

Zadatak 1

Neki elektroenergetski sustav (50 Hz) sastoji se od 5 elektrana s karakteristikama prema tablici 1. Ovaj sustav može se aproksimirati s dinamičkim modelom prema slici 1 u kojem su sve termoelektrane, hidroelektrane i potrošači agregirani u jedan stroj ukupne konstante tromosti H i regulacijske energije potrošnje $D = 2$ p.u.. Agregirani sustav sastoji se od jedne ekvivalentne parne turbine s pregrijanjem pare i jedne ekvivalentne hidroturbine s ekvivalentnim statičnostima σ_T i σ_H . Potrebno je:

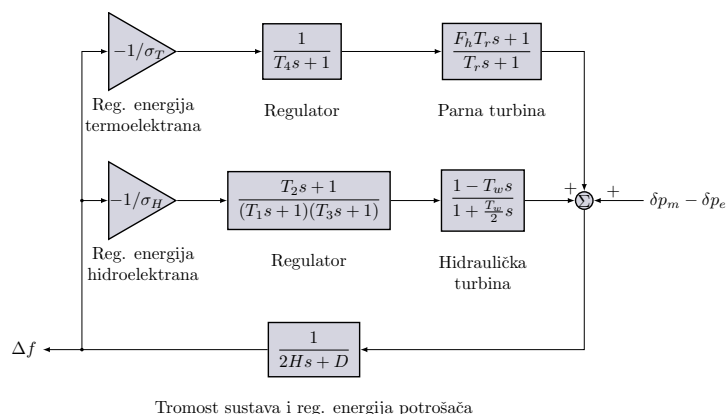
- Odrediti ukupnu konstantu tromosti sustava u normalnom pogonskom stanju.
- Odrediti ekvivalentnu statičnost sustava u normalnom pogonskom stanju.
- Izvesti izraz za odstupanje frekvencije u Laplaceovoj domeni i izračunati odstupanje frekvencije u stacionarnom stanju nakon ispada elektrane E3 koja je prije ispada radila s 50% nazivne snage.
- Izračunati za koliko se promijeni snaga potrošnje sustava nakon poremećaja iz c).
- Izračunati početni RoCoF ($t = 0^+$) neposredno nakon poremećaja iz c).

Koristiti $S_b = 1000$ MVA.

(10 bodova)

Tablica 1: Podaci o agregatima u elektranama

Elektrana	Vrsta	Moment tromosti [kgm^2]	Broj polova	Nazivna snaga [MVA]	Statičnost [%]
E1	Termo	$10 \cdot 10^3$	2	100	5
E2	Termo	$25 \cdot 10^3$	2	200	6
E3	Termo	$50 \cdot 10^3$	2	400	∞
E4	Hidro	$1000 \cdot 10^3$	20	200	2
E5	Hidro	$500 \cdot 10^3$	18	100	4



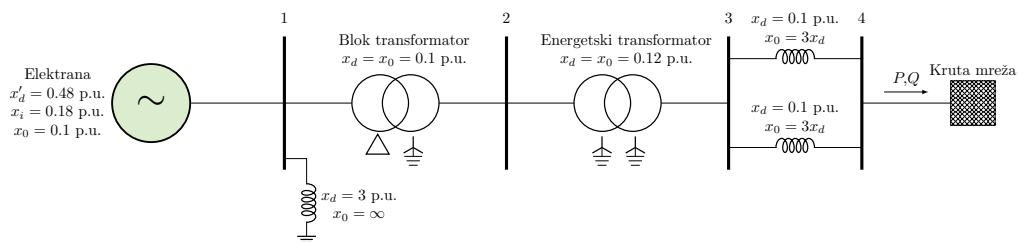
Slika 1: Dinamički model sustava

Zadatak 2

Neka elektrana spojena je na krutu mrežu preko blok-transformatora, energetskog transformatora i dvostrukog dalekovoda prema slici 2. Generator na vlastitim sabirnicama snabdijeva pomoćne asinkrone motore sa strujom magnetiziranja. Motori su trenutno neopterećeni i modelirani su kao pasivni potrošač jalove snage s konstantnom impedancijom. Zvezdište asinkronog motora nije uzetljeno. Agregat u mrežu predaje snagu $P = 0.9$ p.u. pri $\cos \varphi = 1.00$. Napon krute mreže iznosi $1 \angle 0^\circ$ p.u. Na 5% duljine jednog od dva paralelna voda (gledano od sabirnice 3) nastaje dvopolni kratki spoj sa zemljom. Potrebno je 1) odrediti kritični kut uklanjanja kvara i 2) nacrtati nadomjesnu shemu sustava sa slike 2 te odrediti izraz i skicirati krivulje za prijenos električne snage između elektrane i krute mreže za slučajeve:

- prije nastanka kratkog spoja;
- tijekom kratkog spoja;
- nakon isključenja voda u kvaru.

