

## Zadatak 1

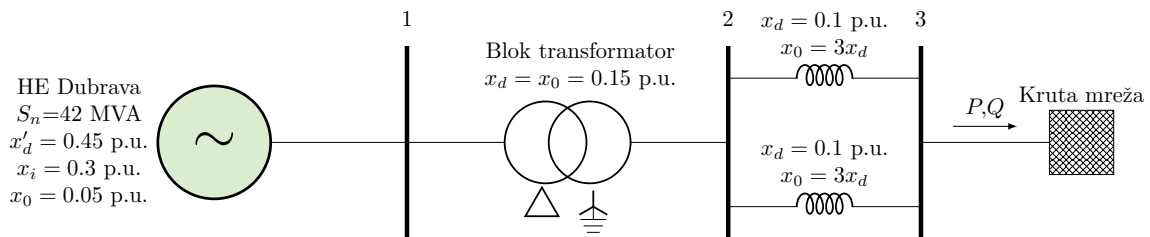
HE Dubrava sastoji se od dva identična agregata. Jedan agregat sastoji se od 48-polnog sinkronog generatora i nazivne snage 42 MVA. Ukupni moment tromosti jednog agregata iznosi  $441 \text{ tm}^2$ . Kolika je ekvivalentna konstanta tromosti HE Dubrava (oba agregata zajedno)? Koliko iznosi maksimalni dozvoljeni poremećaj kako bi početni RoCoF ( $t = 0^+$ ) bio  $< \pm 2 \text{ Hz/s}$ ? Nakon koliko vremena HE Dubrava dostiže frekvenciju 49.2 Hz za maksimalni dozvoljeni poremećaj? U izračunu pretpostaviti da oba agregata rade s konstantnom mehaničkom snagom.

(5 bodova)

## Zadatak 2

Jedan agregat u HE Dubrava (drugi nije u pogonu) spojen je na krutu mrežu preko blok-transformatora i dva paralelna voda te u poduzbuđenom režimu rada u mrežu predaje snagu  $P = 0.9 \text{ p.u.}$  pri  $\cos \varphi = 0.95 \text{ kap.}$  (Slika 1). Napon krute mreže iznosi  $1 \angle 0^\circ \text{ p.u.}$  Na jednom od dva paralelna voda nastaje izravni jednopolni kratki spoj u točki koja se nalazi na 75% duljine voda gledano od sabirnice 2. Nacrtati nadomjesnu shemu sustava sa slike 1 te odrediti izraz i skicirati krivulje za prijenos električne snage između generatora i krute mreže za slučajeve:

- prije nastanka kratkog spoja;
- tijekom kratkog spoja;
- nakon isključenja voda u kvaru.



Slika 1: Spoj HE Dubrava s krutom mrežom

(9 bodova)

## Zadatak 3

Za sustav sa slike 1 odrediti kritični kut i kritično vrijeme uklanjanja kvara za izravni trolepolni kratki spoj na sabirnici 3. Podaci za izračun konstante tromosti jednog agregata nalaze se u Zadatku 1. Generator u naduzbuđenom režimu rada u mrežu predaje snagu  $P = 0.5 \text{ p.u.}$  pri  $\cos \varphi = 0.95 \text{ ind.}$  Napon krute mreže iznosi  $1 \angle 0^\circ \text{ p.u.}$  Nacrtati nadomjesnu shemu sustava te odrediti izraz i skicirati krivulje za prijenos snage između generatora i krute mreže za slučajeve:

- prije nastanka kratkog spoja;
- tijekom kratkog spoja;
- nakon isključenja kvara.

(6 bodova)

## Zadatak 4

Nacrtajte blok dijagram dinamičkog sustava opisanog jednadžbama (1)–(2), gdje su  $H$ ,  $f_n$ ,  $P_m$  i  $C$  konstante, a  $\delta$  i  $\omega$  varijable stanja.

$$\frac{d\delta}{dt} = 2\pi f_n (\omega - 1) \quad (1)$$

$$2H \frac{d\omega}{dt} = P_m - C \sin \delta \quad (2)$$

(2 boda)

## Zadatak 5

Kakve vrste kutne nestabilnosti pri malim poremećajima postoje s obzirom na oscilatornost? Skicirajte te promjene kuta opterećenja u vremenu.

