

Object Representation

- Implicitly $f(x,y,z)=0$ – i.e. all points in 3D space where some function is zero.
- e.g. sphere $(x^2+y^2+z^2)=r^2$
- Any guesses for?:

$$(2x^2 + y^2 + z^2 - 1)^3 - \left(\frac{1}{10}\right)x^2z^3 - y^2z^3 = 0$$

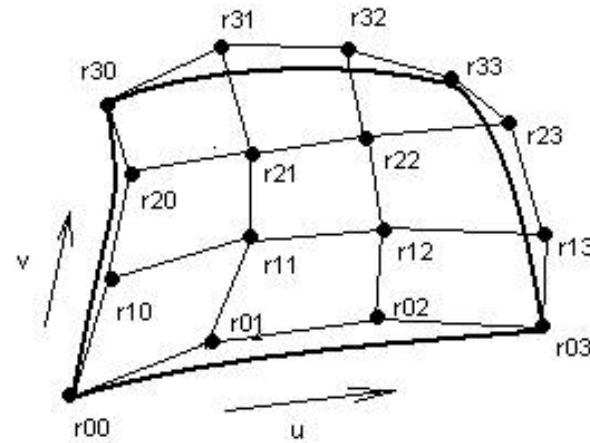
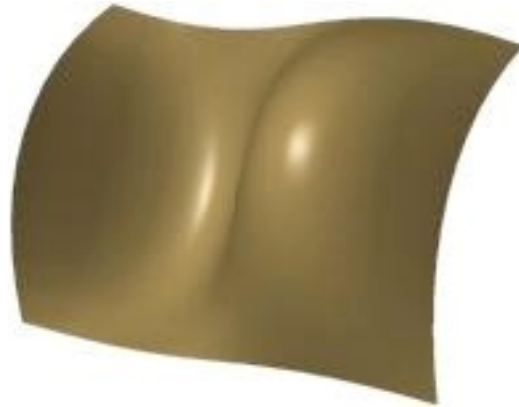
Object Representation

- **Implicitly** $f(x,y,z)=0$ – i.e. all points in 3D space where some function is zero.
- e.g. sphere $(x^2+y^2+z^2)=r^2$
- Any guesses for?:
$$(2x^2 + y^2 + z^2 - 1)^3 - \left(\frac{1}{10}\right)x^2z^3 - y^2z^3 = 0$$
- It's a cartoid (heart!)
- **Implicit:**
 - Extremely compact storage



Object Representation

- Parametrically
e.g. Bezier surface patch



- Smooth joins, very good for curved surfaces

Object Representation

- Polygon meshes (e.g. triangular mesh)
- Bruno Levy (Inria) of Michaelangelo's David

