
$$LDS(x^{(n)}, \theta) = -\Delta_{KL}(r_{v-adv}^{(n)}, x^{(n)}, \theta)$$

- 定義Rv-adv
$$\begin{aligned} \Delta_{KL}(r, x^{(n)}, \theta) &= KL[p(y | x^{(n)}, \theta) || p(y | x^{(n)} + r, \theta)] \\ r_{v-adv}^{(n)} &= \arg \max_r \{ \Delta_{KL}(r, x^{(n)}, \theta); ||r|| \leq \epsilon \} \end{aligned}$$

Deep Contractive Network

- Modifying the Network
- 借由類似Contractive Auto Encoders的平滑度懲罰項，可防禦L-BGFS

Loss function
T:target
Y:model prediction

$$J_{DCN}(\theta) = \sum_{i=1}^m (L(t^{(i)}, y^{(i)}) + \lambda \left\| \frac{\partial y^{(i)}}{\partial x^{(i)}} \right\|_2)$$

Loss function(layer wise)
h:h-th hidden layer

$$J_{DCN}(\theta) = \sum_{i=1}^m (L(t^{(i)}, y^{(i)}) + \sum_{j=1}^{H+1} \lambda_j \left\| \frac{\partial h_j^{(i)}}{\partial h_{j-1}^{(i)}} \right\|_2)$$

Gradient Regularization/Masking

- Modifying the Network
- training時減少gradient的變化，或隱藏gradient，有利於對抗基於gradient的攻擊方法
- Masking-based Defense
- 通過在網絡的logit輸出中添加noise，實現了masking based的對於C&W攻擊的防禦。

A Learning and Masking Approach to Secure Learning

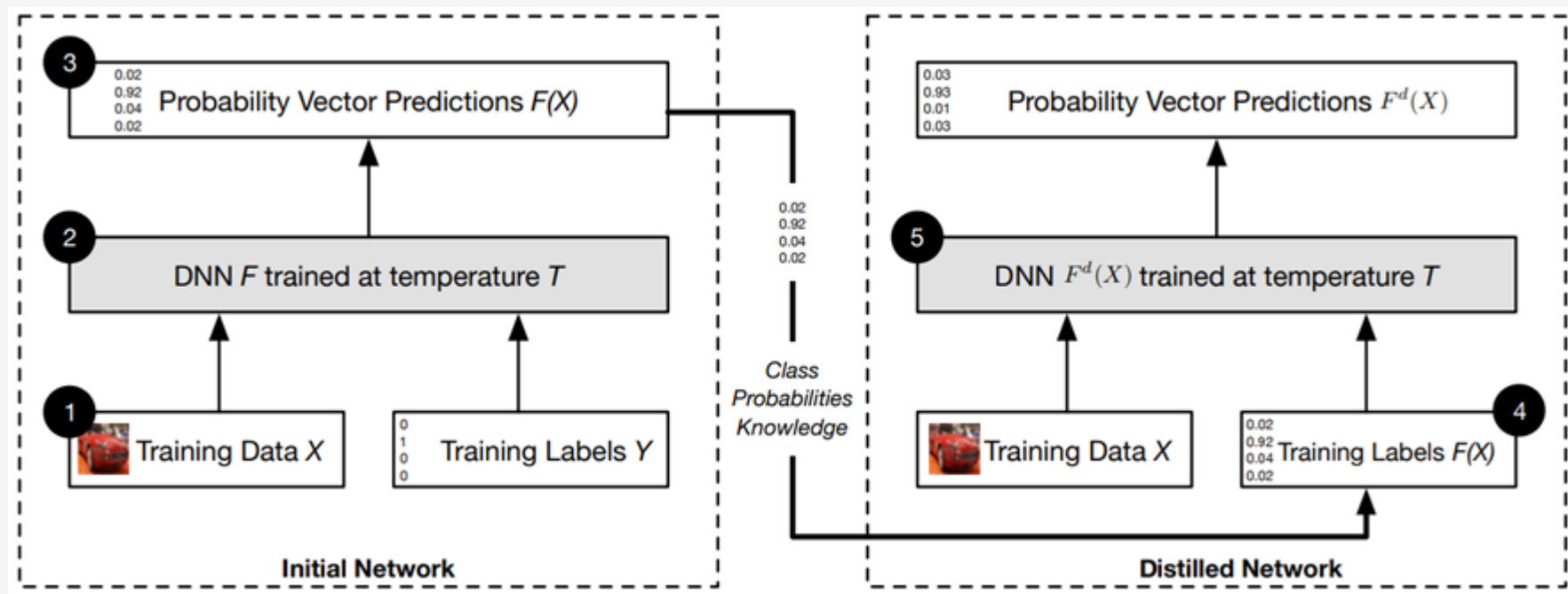
- 攻擊方法: ALN
- 防禦方法: DLN、NAC
- DLN

$$\overline{\alpha sim}(x, D(x')) + \overline{opsim}(Cat(y_x), C_p(D(x'))))$$

- a. 去噪前後相似
 - b. 去噪後要能辨識回原類別
 - c. Cat(y)-原類別、D(x)-去噪器、Cp(x)-分類器
- NAC
 - a. 對於低干擾的對抗樣本，它們大多在分類邊界附近，因此可以通過屏蔽分類邊界來愚弄低干擾對抗樣本
 - b. 在模型輸出中加入noise

