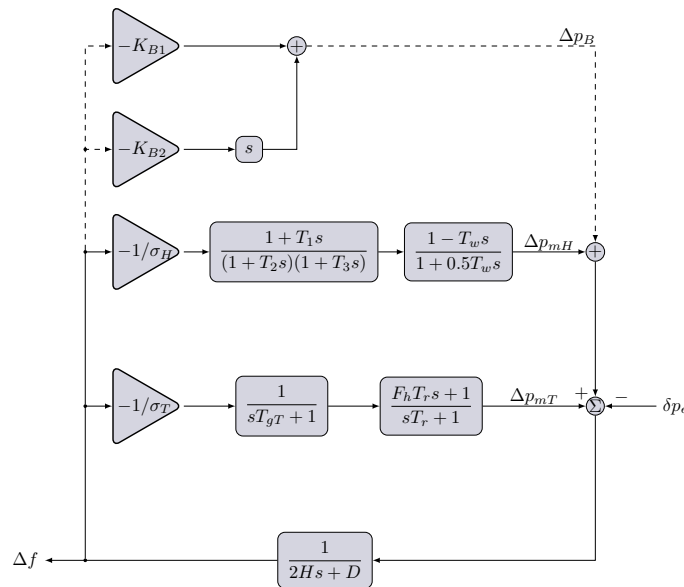


Zadatak 1

Sinkroni sustav kontinentalne Europe sastoji se od nekog udjela termoelektrana i nekog udjela hidroelektrana koje sudjeluju u regulaciji frekvencije (Slika 1). Parametri sustava su sljedeći: bazna snaga sustava iznosi 500 GW; regulacijska energija potrošnje iznosi 0.5 p.u.; $T_{gT} = 0.2$ s, $F_h = 0.3$ p.u., $T_r = 6$ s; $T_1 = 5$ s, $T_2 = 0.4$ s, $T_3 = 48$ s, $T_w = 0.8$ s; $T_b = 0.02$ s. [Napomena: U podzadacima a) i b) Zanimarite iscrtkanu granu (baterijski spremnici) na slici 1.]

- Ako za ispad elektrane od 3000 MW odstupanje frekvencije u ustaljenom stanju mora biti > -200 mHz, koliko iznosi minimalna regulacijska energija proizvodnje?
- Ako je za poremećaj snage od 5% maksimalni dozvoljeni početni RoCoF 0.5 Hz/s, kolika je minimalna konstanta tromosti sustava?
- Ako je zbog velikog udjela obnovljivih izvora energije spojenih preko energetske elektronike trenutna konstanta tromosti sustava 1 s, koliko mora iznositi pojačanje K_{B2} baterijskih spremnika (iscrtkana grana na slici 1) u sustavu da bi početni RoCoF bio < 2 Hz/s za poremećaj snage od 10%?
- Koliko iznosi minimalna statičnost baterijskih spremnika ako je dozvoljeno odstupanje frekvencije u stacionarnom stanju ± 0.15 Hz za poremećaj od 20% uz $\sigma_H = 0.04$ p.u. i $\sigma_T = 0.08$ p.u.?

(Dodatna pomoć: teorem početne vrijednosti glasi $y(0) = \lim_{s \rightarrow \infty} sY(s)$)
(8 bodova)



Slika 1: Pojednostavljeni model sinkronog sustava kontinentalne Europe

Zadatak 2

Nacrtajte blok dijagram dinamičkog sustava opisanog jednadžbama (1)–(2), gdje su T , K , P_m , E' , U , X i D_1, D_2 konstante, a δ i ω varijable stanja.

$$\frac{1}{K} \frac{d\delta}{dt} = (\omega - 1) \quad (1)$$

$$T\omega \frac{d\omega}{dt} + (D_1 + D_2)(\omega - 1) = P_m - \frac{E'U}{X} \sin \delta \quad (2)$$

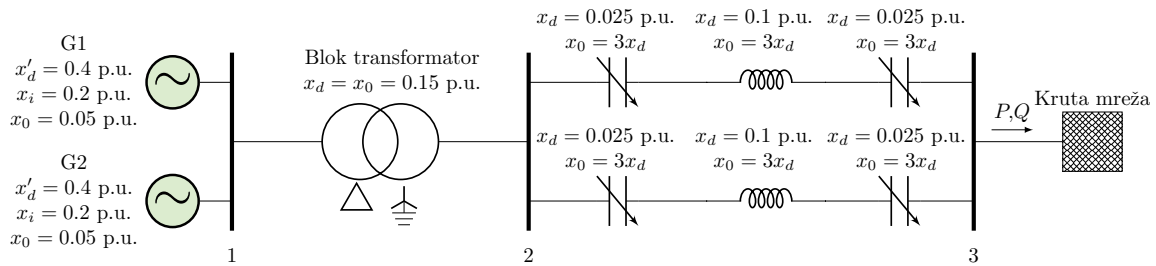
(2 boda)

Zadatak 3

Dva identična agregata neke elektrane spojena su na krutu mrežu preko blok-transformatora i dvostrukog dalekovoda kompenziranog s oba kraja preko tiristorski upravljanih serijskih kondenzatora (TCSC) koji su podešeni prema slici 2. Agregati u poduzbuđenom režimu rada u mrežu predaju snagu $P = 0.9$ p.u. pri $\cos \varphi = 0.95$ kap. Napon krute mreže iznosi $1 \angle 0^\circ$ p.u. Na jednom od dva paralelna voda nastaje dvopolni kratki spoj na 50% duljine voda. Potrebno je 1) odrediti kritični kut uklanjanja kvara i 2) nacrtati nadomjesnu shemu sustava sa slike 2 te odrediti izraz i skicirati krivulje za prijenos električne snage između elektrane i krute mreže za slučajeve:

- prije nastanka kratkog spoja;
- tijekom kratkog spoja;
- nakon isključenja voda u kvaru.