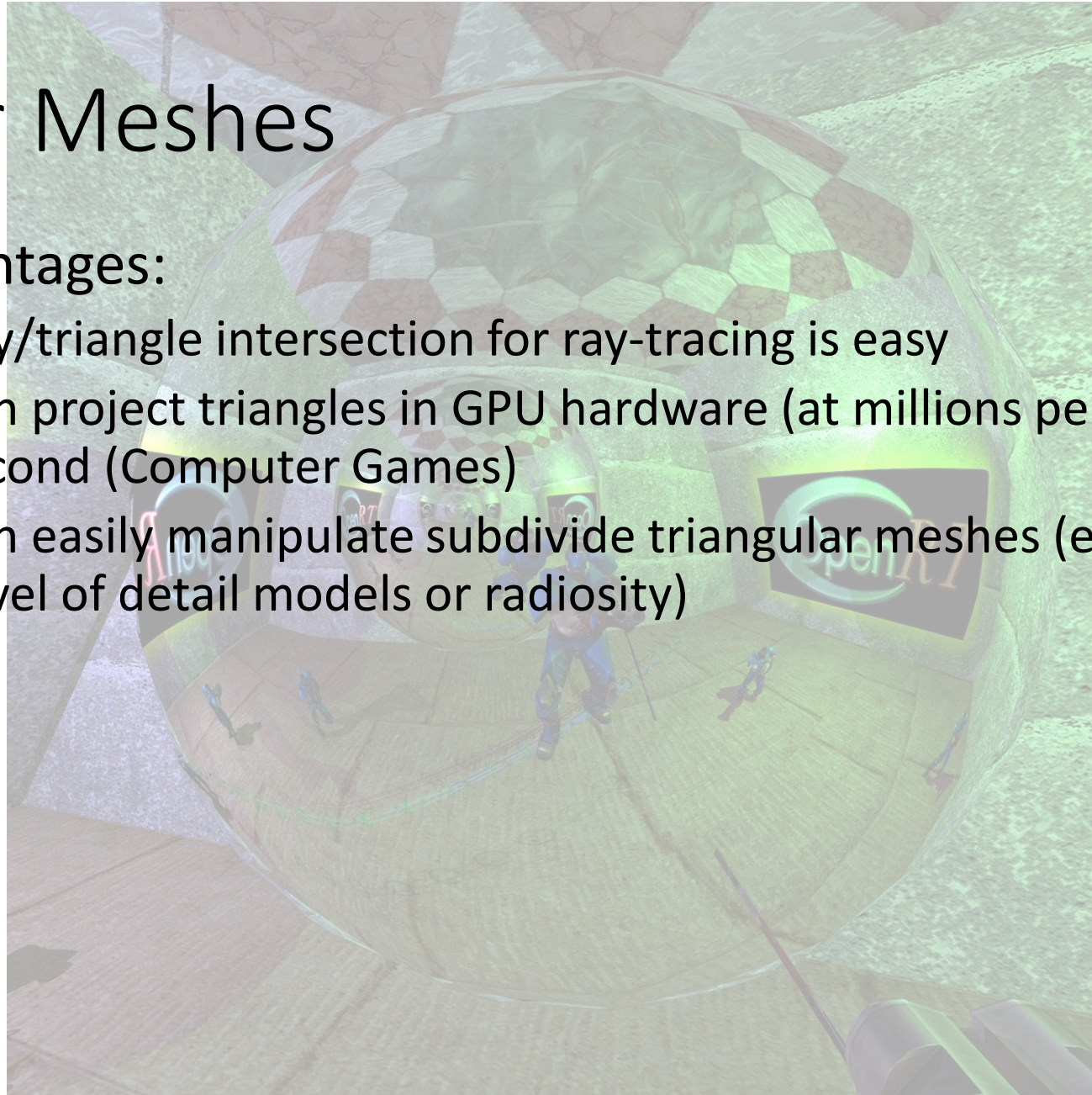


2 billion polygons, 32GB



Triangular Meshes

- Advantages:
 - Ray/triangle intersection for ray-tracing is easy
 - Can project triangles in GPU hardware (at millions per second (Computer Games))
 - Can easily manipulate subdivide triangular meshes (e.g. for Level of detail models or radiosity)



