

Zadatak 1

Tri sustava rade paralelno. Snage proizvodnje i potrošnje u sustavima zadani su u tablici ispod. Što će se dogoditi ako se istodobno smanji proizvodnja u sustavima 1 i 2 za po 100 MW svaki. Odstupanja u ravnoteži proizvodnje i potrošnje do 10 MW su dopuštena.

Izračunati konačno stanje u svim sustavima te sva međustanja koja sustavi prolaze prije novog konačnog stacionarnog stanja. U sekundarnoj regulaciji sudjeluje samo sustav 3.

(9 bodova)

Proizvodnja		Potrošnja	
Snaga	Regulacijska energija	Snaga	Regulacijska energija
$P_{g1} = 400 \text{ MW}$	$K_{g1} = 150 \frac{\text{MW}}{\text{Hz}}$	$P_{l1} = 200 \text{ MW}$	$K_{l1} = 50 \frac{\text{MW}}{\text{Hz}}$
$P_{g2} = 350 \text{ MW}$	$K_{g2} = 250 \frac{\text{MW}}{\text{Hz}}$	$P_{l2} = 300 \text{ MW}$	$K_{l2} = 100 \frac{\text{MW}}{\text{Hz}}$
$P_{g3} = 550 \text{ MW}$	$K_{g3} = 300 \frac{\text{MW}}{\text{Hz}}$	$P_{l3} = 800 \text{ MW}$	$K_{l3} = 100 \frac{\text{MW}}{\text{Hz}}$

Zadatak 2

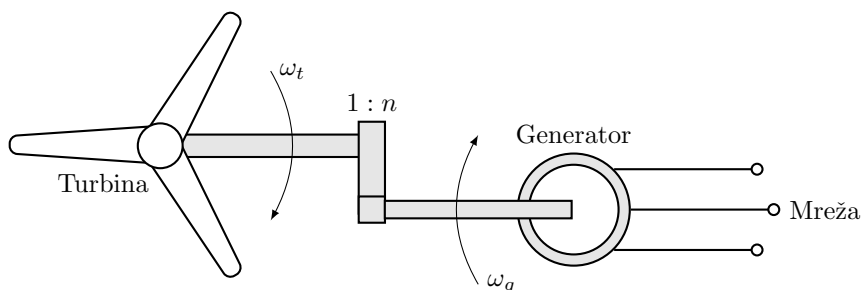
Na slici 1 prikazan je vjetroagregat kojem je rotor turbine povezan s rotorom generatora preko idealnog multiplikatora s prijenosnim omjerom $1 : n$; drugim riječima, mehanička brzina rotora generatora n je puta veća od mehaničke brzine rotora turbine:

$$\omega_g = n \cdot \omega_t = 100 \cdot \omega_t \quad (1)$$

Moment tromosti turbine iznosi $J_t = 5 \cdot 10^6 \text{ kgm}^2$, a moment tromosti 6-polnog generatora iznosi $J_g = 100 \text{ kgm}^2$. Nazivna snaga vjetroagregata iznosi 2 MVA, dok je frekvencija mreže 50 Hz. Potrebno je izračunati:

- konstantu tromosti turbine H_t pri sinkronoj brzini
- konstantu tromosti generatora H_g pri sinkronoj brzini;
- ukupnu konstantu tromosti vjetroagregata H pri sinkronoj brzini;
- promjenu kinetičke energije vjetroagregata ako se brzina vrtnje rotora smanji s 1 p.u. sinkrone brzine na 0.8 p.u. sinkrone brzine.

(8 bodova)



Slika 1: Vjetroagregat

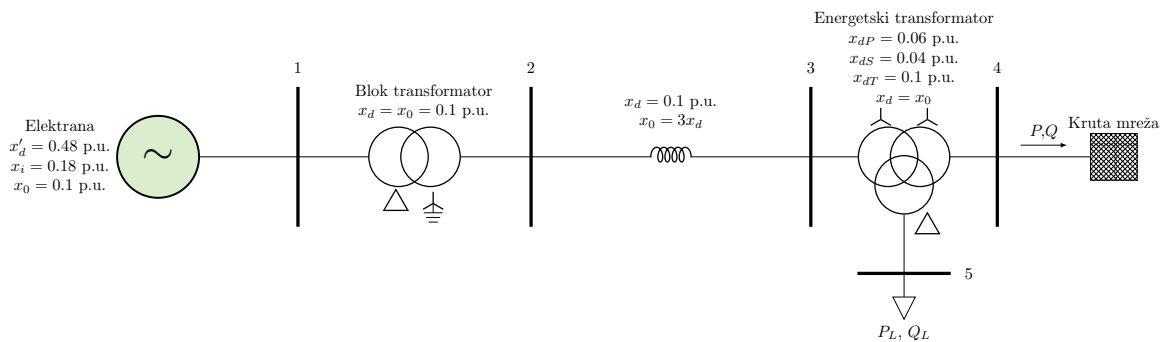
Zadatak 3

Neka elektrana spojena je na krutu mrežu preko blok-transformatora, dalekovoda i tronamotnog energetskog transformatora prema slici 2. Tercijar (T) tronamotnog transformatora napaja lokalnu potrošnju $P_L = 0.1$ p.u., $\cos \varphi_L = 1.00$. Potrošnju modelirajte kao konstantnu impedanciju koja bi trošila zadanu snagu pri naponu $|v_L| = |v_5| = 1.0$ p.u. Sekundarom (S) tronamotnog transformatora smatrajte namot priključen na sabirnicu 4.