(15 bodova)

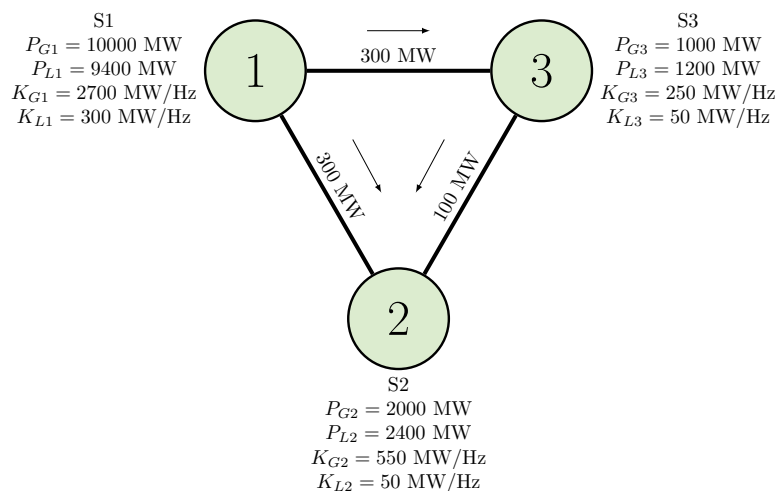


Slika 2: Spoj elektrane s dva agregata s krutom mrežom

Zadatak 4

Tri sustava rade u interkonekciji (Slika 3). Joža je dispečer u operatoru sustava 1. Joži je ispao tanjur s grahom na tipkovnicu i slučajno je isključio vod između sustava 1 i 3. Sekvencijalno opišite što će se dogoditi od tog trenutka pa sve do konačnog stacionarnog stanja. Navedite i naznačite sva međustanja. Potrebno je izračunati konačno stanje u svim sustavima te sva međustanja kroz koja sustavi prolaze. Maksimalno dozvoljeno opterećenje svih vodova iznosi 500 MW. Preopterećeni vod prekostrujna zaštita automatski isključuje. Svi sustavi jednako sudjeluju u sekundarnoj regulaciji.

(10 bodova)

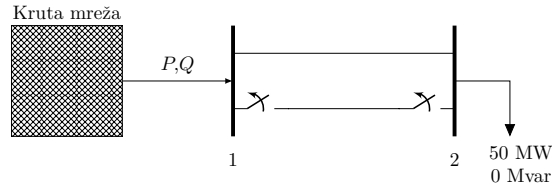


Slika 3: Tri sustava u interkonekciji

Zadatak 5

U slabo opterećenim visokonaponskim mrežama regulacija napona može se vršiti isključivanjem dalekovoda. Za koliko se promjeni napon sabirnice 2 ako se isključi jedan dalekovod (Slika 4)? Pri oba dalekovoda uključena, kruta mreža u dvostruki dalekovod injektira $P = 50.4$ MW i apsorbira $Q = 63.5$ Mvar. Ako se jedan dalekovod isključi, kruta mreža u dalekovod injektira $P = 50.6$ MW i apsorbira $Q = 27.8$ Mvar. Napon krute mreže iznosi 220 kV. Parametri voda su sljedeći: $R = 0.05 \Omega/\text{km}$, $L = 1.553 \text{ mH}/\text{km}$, $C = 10.73 \text{ nF}/\text{km}$. Parametri su izraženi po fazi za jedan dalekovod. Napon krute mreže iznosi 220 kV. Duljina dalekovoda je 200 km. Frekvencija sustava je 50 Hz.

(5 bodova)



Slika 4: Prijenos snage preko dalekovoda

Zadatak 6

Objasnite princip rada primarne regulacije frekvencije. Koji sve faktori utječu na dinamičko vladanje frekvencije nakon nastanka poremećaja i kako?

(3 boda)

Zadatak 7

Što je kritični kut uklanjanja kvara i kako se može odrediti? Skicirati krivulje za prijenos snage za različite vrste kvarova.

(2 boda)

Zadatak 8

Koji element je najveći potrošač jalove snage u EES-u? Kako se regulira proizvodnja/potrošnja jalove snage sinkronog generatora? Nacrtati sustav regulacije jalove snage sinkronog generatora.

(2 boda)

Zadatak 9

Što je slom napona i koji element EES-a je najčešći uzrok sloma napona? Skicirajte pojavu sloma napona u vremenskoj domeni.

(1 bod)

Zadatak 10

Koje vrste potrošača imaju regulacijsku energiju? Koja je uloga podfrekvencijskog rasterećenja?

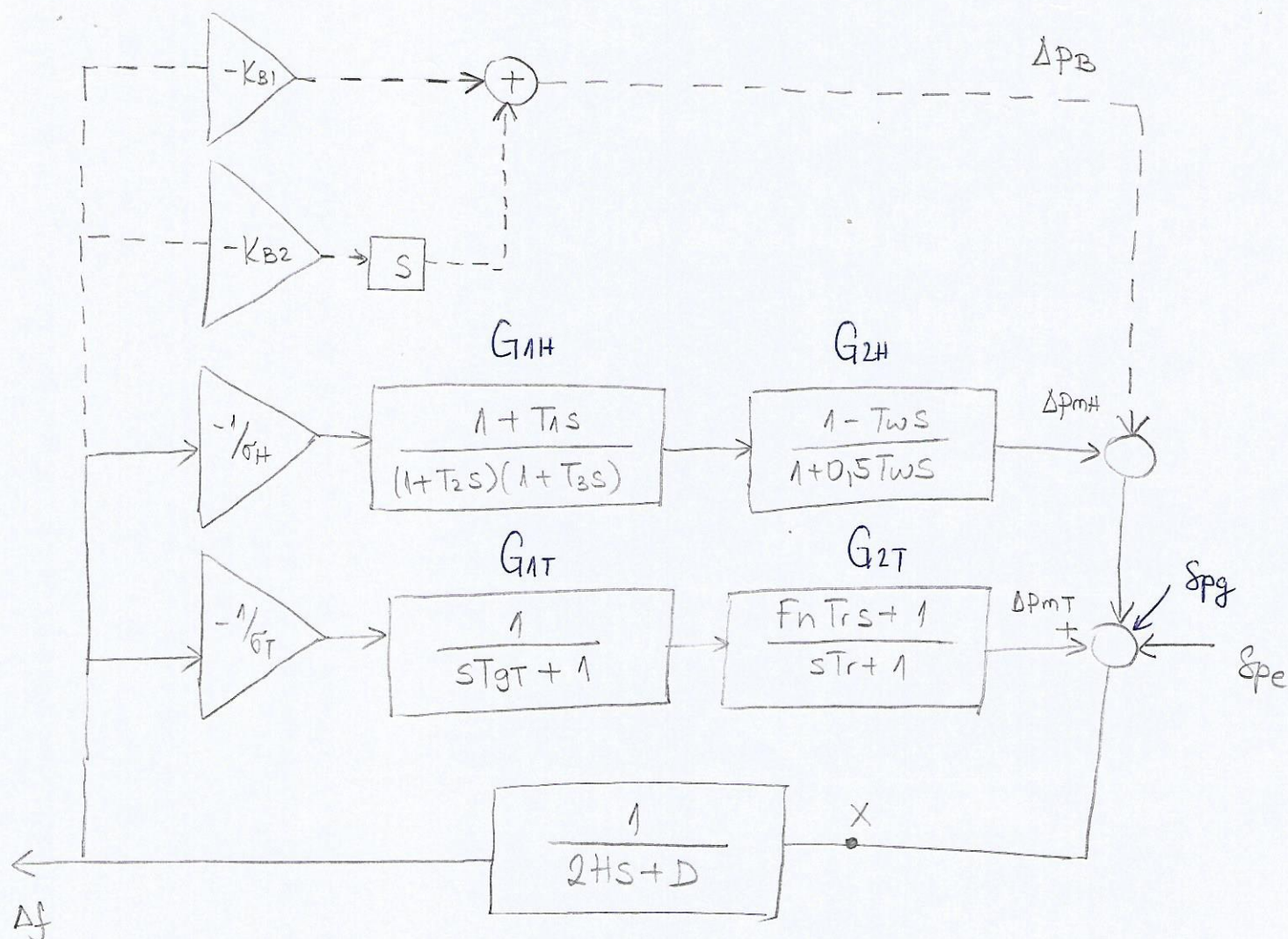
(1 bod)