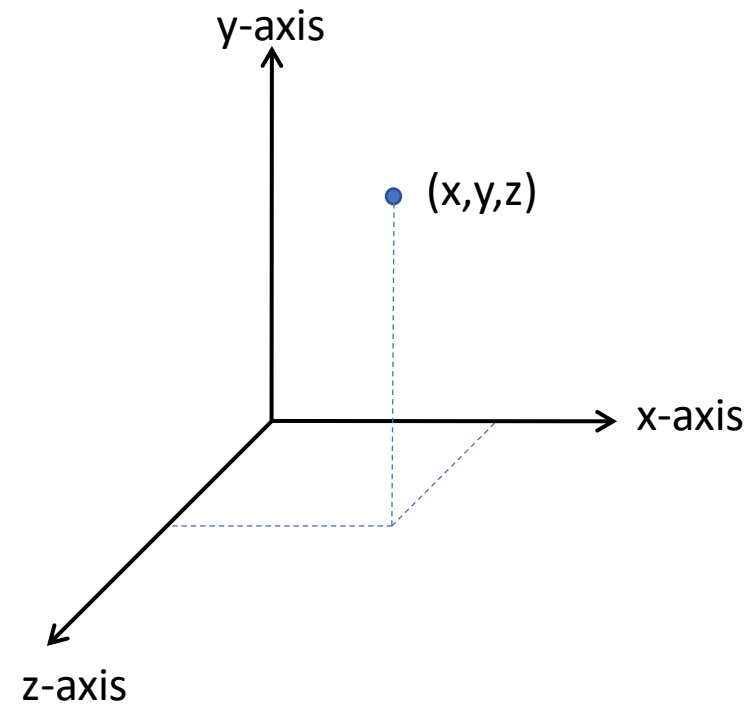
Terminology

- GPU (Graphics Processing Unit) – a chip dedicated to the processing of vertices for the purposes of display
- OpenGL – Open Graphics Language – a language for programming graphics applications. The language maps to GPU hardware and is OS independent
- Direct3D – Microsoft's graphical programming language. The language maps to GPU hardware and is OS dependent (Windows)

Modelling: 3D Primitives

- Point
- 3D location in space
- Represented by coordinates

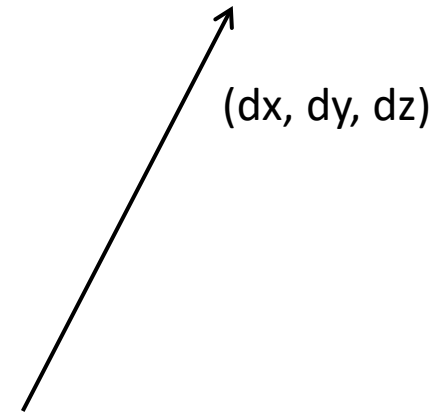
```
class Point {  
private:  
    float x, y, z;  
    ...  
};
```



Modelling: 3D Primitives

- Vector
- 3D direction and magnitude (no position)

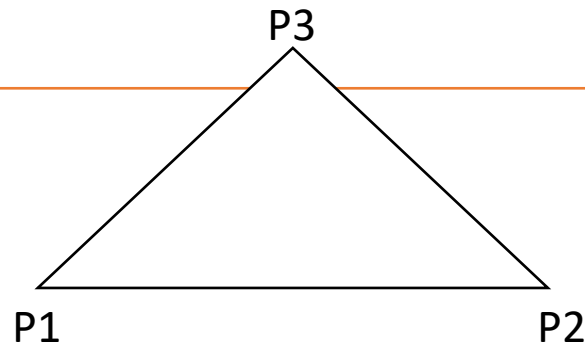
```
class Vector {  
private:  
    float dx, dy, dz;  
public:  
    float Magnitude() const {  
        return  
            sqrt(dx*dx+dy*dy+dz*dz);  
    }  
    ...  
};
```



Modelling: 3D Primitives

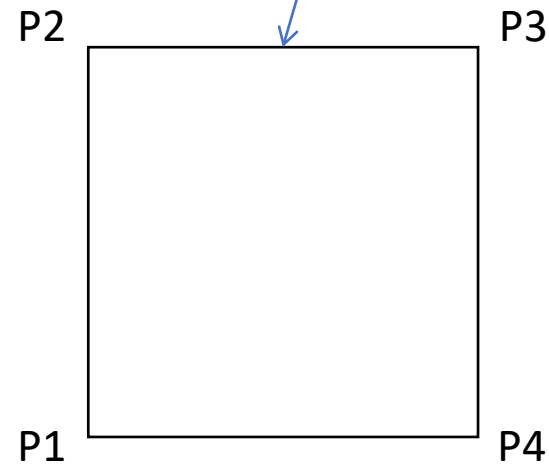
- Triangle
- These explicit representations lead to duplicated points
- This problem is examined in the next slides

```
class Triangle {  
private:  
    Point P1, P2, P3;  
    ...  
};
```