(2 boda)

## Zadatak 6

Nacrtajte karakteristiku snaga-kut za slučaj dugog otklanjanja kvara (nestabilno stanje) i slučaj kratkog otklanjanja kvara (nestabilno stanje). Označite površine ubrzavanja i usporavanja generatora. O čemu ovisi stabilnost odziva?

(2 boda)

## Zadatak 7

Što su FACTS uređaji? Prikažite osnovnu podjelu FACTS uređaja. Objasnite osnovnu ideju serijske kapacitivne kompenzacije i nabrojite neke FACTS uređaje za takvu vrstu kompenzacije.

(2 boda)

## Zadatak 8

Što je osnovni građevni element Wide Area Monitoring sustava? Koja je uloga GPS-a u WAMS-u?

(1 bod)

## Zadatak 9

Objasnite princip rada transformatora s poprečnom regulacijom kuta (*Phase shifting transformer*).

(1 bod)

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## 1. ZADATAK

2 identična agregata

$$p = 24$$

$$S_n = 42 \text{ MVA}$$

$$J = 441 \cdot 10^3 \text{ kgm}^2$$

$$H_{\text{exv}} = ?$$

$$\frac{df}{dt}(t=0) < \pm 2 \frac{\text{Hz}}{\text{s}}$$

$$\delta p_e = ?$$

$$f' = 49,2 \text{ Hz}$$

$$t = ?$$

$$a) \quad E_k = \frac{J \left( 2\pi \frac{f}{p} \right)^2}{2} = \frac{441 \cdot 10^3 \left( 2\pi \frac{50}{24} \right)^2}{2} = 37,78 \text{ Ws}$$

$$E_{\text{uk}} = 2 \cdot E_k = 75,56 \cdot 10^6 \text{ Ws}$$

$$H_{\text{exv}} = \frac{E_{\text{uk}}}{\sum S_n} = \frac{75,56 \cdot 10^6 \text{ Ws}}{84 \text{ MW}} = 0,9 \text{ s}$$

$$b) \quad \text{PoCoF}(t=0+) < \pm 2 \text{ Hz/s} \quad /: 50 \text{ Hz} \\ < \pm 0,04 \text{ pu/s}$$

$$\frac{d\omega_e}{dt} = \pm 0,04 \text{ pu/s}$$

$$2H \frac{d\omega_e}{dt} = p_m - p_e \rightarrow 2H \frac{d\omega_e}{dt} = \delta p$$

$$2 \cdot 0,9 \cdot 0,04 = \delta p_{\text{max}}$$

$$\delta p_{\text{max}} = 0,072 \text{ p.u.} / \cdot S_B$$

$$\delta p_{\text{max}} = 6,048 \text{ MVA}$$

$$c) \quad f(t_1) = 49,2 \text{ Hz}$$

$$\delta p = 6,048 \text{ MVA}$$

$$t_1 = ?$$

$$\frac{df}{dt} = 2 \frac{\text{Hz}}{\text{s}}$$

$$\Delta f(t_1) = 0,8 \text{ Hz}$$

$$\Delta f = \frac{df}{dt}$$

$$\Delta f(t_1) = \int_0^{t_1} \frac{df}{dt} dt$$

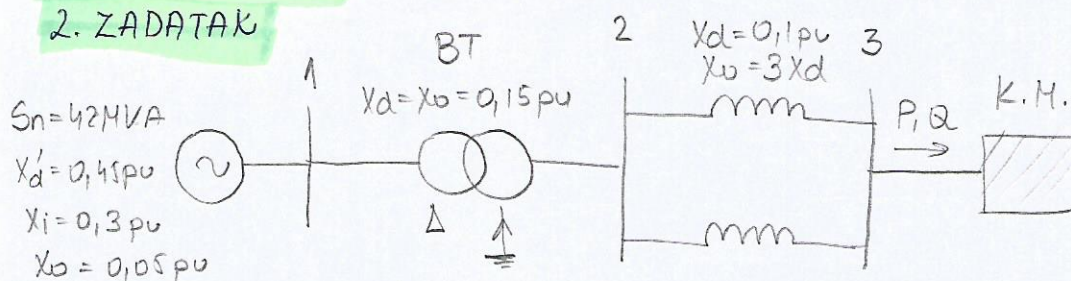
$$0,8 = \int_0^{t_1} 2 dt = 2(t_1 - 0) = 2t_1$$