(9 bodova)

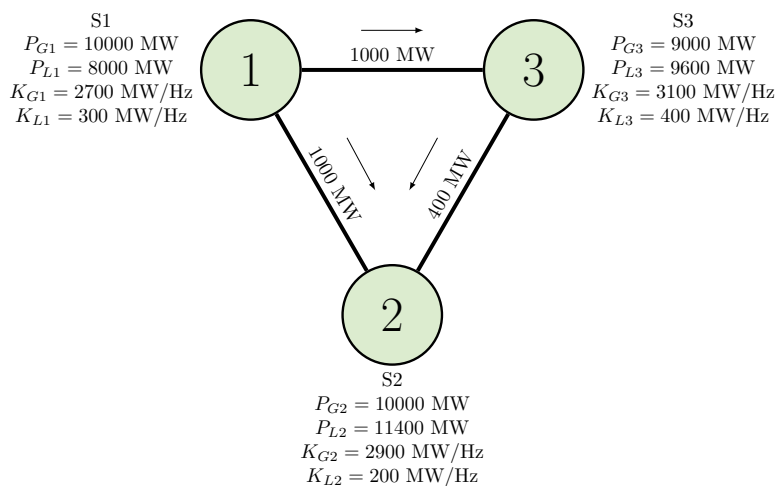


Slika 2: Spoj elektrane s krutom mrežom

Zadatak 3

Tri sustava rade u interkonekciji (Slika 3). Joži je dispečer u operatoru sustava 1. Joži je ispao tanjur s buncekom, pečenicama i kuhanim krumpirom na tipkovnicu i slučajno je isključio vod između sustava 1 i 3. Sekvencijalno opišite što će se dogoditi od tog trenutka pa sve do konačnog stacionarnog stanja. Navedite i naznačite sva međustanja. Potrebno je izračunati konačno stanje u svim sustavima te sva međustanja kroz koja sustavi prolaze. Maksimalno dozvoljeno opterećenje vodova 1–2 i 1–3 iznosi 1500 MW, dok je prijenosna moć voda 2–3 zbog radova smanjena i iznosi 500 MW. Preopterećeni vod prekostrujna zaštita automatski isključuje. Svi sustavi jednako sudjeluju u sekundarnoj regulaciji. Dozvoljena su odstupanja između proizvodnje i potrošnje do 100 MW zbog numeričke nepreciznosti tijekom proračuna.

(6 bodova)



Slika 3: Tri sustava u interkonekciji

Zadatak 4

Nacrtajte blok dijagram dinamičkog sustava opisanog jednadžbama (1)–(2), gdje su T_1 , H , D i R konstante, a $\Delta p_e(t)$ je step poremećaj amplitude A . Matematički dokazati da smanjenje statičnosti uzrokuje smanjenje odstupanja brzine vrtnje u stacionarnom stanju nakon poremećaja, odnosno: $R \rightarrow 0^+ \Rightarrow [\Delta\omega(t \rightarrow \infty)] \rightarrow 0$.

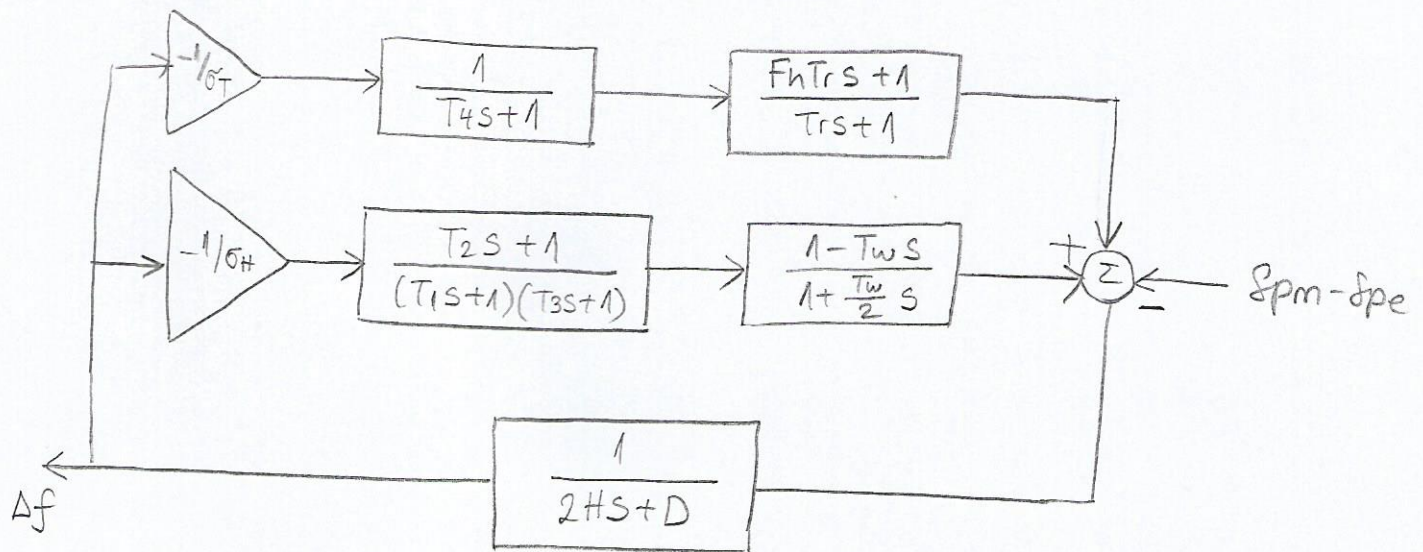
$$2H \frac{d\Delta\omega}{dt} + D\Delta\omega = \Delta p_m(t) - \Delta p_e(t) \quad (1)$$

