University of Bucharest Faculty of Mathematics and Computer Science Department of Computer Science Artificial Intelligence Master May 2020

Big Data Project Report- Insolvency Analysis -

SupervisorsBogdan Ichim
Ciprian Păduraru

Matei Bejan Tiberiu Marin Florin Iordache Andreea Cîrstoiu David Ivan Mihaela Nistor

Students

Dataset	3
Overview	3
Data	3
Goal	4
Preprocessing	4
Missing data imputation	5
Mean and median	5
K-Nearest Neighbours	5
Softimpute	5
Standardization and normalization	6
Feature engineering	6
Algorithms used	6
Modelling with Scikit-Learn	7
SVM	7
KNN	7
Random Forest	8
XGBoost	8
Neural Network	9
Modelling with Spark MLlib	10
LinearSVC	10
Logistic Regression	11
Random Forest	11
Boosted Trees Classifier	11
Neural Network	11
Data Engineering	13
Apache Hadoop	13
HDFS	13
Main features of HDFS	13
Architecture	13
Data storage in HDFS	14
HDFS commands	14
MapReduce	15
MapReduce architecture	15
Spark	16
Apache Spark Streaming	16
Results comparison	18
Sklearn	18
Spark	20
Conclusions	22
Further research	23

Dataset

a. Overview

The main purpose of this project is the study of company insolvency in the pre-covid-19 economical setting. For this we have employed both data science and big data methodologies, in order to scale our models up to the size of the given datasets.

In this project we will compare two Python machine learning libraries: scikit-learn and Spark's MLlib, in order to assess which one offers the best scalability-versus-accuracy trade-off. Furthermore, we have added Apache's Hadoop DFS and Apache Kafka in our architecture in order to increase scalability and to be able to process real-time data streams, respectively.

The project has been developed in Python. The libraries used are: numpy, pandas, scikit-learn, pySpark and softimpute. The technologies we used are Apache Spark, HDFS and Kafka.

b. Data

Our data is formed of two datasets: Firme.csv and FirmeInInsolventa.csv and have been forwarded to us for this study by prof. Bogdan Ichim. Both datasets contain raw economic KPIs for romanian companies. Given that the current study occurs during the Covid-19 pandemic, the results cannot be applied to companies in the current economic setting, but may offer insight on the economy before Covid-19 and may be useful in the future, after the pandemic goes away.

Firme.csv contains 115 features collected over 5 years, labeled t0 to t4, thus 23 features per year per company.

FirmeInInsolventa.csv contains 92 features collected over 4 years - labeled t1 to t4 - and for companies that have declared insolvency.

In total there are a bit over 170 000 samples on both datasets.

As the data received is raw, data cleaning and feature engineering are mandatory for the models to provide accurate information. This will be discussed in the **Preprocessing** section.

c. Goal

We are challenged with a classification problem. We ought to build and train our models on both Firme.csv and FirmeInInsolventa.csv by using the data for years t1-t4 and apply our predictors on the t0-t3 data on Firme.csv.

Our goal for this project was to provide an accurate classifier by testing both the sklearn and Spark MLlib option, while also tackling the big data aspect by using appropriate technologies like HDFS and extending our application's use cases to real-time data flows with Kafka.

Preprocessing

The first step in our preprocessing pipeline was to prepare our data for the imputation phase.

We replaced all "-" values - which signify a missing element - with numpy.nan, so that our imputation techniques can properly detect the NaN values. We also decided to deal with categorical values via mode imputation and to map all non-numeric columns to integers.

d. Splitting

The data underwent a 60-30-10 train-validation-test split.

In this scenario, the test data represents the values on which our models are supposed to be called on (see section b. Data). However, since none of the companies in Firme.csv have declared insolvency, we have a unique label for all samples in the test set. That is why we decided to create a validation set, containing both types of labels, which can give us a better understanding of our models' predictive power.

e. Dropping features with high NaN count

We decided on removing all features whose NaN percentage exceeded a 50% threshold. Our reasoning is that those features will fail to provide enough useful information for both the imputation and the prediction phases. In fact, regarding imputation the lack of information in this case would not only bring little to no useful data to our imputation methods, but it would damage the results of those which are more complex than simple mean or median NaN replacement.

This is why all those features represented in the table to the right right have been removed from the dataset.

Note that this image illustrates NaN counts for the training set. However, it is illustrative for both the validation and test sets, whose NaN counts we haven't uploaded due to them being highly similar to the train set.

column_name	percent_missing
t1_cheltuieli_in_avant	71.034694
t1_venituri_in_avans	86.172054
t1_provizioane	92.442501
t1_tip_bilant	95.847310
t2_cheltuieli_in_avant	69.982856
t2_venituri_in_avans	85.631227
t2_provizioane	91.864404
t2_tip_bilant	95.371084
t3_cheltuieli_in_avant	70.732394
t3_venituri_in_avans	85.929386
t3_provizioane	92.076428
t3_tip_bilant	94.860901
t4_cheltuieli_in_avant	72.165213
t4_venituri_in_avans	86.683065
t4_provizioane	92.377072
t4_tip_bilant	94.359828

f. Missing data imputation

Please note that the imputation methods were applied separately on our three datasets and thus provide pristing real-life-like data (by which we mean that those values from the train set do not interfere in the test set and vice versa).

In total, we have produced 18 imputed datasets, 3 per imputation method.

i. Mean and median

Following this simple approach, we replaced all missing data in our train, validation and test sets with the mean or the median.

These are used relatively frequently and they can provide a good benchmark for the other imputation methods.

ii. K-Nearest Neighbours

This approach is based on Beretta and Santaniello's insight on the matter of nearest neighbour imputation. In their paper, the authors suggest that kNN gives an adequate trade-off between the precision of imputation and the ability to preserve the nature of the data when the maximum percentage of missing values lies between 15% and 30%. Furthermore, they note that a value of k=3 has given the best results in respect to the precision-preservation trade-off mentioned above.

Since our own data rarely presented features that had an above-10% NaN count, we decided to use the same approach as Beretta and Santaniello suggest in their paper. That is, set k to 3.

iii. Softimpute

The softimputation method offered by the fancyimpute Python library is inherited from the R package with the same name.

Softimpute is an iterative method for matrix completion that uses nuclear-norm regularization. That being said, for this method to converge, a preliminary normalization of the data via fancyimpute's BiScaler procedure. One downside of bi-scaling is that it is not guaranteed to converge. However, it works well in practice.

Note that if we apply bi-scaling to our data, there is no way of re-scaling our data back to its original space. Moreover, it makes no sense to apply standard scaling or to normalize a second time.

g. Standardization and normalization

We applied both standardization and normalization to each of our imputed datasets, apart from the softimputed one, as it was already normalized via the bi-scaling

procedure. The reason why we chose to do both types of data transformations is the uncertainty regarding the data's distribution, so we planned on trying both approaches.

h. Feature engineering

As we have previously specified, our data contains raw features. This being the case, we ought to process them and generate new features based on the ones.

Our main source of inspiration for calculating financial KPIs based on our data was Wikipedia: https://en.wikipedia.org/wiki/Financial ratio.

The new features that have been added to the dataset in this phase are as follows: gross margin, profit margin, total assets, return on assets, return on net assets, debt ratio, current liquidity, immediate liquidity and asset turnover.

As a final step, we have removed those features used in computing the new features since they will only be increasing our data's dimensionality and therefore increasing our models' training time and lowering their accuracy. The dropped features are: cifra_de_afaceri_neta, profit_brut, profit_net, active_circulante, datorii, capital_social, stocuri and venituri_total.

Algorithms used

Scikit-Learn was a pioneer on this front. It provides an interface with which users can chain together their operations into a pipeline, where all preprocessing, feature creation, and feature indexing is done in stages. The pipeline can feed directly into a model, creating a unified workflow for both feature preprocessing and modeling. Scikit-Learn also provides users with a set of pre-baked preprocessing steps that are commonly used in machine learning pipelines, but also allows you to define your own steps for custom data transformations. Spark ML also uses the standard that Scikit-Learn pioneered, with the difference that its transformers do not modify data in place, they append a new column.

We started modelling by creating a parameter grid - a dictionary of lists - on which the best parameters will be searched on. We have then fed this list to the RandomisedSearchCV procedure, with 10 iterations and negative mean squared error as scoring metric. Other parameters that we have chosen are the number of concurrent workers, 100, so the search completes relatively fast, and the level of verbosity, 10, in order to trace back any error that might come up.

Another important parameter for the RandomisedSearchCV is the cross-validation option, for which I have employed the K-Fold algorithm with 10 folds. Using K-Fold helps reduce both underfitting, since the whole initial training set is used for training, and overfitting, since the whole training set is used for testing. Our choice of K is based on James' and Witten's proposal that the value of K should be either 5 or 10, since these values lead to a healthy bias-variance trade-off.

We chose the randomized grid search over its exhaustive counterpart because, even though the latter yearns the best set of parameters, the search space scales exponentially with more parameters or more choices for parameters adding to the grid.

Please note that only the sklearn algorithms underwent a hyperparameter search phase, as the MLlib does not offer any option to do that.

a. Modelling with Scikit-Learn

ii. SVM

SVM (Support Vector Machines) is a supervised model that analyzes the data through classification or regression. Support vector machine algorithms search a hyperplane in an N-dimensional space, where N is the number of features, that distinctly classifies the data points. For data that has just 2 features, the hyperplane will be a line and for 3 features, the hyperplane will be a two-dimensional plane. If the number of features is greater than 3, it becomes hard to imagine how the hyperplane looks. Data points on either side of the hyperplane can be attributed to different classes. SVM algorithm uses a regularization parameter (lambda) that serves as a degree of importance that is given to miss-classifications. This parameter helps maximizing the margin between both classes and minimizing the amount of miss-classifications.