$$t_1 = \frac{0,8}{2} = 0,4 \text{ s}$$



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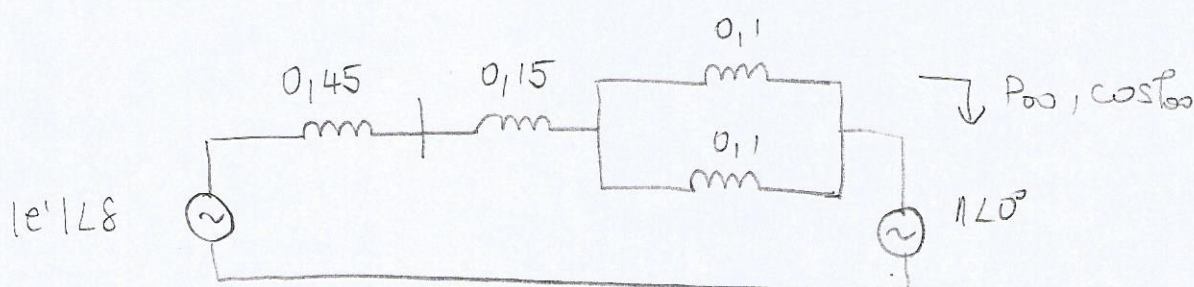
## 2. ZADATAK



$P = 0,9 \text{ p.u.}$   
 $\cos \varphi = 0,95 \text{ kap.}$   
 $U_{00} = 1 \angle 0^\circ \text{ p.u.}$   
 1PKS, 75% dv od sab. 2

Prilje KUARA

$$X_f = X_i + X_0$$



$$X_d = 0,45 + 0,15 + 0,05 = 0,65 \text{ p.u.}$$

$$|e'| 128 = |U_{00}| \angle 0^\circ + j I_{00} X_d$$

$$S_{00} = P_{00} + j Q_{00} = U_{00} \cdot I_{00}^*$$

$$I_{00} = \left( \frac{S_{00}}{U_{00}} \right)^* = \left( \frac{P_{00} + j P_{00} \tan \varphi_{00}}{U_{00}} \right)^* = 0,9 - j 0,9 \cdot \tan (\arccos (0,95))$$

$$= 0,9 + j 0,3 = 0,95 \angle 18,43^\circ$$

$$|e'| 128 = |U_{00}| \angle 0^\circ + j I_{00} X_d = 1 + 0,65 \angle 90^\circ \cdot 0,95 \angle 18,43^\circ =$$

$$= 1 - 0,195 + j 0,586 = 0,805 + j 0,586 =$$

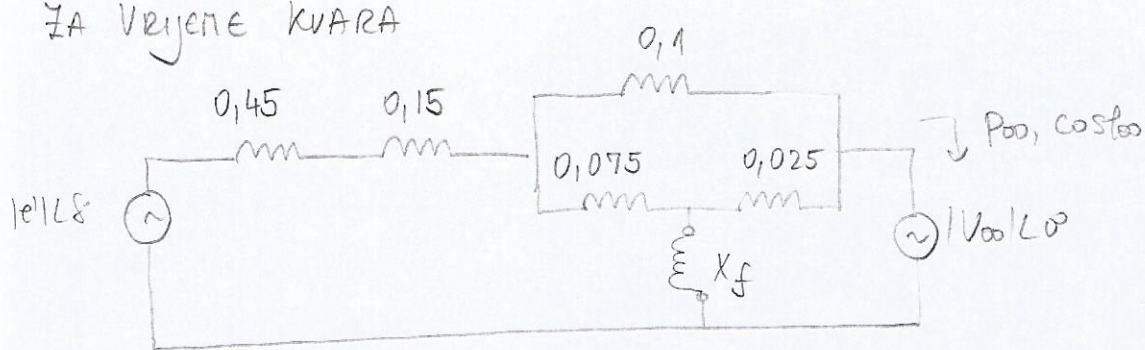
$$= 0,996 \angle 36,05^\circ$$

$$P_e = \frac{|e'| |U_{00}|}{X_d} \sin \delta = \frac{0,996 \cdot 1}{0,65} \sin \delta = 1,532 \sin \delta$$