Defensive Distillation

- Modifying the Network
- Distillation 是指將複雜網絡的知識遷移到簡單網絡上



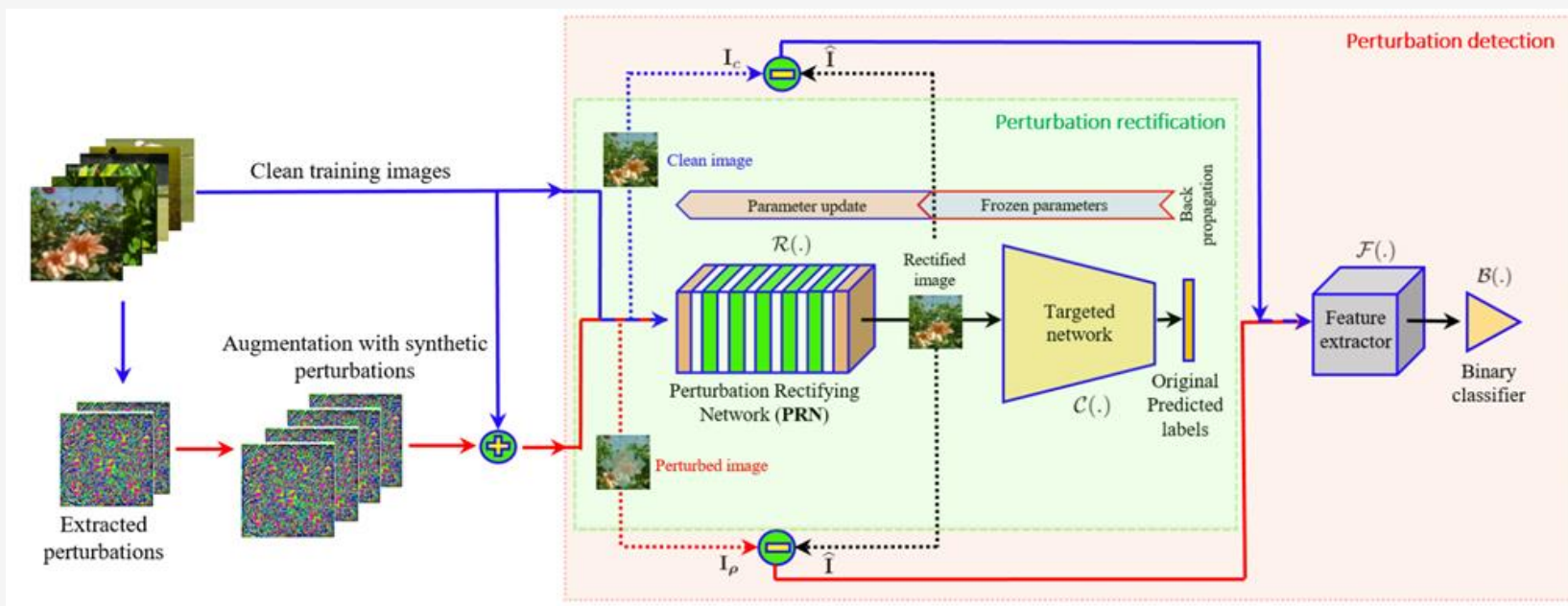
• Detector Subnetwork •

- Modifying the Network-Detection Only Approaches
- 增加一個子網路辨識是否為擾動樣本，可防禦FGSM、BIM、DeepFool
- Additional Class Augmentation
- 方法：增加一個class來辨識攻擊樣本
- 缺點：依舊會被找到漏洞

Defense Against Universal Perturbations

- Network Add-ONS
- 增加一個預輸入層-Perturbation Rectifying Network (PRN)

$$\mathcal{J}(\theta_p, \mathbf{b}_p) = \frac{1}{N} \sum_{i=1}^N \mathcal{L}(\ell_i^*, \ell_i),$$



MagNet

- Network Add-ONS Detection Only Approaches
- 訓練一個detector來辨識乾淨圖片的manifold，並訓練一個reformer來重構接近manifold邊界的圖片