In this project, the SVM algorithm was used for classification and for obtaining the best parameters for this dataset, it was used in RandomizedSearch.

The accuracies using SVM from Scikit-Learn, are between 80.3% and 97.1% (obtained with mean and soft normalization).

We didn't plot the ROC/AUC curve because it took too much time.

SVM confusion matrix figure.

iii. KNN

KNN (K-Nearest Neighbors) is a method used for classification and regression that uses for prediction the k closest training examples in the feature space. When it is used for classification, the output is the label of the majority in the group of k nearest neighbours, and when it is used for regression, the output is the average of this group of k values. To find the best number k of neighbours, it was used again in the Randomized Search, and we obtained the number 96.

The accuracies using KNN from Scikit-Learn, are between 82.6% and 96.8% (obtained with mean and knn normalization).

KNN confusion matrix figure.
KNN ROC/AUC plot figure.

iv. Random Forest

Random Forest algorithm, when it is used for classification, it is based on many classification trees. Every classification tree predicts a class for every point in the array

of data based on the features and then the forest predicts the classes with the most votes from the trees.

We found the best parameters with Random Searched as being: the number of trees: 1450, the maximum depth: 460 and the function that measures the quality of a split: Gini (Gini measures the probability of a point to be wrongly classified).

The accuracies using the Random Forest classifier from Scikit-Learn, are between 89.1% and 96.4% (obtained with median and soft normalization).

Random Forest confusion matrix figure.

Random Forest ROC/AUC plot figure.

v. XGBoost

XGBoost is basically an acronym which stands for 'eXtreme Gradient Boosting'. In order to use the XGBoost algorithm in our project, we used a library which is now part of sk-learn. The principle behind this library is that it uses gradient boosting to create an ensemble of 'weak' trees whose prediction scores are then summed up in order to get a final classification result. The tree ensemble model consists of a set of classification and regression trees (CART). As per the official documentation, XGBoost creates the same kind of model as the one in random forest, with the only difference being in the way the models are trained.

The 'boosting' part is a reference to the fact that the method uses lots of 'weak' learners by giving higher weights to the trees with bigger errors, in order to focus on those in the future iterations. The idea behind this is that the cases with bigger errors are the edge cases or the problem. The 'gradient' part refers to the gradient descent method used here, as well as in neural networks, to minimize the difference between the expected result and the actual obtained result, from one iteration to another. That's how the algorithm knows how to modify the parameters of the trees at training time in order to obtain a model that best fits the data.

One thing worth mentioning is that XGBoost is really, really fast, unlike SVM, for example. The library was built from the beginning as very efficient and its creators had this desiderate in mind, to make it highly computationally effective. This proved very useful in this project because we had limited resources and time to actually run the algorithms, because we needed our computers for work.

As specified before, we used RandomizedSearch in order to find the best model for our problem. We chose the parameters used in the RandomizedSearch from the official documentation found here.

The results using boosted trees were very good, taking into consideration the time it took to train and test the model. All imputation methods had a percentage over 90% (with the highest being 98.2%, when the data was imputed using soft_norm), with the exception of the data imputed with KNN, which had a disappointing accuracy of just 25%.

XGBoost confusion matrix figure. XGBoost ROC/AUC plot figure.

vi. Neural Network

The last method we used from the scikit-learning package was one based on neural networks. We used MLPClassifier, which stands for Multi Layer Perceptron Classifier. We chose a neural network with one hidden layer consisting of 30 neurons and with *tanh* as activation function and Limited Memory BFGS optimization algorithm. We chose this optimization algorithm for speed reasons, considering our limited home-resources.

The results seem to be the poorest of all of the algorithms presented in this section, with an accuracy between 74.9% and 79.4%. This suggests that the neural network was too simple for the complexity of the data, and that a more complex network should be used. However, we settled for this network because we wanted to see how a very simple model will perform on this rather complex dataset. Taking into consideration the really fast training time, we consider that this model is a good starting point and benchmark for the other models we analyzed as part of this assignment. This model can be thought of as being a prototype model.

Neural Network confusion matrix figure.

Neural Network ROC/AUC plot figure.

Model	Best accuracy score	Best imputation method
XGBoost	98.2 %	Soft normalized
SVM	97.1 %	Soft normalized
KNN	96.8 %	KNN normalized
Random Forest	96.4 %	Soft normalized
Neural Network	79.4 %	Soft normalized

i. Modelling with Spark MLlib

Spark uses DataFrame which is a Dataset organized into name columns. This concept is equivalent to a table in a relational database or a data frame in R/Python, but with significant optimizations under the hood. They can be constructed from sources like: structured data files, tables in Hive, external databases or existing RDDs.

We can think of a Spark DataFrame as a table distributed across a cluster and has functionality that is similar to dataframes in R and Pandas. For distributed

computation using PySpark, we will have to perform operations on Spark dataframes, not usual Python data types. For ease of use, Pyspark provides a way to convert a Pandas dataframe into a Spark one and the other way around.

One of the key differences between Pandas and Spark dataframes is eager versus lazy execution. In PySpark, operations are delayed until a result is actually needed in the pipeline. For example, you can specify operations for loading a data set from S3 and applying a number of transformations to the dataframe, but these operations won't immediately be applied. Instead, a graph of transformations is recorded, and once the data is actually needed, for example when writing the results back to S3, then the transformations are applied as a single pipeline operation. This approach is used to avoid pulling the full data frame into memory and enables more effective processing across a cluster of machines. With Pandas dataframes, everything is pulled into memory, and every Pandas operation is immediately applied.

In general, it's a best practice to avoid eager operations in Spark if possible, since it limits how much of your pipeline can be effectively distributed.

Spark SQL is a Spark module for structured data processing. Unlike the basic Spark RDD API, the interfaces provided by Spark SQL provide Spark with more information about the structure of both the data and the computation being performed. Internally, Spark SQL uses this extra information to perform extra optimizations. There are several ways to interact with Spark SQL including SQL and the Dataset API. Spark SQL operations are very similar to the regular SQL instructions. We can select columns, filter the data or use aggregate functions.

i. LinearSVC

Should Spark ML and Sklearn behave the same? Yes. They are the same model and algorithm. They do provide slightly different APIs, especially in terms of default algorithm parameters, so comparing them is a delicate subject.

The models are essentially the same: linear model using hinge loss, supporting L1 and/or L2 regularization. MLlib provides a binary classifier in LinearSVC. To get a multiclass version, you can use OneVsRest with LinearSVC as the base estimator. sklearn takes the same approach, except that it automatically calls OneVsRest under the hood.

Several parameters a bit different as well:

- convergence tolerance and maxIter. They can be sensitive to scaling/preprocessing of data, so it can be good to tune them for each use of LinearSVC.
- regParam (MLlib) and C (sklearn): they are (scaled) inverses of each other. MLlib
 uses regParam to scale the penalty (regularization) term, whereas sklearn uses
 C to scale the loss (error) term. I.e., use a small regParam or big C to reduce
 regularization strength; use a big regParam or small C to increase regularization.
 These are (scaled) inverses of each other. The easiest way to get the best
 results for each implementation is to tune each separately.

 dual (sklearn param for solving the dual or not): This defaults to True; set this to False to match MLlib

Linear SVC confusion matrix figure.

ii. Logistic Regression

Logistic regression is the appropriate regression analysis to conduct when the dependent variable is dichotomous (binary). It is the simplest and most extensively used statistical technique for predictive modelling analysis. Logistic regression is used to describe data and to explain the relationship between one dependent binary variable and one or more nominal, ordinal, interval or ratio-level independent variables.

Logistic regression confusion matrix figure.

Logistic regression ROC/AUC plot figure.

iii. Random Forest

Random Forests are algorithms for learning ensembles of decision trees, in parallel.

They can be less prone to overfitting, meaning that the greater the number of trees we use, the smaller likelihood of overfitting. Also, Random Forests can be easier to tune, considering the fact that the performance improves monotonically with the number of trees.

Random forest confusion matrix figure.

Random forest ROC/AUC plot figure.

iv. Boosted Trees Classifier

Gradient-Boosted Trees are ensembles of decision trees. The idea behind them is to iteratively train decision trees in order to minimize a loss function. Just like decision trees, gradient-boosted trees handle categorical features, extend to the multiclass classification setting and there is no need for feature scaling because they are able to capture non-linearities and feature interactions.

The main difference between them and random forests is that GBT's train one tree at a time, therefore they can take longer time to train. This happens because the process of boosting takes the residuals of each tree and trains the new tree using them. Because of this, training smaller trees using GBT rather than large trees like in Random forests is quite reasonable

Boosted trees confusion matrix figure.

Boosted trees ROC/AUC plot figure.

v. Neural Network

Multilayer perceptron classifier (MLPC) is a classifier based on the feedforward artificial neural network. MLPC consists of multiple layers of nodes. Each layer is fully connected to the next layer in the network. Nodes in the input layer represent the input data. All other nodes map inputs to outputs by a linear combination of the inputs with the node's weights w and bias b and applying an activation function. A feedforward neural network is an artificial neural network where connections between the nodes do not form a cycle.

Each layer has sigmoid activation function and the output one has softmax. Number of inputs has to be equal to the size of feature vectors. Number of outputs has to be equal to the total number of labels.

We used one hidden layer with 30 neurons.

Neural network confusion matrix figure.