Elektrana u poduzbuđenom režimu rada u krutu mrežu predaje snagu $P = 0.7$ p.u. pri $\cos \varphi = 0.95$. Napon krute mreže iznosi $1\angle 0^\circ$ p.u. Na polovici dalekovoda nastaje dvopolni kratki spoj sa zemljom. Potrebno je 1) odrediti kritični kut uklanjanja kvara i 2) nacrtati nadomjesnu shemu sustava sa slike 2 te odrediti izraz i skicirati krivulje za prijenos električne snage između elektrane i krute mreže za slučajeve:

- prije nastanka kratkog spoja;
- tijekom kratkog spoja;
- nakon prolaska kratkog spoja (bez isključenja voda).

(15 bodova)



Slika 2: Spoj elektrane s krutom mrežom

Zadatak 4

Na slici 3 prikazan je dvostruki dalekovod u praznom hodu. Za koliko se promjeni napon sabirnice 2 ako se uključi prigušnica u spoju zvijezda nazivne snage $S_n = 50$ MVA (nazivna snaga odnosi se na nazivni napon prigušnice 220 kV)? Napon krute mreže iznosi 220 kV. Parametri voda su sljedeći: $R = 0.05 \Omega/\text{km}$, $L = 1.553 \text{ mH/km}$, $C = 10.73 \text{ nF/km}$. Parametri su izraženi po fazi za jedan dalekovod. Duljina dalekovoda je 200 km. Frekvencija sustava je 50 Hz.

(8 bodova)



Slika 3: Dalekovod u praznom hodu

Zadatak 5

Nacrtajte fazorski dijagram sustava sa slike 2 u direktnom sustavu prije nastanka kvara. Zanimarite grupu spoja i satni broj transformatora u modelu.

(5 bodova)

Zadatak 6

Dva trofazna asinkrona motora opterećena nazivnim mehaničkim opterećenjem ($P_{n1}^m = 3 \text{ MW}$, $\cos \varphi_1 = 0.8$, $\eta_1 = 0.95$, $P_{n2}^m = 4.0 \text{ MW}$, $\cos \varphi_2 = 0.70$, $\eta_2 = 0.98$) paralelno su priključena na zajedničke sabirnice u mreži nazivnog napona 1 kV. η predstavlja učinkovitost motora. Potrebno je izračunati:

- ukupnu struju koja teče iz mreže prema sabirnicama na koje su motori priključeni;
- $\cos \varphi$ na predmetnim sabirnicama;
- snagu kondenzatorske baterije koju treba paralelno priključiti na motorske sabirnice da bi na njima $\cos \varphi$ iznosio 0.95; zašto se kompenzira do tog iznosa $\cos \varphi$?
- Koliko iznosi kapacitet kondenzatorske baterije po fazi ako je ona spojena u spoj trokut?

(5 bodova)

1. ZADATAK

$$\delta g_1 = \delta g_2 = -100 \text{ MW}$$

Sekundarna regul. \rightarrow Sustav 3

Smanjila se proizvod \rightarrow Frekv. se smanji

PROIZVODNJA		POTROŠNJA	
Snaga	Reg.en.	Snaga	Reg.en.
$P_{g1} = 400$	$K_{g1} = 150$	$P_{11} = 200$	$K_{11} = 50$
$P_{g2} = 350$	$K_{g2} = 250$	$P_{12} = 300$	$K_{12} = 100$
$P_{g3} = 550$	$K_{g3} = 300$	$P_{13} = 800$	$K_{13} = 100$

$$\Delta f = \frac{-200}{700+250} = -0,2 \text{ Hz}$$

$$\Delta P_{g1} = -K_{g1} \cdot \Delta f = -150 \cdot (-0,2) = 30 \text{ MW}$$

$$\Delta P_{g2} = 50 \text{ MW}$$

$$\Delta P_{g3} = 60 \text{ MW}$$

$$\Delta P_{e1} = K_{e1} \cdot \Delta f = 50 \cdot (-0,2) = -10 \text{ MW}$$

$$\Delta P_{e2} = -20 \text{ MW}$$

$$\Delta P_{e3} = -20 \text{ MW}$$

$$P_{g1}' = P_{g1} + \Delta P_{g1} + \delta P_{g1} = 400 + 30 - 100 = 330 \text{ MW}$$

$$P_{g2}' = P_{g2} + \Delta P_{g2} + \delta P_{g2} = 350 + 50 - 100 = 300 \text{ MW}$$

$$P_{g3}' = P_{g3} + \Delta P_{g3} + \delta P_{g3} = 550 + 60 + 0 = 610 \text{ MW}$$

$$\sum P_g' = \sum P_e'$$

$$1240 \approx 1250$$

$$P_{e1}' = P_{e1} + \Delta P_{e1} + \delta P_{e1} = 200 - 10 + 0 = 190 \text{ MW}$$

$$P_{e2}' = P_{e2} + \Delta P_{e2} + \delta P_{e2} = 300 - 20 + 0 = 280 \text{ MW}$$

$$P_{e3}' = P_{e3} + \Delta P_{e3} + \delta P_{e3} = 800 - 20 + 0 = 780 \text{ MW}$$

