

# Knowledge Representation

## Lecture 10: Discussion Games

\*slides adapted from Martin Caminada at the Summer School for Argumentation in Cardiff

Atefeh Keshavarzi

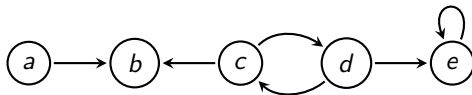
27, November 2023

# Flashback: Dung's Abstract Argumentation Frameworks

## Definition

An **argumentation framework** (AF) is a pair  $(A, R)$  where

- ▶  $A$  is a set of arguments
- ▶  $R \subseteq A \times A$  is a relation representing the conflicts (“attacks”)

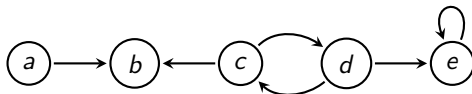


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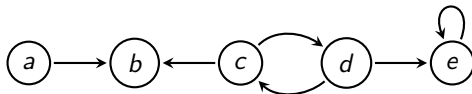


## How can we assess the credibility of an argument in an AF?

An argument is believable if it can be argued successfully against the counterarguments.

- ▶ **Semantics:** Methods used to clarify the acceptance of arguments
  - ▶ Extension-based semantics
  - ▶ Labelling-based semantics

## Flashback: Semantics of AFs



- ▶  $cf(F) = \{\{a, c\}, \{a, d\}, \{b, d\}, \{a\}, \{b\}, \{c\}, \{d\}, \{\}\}$
- ▶  $adm(F) = \{\{a, c\}, \{a, d\}, \{a\}, \{c\}, \{d\}, \{\}\}$
- ▶  $pref(F) = \{\{a, c\}, \{a, d\}\}$
- ▶  $stb(F) = \{\{a, d\}\}$
- ▶  $comp(F) = \{\{a, c\}, \{a, d\}, \{a\}\}$
- ▶  $grd(F) = \{\{a\}\}$

# Labelling-based Semantics of AFs

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- ▶ Extension-based semantics
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# Labelling-based Semantics of AFs

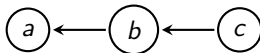
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## Definition

Given an AF  $F = (A, R)$ . A **labelling** is a **function**  $\mathbb{L} : A \rightarrow \{\text{in}, \text{out}, \text{undec}\}$

- ▶  $\mathbb{L}(a) = \text{in}$ , i.e.,  $a$  is accepted;
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- ▶  $\mathbb{L}_1(A) = \{a \mapsto \text{undec}, b \mapsto \text{undec}, c \mapsto \text{in}\}$

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- ▶  $\mathbb{L}_2(A) = \{a \mapsto \text{undec}, b \mapsto \text{out}, c \mapsto \text{in}\}$



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- ▶  $\mathbb{L}_3(A) = \{a \mapsto \text{in}, b \mapsto \text{out}, c \mapsto \text{in}\}$
- ▶ labelling-based argumentation semantics provides a way to select **reasonable** labellings among all the possible ones, according to some criterion.

# Labelling-based Semantics of AFs (ctd.)

Each argument is labelled **in**, **out** or **undec**

an argument is **in**  $\Leftrightarrow$

all its attackers are **out**

an argument is **out**  $\Leftrightarrow$

it has an attacker that is **in**

an argument is **undec**  $\Leftrightarrow$

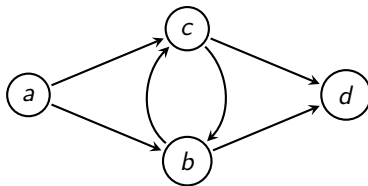
not all its attackers are **out** and it does not have an attacker that is **in**

# Applying Argument Labellings

**in**  $\Leftrightarrow$  all attackers are **out**

**out**  $\Leftrightarrow$  there is an attacker that is **in**

**undec**  $\Leftrightarrow$  not all attackers are **out**, and no attacker is **in**

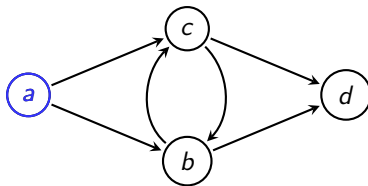


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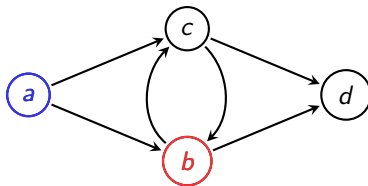