Neural network ROC/AUC plot figure.

vi. Decision Trees

The decision tree is one of the most powerful and popular tools for classification and prediction. Each node represents a test on an attribute and each branch is an outcome of the test and each leaf node holds a class label. Its learning process is called recursive partitioning and the idea behind it is to split the source set into subsets based on an attribute value test. This is repeated on each derived subset. This whole process is completed when the subsets of the nodes have the value of the target variable, when splitting no longer adds value to the predictions.

Advantages:

- decision trees are able to generate understandable rules
- support for both continuous and categorical variables
- the usage of a white box model
- they can handle high dimensional data

Disadvantages:

- they are prone to errors in classification when using a small number of training examples
- high computational price to train
- they are unstable, therefore a small change in the data can cause a significant change in its structure
- relatively inaccurate. A solution to this is using a random forest of decision trees, but it would be far more complicated to interpret.

<u>Decision trees confusion matrix figure.</u>
<u>Decision trees ROC/AUC plot figure.</u>

Model	Best accuracy score	Best imputation method	
Gradient Boosted Trees	95.36%	Soft normalized	
Decision Trees	95.34%	Mean normalized	
Random Forest	95.08%	Soft normalized	
Neural Network	85.58%	Mean scaled	
Logistic Regression	82.43%	Mean normalized	
Linear SVC	77.62%	Mean scaled	

Data Engineering

Apache Hadoop

Hadoop is the most used system for big data applications. Its key features are: open source, fast, low-cost, fault tolerant and configurable. They help with large-scale, parallel and distributed data processing.

The architecture of Hadoop revolves around two major components: distributed computing, which is handled by HDFS, and parallel processing, which is handled by MapReduce. We can say that Hadoop is a combination of these two.

The open source Hadoop is maintained by the Apache Software Foundation, and can be deployed in 3 separate modes:

- Standalone, for simple analysis or debugging
- Pseudo distributed, for simulation of multi-node installations on a single node. Each of the workers run in a separate JVM.
- Distributed, cluster with multiple worker nodes

HDFS

Hadoop Distributed File System is the default storage filesystem in Hadoop, which is distributed, considerably simple in design and extremely scalable, flexible, and with high fault tolerance capability. HDFS architecture has a master-slave pattern due to which the slave nodes can be better managed and utilized. HDFS is designed to be best suited for MapReduce programming.

Main features of HDFS

- Scalability: scalable to petabytes (1 million GBs) and flexible to add or remove nodes
- Reliability and fault tolerance: HDFS replicates the data by storing it in multiple nodes, so if some nodes are down, data can be accessed from other available nodes.
- Data coherency: HDFS uses the Write Once, Read Many model
- Hardware failure recovery
- Portability
- Computation closer to odata: HDFS moves the computation process toward data, which is faster than pulling data out for computation

Architecture

HDFS is managed by daemon processes, from which we mention:

NameNode

- The master process daemon server that coordinates all the operations related to storage in Hadoop, including read and writes in HDFS.
- Manages the filesystem namespace, by holding the metadata above all the file blocks, and in which all nodes of data blocks are present in the cluster.
- Does not store data. Instead, it caches data and stores metadata in RAM for faster access, so it requires a system with high RAM.

DataNode

- Holds the actual data in HDFS and is responsible for creating, deleting and replicating data blocks, as assigned by NameNode.
- Sends messages to NameNode, which are called as heartbeat in a periodic interval. If a DataNode fails to send the heartbeat message, then NameNode will mark it as a dead node.
- If the file data present in the DataNode becomes less than the replication factor, then NameNode replicates the file data to other DataNodes.

Data storage in HDFS

In HDFS, files are divided in blocks, which are stored in multiple DataNodes, and their metadata is stored in NameNode. Blocks have a configurable size, with the default of 128 MBytes in newer versions of Hadoop. Block size is high to minimize the cost of disk seek rate, leverage transfer rate and reduce the metadata size in NameNode for a file.

Each file divided into blocks is stored in multiple DataNodes, and the number of replication factors can be configured. The default value is 3. The higher the number of the replication factor, the system will be highly fault tolerant and will occupy that many numbers of time the file is saved, and also increase the metadata in NameNode. This value should be balanced.

HDFS commands

The Hadoop command line environment is Linux-like. The Hadoop filesystem provides various shell commands to perform operations like copying files and viewing contents of folders.

The syntax of Hadoop filesystem shell commands is: hadoop fs <args>

- 1. Creating a folder: hadoop fs -mkdir <paths>
- 2. Listing contents of a folder: hadoop fs -ls <args>
- Adding data to HDFS from local computer: hadoop fs -put <local_src> <hdfs dest path>
- 4. Downloading data from HDFS to local computer: hadoop fs -get <hdfs src> <local dest path>
- 5. Viewing content of a file: hadoop fs -cat <path filename>

Sample HDFS put command and its result:

```
(base) florin@DESKTOP-J2079BR:~/hadoop-3.1.3$ bin/hadoop fs -put ~/datasets/*.csv /user/florin/datasets
```

```
(base) florin@DESKTOP-J2079BR:~/hadoop-3.1.3$ bin/hadoop fs -ls /user/florin/datasets
Found 23 items
-rw-r--r-- 1 florin supergroup
                                 13472257 2020-05-20 07:55 /user/florin/datasets/x_test_knn_normalized_fe.csv
-rw-r--r--
            1 florin supergroup
                                 16012150 2020-05-20 07:55 /user/florin/datasets/x test knn scaled fe.csv
                                 13751790 2020-05-20 07:55 /user/florin/datasets/x test mean normalized fe.csv
-rw-r--r-- 1 florin supergroup
                                 15286519 2020-05-20 07:55 /user/florin/datasets/x test mean scaled fe.csv
-rw-r--r-- 1 florin supergroup
                                 13751790 2020-05-20 07:55 /user/florin/datasets/x test median normalized fe.csv
-rw-r--r-- 1 florin supergroup
-rw-r--r-- 1 florin supergroup 15980571 2020-05-20 07:55 /user/florin/datasets/x test median scaled fe.csv
-rw-r--r-- 1 florin supergroup 159682787 2020-05-20 07:55 /user/florin/datasets/x_train_knn_normalized_fe.csv
-rw-r--r-- 1 florin supergroup 196702265 2020-05-20 07:55 /user/florin/datasets/x_train_knn_scaled_fe.csv
-rw-r--r-- 1 florin supergroup 171716560 2020-05-20 07:55 /user/florin/datasets/x_train_mean_normalized_fe.csv
-rw-r--r- 1 florin supergroup 187253042 2020-05-20 07:55 /user/florin/datasets/x_train_mean_scaled_fe.csv
-rw-r--r- 1 florin supergroup 166019235 2020-05-20 07:55 /user/florin/datasets/x_train_median_normalized_fe.csv
-rw-r--r-- 1 florin supergroup 196686854 2020-05-20 07:55 /user/florin/datasets/x_train_median_scaled_fe.csv
-rw-r--r- 1 florin supergroup 63824245 2020-05-20 07:55 /user/florin/datasets/x_val_knn_normalized_fe.csv
-rw-r--r-- 1 florin supergroup 78729587 2020-05-20 07:55 /user/florin/datasets/x_val_knn_scaled_fe.csv
-rw-r--r- 1 florin supergroup 68642065 2020-05-20 07:55 /user/florin/datasets/x_val_mean_normalized_fe.csv
-rw-r--r- 1 florin supergroup 74106283 2020-05-20 07:55 /user/florin/datasets/x_val_mean_scaled_fe.csv
                                 68642065 2020-05-20 07:55 /user/florin/datasets/x_val_median_normalized_fe.csv
           1 florin supergroup
-rw-r--r--
           1 florin supergroup 74106283 2020-05-20 07:55 /user/florin/datasets/x_val_median_scaled_fe.csv
           1 florin supergroup 42412105 2020-05-20 07:55 /user/florin/datasets/x_val_norm_soft_fe.csv
           1 florin supergroup
                                40011 2020-05-20 07:55 /user/florin/datasets/y_test.csv
           1 florin supergroup
                                   482966 2020-05-20 07:55 /user/florin/datasets/y_train.csv
                                   192982 2020-05-20 07:55 /user/florin/datasets/y_val.csv
-rw-r--r--
           1 florin supergroup
-rw-r--r-- 1 florin supergroup
                                   192786 2020-05-20 07:55 /user/florin/datasets/y_val_norm_soft_fe.csv
```

MapReduce

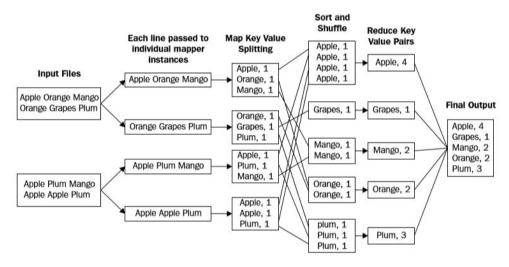
MapReduce is a massive parallel processing framework that processes faster, scalable and fault tolerant data in a distributed environment. It can process a large volume of data in parallel, by dividing a task into independent sub-tasks and also has a master-slave architecture.

Input, output and intermediary results in a MapReduce job are in the form of <Key, Value> pair. Key and Value have to be serializable.

MapReduce architecture

Uses the following two daemon processes:

JobTracker



- Master coordinator daemon process, responsible for coordinating and completing a MapReduce job in Hadoop.
- Primary functions of JobTracker are resource management, tracking resource availability and task process cycle.
- It identifies the TaskTracker to perform certain tasks and monitors the progress and status of a task.