Zadatak 11

Nabrojite i opišite načine kompenzacije jalove snage kondenzatorskim baterijama.

(1 bod)

ZADATAK 1.



$S_B = 500 \text{ GW}$ $F_n = 0.3 \text{ pu}$ $T_2 = 0.4 \text{ s}$ $T_b = 0.02 \text{ s}$
 $D = 0.5 \text{ p.u.}$ $T_r = 6 \text{ s}$ $T_3 = 48 \text{ s}$
 $T_{gT} = 0.2 \text{ s}$ $T_1 = 5 \text{ s}$ $T_w = 0.8 \text{ s}$

a) Ispad elektrane od 3000 MW $\Rightarrow \Delta P_g = -3000 \text{ MW}$

$\Delta f_{\infty} > -200 \text{ mHz}$

$K = ?$ (min. en. proizv.)

$$\Delta P_g = - \frac{3000 \text{ M}}{500 \text{ G}} = -0.006 \text{ p.u.}$$

$$\Delta f_{\infty} > -200 \text{ mHz} / : 50 \rightarrow \Delta f_{\infty} > -0.004 \text{ p.u.}$$

$$\Delta f(2HS + D) = X$$

poremedaj
proizvodnje

poremedaj
potrošnje

$$\left. \begin{array}{l} \text{poremedaj} \\ \text{proizvodnje} \end{array} \right\} X = X$$

$$X = \Delta p_{MT}(s) + \Delta p_{MH}(s) + \underbrace{\delta p_g(s)}_{=0} - \underbrace{\delta p_e(s)}_{=0}$$

$$\Delta p_{MT}(s) = \Delta f(s) \left(-\frac{1}{G_T} \right) G_{1T}(s) G_{2T}(s)$$

$$\frac{t}{C} \rightarrow \frac{s}{C/s}$$

$$\Delta p_{MH}(s) = \Delta f(s) \left(-\frac{1}{G_H} \right) G_{1H}(s) G_{2H}(s)$$

$$\delta p_g(t) = -0,006 \text{ p.u. / s}$$

$$\delta p_g(s) = -\frac{0,006}{s}$$

$$\Delta f(s) = \frac{\delta p_g(s)}{2HS + D + \frac{1}{G_T} G_{1T}(s) G_{2T}(s) + \frac{1}{G_H} G_{1H}(s) G_{2H}(s)}$$

$$\Delta f_{\infty} = \lim_{s \rightarrow 0} s \frac{\frac{\delta p_g(0)}{s}}{2H \cdot 0 + D + \frac{1}{G_T} G_{1T}(0) G_{2T}(0) + \frac{1}{G_H} G_{1H}(0) G_{2H}(0)}$$

$$\Delta f_{\infty} = \frac{\delta p_g}{D + \frac{1}{G_T} + \frac{1}{G_H}} = \frac{\delta p_g}{D + K_{UK}} > -0,004 \text{ p.u.}$$

$$\frac{-0,006}{0,5 + K_{UK}} > -0,004 \rightarrow K_{UK} > 1,5 - 1 \rightarrow \underline{\underline{K_{UK} > 1}}$$

SI:

$$K_{UK}^{SI} > 1 \text{ p.u.} \frac{S_B}{f_B} = \frac{5000}{50}, K_{UK}^{SI} > 10 \frac{GW}{Hz}$$

b) poremedaj snage $5\% = 0,05$
 max dozvoljeni RoCoF $0,5 \frac{\text{Hz}}{\text{s}}$

$$H_{\min} = ?$$

$$G_{1H} \cdot G_{2H} = G_H \quad G_{1T} \cdot G_{2T} = G_T$$

$$\Delta f(s) = \frac{s p_p}{2Hs + D + \frac{1}{G_T} G_T(s) + \frac{1}{G_H} G_H(s)}$$

$$\begin{array}{c} t \quad s \\ \hline \frac{d}{dt} \quad \circ \longrightarrow \circ \quad s \\ \Delta f(t) \quad \circ \longrightarrow \circ \quad \Delta f(s) \\ \frac{d\Delta f(t)}{dt} \quad \circ \longrightarrow \circ \quad s \Delta f(s) \end{array}$$

$$s \Delta f(s) = \text{RoCoF}(s) = 2$$

$$s \Delta f(s) = \frac{s p_p}{2Hs + D + \frac{1}{G_H} G_H + \frac{1}{G_T} G_T}$$

$$\left. \frac{df}{dt} \right|_{t=0+} = \lim_{s \rightarrow \infty} s \cdot s \Delta f(s) = \lim_{s \rightarrow \infty} s^2 \Delta f(s)$$

$$\left. \frac{df}{dt} \right|_{t=0+} = \lim_{s \rightarrow \infty} s^2 \frac{\frac{p_p}{s}}{2Hs + D + \frac{1}{G_T} G_T + \frac{1}{G_H} G_H}$$

$$= \lim_{s \rightarrow \infty} \frac{p_p}{2H + \frac{D}{s} + \frac{1}{s G_T} G_T + \frac{1}{s G_H} G_H}$$

$$\left. \frac{df}{dt} \right|_{t \rightarrow \infty} = \frac{p_p}{2H} = \left. \frac{df}{dt} \right|_{\max}$$