Sekundarna regulacija: $\Delta f = +0,2 \text{ Hz}$

$$\Delta P = \Delta f (\sum K_g + \sum K_e) = 0,2 \cdot 950 = 190 \text{ MW}$$

$$\Delta P_{g1}' = -30 \text{ MW}$$

$$\Delta P_{e1}' = 10 \text{ MW}$$

$$\Delta P_{g2}' = -50 \text{ MW}$$

$$\Delta P_{e2}' = 20 \text{ MW}$$

$$\Delta P_{g3}' = -60 \text{ MW}$$

$$\Delta P_{e3}' = 20 \text{ MW}$$

$$P_{g1}'' = P_{g1}' + \Delta P_{g1}' + \delta P_{g1}' = 330 - 30 + 0 = 300 \text{ MW}$$

$$P_{e1}'' = 190 + 10 + 0 = 200 \text{ MW}$$

$$P_{g2}'' = 300 - 50 + 0 = 250 \text{ MW}$$

$$P_{e2}'' = 280 + 20 + 0 = 300 \text{ MW}$$

$$P_{g3}'' = 610 - 60 + 190 = 740 \text{ MW}$$

$$P_{e3}'' = 780 + 20 + 0 = 800 \text{ MW}$$

LIR 2019./2020.

2. ZADATAK

$$\omega_g = n \cdot \omega_t = 100 \omega_t$$

$$J_t = 5 \cdot 10^6 \text{ kgm}^2$$

$$p = 3$$

$$J_g = 100 \text{ kgm}^2$$

$$S_n = 2 \text{ MVA}$$

$$f = 50 \text{ Hz}$$

$$a) H_t = ?$$

$$b) H_g = ?$$

$$c) H_{uk} = ?$$

$$d) \Delta E_k = ?$$

$$1 \text{ p.u.} \rightarrow 0.8 \text{ p.u.}$$

$$\omega_g = 2\pi f_g = 2\pi \frac{f_n}{p} = 2\pi \frac{50}{3} = \frac{100\pi}{3} \frac{\text{rad}}{\text{s}}$$

$$\omega_t = \frac{\omega_g}{100} = \frac{\pi}{3} \frac{\text{rad}}{\text{s}}$$

$$E_{kg} = \frac{J \omega_g^2}{2} = \frac{100 \cdot \left(\frac{100\pi}{3}\right)^2}{2} = 548311 \text{ Ws}$$

$$E_{kt} = \frac{J \omega_t^2}{2} = \frac{5 \cdot 10^6 \cdot \left(\frac{\pi}{3}\right)^2}{2} = 2741556 \text{ Ws}$$

$$a) H_t = \frac{E_{kt}}{S_n} = \frac{2741556}{2 \text{ M}} = 1.37 \text{ s}$$

$$b) H_g = \frac{E_{kg}}{S_n} = \frac{548311}{2 \text{ M}} = 0.274 \text{ s}$$

$$c) H_{uk} = \frac{\sum H_i S_i}{S_n} = \frac{1.37 \cdot 2 \text{ M} + 0.274 \cdot 2 \text{ M}}{2 \text{ M}} = 1.6 \text{ s}$$

$$d) 1 \text{ p.u.} \rightarrow 0.8 \text{ p.u.}$$

$$E'_{kg} = \frac{J (0.8 \omega_g)^2}{2} = 0.8^2 E_{kg}$$

$$E'_{kt} = 0.8^2 E_{kt}$$

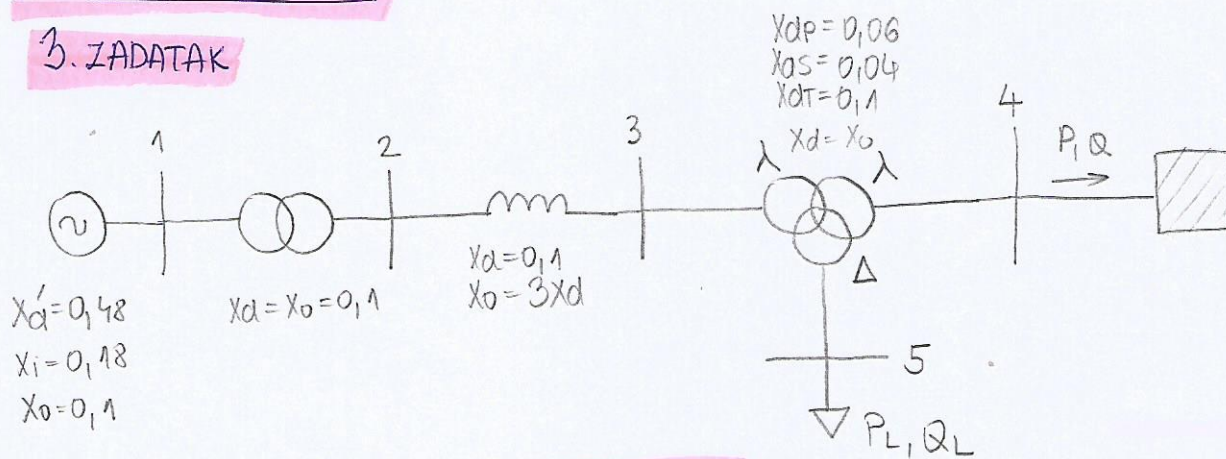
$$\Delta E_k = E'_k - E_k$$

$$= 0.8^2 E_{kuk} - E_{kuk}$$

$$= -1184352.12 \text{ Ws}$$

KIR 2019./2020.