TaskTracker

- Is the slave daemon process that performs a task assigned by JobTracker.
- Sends heartbeat messages to JobTracker periodically to notify about the free slots and sends the status to JobStracker about the task, and checks if any task has to be performed.

The principle of MapReduce can be seen in this example, in which we want to count the number of words of a file divided into blocks.

Spark

Apache Spark Streaming

Stream data processing is used when dynamic data is generated continuously, and it is often found in big data use cases. In most instances data is processed in near-real time, one record at a time, and the insights derived from the data are also

used to provide alerts, render dashboards, and feed machine learning models that can react quickly to new trends within the data.



Spark streaming is based on the idea of discretized streams (DStreams). Each discretized stream is represented as a sequence of RDD. Since the alpha version of Spark (0.7.0) there have been many improvements undergoing because it's a very low-level API.



As a solution to the challenges, Spark Structured Streaming was introduced in Spark 2.0 (and became stable in 2.2) as an extension built on top of Spark SQL. Because of that, it takes advantage of Spark SQL code and memory optimizations. Structured Streaming also gives very powerful abstractions like Dataset/DataFrame APIs as well as SQL. No more dealing with RDD directly.

Both Structured Streaming and Streaming with DStreams use micro-batching(streaming's receivers accept data in parallel and buffer it in the memory of Spark's workers nodes). The biggest difference is latency and message delivery guarantees: Structured Streaming offers exactly-once delivery with 100+ milliseconds latency, whereas the Streaming with DStreams approach only guarantees at-least-once delivery, but can provide millisecond latencies. Unlike the traditional continuous operator model, where the computation is statically allocated to a node, Spark tasks are assigned dynamically to the workers based on the locality of the data and available resources.

Basic streaming demo

```
PythonRDD[139] at RDD at PythonRDD.scala:53
['123.csv']
<class 'list'>
             features|label|
                                rawPrediction|
                                                       probability|prediction|
|[-0.0096628482841...|
                                [814.0,868.0] | [0.48394768133174... |
                                                                           1.0|
|[-0.0117515564284...|
                          1|[29079.0,3935.0]|[0.88080814200036...|
                                                                           0.0|
|[-0.0083500679534...|
                          0|[29079.0,3935.0]|[0.88080814200036...|
                                                                           0.0|
|[-0.0113456992045...|
                          0|[29079.0,3935.0]|[0.88080814200036...|
                                                                           0.0|
|[-0.0106453505542...|
                          0| [360.0,7580.0]|[0.04534005037783...|
                                                                           1.0|
only showing top 5 rows
Test Error = 0.166852
```

Data frame created after parsing the .csv file and making predictions using DecisionTreeClassifier which had been already trained.

Results comparison

Sklearn

We can say that we solved this binary classification problem using the sklearn framework for machine learning because we can see that most of the results obtained using the algorithms presented above are over 90%.

Another indicator that the problem is solved can be deducted from the confusion matrices in the annexes below and from the roc curves. In the majority of cases, the main diagonal of the confusion matrix (containing the true positives and the true negatives) has higher numbers than the secondary diagonal. This means that our model correctly predicts most of the examples. This fact is true for the ROC curves as well, where we can see that the curves are over the main diagonal of the plot in most of the cases.

There are 2 notable outliers, the boosting tree method on knn-based imputations, which have a very low accuracy (23% and 24%), which are way lower than the third lowest-scoring algorithm - neural network with mean_norm, which has an accuracy of 74,9%.

Despite the 2 outliers, the boosting tree method has the highest accuracy of all the tests when used with the soft-norm imputed dataset - **98.2%**.

We can see that the soft_norm imputation strategy works best on this dataset. As it can be seen in the chapter below, the KNN-based imputation strategies give the poorest results. This might be due to the fact that, given the computational demands of KNN imputation, neither our own machines, nor Google Colab could apply KNN imputation on the whole train test in a single run. We were thus forced to split the train set into approximately 30 000-sample subsets, run the imputation on those and then concatenate them.

As for the prediction algorithms, the neural network returns the worst results. This can be explained by the fact that we considered the neural network as a prototyping model, and as a starting point and benchmark for the other algorithms. The methods working with trees (XGBoost and Random Forest) give the best results.

						-	
(5)) (2)	Name	Strategy	Accuracy	Precision	Recall	F Score	Predicted Insolvency
0	SVM	median_norm	93.758939	0.980803	0.769832	0.862606	26.160
1	knn	median_norm	93.273914	0.973974	0.755905	0.851195	5.840
2	nn	median_norm	77.655716	0.796751	0.163789	0.271720	0.930
3	svm	knn_scaled	93.302933	0.948271	0.779361	0.855559	20.950
4	knn	knn_scaled	88.324179	0.939426	0.578514	0.716064	6.700
5	nn	knn_scaled	75.825474	0.677643	0.095537	0.167464	2.950
6	random_forest	knn_scaled	95.153902	0.956885	0.847777	0.899033	100.000
7	random_forest	median_norm	95.448233	0.960618	0.856247	0.905435	1.210
8	SVM	knn_normalized	96.387190	0.978298	0.877504	0.925164	44.330
9	knn	knn_normalized	96.805887	0.988801	0.884509	0.933752	4.740
10	nn	knn_normalized	76.283553	0.843750	0.083564	0.152068	0.500
11	SVM	mean_scaled	91.240543	0.940481	0.700114	0.802689	23.900
12	knn	mean_scaled	86.556120	0.945676	0.500489	0.654559	9.760
13	nn	mean_scaled	75.294849	0.543139	0.184069	0.274956	5.460
14	random_forest	knn_normalized	96.308426	0.973222	0.879133	0.923788	99.890
15	svm	tibi_mean	85.940759	0.804979	0.485303	0.605540	0.000
16	svm	tibi_median	80.350438	0.791594	0.258877	0.390160	0.000
17	knn	tibi_mean	84.814351	0.813350	0.411507	0.546512	0.580
18	nn	tibi_mean	87.623418	0.765941	0.638524	0.696453	53.557
19	knn	tibi_median	82.644973	0.808168	0.373998	0.511355	0.043
20	nn	tibi_median	84.856070	0.769042	0.537801	0.632963	13.076
21	random_forest	tibi_median	89.180921	0.881102	0.640893	0.742042	24.632
22	random_forest	tibi_mean	90.960923	0.882353	0.684803	0.771127	99.892
23	svm	mean_norm	96.573738	0.987520	0.876446	0.928673	28.830
24	knn	mean_norm	96.492901	0.993382	0.867975	0.926454	6.590
25	nn	mean_norm	74.998445	0.805085	0.023212	0.045123	0.240
26	random_forest	mean_norm	95.512488	0.975906	0.844519	0.905471	1.010
27	SVM	soft_norm	97.128392	0.998347	0.888380	0.940159	5.010
28	knn	soft_norm	92.200598	0.970376	0.714659	0.823114	2.270
29	nn	soft_norm	79.429828	0.691433	0.342948	0.458488	6.030
30	random_forest	soft_norm	96.454063	0.973980	0.883968	0.926794	100.000
31	random_forest	mean_scaled	95.879366	0.960939	0.873595	0.915188	4.010
32	SVM	median_scaled	89.524303	0.928979	0.637074	0.755822	19.750
33	knn	median_scaled	86.112551	0.942277	0.483955	0.639475	6.770
34	nn	median_scaled	79.405120	0.739077	0.294836	0.421518	2.380
35	random_forest	median_scaled	94.842989	0.940119	0.851604	0.893675	12.060
36	boosting_tree	tibi_mean	90.653562	0.881522	0.693540	0.776313	7.122
37	boosting_tree	tibi_median	89.919309	0.858933	0.686813	0.763290	1.481
38	boosting_tree	knn_scaled	23.992124	0.241226	0.925965	0.382743	99.700
39	boosting_tree	knn_normalized	24.636750	0.241137	0.913504	0.381555	99.660
40	boosting_tree	median_scaled	93.188931	0.866960	0.865125	0.866042	89.660
41	boosting_tree	median_norm	95.052337	0.904805	0.900309	0.902552	1.880
40	Barrier Land		OF 03376F	0 000007	0.073676	0.044337	00 200

mean_norm 96.368536 0.986594 0.869115 0.924136

0.958967 0.873676 0.914337

0.990432 0.938879 0.963967

89.380

1.520

100.000

42 boosting_tree

43 boosting_tree

44 boosting_tree

mean scaled 95.833765

soft norm 98.217694

Spark

This binary classification problem has been successfully learned by machine learning models using big data tools like Spark.

As it can be seen from the results tables and figures, the **best models** are the ones **based on trees**, with GBT and Decision trees obtaining the **highest** accuracies, followed up by Random forests. The largest validation accuracy is **95%** using **GBT** with **soft normalized** imputation. On the other hand, the **worst** performing models are **Linear Support Vector Classifier** and **Logistic Regression**, due to the high number of parameters involved. With the same imputation method, **soft normalized**, the Logistic regression model obtained an accuracy of **49%**.

As for the **imputation strategy**, the ones based on **mean and median** with **standardization and normalization**, along with **soft imputation** have obtained the **best** results, while those based on **KNN did not perform** as well as expected. A GBT model using soft normalized imputation obtained an accuracy of **95%**, while one using KNN imputation obtained only **33%** accuracy.

Ideally, the **confusion matrix** should have **sum on the principal diagonal equal to 1** (if normalized) and 0 on the secondary diagonal. The models used in the project achieved good results, obtaining **larger sums on the principal diagonal** for most of the experiments. Because our dataset is not balanced and there are more examples of firms which did not go into insolvency, most of the confusion matrices have a really large percentage of true negatives.