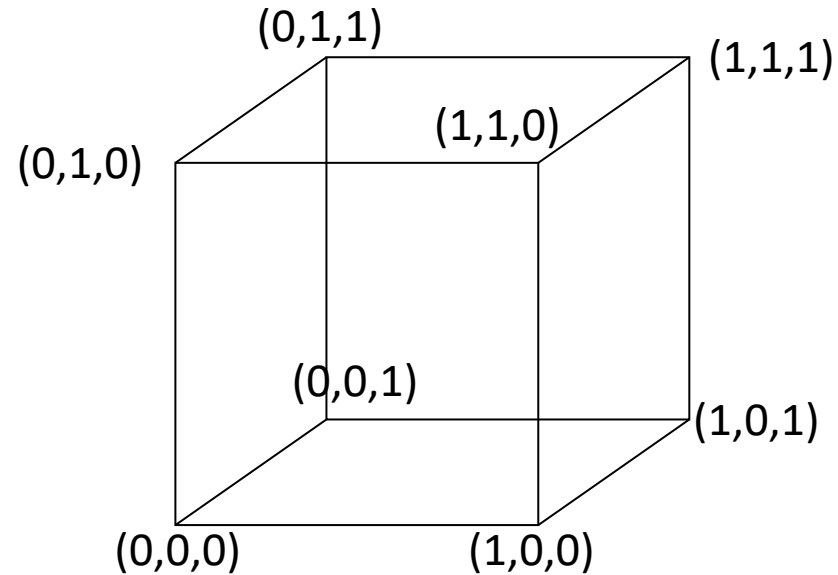
- Quad

```
class Quad{  
private:  
    Point P1, P2, P3, P4;  
    ...  
};
```



Explicit Representation

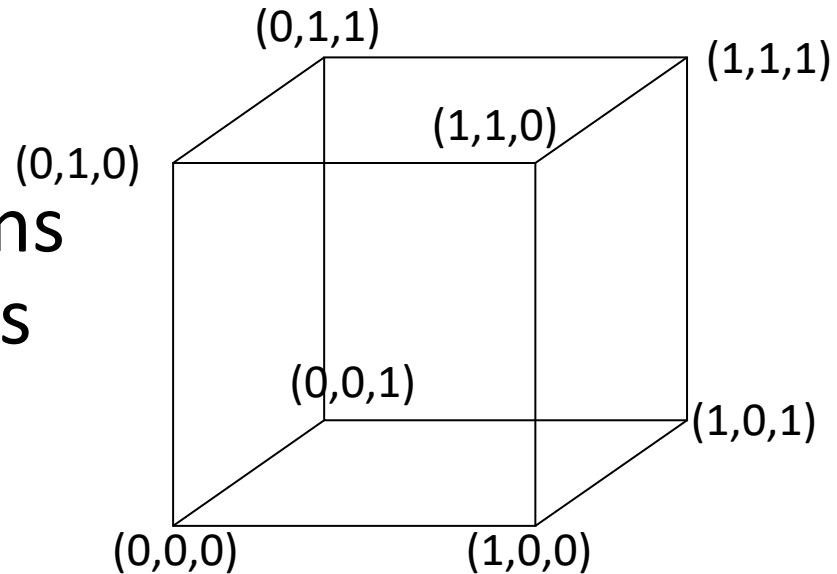
- Cube (6 faces / quads)
- (0,0,0) (0,0,1) (1,0,1) (1,0,0)
- (1,0,0) (1,1,0) (0,1,0) (0,0,0)
- (1,1,0) (1,1,1) (0,1,1) (0,1,0)
- (1,1,1) (1,0,1) (0,0,1) (0,1,1)
- (1,0,0) (1,0,1) (1,1,1) (1,1,0)
- (0,0,1) (0,0,0) (0,1,0) (0,1,1)
- Drawbacks:
- 3D transformations of 24 vertices (not 8)
- Draw 24 edges (rather than 12)
- Rounding errors – consider picking vertices



