CENTRAL EUROPEAN OLYMPIAD IN INFORMATICS



Münster, Germany July 5-12, 2003

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Input File:register.in100 PointsOutput File:register.outTime Limit: 1.5 sSource Code:register.pas/.c/.cppMemory Limit: 16 MB

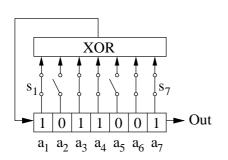
Shift Register

A register of a computer stores N bits for computation. A shift register is a special kind of register, with bit values that can be easily shifted by one position.

Using a feedback shift register, binary pseudo-random numbers can be generated in the following way: A shift register of size N is initially filled with the bit values a_1, a_2, \ldots, a_N . At each clock tick, the register outputs the value of the rightmost bit, a_N . The other bit values are shifted by one position to the right. The first position is assigned a new value a_1 as follows:

Each bit of the register is connected to an XOR gate via a switch (see figure below). For each bit i there is a switch s_i (which can be 1 or 0) that determines whether the bit value a_i is forwarded or not to the XOR gate. Let $k_i = s_i \cdot a_i$. The new value a'_1 is set to the output value of the XOR gate, $XOR(k_1, \ldots, k_N)$. (Remark: If the number of ones in k_1, \ldots, k_N is odd, the value of $XOR(k_1, \ldots, k_N)$ is 1, else 0). Below are the formal definitions:

$$\begin{array}{rcl} a_1' & = & \mathrm{XOR}(k_1, \dots, k_N) \\ a_i' & = & a_{i-1} \ \mathrm{for} \ 2 \leq i \leq N \\ \mathrm{output} & = & a_N \end{array}$$



| tick | a_1 | a_2 | a_3 | a_4 | a_5 | a_6 | a_7 | output |
|------|-------|-------|-------|-------|-------|-------|-------|--------|
| 0 | 1 | 0 | 1 | 1 | 0 | 0 | 1 | - |
| 1 | 0 | 1 | 0 | 1 | 1 | 0 | 0 | 1 |
| 2 | 1 | 0 | 1 | 0 | 1 | 1 | 0 | 0 |
| 3 | 1 | 1 | 0 | 1 | 0 | 1 | 1 | 0 |
| 4 | 0 | 1 | 1 | 0 | 1 | 0 | 1 | 1 |
| 5 | 0 | 0 | 1 | 1 | 0 | 1 | 0 | 1 |
| 6 | 1 | 0 | 0 | 1 | 1 | 0 | 1 | 0 |
| 7 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 1 |
| 8 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | 0 |
| 9 | 1 | 0 | 1 | 1 | 0 | 0 | 1 | 1 |
| 10 | 0 | 1 | 0 | 1 | 1 | 0 | 0 | 1 |
| 11 | 1 | 0 | 1 | 0 | 1 | 1 | 0 | 0 |
| 12 | 1 | 1 | 0 | 1 | 0 | 1 | 1 | 0 |
| 13 | 0 | 1 | 1 | 0 | 1 | 0 | 1 | 1 |
| 14 | 0 | 0 | 1 | 1 | 0 | 1 | 0 | 1 |

In the example above, the value a_1 at tick 1 is calculated as follows: $\mathbf{YOP}(1, 1, 0, 0, 1, 1, 1, 1, 0, 0, 1, 0, 1, 1) = 0$

 $XOR(1 \cdot 1, 0 \cdot 0, 1 \cdot 1, 1 \cdot 1, 0 \cdot 0, 1 \cdot 0, 1 \cdot 1) = 0.$

You are given the first 2N output values of such a feedback shift register. From those values, you shall try to determine the switch values s_i .

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Input

The first line of the input file register. in contains the size N of the shift register ($1 \le N \le 750$). The second line contains 2N numbers 0 or 1, which are the first 2N output bit values of the shift register.

Output

The output file register. out consists of exactly one line. If there is a switch setting that produces the given register output values, output the switch values s_i of any such switch setting, starting with s_1 . If there are no such switch settings, output the number -1 only.

Examples

| register.in | register.out |
|----------------|---------------|
| 7 | 1 0 1 1 0 1 1 |
| 10011010110011 | |

| register.in | register.out | | | |
|-------------|--------------|--|--|--|
| 3 | -1 | | | |
| 0 0 0 1 1 1 | | | | |