The **ROC curves** tell us how good the model is for discriminating positive and negative examples. If the **curve is above the diagonal of the plot**, then the model does a good job with this separation. In the figures obtained by our models we can see some examples of ROC curves which are high above the diagonal line, such as the ones obtained by Gradient Boosted Trees.

When it comes to differences compared to using plain Sklearn, one major one which is in favor of Spark approach is **scalability**, as the code would be able to run on separate machines and be faster to train. Another difference which comes as a drawback is the fact that PySpark API does not allow the same level of model configurations as the one from Sklearn. That's why the best result achieved on Sklearn (98.22% validation accuracy on GBT with soft imputation) is higher than the best on Spark.

	Name	Strategy	Val_Accuracy	Test_Accuracy	Precision	Recall	Sensitivity (TPR)	Specificity (TNR)	F Score
0	linear_svc	tibi_mean	0.776204	0.59285	0.801187	0.065013	0.065013	0.995036	0.120267
1	logistic_regression	tibi_mean	0.789093	0.67117	0.792261	0.140501	0.140501	0.988664	0.238675
2	neural_network	tibi_mean	0.865836	0.59369	0.763897	0.622080	0.622080	0.940839	0.685733
3	<pre>gradient_boosted_trees</pre>	tibi_mean	0.890057	0.00191	0.871661	0.624729	0.624729	0.971697	0.727821
4	random_forest	tibi_mean	0.876289	0.00001	0.887773	0.542861	0.542861	0.978884	0.673739
5	decision_tree	tibi mean	0.879745	0.00139	0.885221	0.561763	0.561763	0.977588	0.687339
6	linear_svc	tibi median	0.774334	0.81536	0.796820	0.054324	0.054324	0.995740	0.101714
7	logistic regression	tibi median	0.783286	0.84696	0.809298	0.102746	0.102746	0.992555	0.182343
8	neural network	tibi median	0.845184	0.80350	0.740791	0.525656	0.525656	0.943440	0.614951
9	gradient boosted trees	tibi median	0.878385	0.00068	0.831926	0.605155	0.605155	0.962405	0.700648
10	random forest	tibi median	0.863768	0.99977	0.852046	0.509154	0.509154	0.972813	0.637412
11	decision tree	tibi_median	0.863371	0.00143	0.837570	0.519875	0.519875	0.968998	0.641546
12	linear svc	knn normalized fe	0.745507	1.00000	NaN	0.000000	0.000000	1.000000	NaN
13	logistic regression	knn normalized fe	0.745507	1.00000	NaN	0.000000	0.000000	1.000000	NaN
14	neural network	knn normalized fe	0.764556	0.93690	0.584732	0.258267	0.258267	0.937387	0.358285
15	gradient boosted trees	knn normalized fe	0.649497	0.00000	0.411135	0.872699	0.872699	0.573303	0.558946
16	random forest	knn normalized fe	0.624686	0.01650	0.390189	0.843460	0.843460	0.550004	
17	decision tree	knn normalized fe	0.646181	0.00000	0.407754	0.862600	0.862600		0.553749
18	linear svc	knn scaled fe	0.754109	0.95010	0.604429	0.097817	0.097817	0.978147	
19	logistic regression	knn scaled fe	0.409721	0.97760	0.276404	0.815524	0.815524	0.271193	
20	neural network	knn scaled fe	0.759146	0.98770	0.701593	0.093256	0.093256	0.986460	
21	gradient boosted trees	knn scaled fe	0.330936	0.00000	0.274372	0.990471	0.990471	0.105791	
22	random forest	knn scaled fe	0.272277	0.32830	0.242981	0.878971	0.878971	0.065171	
23	decision tree	knn scaled fe	0.686434	0.00000	0.438694	0.830510	0.830510		0.574123
24	linear svc	mean normalized fe	0.590072	0.75170	0.366628	0.839469	0.839469	0.504935	
25	logistic_regression	mean normalized fe	0.824376	0.34570	0.818623	0.398110	0.398110	0.969889	
26	neural network	mean normalized fe	0.779563	0.90850	0.603948	0.388744	0.388744		0.473019
27	gradient boosted trees	mean normalized fe	0.951684	0.98750	0.972631	0.833605	0.833605	0.991993	
28	random forest	mean normalized fe	0.948741	0.98460	0.964648	0.828962	0.828962	0.989629	
29	decision tree	mean normalized fe	0.953467	0.98880	0.972764	0.840691	0.840691	0.991965	0.901918
30	linear_svc	mean scaled fe	0.641434	0.90200	0.303113	0.314791	0.314791	0.752940	0.308842
31	logistic regression	mean scaled fe	0.689066	0.00840	0.383861	0.366509	0.366509	0.799177	0.374984
32	neural_network	mean scaled fe	0.806902	0.89220	0.846676	0.294592	0.294592	0.981789	0.437100
33	gradient boosted trees	mean scaled fe	0.939455	0.96210	0.888806	0.871070	0.871070	0.962799	0.879849
34	random forest	mean scaled fe	0.946792	0.98170	0.923950	0.861867	0.861867	0.975783	0.891829
35	decision_tree	mean scaled fe	0.933879	0.97140	0.885542	0.850057	0.850057	0.962493	0.867437
36	linear_svc	median scaled fe	0.754938	0.95300	0.622642	0.094071	0.094071	0.980538	0.163447
37	logistic regression	median scaled fe	0.813742	0.01180	0.948013	0.283678	0.283678	0.994690	0.436685
38	neural network	median scaled fe	0.799627	0.88650	0.709383	0.360238	0.360238	0.949620	0.477826
39	gradient boosted trees	median scaled fe	0.952596	0.98030	0.955337	0.853641	0.853641	0.986376	0.901630
40	random forest	median scaled fe	0.935061	0.98290	0.945099	0.790764	0.790764	0.984319	
41	decision tree	median scaled fe	0.951083	0.98540	0.960104	0.842808	0.842808	0.988045	
42	S0000 77 - 00 -00	median normalized fe	0.489253	0.50230		0.927920	0.927920		0.480444
43		median normalized fe	0.745507	1.00000		0.000000	0.000000	1.000000	
44		median_normalized_fe	0.778796	0.96830	0.693215		0.234647		0.350615
45	gradient_boosted_trees		0.950959	0.98790		0.833360	0.833360	0.991103	
46	random forest		0.948948	0.98180	0.956299		0.837677	0.986932	
47	decision tree	median normalized fe	0.950337	0.98720		0.833360	0.833360	0.990269	
48	linear svc	norm soft fe	0.770437	0.97750	0.739007	0.148309	0.148309	0.982174	
49	logistic_regression	norm_soft_fe	0.746079	1.00000		0.000000	0.000000	1.000000	NaN
50	neural network	norm_soft_fe	0.767180	0.97620		0.147900	0.147900		0.243919
51	gradient_boosted_trees	norm_soft_fe	0.953668	0.00000	0.967917		0.845563	0.990461	
52	random forest	norm_soft_fe	0.950847	0.05410		0.835104	0.835104	0.990239	
53	decision tree	norm_soft_fe	0.951593	0.00000	0.962980		0.841723	0.988987	
80 E ()			VVIII.000000000000000000000000000000000						

Conclusions

Modelling on microeconomic data has proven an interesting and insightful task, given the demand for feature engineering and the nature of the raw features. Even though the number of predictors was not high compared to other datasets, the variance in their nature, NaN count and type definitely put us in a pinch a couple of times.

Another problem was to find a way to correctly assess the performance of our models. Training on both labels and predicting on a set with an unique label would've given partially flawed results, as we had no idea how our models behaved on the other label. We bypassed this by applying the 60-30-10 train-validation-test split, where the validation set acted as the actual test set with both labels and the test set was used to test the prediction power on an insolvency-free.

From a computational time perspective, the SKLearn models took way longer to train and use. The Random Forest model took about 4 hours to train on a machine with an 8-core CPU. The SVM took about 6 hours. However, the XGBoost algorithm was really fast, with about 30 minutes per imputation method. The same thing can be said about the neural network, but that happened because it only had one layer with 30 neurons, since it was the first model we considered and we wanted to have a fast prototype in order to have a rough idea about the dataset and the results we should expect. The RAM usage wasn't high for the SKLearn models, but the CPU was under some stress.

For the PySpark module, training all the models for one imputation method took about 20-30 minutes on a 6 core (12 threads) CPU, so it offered a considerable improvement in time over Sklearn. However, there are some drawbacks when it comes to memory consumption, because training all the algorithms on all the imputation methods in one run caused the RAM to fill up, even dumping memory to disk and blocking the computer. So, in order to avoid this, for each imputation method we had to manually start the training process for all algorithms.

It comes as no surprise that the Sklearn approach yielded better results than the Spark MLlib. The main reason for this would be that Sklearn, as a machine learning-specialized library, has had its algorithms especially designed for prediction performance.

On the other hand, Spark was built in order to fit the role of a scalable big data engineering library. Thus, it's MLlib component has only later been added and has not experienced much development. This is why it lacks Sklearn's versatility when it comes to hyperparameter tuning and cross-validation methods.

However, Spark does bear one important quality and that is scalability. As we have seen, the KNN imputation method has been too computationally exhausting for both our machines and Google Colab. In this scenario, with enough commodity hardware to run on - an AWS, Azure or GCP hardware cluster is not expensive even for a small company - Spark, in combination with KNN imputation, would've offered much better results than our KNN approach.