$$T_1 \frac{d\Delta p_m(t)}{dt} + \Delta p_m(t) = -\frac{1}{R} \Delta\omega \quad (2)$$

(5 bodova)

1. ZADATAK

Elektrana	Vrsta	J [kgm ²]	Br. polova	S _n [MVA]	Statičnost [%]
E1	Termo	10 · 10 ³	2	100	5
E2	-II-	25 · 10 ³	2	200	6
E3	-II-	50 · 10 ³	2	400	∞
E4	Hidro	1000 · 10 ³	20	200	2
E5	-II-	500 · 10 ³	18	100	4



$$D = 2 \text{ p.u.}$$

a) $H_{UK} = ?$

$$S_B = 1000 \text{ MVA}$$

$$H = \frac{E_{kin}}{S_B} = \frac{J \omega_m^2}{2 S_B}$$

$$H_{UK} = \sum \frac{J_i \left(\frac{\omega_{ei}}{\pi f_i} \right)^2}{2 S_B} = \frac{\sum J_i (2\pi \frac{f}{f_i})^2}{2 S_B}$$

$$H_{UK} = (2\pi f)^2 \frac{\sum J_i \left(\frac{1}{f_i} \right)^2}{2 S_B}$$

$$H_{UK} = \frac{(2\pi \cdot 50)^2}{2 \cdot 1000 \text{ M}} \left[\frac{10 \cdot 10^3}{1} + \frac{25 \cdot 10^3}{1} + \frac{50 \cdot 10^3}{1} + \frac{1000 \cdot 10^3}{10^2} + \frac{500 \cdot 10^3}{9^2} \right]$$

$$H_{UK} = 4,99 \text{ s} \approx 5 \text{ s}$$

b) $\sigma'_{UK} = ?$

$$\sigma'_1 = \sigma_1 \frac{S_B}{S_{n1}} = 0,05 \frac{1000}{100} = 0,5 \quad \sigma'_4 = 0,02 \frac{1000}{200} = 0,1$$

$$\sigma'_2 = 0,06 \frac{1000}{200} = 0,3$$

$$\sigma'_5 = 0,04 \frac{1000}{100} = 0,4$$

$$\sigma'_3 = \infty$$

$$K_{UK} = \sum \frac{1}{\sigma'_i} = 17,83 \text{ pu}$$

$$\sigma_{UK} = \frac{1}{K_{UK}} = \frac{1}{17,83} = 0,056 \text{ p.u.}$$

c) Izvesti izraz za odstupanje fr. u Laplaceovoj domeni

$$\Delta f = \frac{1}{2Hs + D} \left[\Delta f \left(-\frac{1}{\sigma_T} \right) G_T(s) + \Delta f \left(-\frac{1}{\sigma_H} \right) G_H(s) + \delta p_m - \delta p_e \right]$$

$$\Delta f \left[2Hs + D + \frac{1}{\sigma_T} G_T(s) + \frac{1}{\sigma_H} G_H(s) \right] = \delta p_m - \delta p_e$$

$$\Delta f = \frac{\delta p_m - \delta p_e}{2Hs + D + \frac{1}{\sigma_T} G_T(s) + \frac{1}{\sigma_H} G_H(s)}$$

Ispad elektrane E3 koja je prije ispada radila s 50% Sn

$$\Delta f(t \rightarrow \infty) = \lim_{s \rightarrow 0} s \cdot \Delta f = \lim_{s \rightarrow 0} s \cdot \frac{\frac{\delta p_m - \delta p_e}{s}}{2Hs + D + \frac{1}{\sigma_T} G_T(s) + \frac{1}{\sigma_H} G_H(s)}$$

$$\Delta f(t \rightarrow \infty) = \frac{\delta p_m - \delta p_e}{D + \frac{1}{\sigma_T} + \frac{1}{\sigma_H}} = \frac{-0,2}{2 + \frac{1}{0,5} + \frac{1}{0,3} + \frac{1}{0,1} + \frac{1}{0,4}} = -0,01 \text{ p.u.} / 50 \text{ Hz}$$