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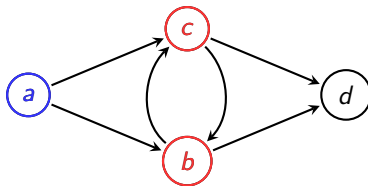


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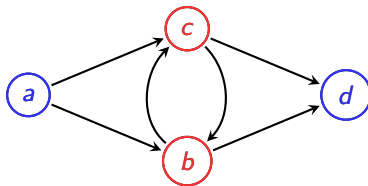


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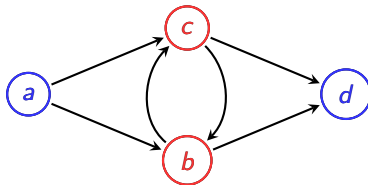


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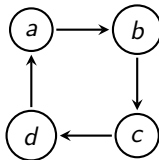
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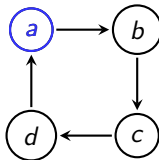


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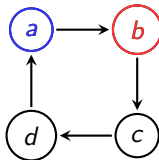


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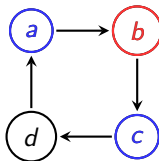


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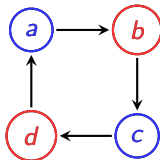


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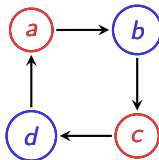
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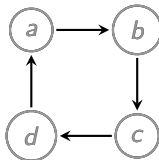
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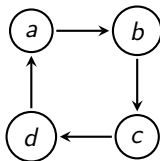


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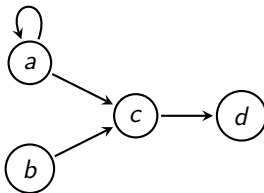
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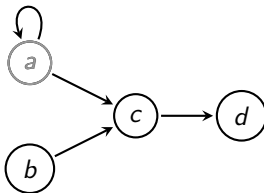


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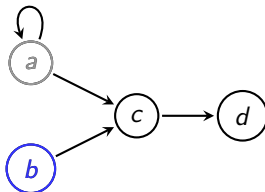


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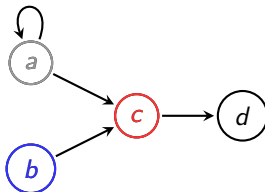


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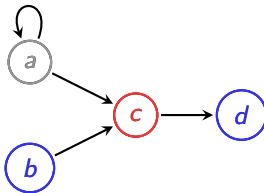


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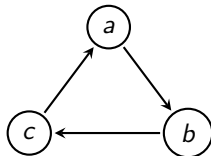
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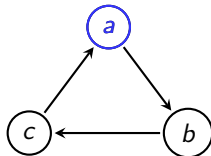


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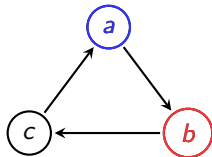


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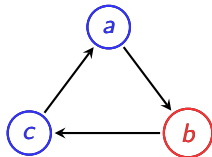


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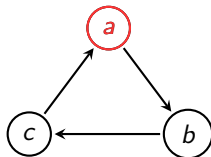


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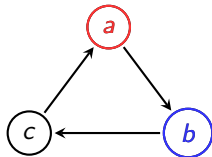


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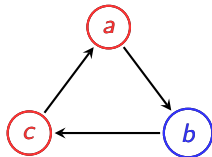


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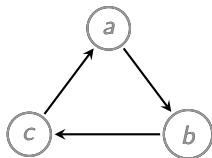


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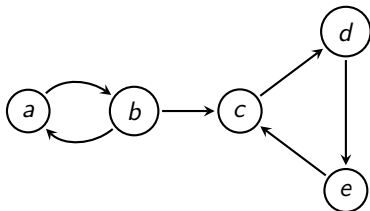
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## Applying Argument Labellings (ctd.)