An industry standard is to combine the two approaches that we have presented in this report. In other words, to distribute Sklearn models on a cloud hardware cluster using Spark. This way we would get the best out of both worlds: Sklearn's predictive performance and Sparks computational optimizations.

Another expected result on the validation set is the fact that the best performing model is the gradient boosted trees algorithm. However, as the Spark results figure has shown, the random forest and gradient boosted trees perform extremely poorly, up to the point in which the boosted trees have 0% accuracy. This is an interesting result that could be used to our advantage. Given that the boosted trees algorithm always marks a company that has not declared insolvency as one that has, all we must do is to invert the labels of the algorithm's output. This way we achieve a 100% score on the boosted trees classifier.

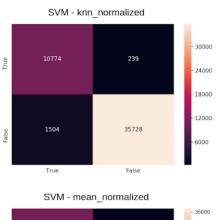
Further research

As we have discussed in the previous section, a worthwhile research direction regarding the problem of insolvency analysis would be a hybrid approach using Spark to leverage computational strain on a commodity cluster and Sklearn to assure a high performance in classification.

In this scenario, the Sklearn models would be distributed across the Spark cluster either via Spark streams or as .py files that would be run. After this, the results would be aggregated to the Spark master node and a few custom metrics would need to be designed and computed in order to obtain unflawed, correct feedback from the workers.

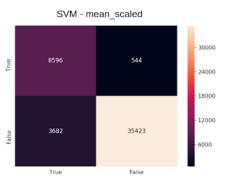
The big data technologies play a bigger role than just distributing datasets across a cluster. HDFS would be a suitable candidate here for data storage, as its size grows larger with each imputed dataset. Moreover, Spark and HDFS are optimized to work well together, as part of the same technology stack, resulting in faster computations, retrieval and storage.

Another possible improvement would be receiving feedback from an industry expert, such a financial analyst or an economist, on how to best treat our raw KPIs in the preprocessing stage, what new features to compute based on the raw ones and how to interpret them.

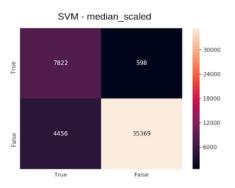








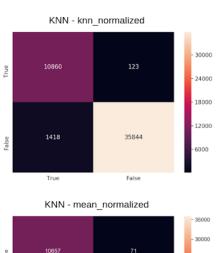


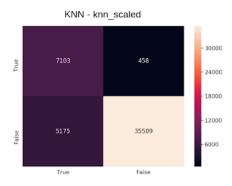


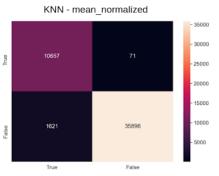


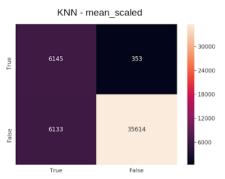


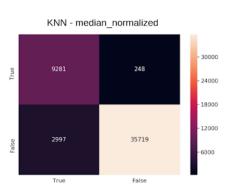


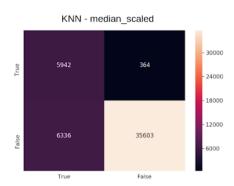


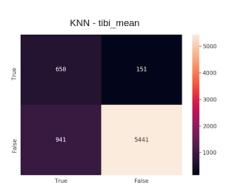


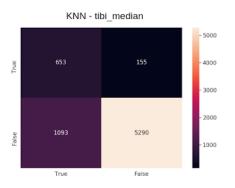




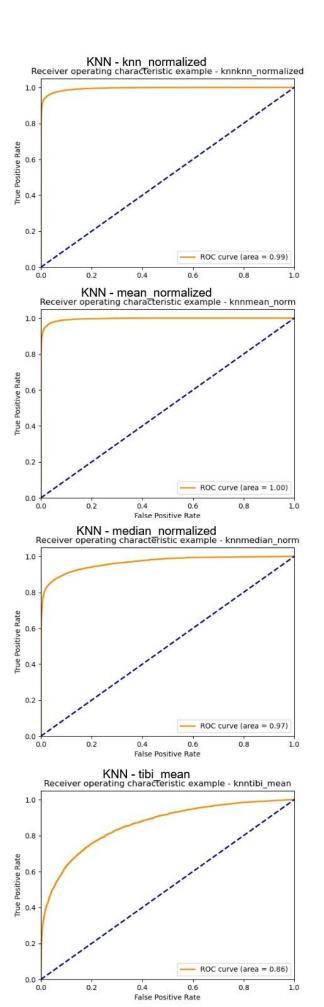


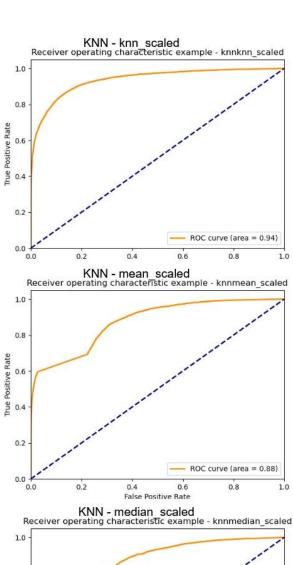


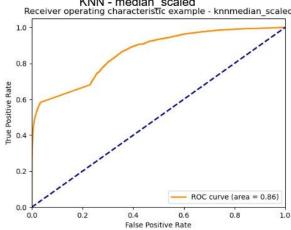


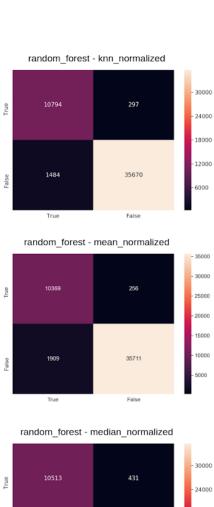


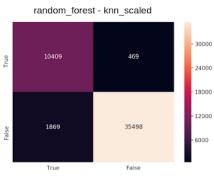


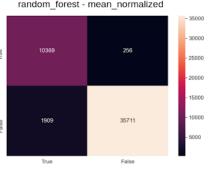


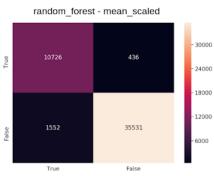


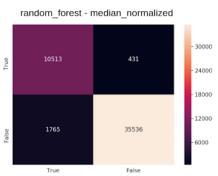


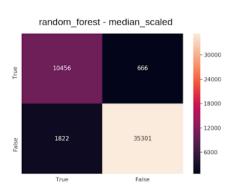


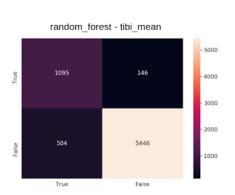


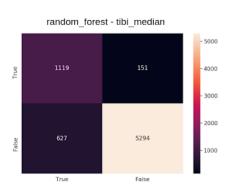


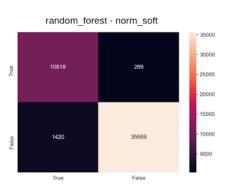


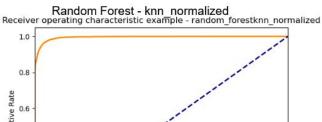


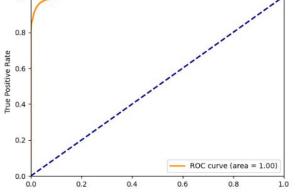


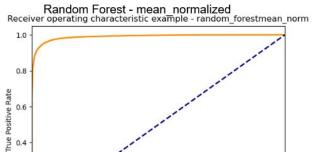








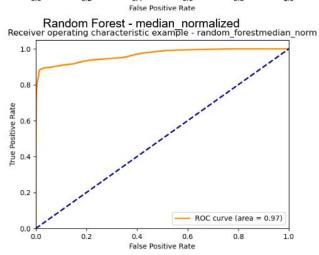




0.6

ROC curve (area = 0.99)