$$\Delta f(t \rightarrow \infty) = -0,5 \text{ Hz}$$

d) $\Delta P_m = D \cdot \Delta f = 2 \cdot (-0,01) = -0,02 \text{ p.u.}$
 $= -20 \text{ MVA}$

e) $\frac{df}{dt} (t=0^+) = ?$

$$\frac{df}{dt} \Big|_{t=0^+} = \lim_{s \rightarrow \infty} s^2 \Delta f(s) = \lim_{s \rightarrow \infty} s^2 \frac{\frac{\delta p_m - \delta p_e}{s}}{2Hs + D + \frac{1}{\sigma_T} G_T + \frac{1}{\sigma_H} G_H} =$$

$$= \lim_{s \rightarrow \infty} \frac{\delta p_m - \delta p_e}{2H + \frac{D}{s} + \frac{1}{s\sigma_T} G_T + \frac{1}{s\sigma_H} G_H} = \frac{\delta p}{2H} = \frac{-0,2}{2 \cdot 2,526} = -0,0396 \frac{\text{p.u.}}{\text{s}} = -1,98 \frac{\text{Hz}}{\text{s}}$$

$$* H = H_{uc} - H_3 = 4,993 - \frac{50 \cdot 10^3 \left(2\pi \cdot \frac{50}{1} \right)^2}{2 \cdot 1000 \text{ M}} = 2,526 \text{ s}$$

M1 2020/2021.

2. ZADATAK

$$P = 0,9 \text{ p.u.}$$

$$\cos \varphi = 1$$

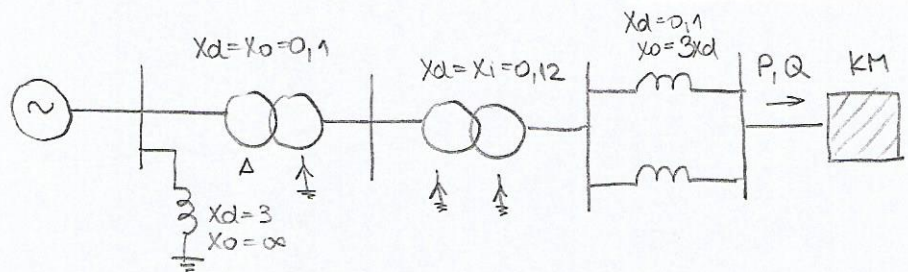
$$U_{\infty} = 1 \angle 0^\circ$$

$$2 \text{ KSZ, } 5\% \text{ dv}$$

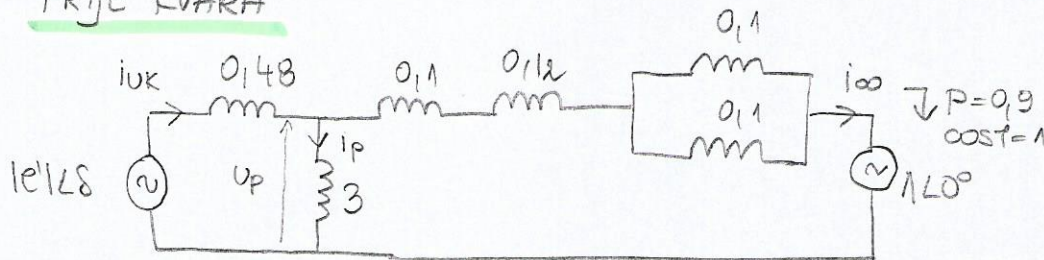
$$X'_d = 0,48$$

$$X_i = 0,18$$

$$X_o = 0,1$$



PRIJE KVARA



$$X_L = 0,27$$

$$X_D = 0,48$$

$$X_{D0} = 3$$

$$i_{\infty} = \left(\frac{S_{\infty}}{U_{\infty}} \right)^* = 0,9 \text{ p.u.}$$

$$\left. \begin{aligned} U_p &= U_{\infty} \angle 0^\circ + j i_{\infty} \cdot X_L \\ U_p &= i_p \cdot X_p \end{aligned} \right\} i_p = \frac{U_{\infty} \angle 0^\circ + i_{\infty} \cdot X_L}{X_p} = \frac{1 \angle 0^\circ + 0,9 \cdot 0,27 \angle 90^\circ}{3 \angle 90^\circ} = \frac{1,029 \angle 13,66^\circ}{3 \angle 90^\circ} = 0,343 \angle -76,34^\circ$$

$$U_p = 1,029 \angle 13,66^\circ$$

$$i_{uk} = i_p + i_{\infty} = 0,081 - j0,333 + 0,9 = 0,981 - j0,333 = 1,036 \angle -18,75^\circ$$

$$|e'| \angle \delta = U_p + j i_{uk} \cdot X'_d = 1,029 \angle 13,66^\circ + 1,036 \angle -18,75^\circ \cdot 0,48 \angle 90^\circ = 1 + j0,243 + 0,1598 + j0,471 = 1,362 \angle 31,62^\circ$$