3. ZADATAK



$$P_L = 0,1 \text{ p.u.}$$

$$\cos \varphi_L = 1$$

$$|U_L| = |U_5| = 1 \text{ p.u.}$$

$$Z_L = \frac{U^2}{P} = \frac{1}{0,1} = 10 \Omega$$

$$P = 0,7$$

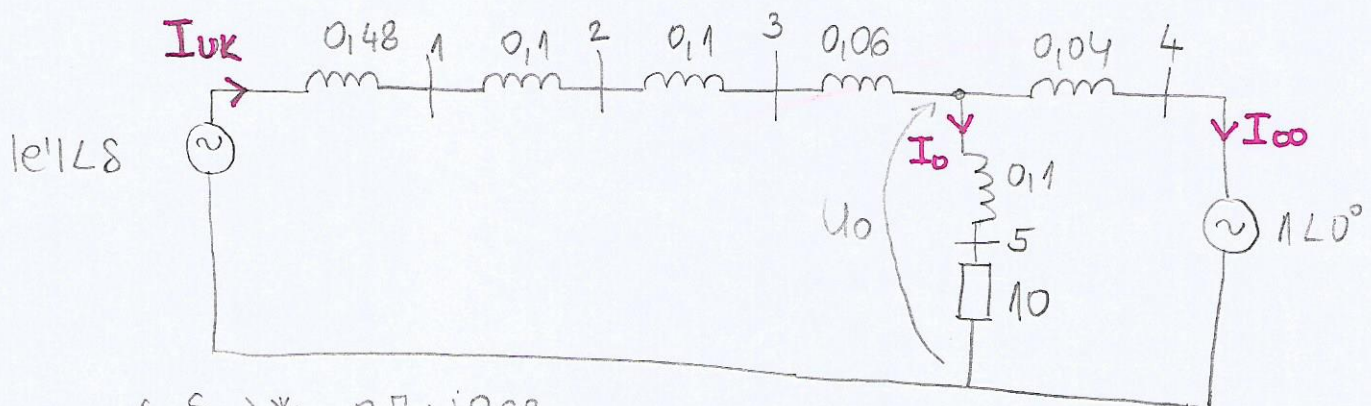
poduzb. režim

$$\cos \varphi = 0,95 \text{ (kap)}$$

$$U_{\infty} = 1 \text{ p.u.}$$

$$Q = P \cdot \tan[\arccos(-0,95)] = 0,7 \cdot \tan[\arccos(-0,95)] = -0,23 \text{ p.u.}$$

2PKS, 50% DV



$$I_{\infty} = \left(\frac{S}{U_{\infty}} \right)^* = \frac{0,7 + j0,23}{1} = 0,7 + j0,23$$

$$U_0 = U_{\infty} + jI_{\infty} \cdot 0,04 = 1 + j0,04(0,7 + j0,23) = 0,9908 + j0,028 = 0,991 \angle 0,028$$

$$I_0 = \frac{U_0}{Z} = \frac{0,991 \angle 0,028}{10 \angle 0,01} = 0,0991 \angle 0,018 = 0,099 + j1,78 \cdot 10^{-3}$$

$$I_{uc} = I_{\infty} + I_0 = 0,832 \angle 0,282$$

$$\begin{aligned}
 |e'| \angle \delta &= I_{uc} \cdot j(0,48 + 0,1 + 0,1 + 0,06) + U_0 = \\
 &= 0,832 \angle 0,282 \cdot 0,74 \angle \pi/2 + 0,9908 + j0,028 = \\
 &= -0,171 + j0,591 + 0,9908 + j0,028 = \\
 &= 1,027 \angle 0,647
 \end{aligned}$$

$$\begin{aligned}
 |e'| &= 1,027 \\
 \delta &= 0,647 \text{ rad}
 \end{aligned}$$

$$Z_d = X_L + X_D + \frac{X_L X_D}{X_{D0}} = j0,74 + j0,04 - \frac{0,0296}{10 \angle 0,01} = 0,78 + 2,9 \cdot 10^{-3} + j2,95 \cdot 10^{-5}$$

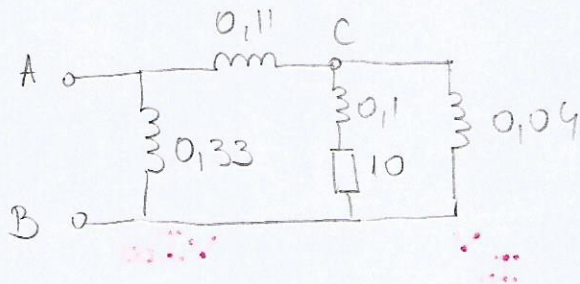
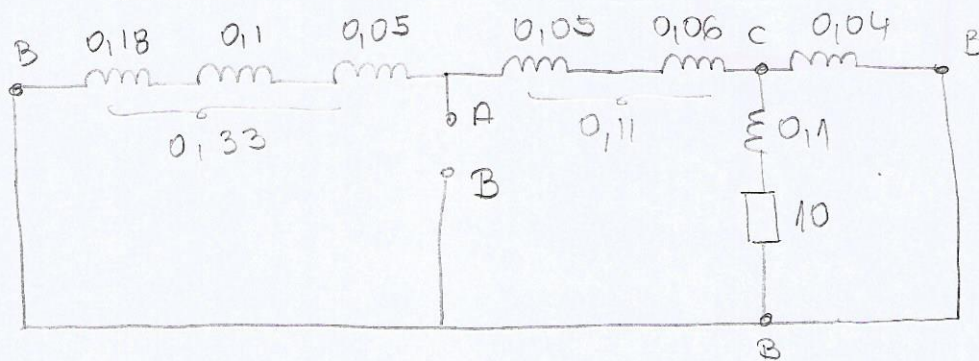
$$X_d \approx 0,78$$