$$P_{pm} = 1,532 \sin (36,05^\circ) = 0,9$$

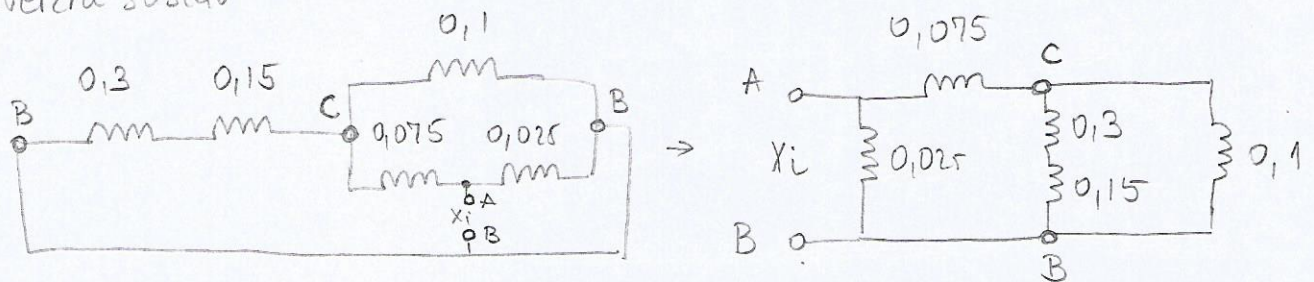


7A Vrijeme kvara



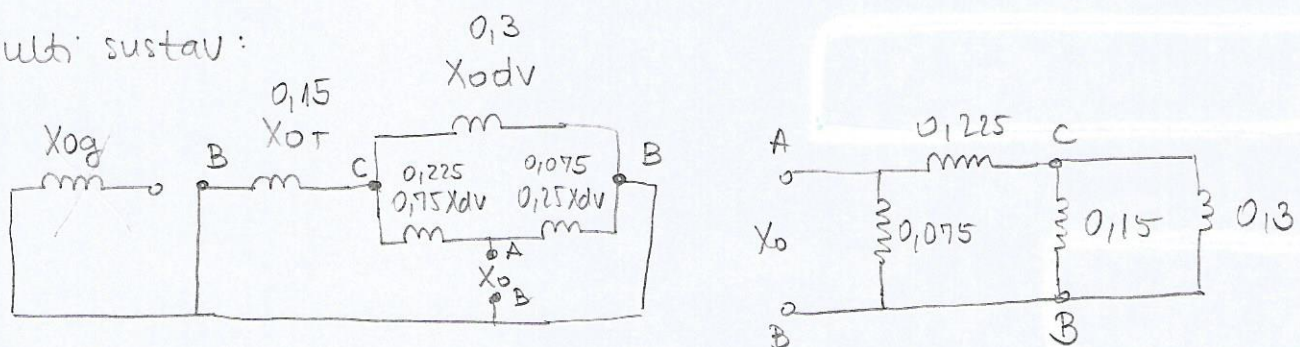
$$X_f = X_i + X_o$$

Inverzni sustav:



$$X_i = [0,111(0,3 + 0,15) + 0,075] \parallel 0,025 = \underline{\underline{0,023}}$$

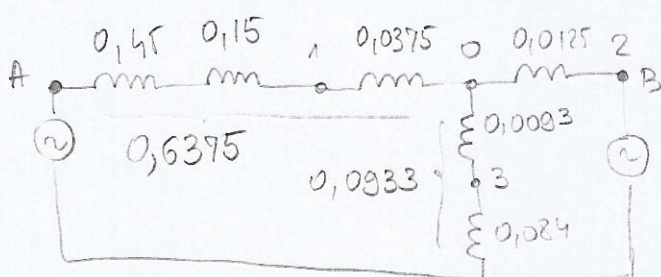
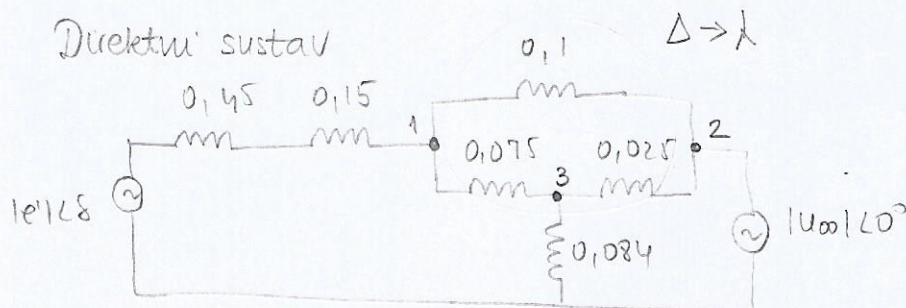
Nulli sustav:



$$X_o = [0,3 \parallel 0,15 + 0,225] \parallel 0,075 = \underline{\underline{0,061}}$$

$$X_f = X_i + X_o = 0,023 + 0,061 = 0,084$$

Direktni sustav



$\Delta \rightarrow \lambda$

$$X_{10} = \frac{X_{12} X_{13}}{X_{12} + X_{13} + X_{23}} = 0,0375$$

$$X_{20} = \frac{X_{12} X_{23}}{X_{12} + X_{13} + X_{23}} = 0,0125$$

$$X_{30} = \frac{X_{13} X_{23}}{X_{12} + X_{13} + X_{23}} = 0,0083$$

$$X_{AB} = X_L + X_D + \frac{X_L X_D}{X_{D0}} =$$

$$= 0,6375 + 0,0125 + \frac{0,6375 \cdot 0,0125}{0,0083} =$$

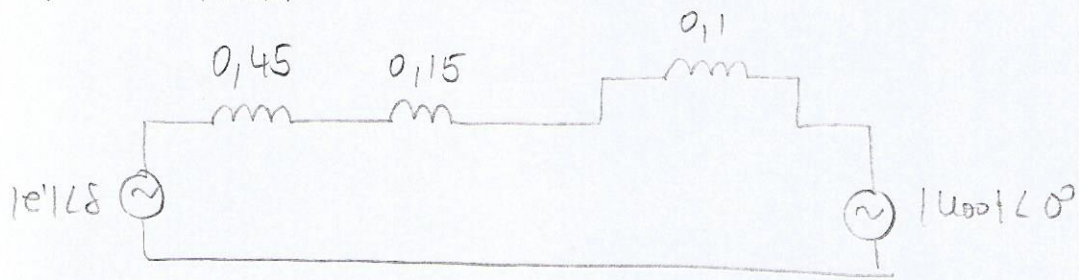
$$= \underline{\underline{0,7354}}$$

$$V_{AB} = X_B = 0,7354$$



$$P_e^B = \frac{|e'| |U_{\infty}|}{X_B} \sin \delta = \frac{0,996 \cdot 1}{0,7354} \sin \delta = 1,35 \sin \delta$$

NAPON KVARA



$$X_{\Sigma} = 0,45 + 0,15 + 0,1 = 0,7$$

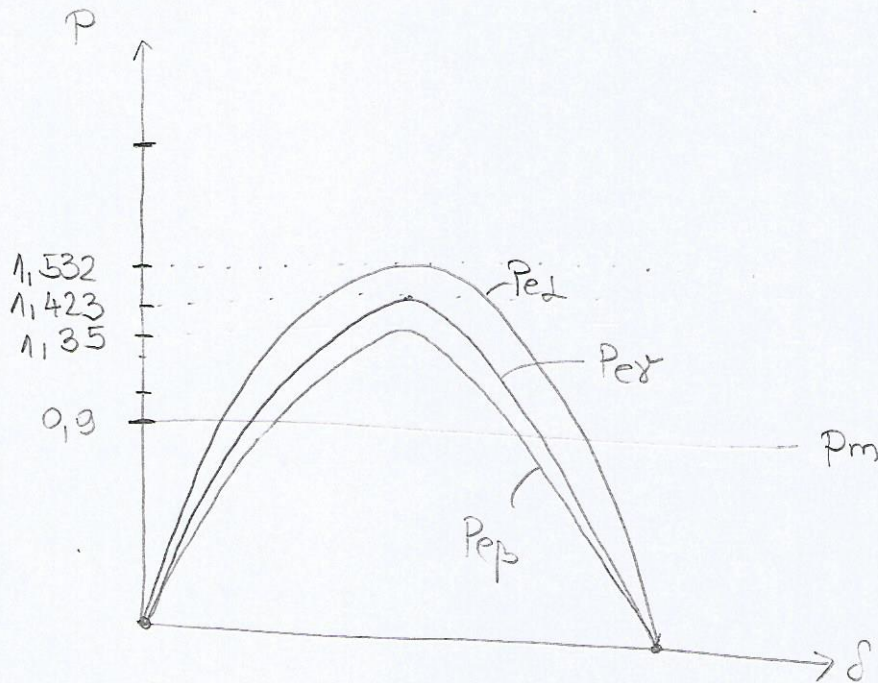
$$P_{e\Sigma} = \frac{|e'| |U_{\infty}|}{X_{\Sigma}} \sin \delta = \frac{0,996}{0,7} \sin \delta = 1,423 \sin \delta$$