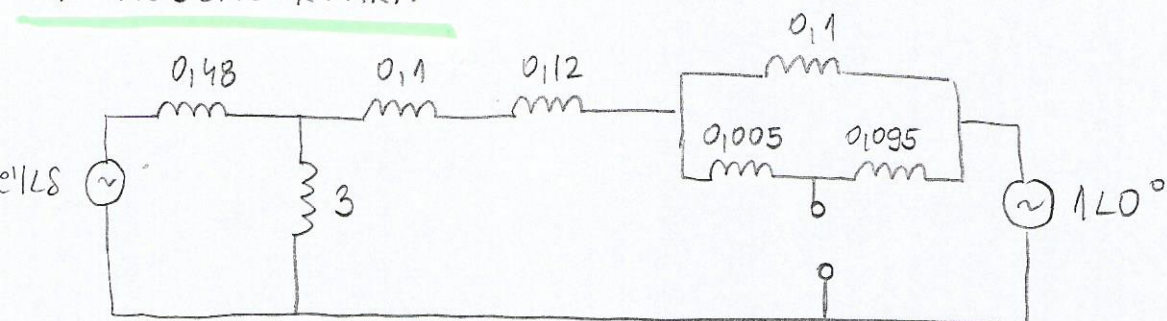
$$|e'| \angle \delta = 1,362 \angle 0,552 \text{ rad}$$

$$X_d = X_L + X_D + \frac{X_L \cdot X_D}{X_{D0}} = 0,27 + 0,48 + \frac{0,27 \cdot 0,48}{3} = 0,7932$$

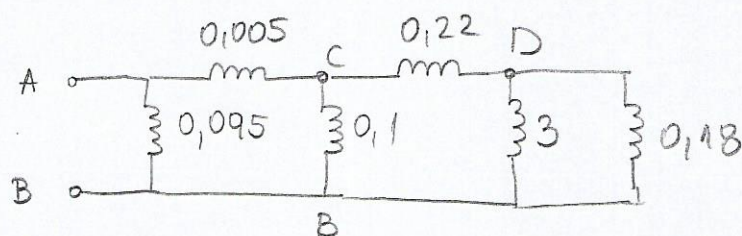
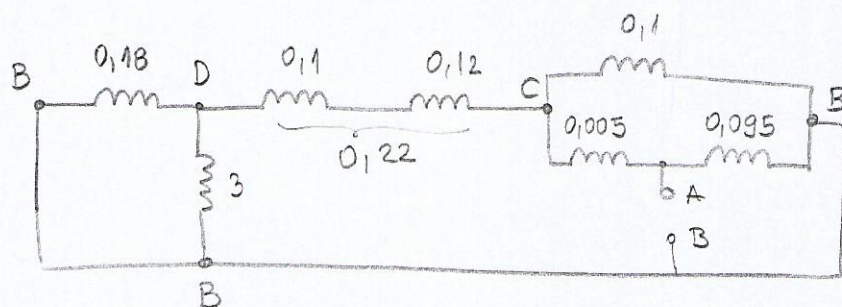
$$P_e^d = \frac{|e'| |U_{\infty}|}{X_d} \sin \delta = \frac{1,362 \cdot 1}{0,7932} \cdot \sin \delta = 1,717 \sin \delta$$

$$P_m = \frac{1,362}{0,7932} \cdot \sin(0,552) = 0,9$$

ZA VRIJEME KVARA



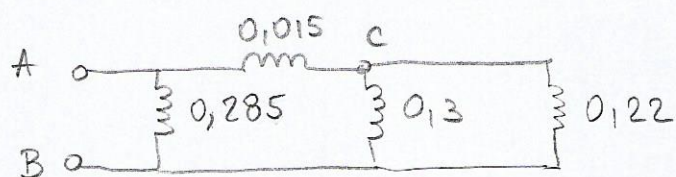
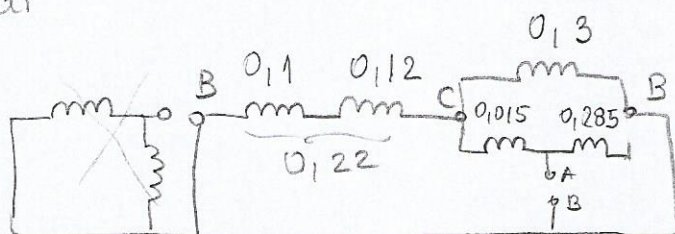
Inverzni:



$$X_i = [(0,18 \parallel 3 + 0,22) \parallel 0,1 + 0,005] \parallel 0,095 = \left[\underbrace{(0,17 + 0,22)}_{0,39} \parallel 0,1 + 0,005 \right] \parallel 0,095$$