Pointers to Vertex List

- Vertices / Points
- 0=(0,0,0)
- 1=(0,0,1)
- 2=(0,1,0)
- 3=(0,1,1)
- 4=(1,0,0)
- 5=(1,0,1)
- 6=(1,1,0)
- 7=(1,1,1)

- Polygons / Quads
- 0 1 5 4
- 4 6 2 0
- 6 7 3 2
- 7 5 1 3
- 4 5 7 6
- 1 0 2 3



Advantages:

3D transformations of just 8 vertices.

Rounding errors not a problem.

Drawbacks:

Draw 24 edges (rather than 12)

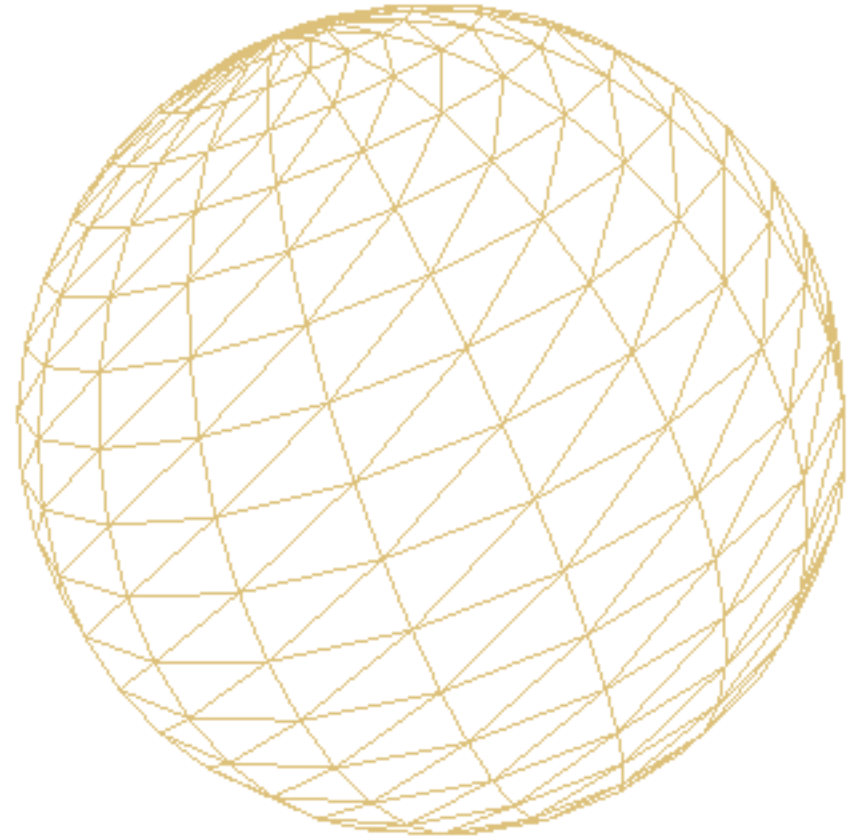
Extra memory

Extra processing during modelling

3D Primitives

- Pointers to Vertex List widely used (although see triangle strips)
- Each triangle vertex is a pointer to a 3D point
- An object is a list of triangles (or quads)

```
class Triangle {  
private:  
    Point *P1, *P2, *P3;  
    ...  
};
```