Početni RoCoF je max RoCoF

$$\left. \frac{df}{dt} \right|_{\max} < \frac{0,5 \frac{\text{Hz}}{\text{s}}}{50 \text{Hz}} = 0,01 \frac{\text{pu}}{\text{s}}$$

$$\frac{p_p}{2H} < 0,01$$

$$H > \frac{p_p}{2 \cdot 0,01} = \frac{0,05}{2 \cdot 0,01} = 2,5 \text{ s}$$

$$H \geq 2,5 \text{ s}$$

c) $H = 1s$

$K_{B2} = 2$

$$\left. \frac{df}{dt} \right|_{t=0+} < 2 \frac{Hz}{s} / 50 \rightarrow \left. \frac{df}{dt} \right|_{t=0+} < 0,04 \frac{pu}{s}$$

$$\left. \frac{df}{dt} \right|_{t=0+} = \lim_{s \rightarrow \infty} [s \cdot \Delta f(s)] \rightarrow \boxed{\left. \frac{df}{dt} \right|_{t=0+} = \frac{-\delta pe}{2H + K_{B2}}}$$

$$\left| \frac{-\delta pe}{2H + K_{B2}} \right| < 0,04 \frac{pu}{s}$$

$$2H + K_{B2} \geq \frac{1}{0,04} |-\delta pe|$$

$$K_{B2} > \frac{1}{0,04} |-\delta pe| - 2H$$

$$K_{B2} > \frac{1}{0,04} \cdot 0,1 - 2 \cdot 1$$

$$\underline{K_{B2} > 0,5 Hz}$$

d) $\sigma_{B1} = ?$ (min)

$$\Delta f_{\infty} < \pm 0,15 Hz$$

$$\delta pe = 20\% = 0,2$$

$$\sigma_H = 0,04 pu$$

$$\sigma_T = 0,08 pu$$

$$\Delta f(t \rightarrow \infty) = \lim_{s \rightarrow 0} s \Delta f(s) \rightarrow$$

$$\boxed{\Delta f_{\infty} = \frac{-\delta pe}{\frac{1}{\sigma_H} + \frac{1}{\sigma_T} + K_{B1} + D}}$$

$$|\Delta f_{\infty}| < \left| \frac{\pm 0,15}{50} \right|$$

$$\frac{|-\delta pe|}{\frac{1}{\sigma_H} + \frac{1}{\sigma_T} + K_{B1} + D} < \left| \frac{\pm 0,15}{50} \right|$$

$$\frac{1}{\sigma_H} + \frac{1}{\sigma_T} + K_{B1} + D > \frac{50}{0,15} |-\delta pe|$$

$$K_{B1} > \frac{50}{0,15} |-\delta pe| - D - \frac{1}{\sigma_T} - \frac{1}{\sigma_H}$$

$$K_{B1} > \frac{50}{0,15} \cdot 0,2 - 0,5 - \frac{1}{0,08} - \frac{1}{0,04}$$

$$K_{B1} > 28,6$$

$$\underline{\underline{\sigma_{B1} = 0,0349 pu}}$$

21R 2019./2020.

ZADATAK 2.

$$\frac{1}{K} \frac{d\delta}{dt} = (\omega - 1)$$

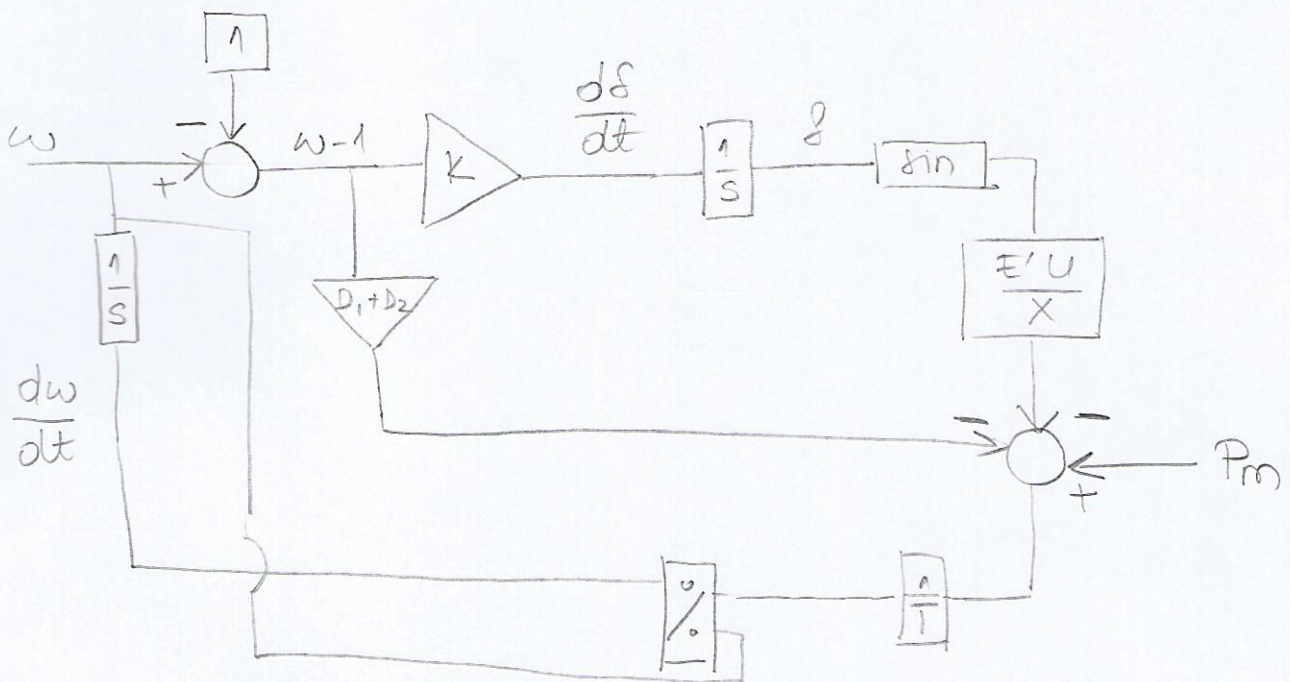
$$T_w \frac{d\omega}{dt} + (D_1 + D_2)(\omega - 1) = P_m - \frac{E'U}{X} \sin \delta$$

$T, K, P_m, E', U, X, D_1, D_2$ konstante

δ, ω variable stanja

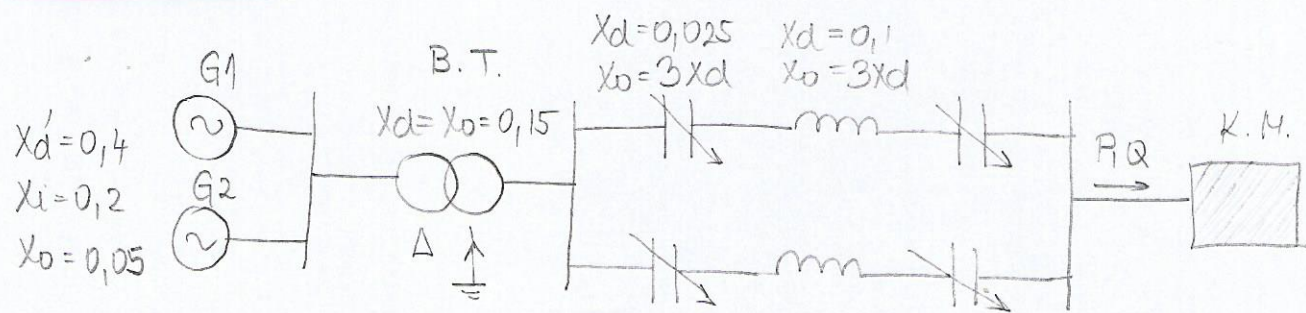
$$\frac{d\delta}{dt} = K(\omega - 1)$$

$$\frac{d\omega}{dt} = \frac{1}{T_w} \left[P_m - \frac{E'U}{X} \sin \delta - (D_1 + D_2)(\omega - 1) \right]$$