$$= \underbrace{(0,079 + 0,005)}_{0,085} \parallel 0,095 = 0,045$$

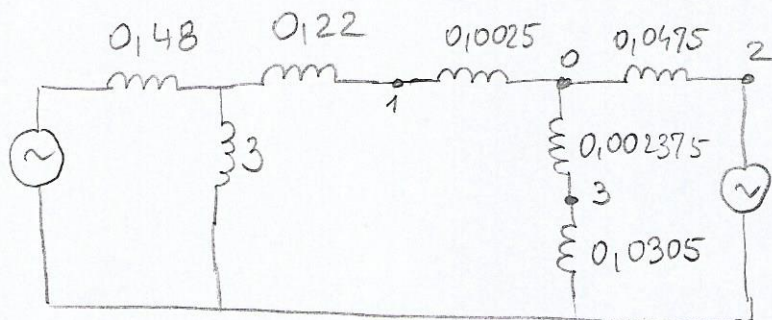
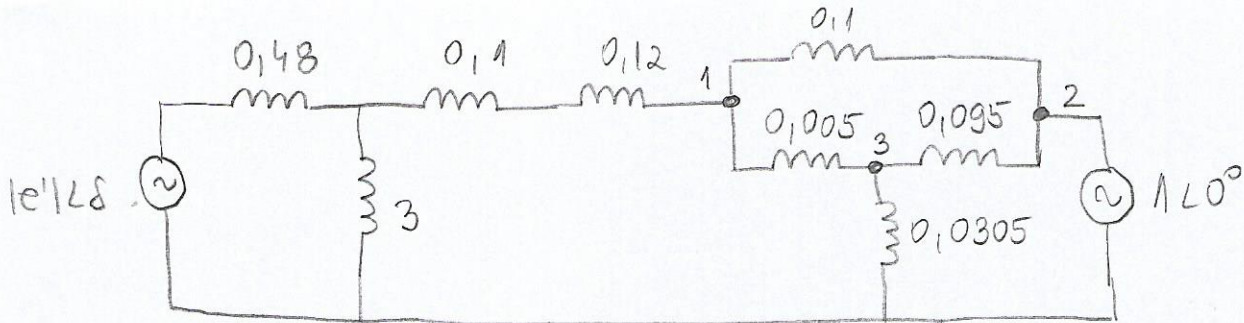
multi



$$X_0 = [0,22 \parallel 0,3 + 0,015] \parallel 0,285$$

$$X_0 = 0,095$$

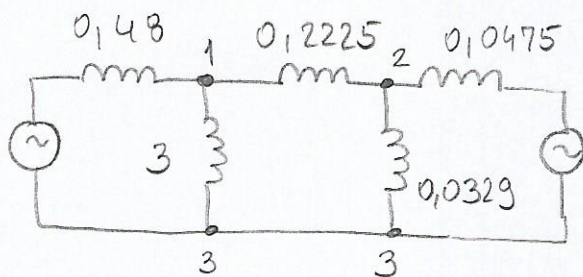
$$X_F = X_i \parallel X_0 = 0,0305$$



$$X_{10} = \frac{X_{12}X_{13}}{X_{12}+X_{13}+X_{23}} = 0,0025$$

$$X_{20} = \frac{X_{21}X_{23}}{N} = 0,0475$$

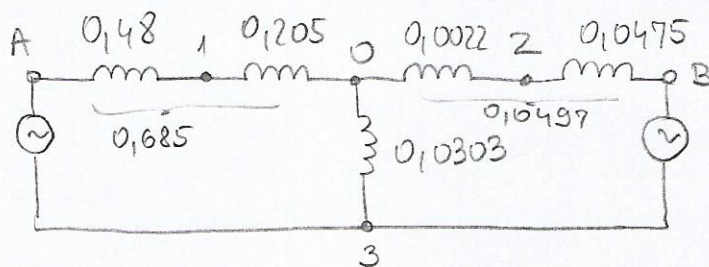
$$X_{30} = \frac{X_{31}X_{32}}{N} = 0,002375$$



$$X_{10} = 0,205$$

$$X_{20} = 0,0022$$

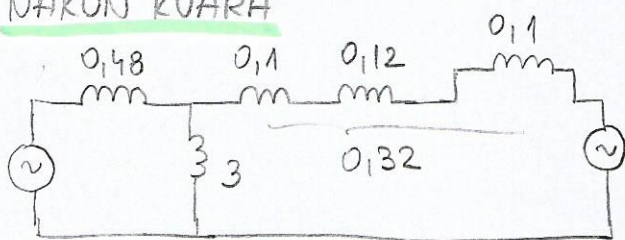
$$X_{30} = 0,0303$$



$$X_p = X_{AB} = X_L + X_D + \frac{X_L X_D}{X_{DO}} = 1,86$$

$$P_{e\beta} = \frac{1e'11u\omega}{X_p} \sin \delta - \frac{1,362}{1,86} \sin \delta = 0,732 \sin \delta$$