Give the three labellings of this argumentation framework.



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5.  $\mathbb{L}_5 = \{a \mapsto \text{out}, b \mapsto \text{in}, c \mapsto \text{out}, d \mapsto \text{in}, e \mapsto \text{out}\}$



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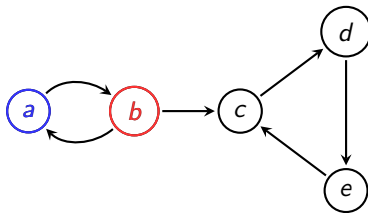
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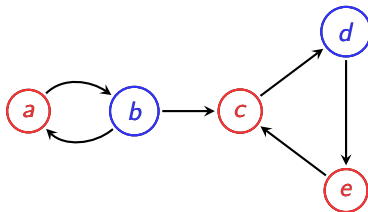
## Applying Argument Labellings (ctd.)

Give the three labellings of this argumentation framework.

**in**  $\Leftrightarrow$  all attackers are **out**

**out**  $\Leftrightarrow$  there is an attacker that is **in**

**undec**  $\Leftrightarrow$  not all attackers are **out**, and no attacker is **in**



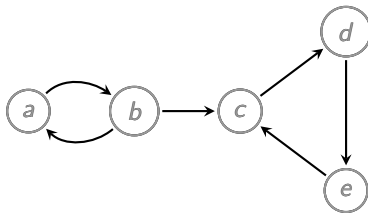
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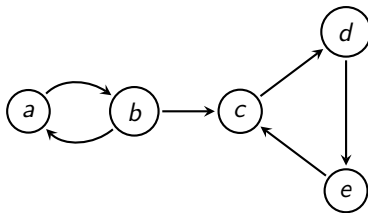
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# Maximisation/Minimisation

*maximal*: there is no other that has the same plus something

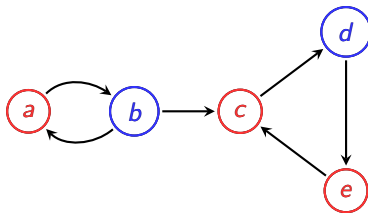
*minimal*: there is no other that has the same minus something



# Maximisation/Minimisation

*maximal*: there is no other that has the same plus something

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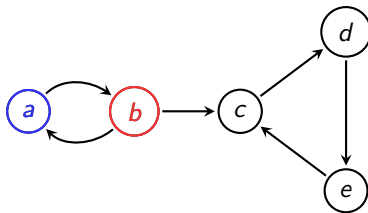


*a*, *b*, *c*, *d*, *e*      max *in*, max *out*, min *undec*

# Maximisation/Minimisation

*maximal*: there is no other that has the same plus something

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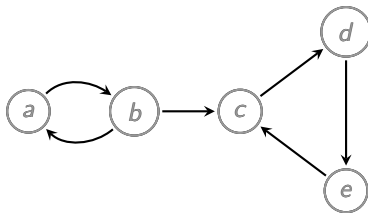


*a*, *b*, *c*, *d*, *e*      max *in*, max *out*

# Maximisation/Minimisation

*maximal*: there is no other that has the same plus something

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$a, b, c, d, e$       min **in**, min **out**, max undec

# Extension-based Semantics vs. Labelling-based Semantics

**in**  $\Leftrightarrow$  all attackers are **out**

**out**  $\Leftrightarrow$  there is an attacker that is **in**

**undec**  $\Leftrightarrow$  not all attackers are **out**, and no attacker is **in**

## restriction on labelling

maximal **in**

maximal **out**

maximal **undec**

minimal **in**

minimal **out**

empty **undec**

# Extension-based Semantics vs. Labelling-based Semantics

**in**  $\Leftrightarrow$  all attackers are **out**

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## restriction on labelling

maximal **in**

maximal **out**

maximal **undec**

minimal **in**

minimal **out**

empty **undec**

## Extension-based semantics

preferred semantics

preferred semantics

grounded semantics

grounded semantics

grounded semantics

Stable semantics

An extension is the in-labelled part of a labelling



# Admissible Labelling

## Definition: Admissible labelling

Given an AF  $F = (A, R)$ . Let  $\mathbb{L}$  be a labelling function on  $A$ .  $\mathbb{L}$  is an **admissible labelling** iff for each argument  $a \in A$  it holds that:

- ▶ if  $\mathbb{L}(a) = \text{in}$  then **for each**  $b$ , such that  $(b, a) \in R$  then  $\mathbb{L}(b) = \text{out}$ ;
- ▶ if  $\mathbb{L}(a) = \text{out}$  then **there exists**  $b \in A$ , such that  $(b, a) \in R$  and  $\mathbb{L}(b) = \text{in}$ .