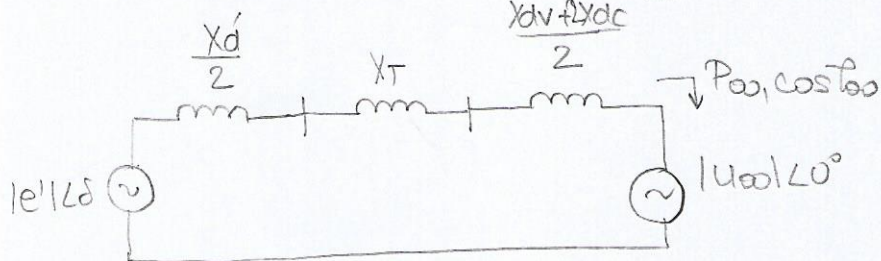
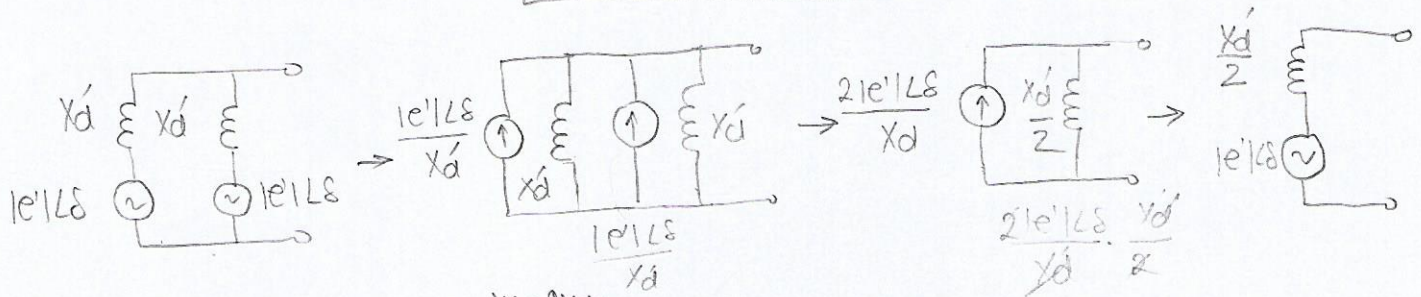
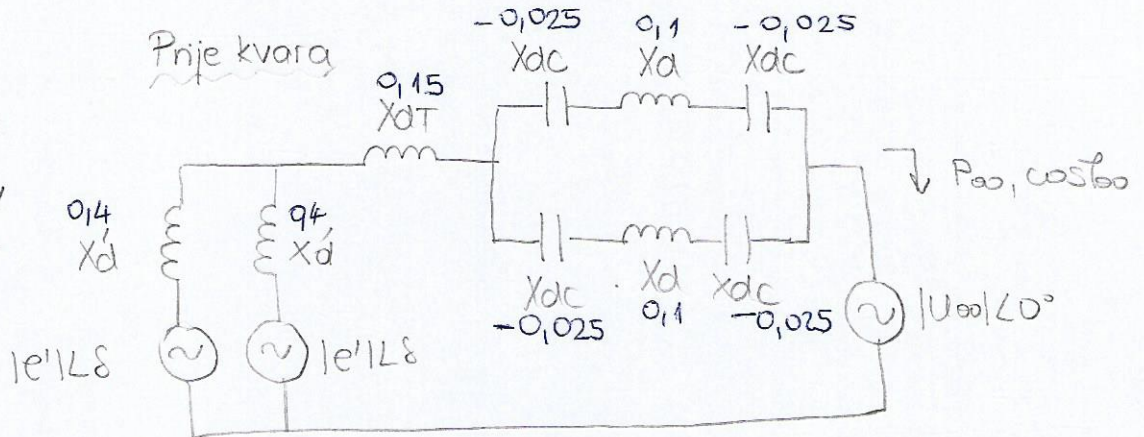


ZIR 2019./2020.

ZADATAK 3.



$P = 0.9 \text{ p.u.}$
 $\cos \phi = 0.95 \text{ kap.}$
 $U_{\infty} = 1 \angle 0^\circ \text{ p.u.}$
 2PKS, 50% dv



$$X_d = \frac{X_d'}{2} + X_T + \frac{X_{dv} - 2X_{dc}}{2}$$

$$= 0.12 + 0.15 + \frac{0.1 - 2 \cdot 0.025}{2}$$

$$= 0.375$$

$$1e'1L8_0 = |U_{\infty}| \angle 0^\circ + 100^\circ j X_d$$

$$i_{\infty} = \left(\frac{S}{U_{\infty} \angle 0^\circ} \right)^* = \left(\frac{P_{00} + jP_{00} \tan \phi_{00}}{U_{\infty} \angle 0^\circ} \right)^* = 0.9 - j0.9 \cdot \tan(\arccos(-0.95)) = 0.9 + j0.296 = 0.947 \angle 0.318 \text{ rad}$$

$$1e'1L8_0 = 1 + 0.947 \angle 0.318 \cdot 0.375 \angle \pi/2 = 0.889 + j0.337 = 0.951 \angle 0.362 \text{ rad}$$