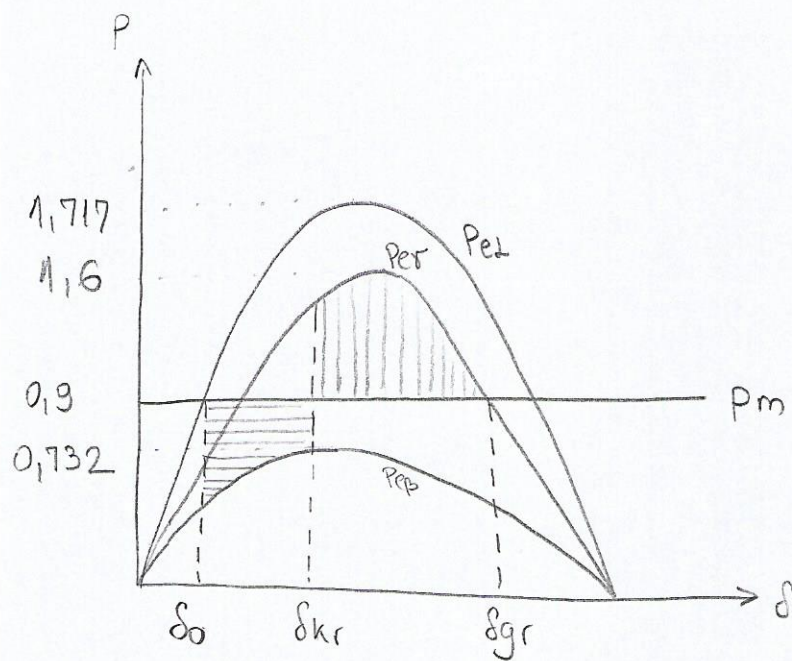
NAKON KUARA



$$X_{AB} = 0,48 + 0,32 + \frac{0,48 \cdot 0,32}{3} \Rightarrow$$

$$X_{\gamma} = 0,8512$$

$$P_{e\gamma} = \frac{1,362}{0,8512} \sin \delta = 1,6 \sin \delta$$



$$P_{ex} = 1,717$$

$$P_{ep} = 0,732$$

$$P_{ex} = 1,6$$

$$P_m = 0,9$$

$$\delta_0 = 0,552 \text{ rad}$$

$$\delta_{gr}: P_x = P_m$$

$$0,9 = 1,6 \sin \delta_{gr} (\pi - \delta)$$

$$\delta_{gr} = 2,544 \text{ rad}$$

$$A_a = \int_{\delta_0}^{\delta_{kr}} (P_m - P_{ep}) d\delta \quad A_d = \int_{\delta_{kr}}^{\delta_{gr}} (P_{ex} - P_m) d\delta$$

$$A_a = A_d$$

$$P_m (\delta_{kr} - \delta_0) - P_{ep} (-\cos \delta_{kr} + \cos \delta_0) = P_{ex} (-\cos \delta_{gr} + \cos \delta_{kr}) - P_m (\delta_{gr} - \delta_{kr})$$

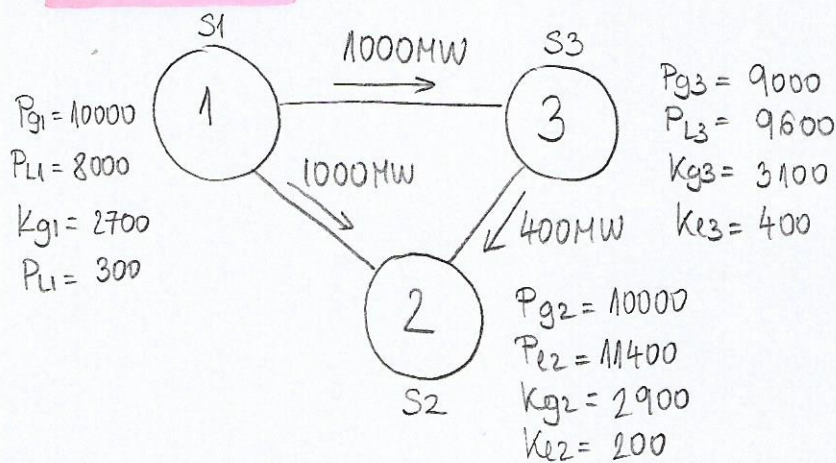
$$\cancel{P_m \delta_{kr}} - \cancel{P_m \delta_0} + P_{ep} \cos \delta_{kr} - P_{ep} \cos \delta_0 = P_{ex} \cos \delta_{kr} - P_{ex} \cos \delta_{gr} - \cancel{P_m \delta_{gr}} + \cancel{P_m \delta_{kr}}$$

$$\cos \delta_{kr} (P_{ex} - P_{ep}) = P_m (\delta_{gr} - \delta_0) + P_{ex} \cos \delta_{gr} - P_{ep} \cos \delta_0$$

$$\cos \delta_{kr} = \frac{0,9 (2,544 - 0,552) + 1,6 \cdot \cos (2,544) - 0,732 \cos (0,552)}{1,6 - 0,732}$$