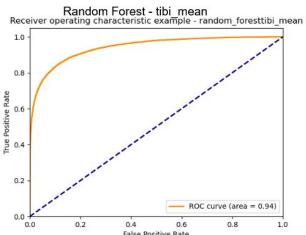
0.8

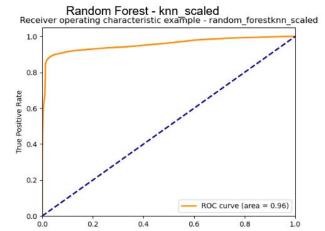


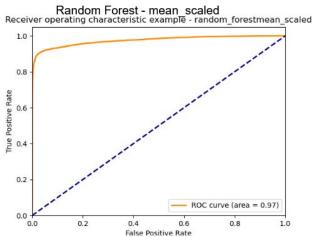
0.0

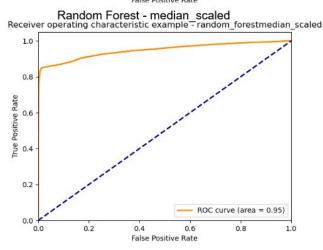
0.0

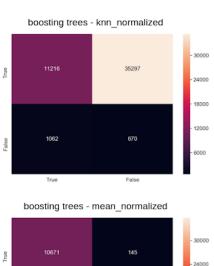
0.2

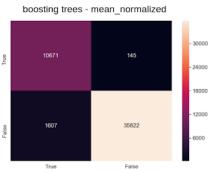


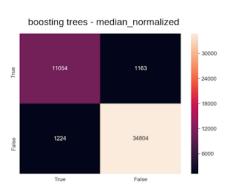


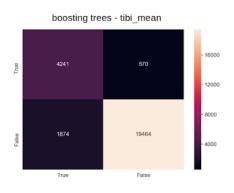




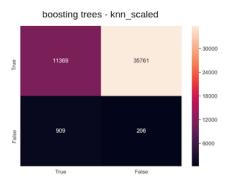


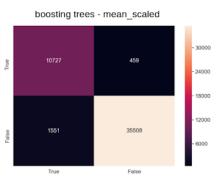


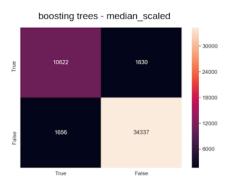


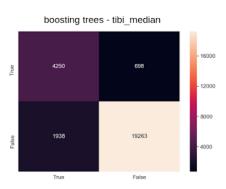


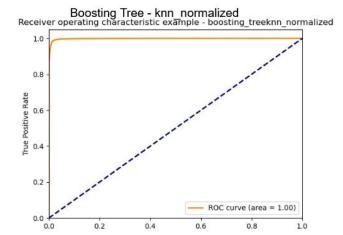


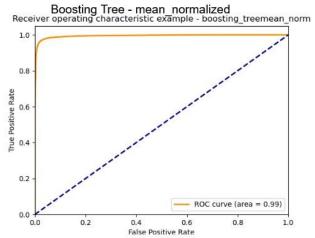


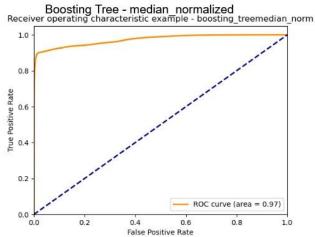


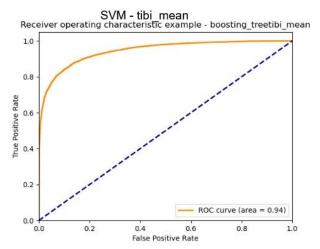


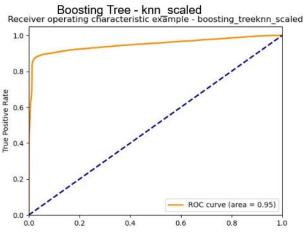


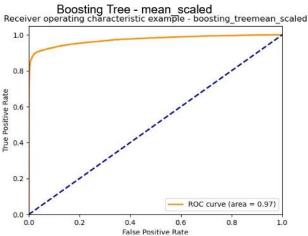


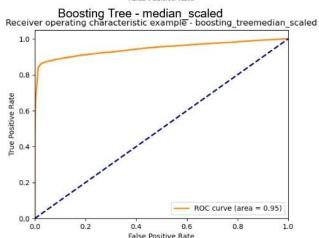


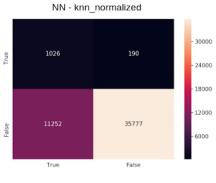


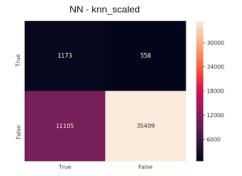


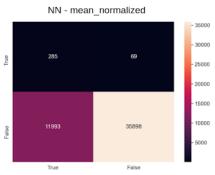


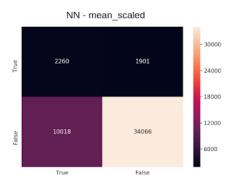


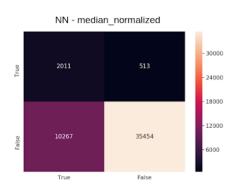


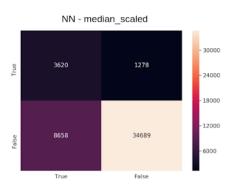


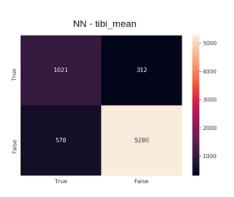


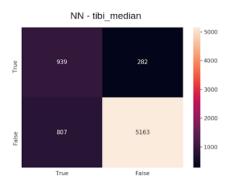


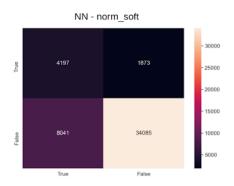


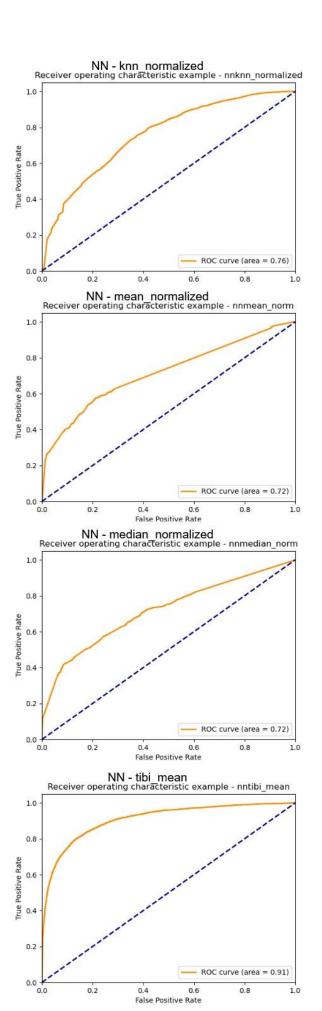


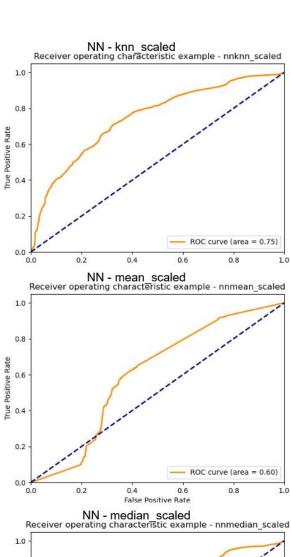


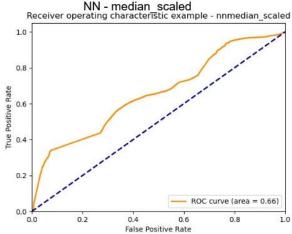


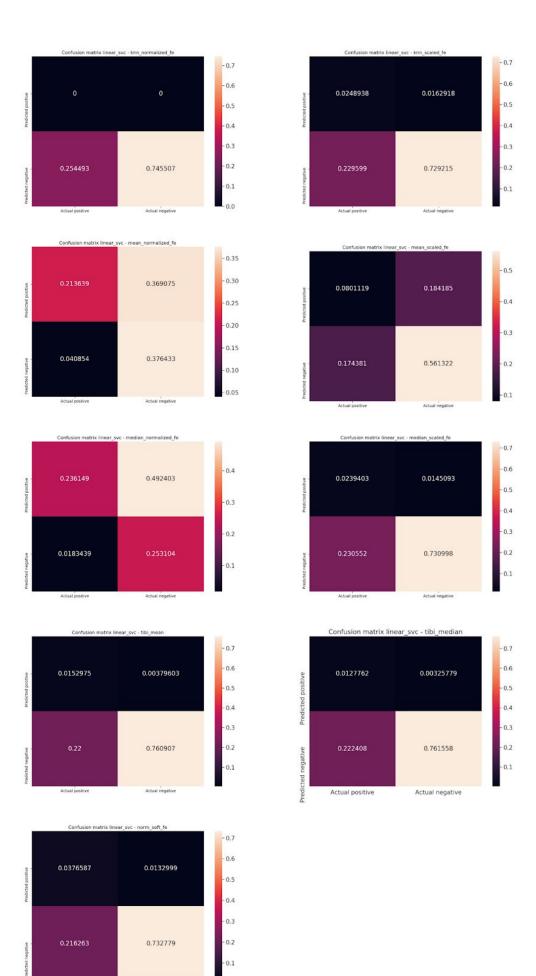


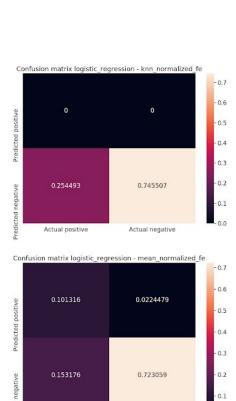


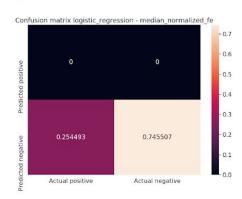






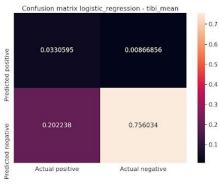


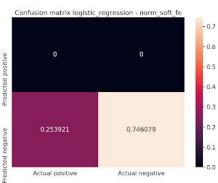


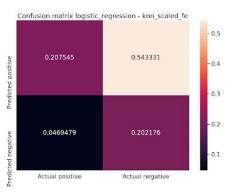


Actual negative

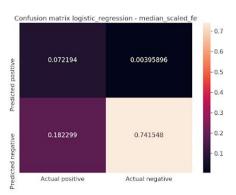
Actual positive