$$P_d = \frac{1e'11U_{00}}{X_d} \sin \delta = \frac{1,027}{0,78} \sin \delta = 1,317 \sin \delta$$

$$P_m = 0,8$$

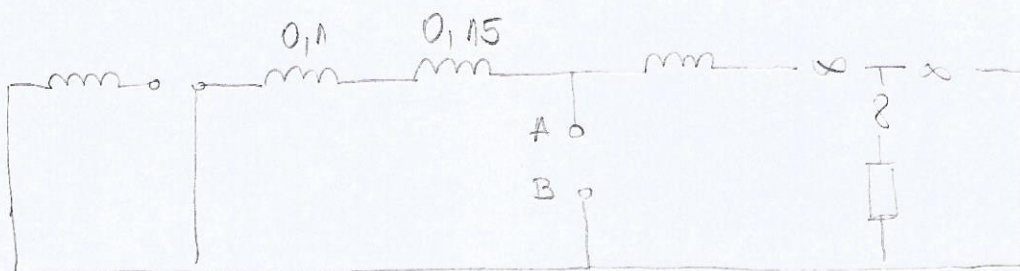
ZA VRIJEME KVARA

$$X_f = \frac{X_i X_0}{X_i + X_0}, \quad 50\% \text{ dv}, \quad \text{Inverzni sustav:}$$



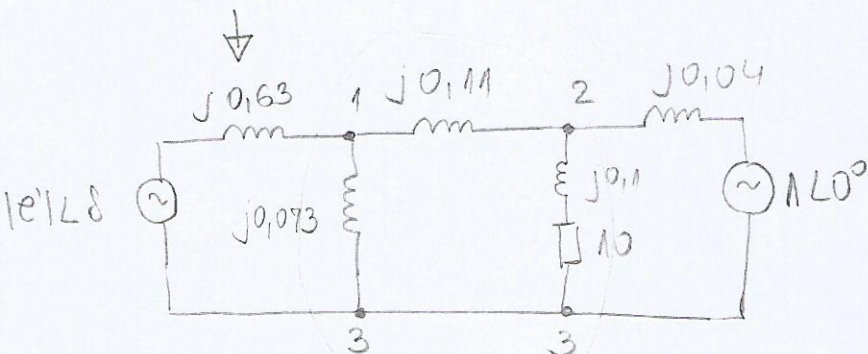
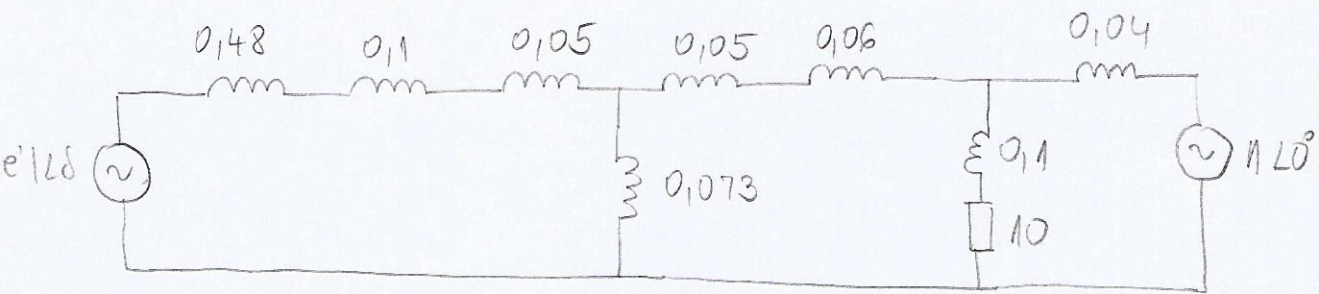
$$\begin{aligned} X_i = X_{AB} &= \left[(j0,04) \parallel (10 + j0,1) + j0,11 \right] \parallel j0,33 = \\ &= \left[\frac{0,04 \angle 90^\circ \cdot 10 \angle 0,573^\circ}{10 \angle 0,8^\circ} + j0,11 \right] \parallel j0,33 = \\ &= [j0,04 + j0,11] \parallel j0,33 = j0,103125 \end{aligned}$$

Multi sustav:



$$jX_0 = jX_{AB} = j0,1 + j0,15 = j0,25$$

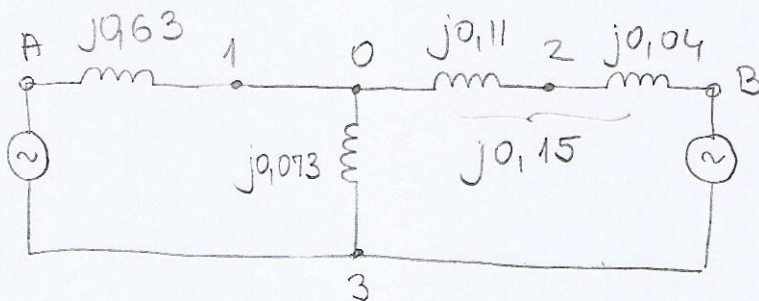
$$X_F = \frac{X_0 X_i}{X_0 + X_i} = 0,073 \text{ p.u.}$$



$$X_{10} = \frac{X_{12} X_{13}}{X_{12} + X_{13} + X_{23}} = \frac{0,00803 \angle 180^\circ}{\frac{10 \angle 1,62^\circ}{N}} \approx 0$$

$$X_{20} = \frac{X_{12} X_{23}}{X_{12} + X_{13} + X_{23}} = \frac{1,1 \angle 90^\circ}{N} = j0,11$$

$$X_{30} = \frac{X_{13} \cdot X_{23}}{X_{12} + X_{13} + X_{23}} = \frac{0,73 \angle 90^\circ}{N} = j0,073$$