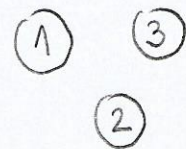
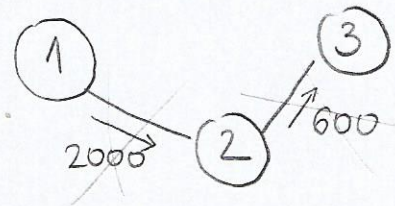
$$\delta_{kr} = 1,748 \text{ rad} = 100^\circ$$

3. ZADATAK



- isključen vod 1-3

- max opterećenje 1-2: 1500 MW
 1-3: 1500 MW
 2-3: 500 MW



SUSTAV 1: gubitak potrošnje 2000 MW
 frekvencija će se povećati

$$\Delta f = \frac{2000}{2700 + 300} = 0,667 \text{ Hz}$$

$$\Delta P_{g1} = -K_{g1} \cdot \Delta f = -2700 \cdot 0,667 = -1800,9 \text{ MW}$$

$$\Delta P_{e1} = K_{e1} \Delta f = 300 \cdot 0,667 = 200,1 \text{ MW}$$

$$P_{g1}' = P_{g1} + \Delta P_{g1} + \delta P_{g1} = 10000 - 1800,9 + 0 = 8199,1 \text{ MW}$$

$$P_{e1}' = P_{e1} + \Delta P_{e1} + \delta P_{e1} = 8000 + 200,1 + 0 = 8200,1 \text{ MW}$$

Sekundarna regulacija: $\Delta f = -0,667 \text{ Hz}$

$$\sum P_g = \sum P_e$$

$$\delta P = \Delta f (K_g + K_e) = -0,667 \cdot 3000 = -2000 \text{ MW}$$

$$P_{g1}'' = 8199,1 - 2700 \cdot (-0,667) - 2000 = 8000 \text{ MW}$$

$$P_{e1}'' = 8200,1 + 300 \cdot (-0,667) + 0 = 8000 \text{ MW}$$

SUSTAV 2 → gubitak proizvodnje → smanjenje frekvencije

$$\Delta f = \frac{-1400}{2900 + 200} = -0,452 \text{ Hz}$$

$$P_{g2}' = 10000 - (-0,452) \cdot 2900 + 0 = 11310,8 \text{ MW}$$

$$P_{e2}' = 11400 + (-0,452) \cdot 200 + 0 = 11309,6 \text{ MW}$$

Sekundarna regulacija: $\Delta f = +0,452 \text{ Hz} \rightarrow \delta P = 1400 \text{ MW}$

$$P_{g2}'' = 11310,8 - 0,452 \cdot 2900 + 1400 = 11400 \text{ MW}$$

$$P_{e2}'' = 11309,6 + 0,452 \cdot 200 + 0 = 11400 \text{ MW}$$

$$\sum P_g = \sum P_e$$

SUSTAV 3 ispad proizvodnje 600 MW

$$\Delta f = \frac{-600}{3100+400} = -0,171 \text{ Hz}$$

$$P_{g3}' = 9000 - (-0,171) \cdot 3100 + 0 = 9530,1 \text{ MW}$$

$$P_{l3}' = 9600 + (-0,171) \cdot 400 + 0 = 9531,6 \text{ MW}$$

Sekundarna regulacija: $\Delta f = +0,171 \text{ Hz}$

$$P_{g3}'' = 9530,1 - 0,171 \cdot 3100 + 600 = 9600 \text{ MW}$$

$$P_{l3}'' = 9531,6 + 0,171 \cdot 400 + 0 = 9600 \text{ MW}$$

$$\sum P_g = \sum P_l$$

M1 2020/2021.

4. ZADATOK

$$2H \frac{d\Delta\omega}{dt} + D\Delta\omega = \Delta p_m(t) - \Delta p_e(t)$$

$$T_1 \frac{d\Delta p_m(t)}{dt} + \Delta p_m(t) = -\frac{1}{R} \Delta\omega$$

T_1, H, D, R
konstante

$\Delta p_e(t)$ step
poremecaj
amplitude A

$$\frac{d\Delta\omega}{dt} = -\frac{D\Delta\omega}{2H} + \frac{1}{2H} [\Delta p_m(t) - \Delta p_e(t)]$$

$$\frac{d\Delta p_m(t)}{dt} = -\frac{1}{T_1} \Delta p_m(t) - \frac{1}{RT_1} \Delta\omega$$