# Admissible Labelling

Admissible labeling:

**in**  $\Rightarrow$  all attackers are **out**

**out**  $\Rightarrow$  there is an attacker that is **in**



# Admissible Labelling

Admissible labeling:

**in**  $\Rightarrow$  all attackers are **out**

**out**  $\Rightarrow$  there is an attacker that is **in**



$$\blacktriangleright \text{adm}_{\mathbb{L}_1}(F) = \{a \mapsto \text{undec}, b \mapsto \text{undec}, c \mapsto \text{undec}\}$$

# Admissible Labelling

Admissible labeling:

**in**  $\Rightarrow$  all attackers are **out**

**out**  $\Rightarrow$  there is an attacker that is **in**



►  $adm_{\mathbb{L}_2}(F) = \{a \mapsto \text{undec}, b \mapsto \text{undec}, c \mapsto \text{in}\}$

# Admissible Labelling

Admissible labeling:

**in**  $\Rightarrow$  all attackers are **out**

**out**  $\Rightarrow$  there is an attacker that is **in**



$$\blacktriangleright \text{adm}_{\mathbb{L}_3}(F) = \{a \mapsto \text{undec}, b \mapsto \text{out}, c \mapsto \text{in}\}$$

# Admissible Labelling

Admissible labeling:

**in**  $\Rightarrow$  all attackers are **out**

**out**  $\Rightarrow$  there is an attacker that is **in**



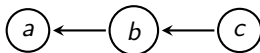
$$\blacktriangleright \text{adm}_{\mathbb{L}_4}(F) = \{a \mapsto \text{in}, b \mapsto \text{out}, c \mapsto \text{in}\}$$

# Admissible Labelling

Admissible labeling:

**in**  $\Rightarrow$  all attackers are **out**

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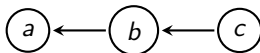
- ▶  $adm_{\mathbb{L}_1}(F) = \{a \mapsto \text{undec}, b \mapsto \text{undec}, c \mapsto \text{undec}\}$
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# Admissible Labelling

Admissible labeling:

**in**  $\Rightarrow$  all attackers are **out**

**out**  $\Rightarrow$  there is an attacker that is **in**



- ▶  $adm_{\mathbb{L}_1}(F) = \{a \mapsto \text{undec}, b \mapsto \text{undec}, c \mapsto \text{undec}\}$      $adm_1(F) = \{\}$
- ▶  $adm_{\mathbb{L}_2}(F) = \{a \mapsto \text{undec}, b \mapsto \text{undec}, c \mapsto \text{in}\}$      $adm_2(F) = \{c\}$
- ▶  $adm_{\mathbb{L}_3}(F) = \{a \mapsto \text{undec}, b \mapsto \text{out}, c \mapsto \text{in}\}$      $adm_3(F) = \{c\}$
- ▶  $adm_{\mathbb{L}_4}(F) = \{a \mapsto \text{in}, b \mapsto \text{out}, c \mapsto \text{in}\}$      $adm_4(F) = \{a, c\}$

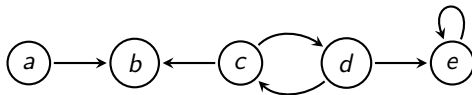


# Complete Labelling

**in**  $\Leftrightarrow$  all attackers are **out**

**out**  $\Leftrightarrow$  there is an attacker that is **in**

**undec**  $\Leftrightarrow$  not all attackers are **out**, and no attacker is **in**

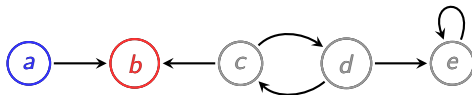
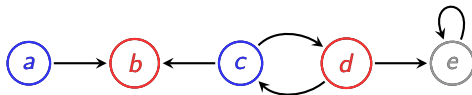
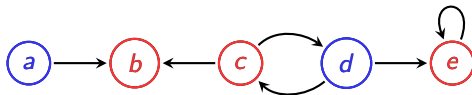