$$1e'1 = 0.951$$

$$\delta_0 = 0.362 \text{ rad}$$

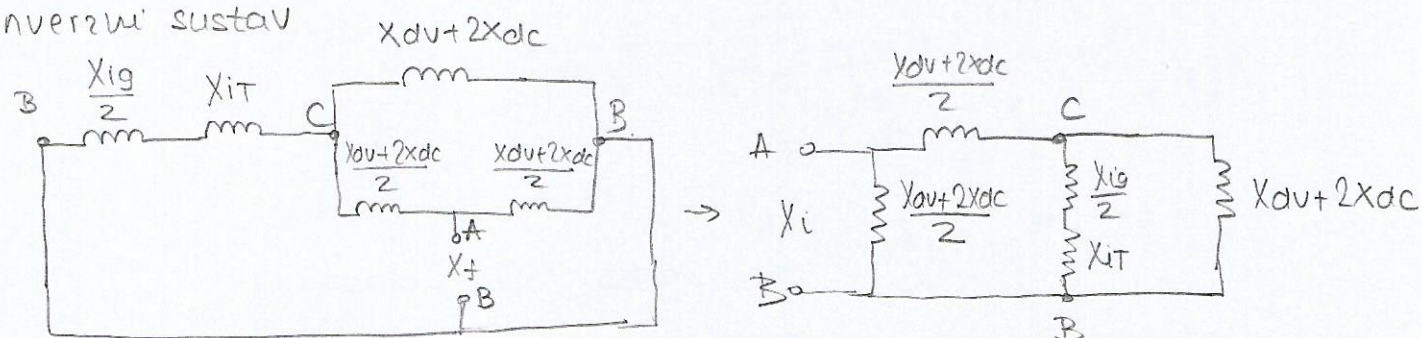
$$P_m = 0.9$$

$$P_d = \frac{0.951 \cdot 1}{0.375} \sin \delta = 2.536 \sin \delta$$

Za vrijeme kvara

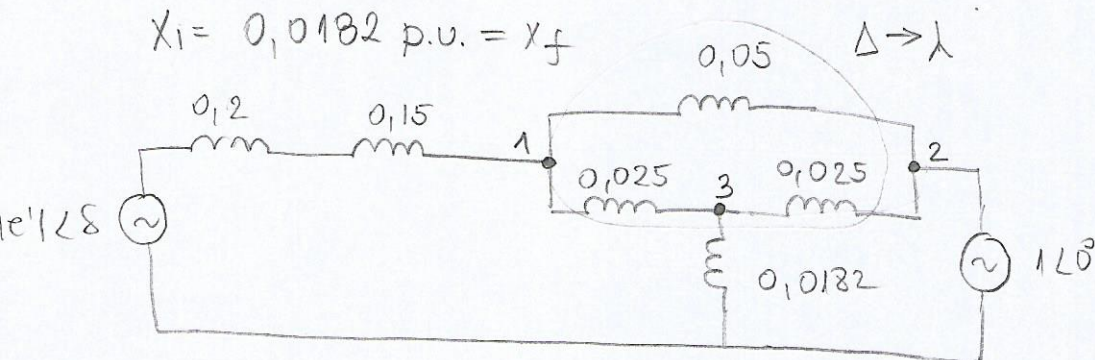
- kvar na 50% dužine dv
- 2PKS, $X_f = X_i$

inverzni sustav



$$X_i = \left[\underbrace{(X_{dv}+2X_{dc})}_{0,05} \parallel \underbrace{\left(\frac{X_{ig}}{2} + X_{it} \right)}_{0,25} + \underbrace{\frac{X_{dv}+2X_{dc}}{2}}_{0,025} \right] \parallel \underbrace{\frac{X_{dv}+2X_{dc}}{2}}_{0,025}$$

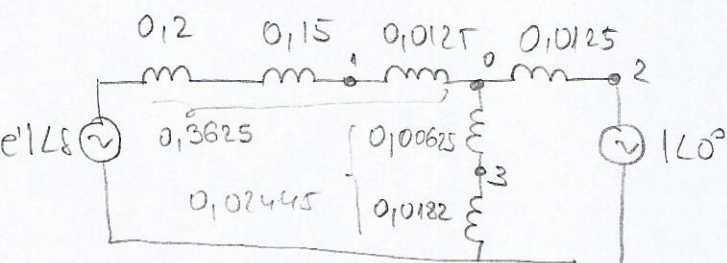
$$X_i = 0,0182 \text{ p.u.} = X_f$$



$$X_{10} = \frac{X_{12} X_{13}}{X_{12} + X_{13} + X_{23}} = \frac{0,0125}{0,0125 + 0,0125 + 0,025} = 0,00625$$

$$X_{20} = \frac{X_{12} X_{23}}{X_{12} + X_{13} + X_{23}} = 0,0125$$

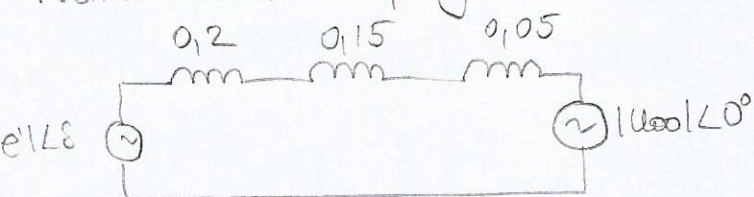
$$X_{30} = \frac{X_{13} X_{23}}{X_{12} + X_{13} + X_{23}} = 0,00625$$



$$X_{AB} = X_L + X_D + \frac{X_L X_D}{X_{D0}} = 0,156 = X_p$$

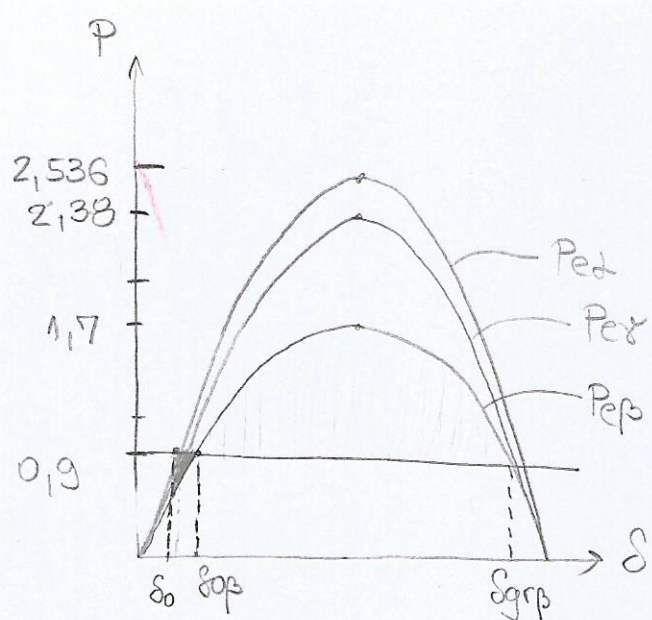
$$P_p = \frac{|e'11000|}{X_p} \sin \delta = \frac{0,951}{0,156} \sin \delta = \underline{\underline{1,7 \sin \delta}}$$

Nakon kvara (isključuje se vod):



$$X_p = 0,4$$

$$P_p = \frac{0,951}{0,4} \sin \delta = \underline{\underline{2,38 \sin \delta}}$$



$$P_m = 0,9$$

$$P_{el} = 2,536 \sin \delta$$

$$P_{po} = 1,7 \sin \delta$$

$$P_{ex} = 2,38 \sin \delta$$

$$A_d > A_a$$

Sustav je stabilan.