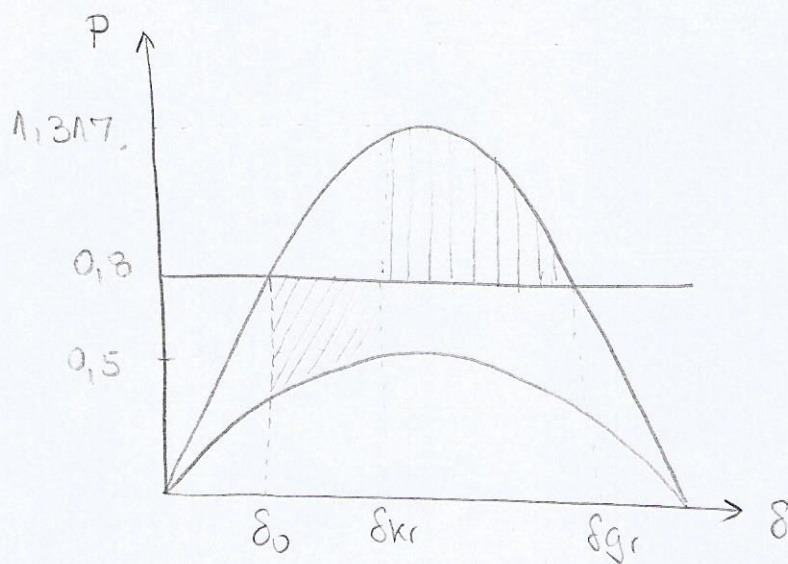
$\lambda \rightarrow \Delta$

$$jX_{\beta} = X_{AB} = X_L + X_D + \frac{X_L X_D}{X_{DO}} = j0,63 + j0,15 + \frac{j0,63 \cdot j0,15}{j0,073} = j2,074$$

$$P_{ep} = \frac{|e| |1| \cos \delta}{X_{\beta}} \sin \delta = \frac{1,027}{2,074} \sin \delta = 0,5 \sin \delta$$

NAKON KVARA

$$P_{ex} = P_{ed} = 1,317 \sin \delta$$



$$P_m = 0,8$$

$$P_d = 1,317 \sin \delta$$

$$P_p = 0,5 \sin \delta$$

$$P_y = 1,317 \sin \delta$$

$$P_m = P_d \sin \delta_{gr} \rightarrow \sin \delta_{gr} = \frac{P_m}{P_d} = 0,6 \rightarrow \delta_{gr} = 37^\circ$$

$$\delta_{gr} = \pi - \delta_{gr}' = 143^\circ = 2,49 \text{ rad}$$

$$A_a = A_d$$

$$\int_{\delta_0}^{\delta_{kr}} (P_m - P_p) d\delta = \int_{\delta_{kr}}^{\delta_{gr}} (P_d - P_m) d\delta$$

$$P_m (\delta_{kr} - \delta_0) - P_p (-\cos \delta_{kr} + \cos \delta_0) = P_d (-\cos \delta_{gr} + \cos \delta_{kr}) - P_m (\delta_{gr} - \delta_{kr})$$

$$\cancel{P_m \delta_{kr}} - P_m \delta_0 + P_p \cos \delta_{kr} - P_p \cos \delta_0 = P_d \cos \delta_{kr} - P_d \cos \delta_{gr} - P_m \delta_{gr} + \cancel{P_m \delta_{kr}}$$

$$\cos \delta_{kr} (P_p - P_d) = P_m (\delta_0 - \delta_{gr}) + P_p \cos \delta_0 - P_d \cos \delta_{gr}$$

$$\cos \delta_{kr} (0,5 - 1,317) = 0,8 (0,647 - 2,49) + 0,5 \cdot \cos (0,647) - 1,317 \cos (2,49)$$

$$-0,817 \cos \delta_{kr} = -0,028, \cos \delta_{kr} = \frac{-0,028}{-0,817}$$

$$\delta_{kr} = 1,54 \text{ rad} \approx 90^\circ$$

4. ZADATAK

$$S_n = 50 \text{ MVA}$$

prigušnica λ

$$U = 220 \text{ kV}$$

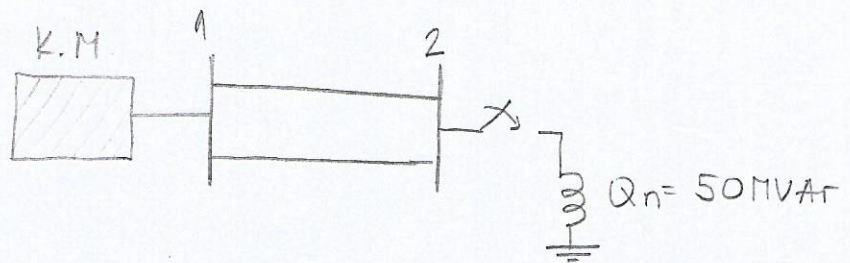
$$R = 0,05 \Omega/\text{km} \rightarrow 10 \Omega$$