# Complete Labelling

**in**  $\Leftrightarrow$  all attackers are **out**

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# Labelling-based Semantics

## Admissible Labelling

**in**  $\Leftrightarrow$  all attackers are **out**

**out**  $\Leftrightarrow$  there is an attacker that is **in**

## Complete labelling

**in**  $\Leftrightarrow$  all attackers are **out**

**out**  $\Leftrightarrow$  there is an attacker that is **in**

**undec**  $\Leftrightarrow$  not all attackers are **out**, and no attacker is **in**

**Grounded labelling:** Complete with min **in** / min **out** / max **undec**

**Preferred labelling:** Complete with max **in** / max **out**

**Stable labelling:** complete with no **undec**

# What is the relation between argumentation semantics and discussion?

- ▶ Preferred Discussion Game

## Socratic Discussion

Answer me this. As soon as one man loves another, which of the two becomes the friend? the lover of the loved, or the loved of the lover? Or does it make no difference?

None in the world, that I can see

How? Are both friends, if only one loves?

I think so

Indeed! is it not possible for one who loves, not to be loved in return (...) ?

It is.

Nay, is it not possible for him even to be hated? (...) Don't you believe this to be true?

Quite true.

Well, in such a case as this, the one loves, the other is loved.

Just so.

Which of the two, then, is the friend of the other? The lover of the loved, whether or not he be loved in return, and even if he be hated, or the loved of the lover? or is neither the friend of the other, unless both love each other?

The latter certainly seems to be the case, Socrates.

If so, I continued, we think differently now from what we did before. (...)

Yes, I'm afraid we have contradicted ourselves.

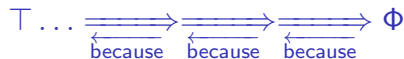
# Traditional Dialogue vs. Socratic Dialogue

- ▶ P: claim tr  
*I think that there will be a tax relief.*
- ▶ O: why tr  
*Why do you think so?*
- ▶ P: because pmp  $\Rightarrow$  tr  
***Because** of the fact that the politicians made a promise.*
- ▶ O: concede tr  
*OK, you are right.*

# Traditional Dialogue vs. Socratic Dialogue

- ▶ P: claim tr  
*I think that there will be a tax relief.*
- ▶ O: **but-then** tr  $\Rightarrow$  bd  
*Then you implicitly also hold that budget deficit.*
- ▶ P: concede bd  
*Yes I do.*
- ▶ O: **but-then** bd  $\Rightarrow$  feu  
*Then you implicitly also hold that fine from EU.*
- ▶ P: concede feu  
*Yes I do.*
- ▶ O: **but-then** feu  $\Rightarrow \neg$ tr  
*Then you implicitly also hold that  $\neg$ tr.*
- ▶ P: concede  $\neg$ tr *Oops, you're right; I caught myself in...*

## *because* versus *but-then*



reasoning goes backward  
proponent constructs path  
originates from true  
both parties become committed



reasoning goes forward  
opponent constructs path  
leads to false  
only proponent becomes committed



# Preferred Semantics as Socratic Discussion

## Recall: Definition

Admissible labeling:

if argument is **in** then all attackers are **out**

if argument is **out** then it has an attacker that is **in**

## Recall: Proposition

An argument is in a preferred extension

iff it is in a complete extension

iff it is in an admissible set

iff it is labelled **in** by an admissible labelling

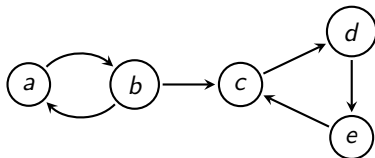
# Flashback: Decision Problems on AFs

## Credulous Acceptance

Given an AF  $F = (A, R)$ ,  $a \in A$ , and  $\sigma \in \{adm, pref, stb, grd, comp, cf\}$ .