$$P_m = 0,9$$

$$P_e^d = 1,532 \sin \delta$$

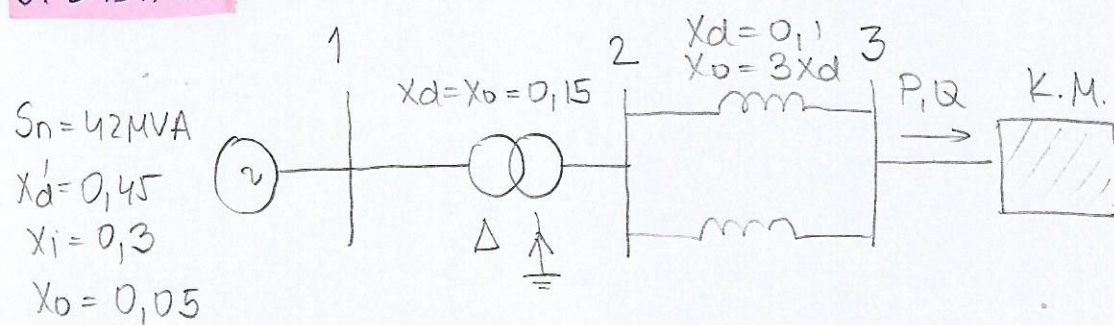
$$P_e^B = 1,35 \sin \delta$$

$$P_e^{\Sigma} = 1,423 \sin \delta$$





## 3. ZADATAK



- odrediti kr. kut i kr. vrijeme uklanjanja kvara
  - 3PKS na sabirnici 3
  - naduzbuđeni režim rada
- $P = 0,5 \text{ p.u.}$ ,  $\cos \varphi = 0,95 \text{ ind.}$   
 $U_{00} = 1 \angle 0^\circ \text{ p.u.}$

$$P = 24$$

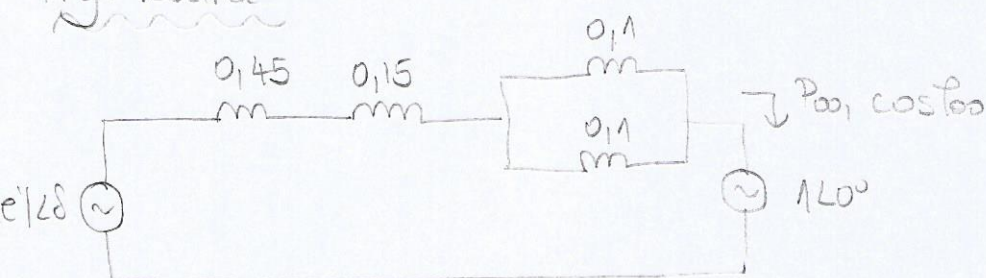
$$S_n = 42 \text{ MVA}$$

$$J = 441 \cdot 10^3 \text{ kgm}^2$$

$$H = \frac{J \left( 2\pi \frac{f}{P} \right)^2}{2 S_n} = \frac{441 \cdot 10^3 \left( 2\pi \frac{50}{24} \right)^2}{2 \cdot 42 \text{ M}}$$

$$\underline{\underline{H = 0,95}}$$

Prije kvara



$$X_d = 0,45 + 0,15 + 0,05 = 0,65$$

$$e' \angle \delta = |U_{00}| \angle 0^\circ + j X_d \cdot I_{00}$$

$$I_{00} = \left( \frac{S}{U_{00}} \right)^* = \left( \frac{P_{00} + j P_{00} \tan \varphi_{00}}{1 \angle 0^\circ} \right)^* = 0,5 - j 0,5 \cdot \tan(\arccos(0,95))$$

$$= 0,5 - j 0,164$$

$$\underline{\underline{I_{00} = 0,526 \angle -18,16^\circ}}$$

$$e' \angle \delta = 1 + 0,526 \angle -18,16^\circ \cdot 0,65 \angle 90^\circ = 1,107 + j 0,325$$

$$\underline{\underline{e' \angle \delta = 1,154 \angle 16,36^\circ}} \quad (\delta = 16,36^\circ = 0,285 \text{ rad})$$

$$P_{ed} = \frac{1,154 \cdot 1}{0,65} \sin \delta = \underline{\underline{1,77 \sin \delta}}$$