$$A_a = \int_{\delta_0}^{\delta_{\beta}} (P_m - 1,7 \sin \delta) d\delta$$

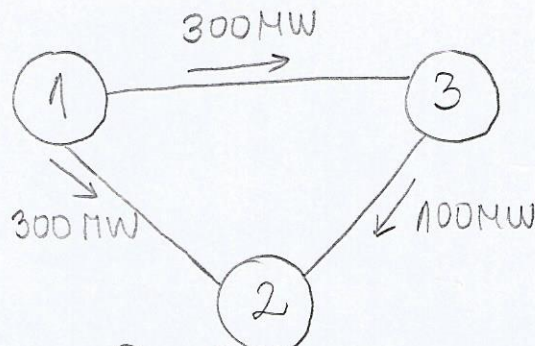
$$A_d = \int_{\delta_{\beta}}^{\delta_{grb}} (1,7 \sin \delta - P_m) d\delta$$

21.11.2019. 12.2020.

4. ZADATAK

- interkonekcija
- isklj. vod 1-3
- max opt. 500MW
- sek. reg. : svi sustavi jednako sudjeluju

$$\begin{aligned} P_{G1} &= 10000 \text{ MW} \\ P_{L1} &= 9400 \text{ MW} \\ K_{G1} &= 2700 \text{ MW/Hz} \\ K_{L1} &= 300 \text{ MW/Hz} \end{aligned}$$



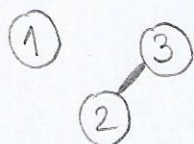
$$\begin{aligned} P_{G2} &= 2000 \\ P_{L2} &= 2400 \\ K_{G2} &= 550 \\ K_{L2} &= 50 \end{aligned}$$

$$\begin{aligned} P_{G3} &= 1000 \\ P_{L3} &= 1200 \\ K_{G3} &= 250 \\ K_{L3} &= 50 \end{aligned}$$

Isključen vod 1-3:

- sustav 1 vidi kao ispad potrošnje 600MW
- sustav 3 vidi kao ispad električne

SUSTAV 1



- 1 u otvorenom pogonu
- gubitak potrošnje 600MW → frekv. raste

$$\Delta f = \frac{\Delta P}{K_G + K_L} = \frac{600}{3000} = +0,2 \text{ Hz}$$

$$f = 50,2 \text{ Hz}$$

Primarna:

$$P_{G1}' = P_{G1} + \Delta P_{G1} + \delta P_{G1} = 10000 - 2700 \cdot 0,2 + 0 = 9460 \text{ MW}$$

$$P_{L1}' = P_{L1} + \Delta P_{L1} + \delta P_{L1} = 9400 + 300 \cdot 0,2 + 0 = 9460 \text{ MW}$$

Sekundarna

$$\Delta f = -0,2 \text{ Hz} \rightarrow f = 49,8 \text{ Hz}, \quad \Delta P = \Delta f (K_G + K_L) = -0,2 \cdot 3000 = -600 \text{ MW}$$

$$P_{G1}'' = P_{G1}' + \Delta P_{G1}' + \delta P_{G1}' = 9460 - 2700 \cdot (-0,2) - 600 = 9400 \text{ MW}$$

$$P_{L1}'' = P_{L1}' + \Delta P_{L1}' + \delta P_{L1}' = 9460 + 300 \cdot (-0,2) + 0 = 9400 \text{ MW}$$

SUSTAV 2-3

Ispad proizvodne jedinice 600MW → Fr. se smanjila

$$\Delta f = \frac{-600}{900} = -0,667 \text{ Hz} \rightarrow f = 49,33 \text{ Hz}$$

$$P_{G2}' = P_{G2} + \Delta P_{G2} + \delta P_{G2} = 2000 - (-0,667) \cdot 550 + 0 = 2366,85 \text{ MW}$$

$$P_{G3}' = P_{G3} + \Delta P_{G3} + \delta P_{G3} = 1000 - (-0,667) \cdot 250 + 0 = 1166,75 \text{ MW}$$

$$P_{L2}' = P_{L2} + \Delta P_{L2} + \delta P_{L2} = 2400 + (-0,667) \cdot 50 + 0 = 2366,65 \text{ MW}$$

$$P_{L3}' = P_{L3} + \Delta P_{L3} + \delta P_{L3} = 1200 + (-0,667) \cdot 50 + 0 = 1166,65 \text{ MW}$$

$$\sum P_G' \approx \sum P_L'$$

Sekundarna regulacja

$$\Delta f = +0,667 \text{ Hz}, f = 50 \text{ Hz}$$

$$P_{g2}'' = P_{g2}' + \Delta P_{g2}' + \delta P_{g2}' = 2366,85 - (-0,667) \cdot 550 + 300 = 2300 \text{ MW}$$

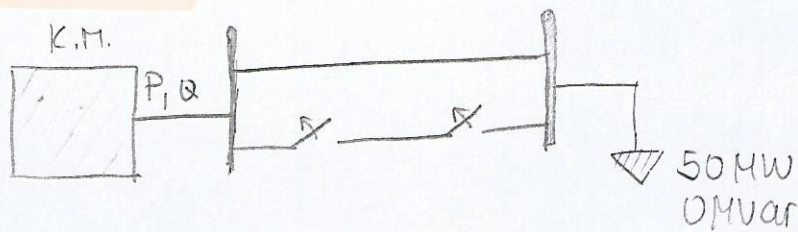
$$P_{g3}'' = P_{g3}' + \Delta P_{g3}' + \delta P_{g3}' = 1166,75 - (-0,667) \cdot 250 + 300 = 1300 \text{ MW}$$

$$P_{e2}'' = P_{e2}' + \Delta P_{e2}' + \delta P_{e2}' = 2366,85 + (-0,667) + 0 = 2400 \text{ MW}$$

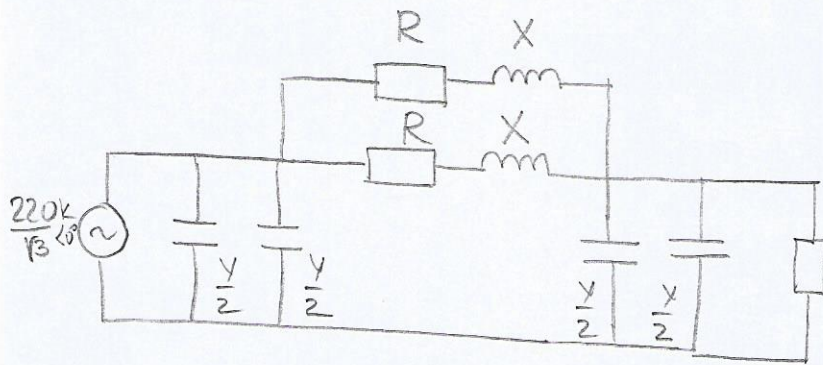
$$P_{e3}'' = P_{e3}' + \Delta P_{e3}' + \delta P_{e3}' = 1166,75 + (-0,667) + 0 = 1200 \text{ MW}$$

$$\sum P_{g}'' \approx \sum P_{e}''$$

5. ZADATAK



2 dalekowoda:



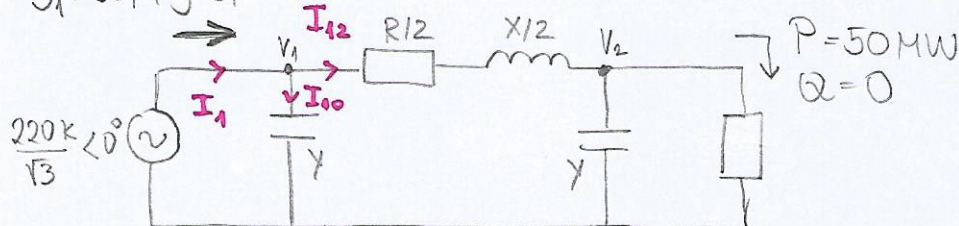
$$R = R \cdot l = 0,05 \cdot 200 = 10 \, \Omega$$

$$X = \omega L \cdot l = 2\pi \cdot 50 \cdot 1,553 \text{ m} \cdot 200 = 97,6 \, \Omega$$

$$Y = j\omega C \cdot l = j2\pi \cdot 50 \cdot 10,73 \text{ n} \cdot 200 = j0,674 \cdot 10^{-3} \, \Omega^{-1}$$

$$\frac{Y}{2} + \frac{Y}{2} = Y$$

$$S_1 = 50,4 - j63,5$$



$$I_1 = \left(\frac{S_1}{\sqrt{3} U_1} \right)^*$$

$$I_{10} = V_1 \cdot Y = \frac{U_1}{\sqrt{3}} \cdot Y$$

$$I_{12} = \left(\frac{S_1}{\sqrt{3} U_1} \right)^* - \frac{U_1}{\sqrt{3}} Y$$

$$U_1 = 220 \angle 0^\circ \text{ kV}$$

$$V_1 = \frac{220 \angle 0^\circ}{\sqrt{3}} \text{ kV}$$

$$V_2 = V_1 - I_{12} \left(\frac{R}{2} + j \frac{X}{2} \right)$$

(FAZNI NAPON)

$$U_2 = V_2 \sqrt{3} = U_1 - I_{12} \left(\frac{R}{2} + j \frac{X}{2} \right) \sqrt{3}$$

(LINIJSKI NAPON)



$$I_{12} = I_1 - I_{10}$$

$$\Delta U_2 = ?$$

Oba dv uključena:

$$P = 50,4 \text{ MW}$$

$$Q = 63,5 \text{ MVar}$$

Jedan dv uključen

$$P = 50,6 \text{ MW}$$

$$Q = 27,8 \text{ MVar}$$

$$U = 220 \text{ kV}$$

$$R = 0,05 \frac{\Omega}{\text{km}}$$

$$L = 1,553 \frac{\text{mH}}{\text{km}}$$

$$C = 10,73 \frac{\text{nF}}{\text{km}}$$

$$l = 200 \text{ km}$$

$$f = 50 \text{ Hz}$$

$$I_1 = \left(\frac{S_1}{\sqrt{3}U_1} \right)^* = \left(\frac{150,4 - j63,514}{\sqrt{3} \cdot 220 \angle 0^\circ (k)} \right)^* = 132,26 + j166,64 \text{ A}$$

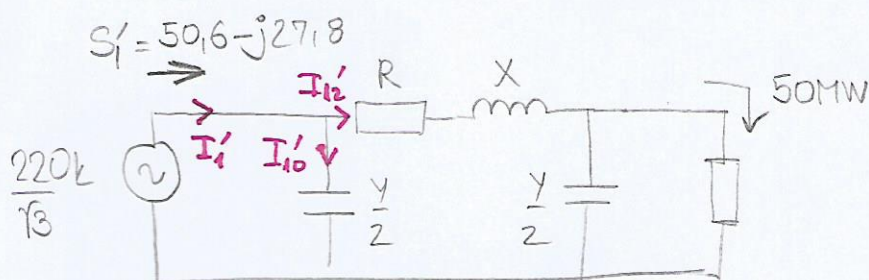
$$I_{10} = \frac{U_1}{\sqrt{3}} \cdot y = \frac{220 k}{\sqrt{3}} \cdot 0,674 \cdot 10^{-3} \angle -90^\circ = -j85,61 \text{ A}$$

$$I_{12} = I_1 - I_{10} = 132,26 + j166,64 + j85,61 = 132,26 - j81,03 \text{ A} \\ = 155,11 \angle -0,55 \text{ A}$$

$$V_2 = V_1 - I_{12} \left(\frac{R}{2} + j \frac{X}{2} \right) = \frac{220 k}{\sqrt{3}} - 155,11 \angle +0,55 \cdot 49,05 \angle 1,469 \\ = \frac{220 k}{\sqrt{3}} + 3296,97 - j6856,67 = \\ = 130494 \angle \approx 0 \Rightarrow U_2 = V_2 \cdot \sqrt{3}$$

$$U_2 = 226 \text{ kV}$$

1 dalekovod:



$$I'_1 = \left(\frac{S'_1}{\sqrt{3}U_1} \right)^* = \frac{50,6 + j27,8 \text{ M}}{\sqrt{3} \cdot 220 k} = 132,79 + j72,96 = 151,51 \angle 0,502$$

$$I'_{10} = \frac{U_1}{\sqrt{3}} \cdot \frac{y}{2} = \frac{220 k}{\sqrt{3}} \cdot \frac{0,674 \cdot 10^{-3}}{2} \angle -\pi/2 = +j42,8$$

$$I'_{12} = I'_1 - I'_{10} = 132,79 + j72,96 - j42,8 = 136,2 \angle 0,223$$

$$V'_2 = V'_1 - I'_{12} (R + jX) = \frac{220 k}{\sqrt{3}} - 136,2 \angle 0,223 \cdot 98,11 \angle 1,469 = \\ = 129,3 \text{ kV}$$

$$U'_2 = V'_2 \cdot \sqrt{3} = 224 \text{ kV}$$

$$\Delta U = |U'_2| - |U_2| = -2 \text{ kV}$$