$Cred_{\sigma}(a, F)$  : is  $a$  contained in **at least one**  $\sigma$ -extension of  $F$ ?

$$Cred_{\sigma}(a, F) = \begin{cases} \text{yes} & \text{if } \exists S \in \sigma\text{-extension } F \text{ s.t. } a \in S, \\ \text{no} & \text{otherwise} \end{cases}$$



- $Cred_{adm}(b, F)$ : is  $b$  contained in **at least one**  $adm$ -extension of  $F$ ?

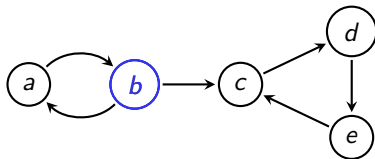
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$adm(F) = \{\{b\}\}$ ,  $Cred_{adm}(b, F)$  : Yes

►  $Cred_{adm}(b, F)$ : is  $b$  contained in **at least one**  $adm$ -extension of  $F$ ?

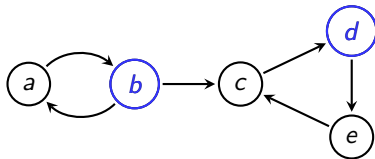
# Flashback: Decision Problems on AFs

## Credulous Acceptance

Given an AF  $F = (A, R)$ ,  $a \in A$ , and  $\sigma \in \{adm, pref, stb, grd, comp, cf\}$ .

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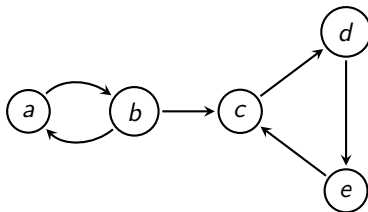
$$Cred_{cf}(a, F) = \begin{cases} \text{yes} & \text{if } (a, a) \notin R, \\ \text{no} & \text{otherwise} \end{cases}$$



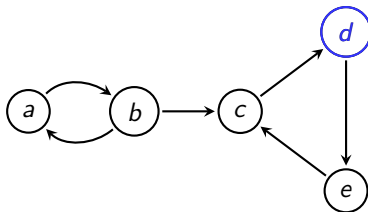
$pref(F) = \{\{b, d\}\}$ ,  $Cred_{pref}(b, F)$  : Yes

►  $Cred_{pref}(b, F)$ : is  $b$  contained in **at least one**  $pref$ -extension of  $F$ ? Yes

# Preferred Semantics as Socratic Discussion

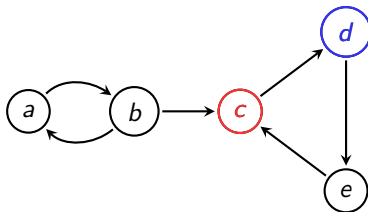


# Preferred Semantics as Socratic Discussion



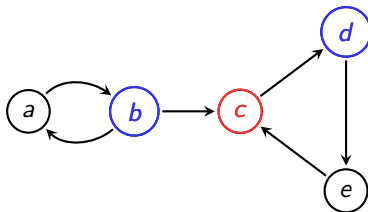
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# Preferred Semantics as Socratic Discussion



- ▶ P: **in**( $d$ ): I have an admissible labelling in which  $d$  is labelled **in**
- ▶ O: **out**( $c$ ): **But then** in your labelling it must also be the case that  $d$ 's attacker  $c$  is labelled **out**. Based on which grounds?

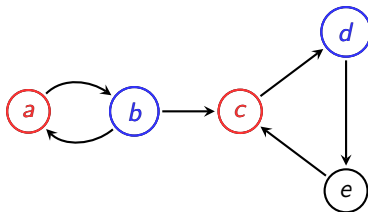
# Preferred Semantics as Socratic Discussion



- ▶ P: **in**( $d$ ): I have an admissible labelling in which  $d$  is labelled **in**
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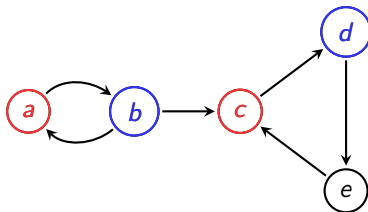