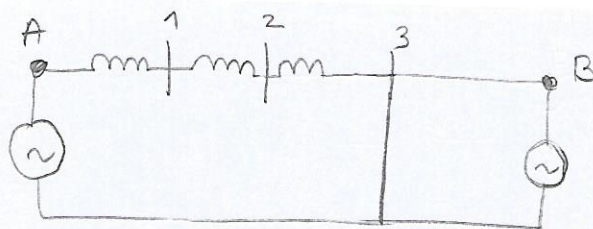
$$\underline{\underline{P_{m} = 0,5}}$$



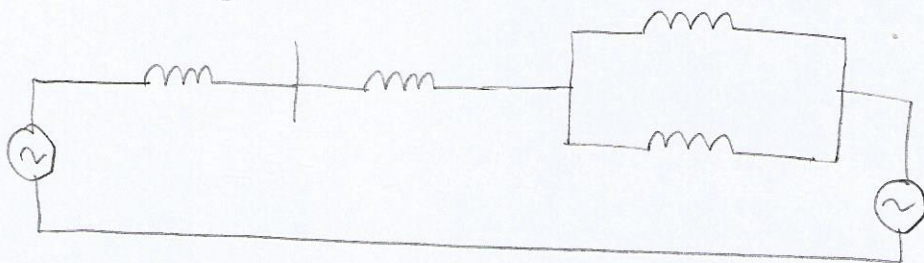
Šta nijeme kvara

$$(P_e^b = 0)$$

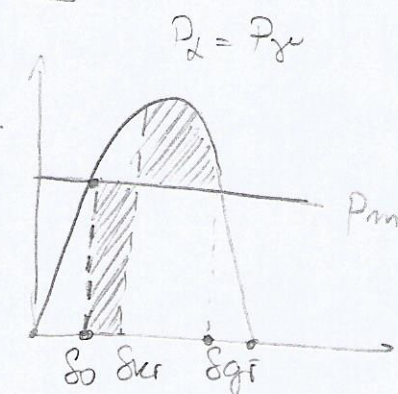
3PKS



Nakon kvara



$$P_e^y = P_e^d = 1,778 \sin \delta$$



Površina ubravanja

$$A_a = p_m (\delta_{kr} - \delta_0)$$

Površina usporavanja

$$A_d = \int_{\delta_{kr}}^{\delta_{gr}} (P_y - p_m) d\delta$$

$$A_a = A_d$$

$$\delta_{gr} = \pi - \delta_0 = \pi - 0,285$$

$$\delta_{gr} = 2,856$$

$$p_m \delta_{kr} - p_m \delta_0 = 1,77 (-\cos \delta_{gr} - (-\cos \delta_{kr})) - p_m (\delta_{gr} - \delta_{kr})$$

$$p_m \delta_{kr} - p_m \delta_0 = -1,77 \cos \delta_{gr} + 1,77 \cos \delta_{kr} - p_m \delta_{gr} + p_m \delta_{kr}$$

$$1,77 \cos \delta_{kr} = 1,77 \cos \delta_{gr} - p_m \delta_0 + p_m \delta_{gr} \quad / : 1,77$$

$$\cos \delta_{kr} = \cos \delta_{gr} + \frac{p_m (\delta_{gr} - \delta_0)}{1,77} = \cos (2,856) + \frac{0,5 (2,856 - 0,285)}{1,77}$$

$$\delta_{kr} = 1,8 \text{ rad} = 103^\circ$$

$$t_{kr} = \sqrt{\frac{4H (\delta_{kr} - \delta_0)}{\omega s p_m}} = \sqrt{\frac{4 \cdot 0,9 (1,8 - 0,285)}{2\pi \cdot 50 \cdot 0,5}} = 0,186 \text{ s} = 186 \text{ ms}$$



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#### 4. ZADATAK

$H, f_n, P_m, C$  konstante

$\delta, \omega$  varijable stanja

$$\frac{d\delta}{dt} = 2\pi f_n (\omega - 1)$$

$$2H \frac{d\omega}{dt} = P_m - C \sin \delta$$

$$\frac{d\delta}{dt} = 2\pi f_n (\omega - 1)$$

$$\frac{d\omega}{dt} = \frac{1}{2H} (P_m - C \sin \delta)$$