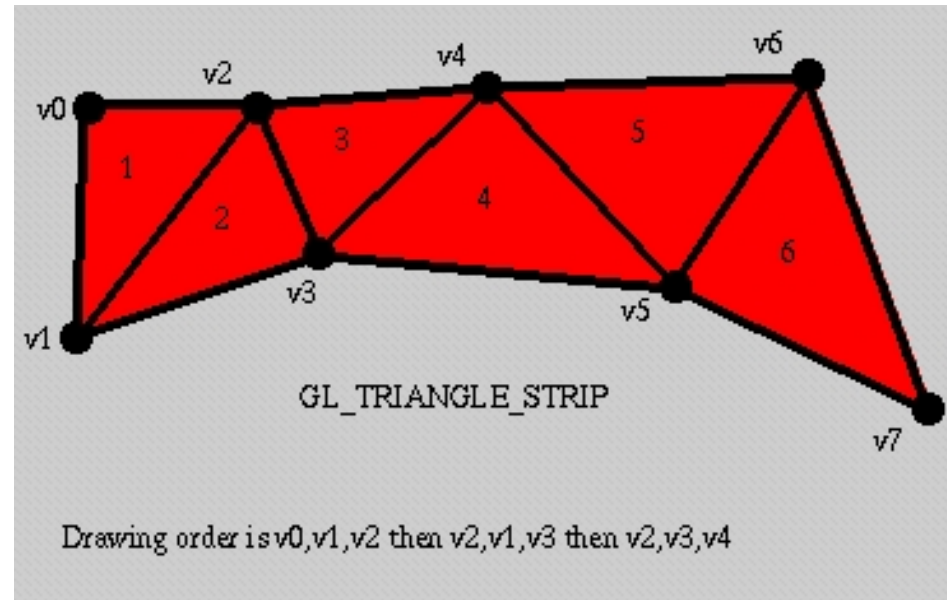


Example

- For example, the previous sphere consists of 382 vertices and 760 triangles
- Each vertex is 3 floats ($3 \times 4 \text{ bytes} = 12$)
- For explicit representation:
 - $760 \text{ triangles} \times 3 \text{ vertices each} \times 12 \text{ bytes per vertex} = 27,360 \text{ bytes}$
- For pointers to vertex list:
 - Each triangle is a list of 3 pointers ($3 \times 4 \text{ bytes} = 12$). $382 \times 12 \text{ (vertex memory)} + 760 \times 12 \text{ (pointers)} = 13,704 \text{ bytes}$
- Using (next) triangular strip model uses $762 \times 12 = 9,144 \text{ bytes}$

Triangular Strips

- Compact (n triangles represented using n+2 vertices)
- Therefore transmission to GPU is lower
- Very efficient when drawing (particularly in hardware)
- Can be hard to create triangle strips from arbitrary geometry

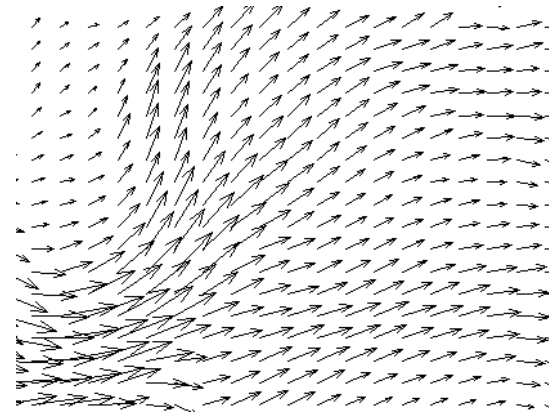
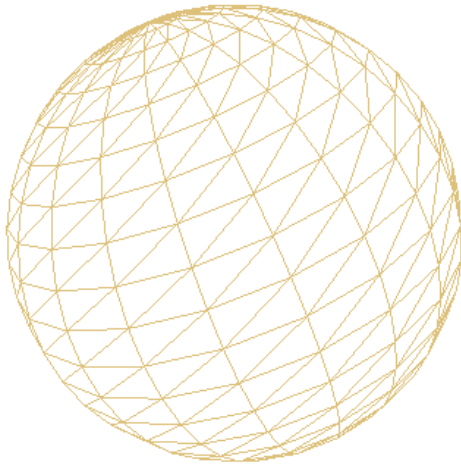
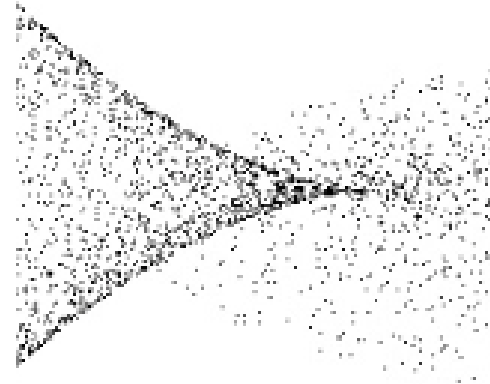
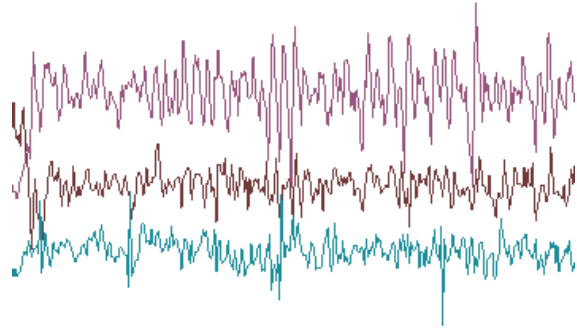