# Preferred Semantics as Socratic Discussion



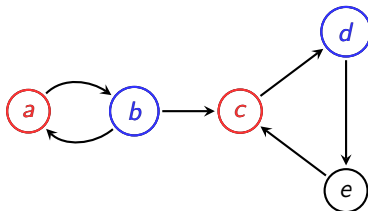
- ▶ P: **in**(d): I have an admissible labelling in which  $d$  is labelled **in**
- ▶ O: **out**(c): **But then** in your labelling it must also be the case that  $d$ 's attacker  $c$  is labelled **out**. Based on which grounds?
- ▶ P: **in**(b):  $c$  is labelled **out** because  $b$  is labelled **in**.
- ▶ O: **out**(a): **But then** in your labelling it must also be the case that  $b$ 's attacker  $a$  is labelled **out**. Based on which grounds?

# Preferred Semantics as Socratic Discussion



- ▶ P: **in**(d): I have an admissible labelling in which *d* is labelled **in**
- ▶ O: **out**(c): **But then** in your labelling it must also be the case that *d*'s attacker *c* is labelled **out**. Based on which grounds?
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- ▶ P: **in**(b): *a* is labelled **out** because *b* is labelled **in**.

# Preferred Semantics as Socratic Discussion



- ▶ P: **in**(d): I have an admissible labelling in which *d* is labelled **in**
- ▶ O: **out**(c): **But then** in your labelling it must also be the case that *d*'s attacker *c* is labelled **out**. Based on which grounds?
- ▶ P: **in**(b): *c* is labelled **out** because *b* is labelled **in**.
- ▶ O: **out**(a): **But then** in your labelling it must also be the case that *b*'s attacker *a* is labelled **out**. Based on which grounds?
- ▶ P: **in**(b): *a* is labelled **out** because *b* is labelled **in**.  
**If O cannot make a move any more, P wins the discussion.**

# Preferred Semantics as Socratic Discussion

- ▶ P:  $\text{in}(d)$ : I have an admissible labelling in which  $d$  is labelled  $\text{in}$
- ▶ O:  $\text{out}(c)$ : **But then** in your labelling it must also be the case that  $d$ 's attacker  $c$  is labelled  $\text{out}$ . Based on which grounds?
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- ▶ O:  $\text{out}(a)$ : **But then** in your labelling it must also be the case that  $b$ 's attacker  $a$  is labelled  $\text{out}$ . Based on which grounds?
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1. Each move of P (except the first) contains an attacker of the directly preceding move of O.

# Preferred Semantics as Socratic Discussion

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- ▶ O:  $\text{out}(c)$ : **But then** in your labelling it must also be the case that  $d$ 's attacker  $c$  is labelled  $\text{out}$ . Based on which grounds?
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- ▶ O:  $\text{out}(a)$ : **But then** in your labelling it must also be the case that  $b$ 's attacker  $a$  is labelled  $\text{out}$ . Based on which grounds?
- ▶ P:  $\text{in}(b)$ :  $a$  is labelled  $\text{out}$  because  $b$  is labelled  $\text{in}$ .

2. Each move of O contains an attacker of some previous move of P.

# Preferred Semantics as Socratic Discussion

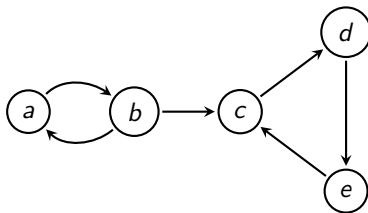
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- ▶ P:  $\text{in}(b)$ :  $c$  is labelled  $\text{out}$  because  $b$  is labelled  $\text{in}$ .
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- ▶ P:  $\text{in}(b)$ :  $a$  is labelled  $\text{out}$  because  $b$  is labelled  $\text{in}$ .

3. O is not allowed to repeat his moves.

# Preferred Semantics as Socratic Discussion

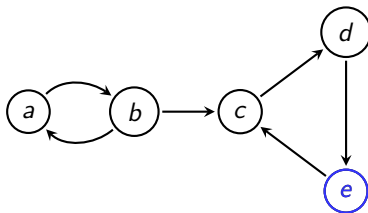
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- 
1. Each move of P (except the first) contains an attacker of the directly preceding move of O.
  2. Each move of O contains an attacker of some previous move of P.
  3. O is not allowed to repeat his moves.
  4. P is allowed to repeat his moves.