$$L = 1,553 \text{ mH/km} \rightarrow X_L = j97,58 \Omega$$

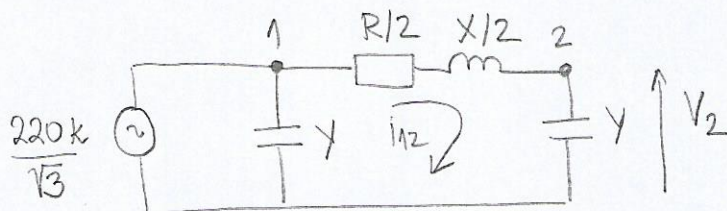
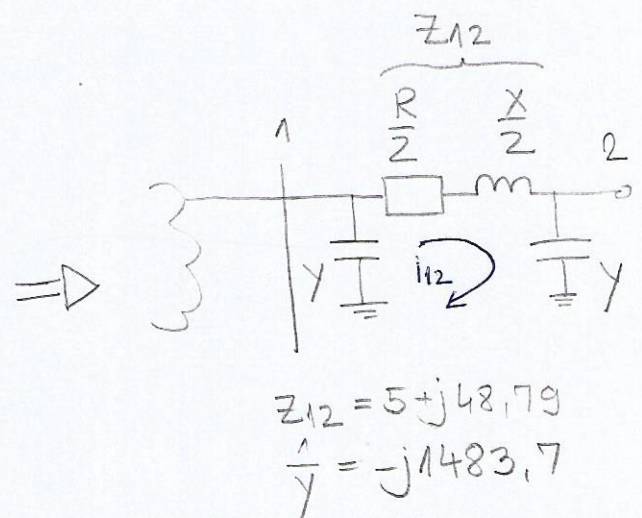
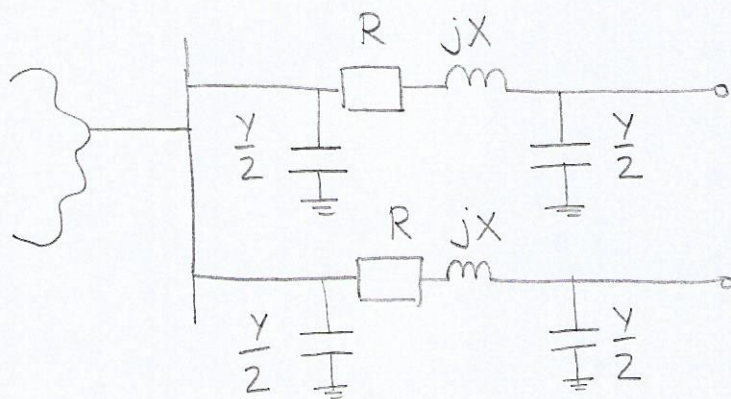
$$C = 10,73 \text{ nF/km} \rightarrow B = 0,674 \cdot 10^{-3} \text{ S} \quad (Y = jB, Z = jX)$$

$$l = 200 \text{ km}$$

$$f = 50 \text{ Hz}$$



$$\Delta U_2 = ?$$



$$V_2 = V_1 - i_{12} \cdot Z_{12}$$

$$i_{12} = \frac{U_1}{Z_{12} + \frac{1}{Y}} = \frac{220 \text{ kV} / \sqrt{3}}{5 + j48,79 - j1483,7}$$

$$i_{12} = \frac{220 \text{ kV} / \sqrt{3}}{1434,9 \angle -1,57} = 88,5 \angle 1,57$$

$$i_{12} = 0,07 + j88,5$$

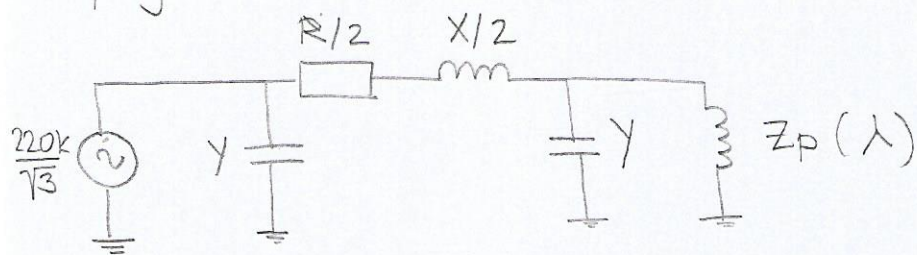
$$V_2 = V_1 - i_{12} \cdot Z_{12} =$$

$$= \frac{220 \text{ kV}}{\sqrt{3}} - 88,5 \angle 1,57 \cdot 49,04 \angle 1,47$$

$$= \frac{220 \text{ kV}}{\sqrt{3}} + 4317,66 - j440,16 = 131335 \angle -3,35 \cdot 10^{-3}$$

$$\Rightarrow U_2 = \sqrt{3} \cdot V_2 = \sqrt{3} \cdot 131335 = 227,5 \text{ kV}$$