OpenGL

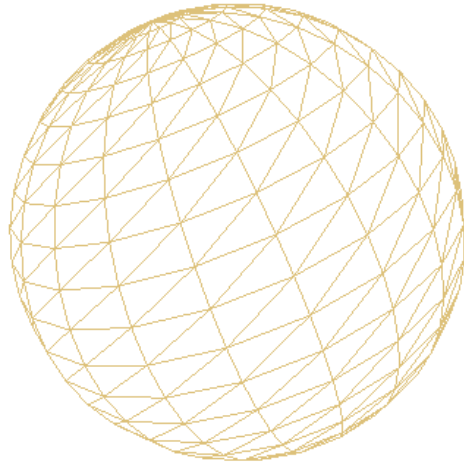
Direct3D Drawing Primitives

- D3D_POINTLIST
A list of isolated points (n vertices= n points)
- D3D_LINELIST
A list of isolated lines (each pair of points are the ends of a line) ($2n$ vertices= n lines)
- D3D_LINESTRIP
The vertices make a continuous line ($n+1$ vertices= n lines)
- D3D_TRIANGLELIST
Each group of 3 points define an isolated triangle ($3n$ vertices= n triangles)
- D3D_TRIANGLESTRIP
(Previous slide) ($n+2$ vertices= n triangles)
- (Direct3D allows pointers to a vertex list using VERTEX BUFFERS)

What shall we use?
(Answers in lecture)

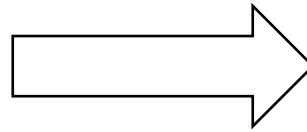


Rendering

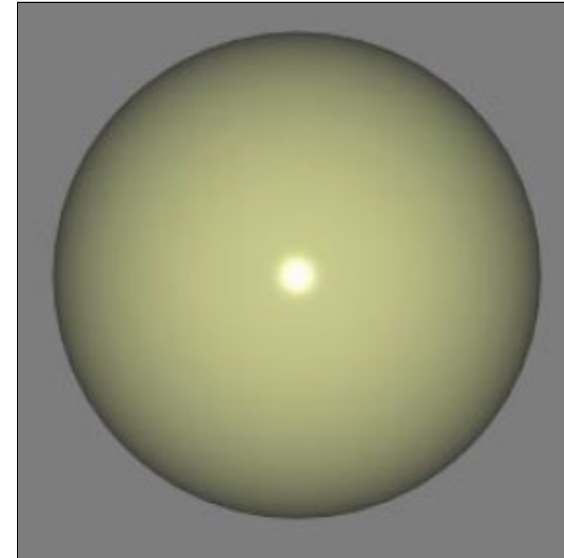


Model / scene comprised of
geometric primitives in 3D
coordinate space

Rendering



Transformation
of 3D space



Raster image