# Preferred Semantics as Socratic Discussion



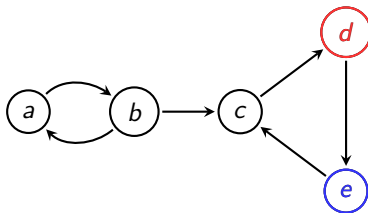


## Preferred Semantics as Socratic Discussion



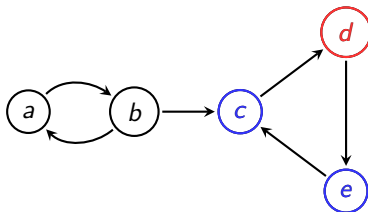
- P: **in**(e): I have an admissible labelling in which e is labelled **in**

# Preferred Semantics as Socratic Discussion



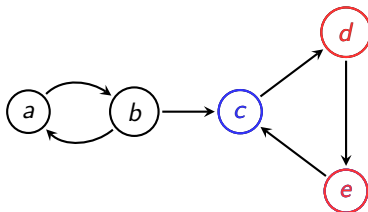
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# Preferred Semantics as Socratic Discussion



- ▶ P: **in**(e): I have an admissible labelling in which e is labelled **in**
- ▶ O: **out**(d): **But then** in your labelling it must also be the case that e's attacker d is labelled out. Based on which grounds?
- ▶ P: **in**(c): d is labelled **out** because c is labelled **in**.

# Preferred Semantics as Socratic Discussion



- ▶ P: **in**(e): I have an admissible labelling in which e is labelled **in**
- ▶ O: **out**(d): **But then** in your labelling it must also be the case that e's attacker d is labelled out. Based on which grounds?
- ▶ P: **in**(c): d is labelled **out** because c is labelled **in**.
- ▶ O: **out**(e): **But then** in your labelling it must also be the case that c's attacker e is labelled **out**.  
This **contradicts** with your earlier claim that e is labelled **in**

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- ▶ O:  $\text{out}(d)$ : **But then** in your labelling it must also be the case that  $e$ 's attacker  $d$  is labelled out. Based on which grounds?
- ▶ P:  $\text{in}(c)$ :  $d$  is labelled  $\text{out}$  because  $c$  is labelled  $\text{in}$ .
- ▶ O:  $\text{out}(e)$ : **But then** in your labelling it must also be the case that  $c$ 's attacker  $e$  is labelled  $\text{out}$ .  
This **contradicts** with your earlier claim that  $e$  is labelled  $\text{in}$
- ▶ If O uses an argument previously used by P, then O **wins the discussion**.

# Preferred Semantics as Socratic Discussion

## Winning rules

1. If O uses an argument previously used by P, then O **wins the discussion**.

# Preferred Semantics as Socratic Discussion

## Winning rules

2. If P uses an argument previously used by O, then O **wins the discussion**.

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## Winning rules

3. If P cannot make a move any more, O **wins the discussion**.



# Preferred Semantics as Socratic Discussion

## Winning rules

1. If O uses an argument previously used by P, then O **wins the discussion**.
2. If P uses an argument previously used by O, then O **wins the discussion**.
3. If P cannot make a move any more, O **wins the discussion**.
4. If O cannot make a move any more, P **wins the discussion**.

# Preferred Semantics as Socratic Discussion

## Theorem

Argument  $a$  is labelled **in** by at least one admissible labelling iff  $M$  can win the Socratic discussion game (for  $a$ ).

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Argument  $a$  is labelled **in** by at least one preferred labelling iff  $M$  can win the Socratic discussion game (for  $a$ ).

# Why These Results Matter

- ▶ argumentation: based on notion of justification (entails what can be defended in rational discussion)
- ▶ discussions can be used by the system to **explain** its answer to the user
- ▶ different semantics express different types of rational discussion
- ▶ allows (in principle) for dynamic and user-based updating of the underlying knowledge base