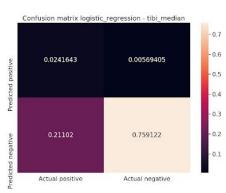


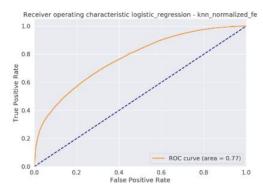


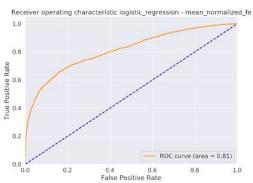


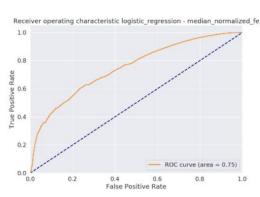


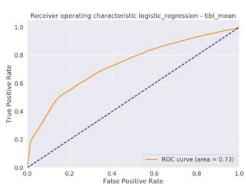


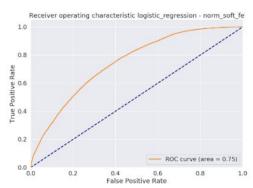


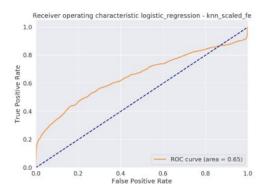




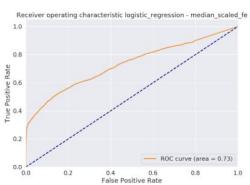


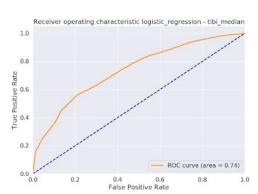


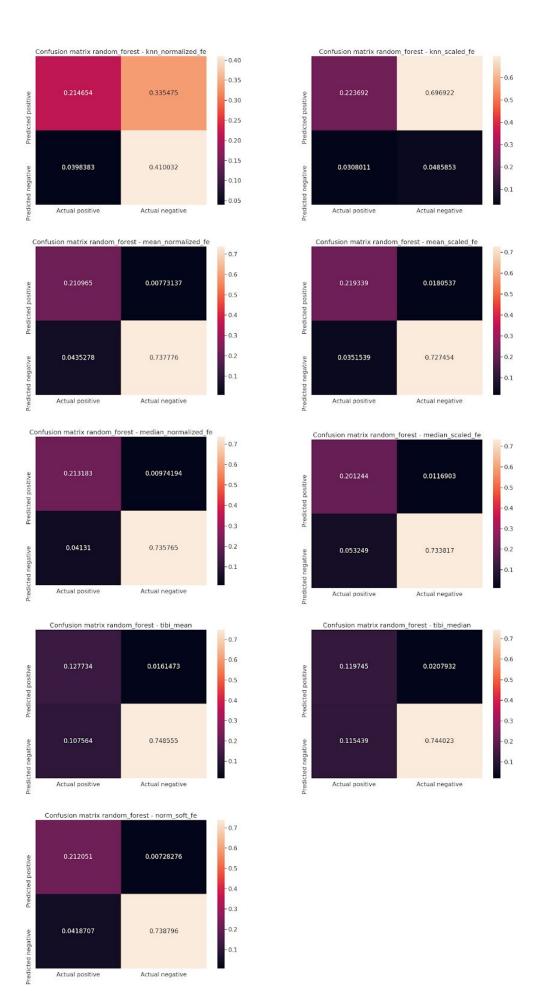


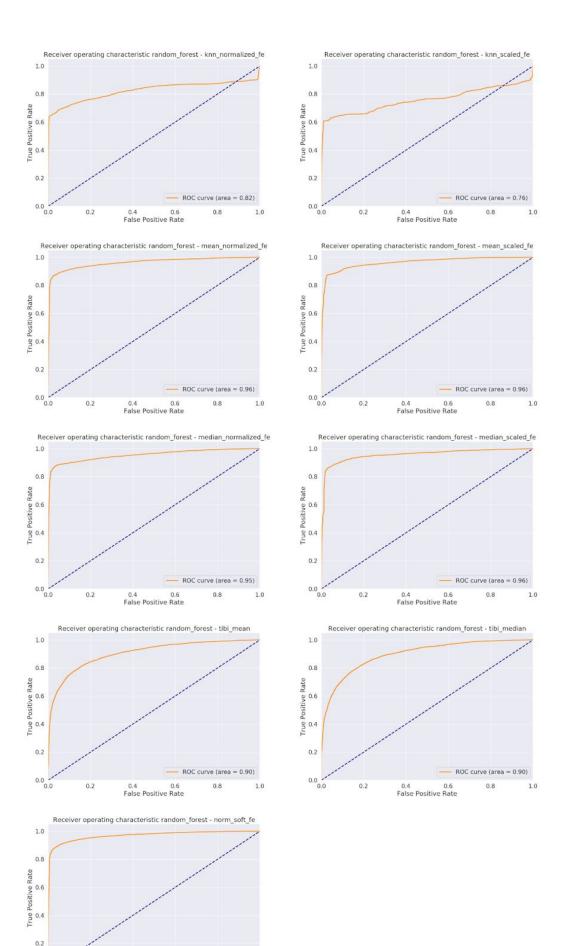












ROC curve (area = 0.97)

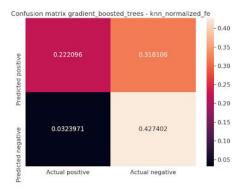
0.8

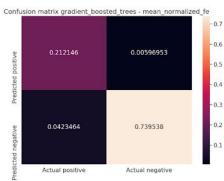
1.0

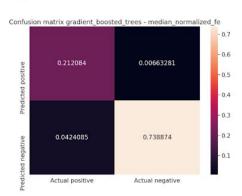
0.0

0.2

0.4 0.6 False Positive Rate

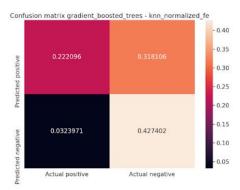


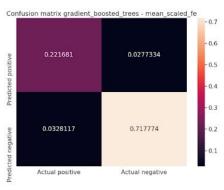


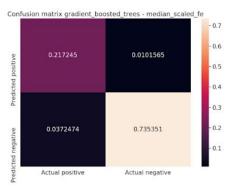


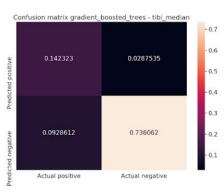


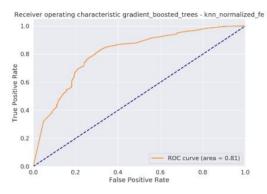


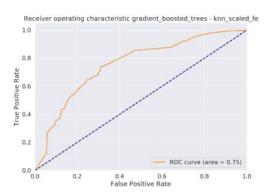


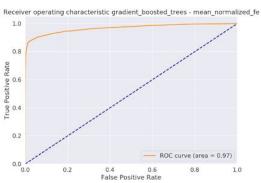


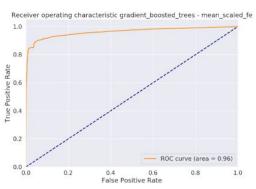


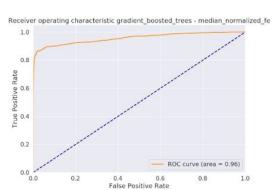


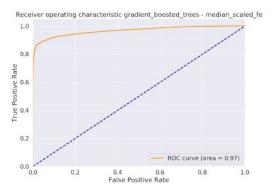


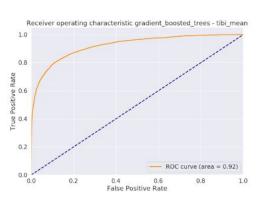


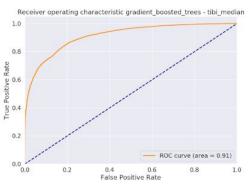


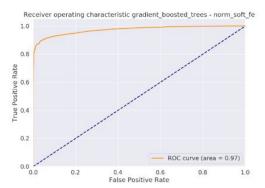


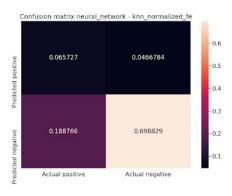


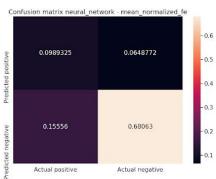


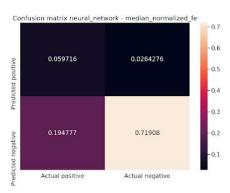


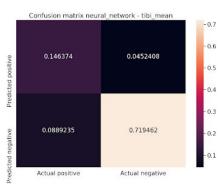


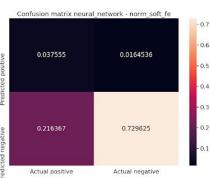


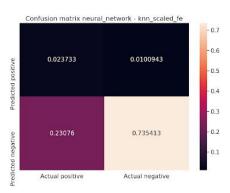


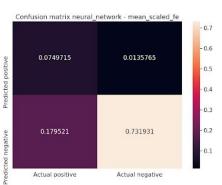


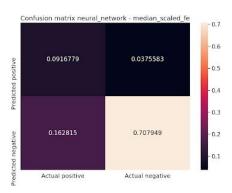


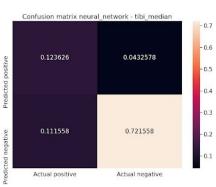


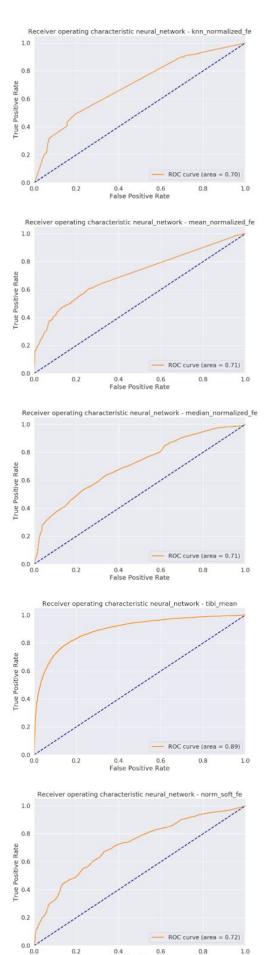












0.2

0.4 0.6 False Positive Rate

0.8

1.0