S prigušnicom



PRIGUŠNICA:

$$U = 220 \text{ kV}$$

$$S_n = 50 \text{ MVA}$$

$$3f:$$

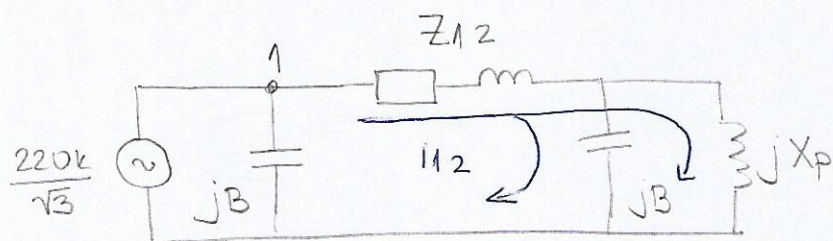
$$S_n = 3 U_f I_f^* =$$

$$= 3 \frac{U_L}{\sqrt{3}} \left(\frac{U_L}{\sqrt{3}} \cdot \frac{1}{Z_L} \right) = \frac{U_L^2}{Z_L}$$

$$S_n = \frac{U_L^2}{(jX)^*} = \frac{U_L^2}{-jX} \cdot j = j \frac{|U_{Ln}|^2}{X}$$

$$S_n = j \frac{|U_{Ln}|^2}{X} = P_n + jQ_n$$

$$Q_n = 50 \text{ M} = \frac{U_{Ln}^2}{X_p} \rightarrow X_p = \frac{|U_{Ln}|^2}{50 \text{ M}} = \frac{(220 \text{ k})^2}{50 \text{ M}} = 968 \rightarrow Z_p = j968 \Omega$$



$$i_{12} = \frac{V_1}{Z_{12} + \left(\frac{1}{jB} \parallel jX_p \right)}$$

$$\frac{1}{j} \parallel jX_p = \frac{1}{j0,674 \cdot 10^{-3} \parallel j968} = \frac{1483,7 \cdot 968}{-j1483,7 + j968} = j2785,06$$

$$i_{12} = \frac{220 \text{ k} / \sqrt{3}}{5 + j48,79 + j2785,06} = \frac{220 \text{ k} / \sqrt{3}}{2833,85 \angle 1,569} = 44,82 \angle -1,569 = 0,08 - j44,82$$

$$V_2' = V_1' - i_{12}' \cdot Z_{12} = \frac{220 \text{ k}}{\sqrt{3}} - 44,82 \angle -1,569 \cdot 49,05 \angle 1,469 = \frac{220 \text{ k}}{\sqrt{3}} - 2187,43 + j219,476 = 124,83 \text{ kV} / \sqrt{3}$$

$$U_2' = 216,211 \text{ kV}$$

$$\Delta U_2 = U_2' - U_2 = 216,211 - 227,5 = -11,289 \text{ kV}$$

Prazno mjesto za 5. zadatak

6. ZADATAK

$$P_{n1}^m = 3 \text{ MW}$$

$$P_{n2}^m = 4 \text{ MW}$$

$$U = 1 \text{ kV}$$

$$\cos \varphi_1 = 0,8$$

$$\cos \varphi_2 = 0,7$$

$$\eta_1 = 0,95$$

$$\eta_2 = 0,98$$

$$a) I = ?$$

$$b) \cos \varphi = ?$$

$$c) Q_{KB} = ?, \cos \varphi' = 0,95$$

$$d) C_{KB} (\Delta) = ?$$

$$P_{e1} = \frac{P_{n1}^m}{\eta_1} = 3,158 \text{ MW} \quad P_{e2} = 4,082 \text{ MW}$$

$$P_{uk} = P_1 + P_2 = 7,24 \text{ MW}$$

$$Q_1 = P_{e1} \tan \varphi_1 = 2,368 \text{ MVAR} \quad Q_2 = P_{e2} \tan \varphi_2 = 4,164 \text{ MVAR}$$

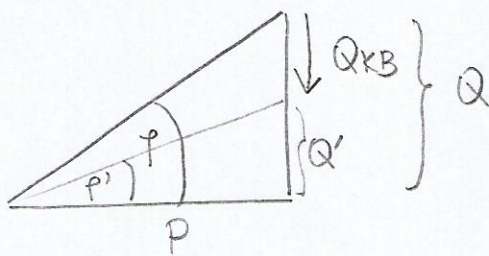
$$Q_{uk} = Q_1 + Q_2 = 6,532 \text{ MVAR}$$

$$a) S = \sqrt{P_{uk}^2 + Q_{uk}^2} = \sqrt{3} \cdot |U| \cdot |I|$$

$$|I| = \frac{|S|}{\sqrt{3} \cdot |U|} = \frac{\sqrt{7,24^2 + 6,532^2} (\text{M})}{\sqrt{3} \cdot 1 (\text{k})} = 5,63 \text{ kA}$$

$$b) \tan \varphi = \frac{Q_{uk}}{P_{uk}} = \frac{6,532}{7,24}, \quad \cos \varphi = \cos \left(\arctan \left(\frac{6,532}{7,24} \right) \right) = 0,74$$

$$c) Q_{KB} = ?, \cos \varphi' = 0,95$$



$$Q' = P \cdot \tan \varphi' = 7,24 \cdot \tan (\arccos 0,95) = 2,37 \text{ MVAR}$$

$$Q_{KB} = Q - Q' = 6,532 - 2,37 = 4,15 \text{ MVAR}$$

$$d) C (\Delta) = ?$$

$$Q_{KB} = 4,15 \text{ MVAR}$$

$$|Q_{KB}| = 3 U_L^2 \omega C = 3 U_L^2 \omega C$$

$$Q_{KB} = 3 U_L^2 \omega C$$

$$C = \frac{Q_{KB}}{3 U_L^2 \omega} = \frac{4,15 \text{ M}}{3 \cdot (1 \text{ k})^2 \cdot 2\pi \cdot 50} = 4,4 \text{ mF}$$