





#### Model električne strane



$$u(t) - L\frac{di(t)}{dt} - Ri(t) - e(t) = 0$$
  
$$L\frac{di(t)}{dt} + Ri(t) + Blv(t) = u(t)$$

### Model mehaničke strane



$$u = \frac{dx}{dt}$$

$$f_b \qquad m$$

$$m\frac{dv(t)}{dt} = f_i - f_b - f_k = Bli(t) - bv(t) - kx$$
$$-Bli(t) + m\frac{dv(t)}{dt} + bv(t) + k\int_{-\infty}^{t} v(t')dt' = 0$$

# Svezani sustav jednadžbi (v,i)

$$L\frac{di(t)}{dt} + Ri(t) + Blv(t) = u(t)$$

$$-Bli(t) + m\frac{dv(t)}{dt} + bv(t) + k\int_{-\infty}^{t} v(t')dt' = 0 \quad ; \quad \frac{d}{dt}$$

$$-Bl\frac{di(t)}{dt} + m\frac{d^2v(t)}{dt^2} + b\frac{dv(t)}{dt} + kdv(t) = 0$$

 Idealni zvučnik – konstantan tlak u cijelom čujnom frekvencijskom području 20 Hz do 20 kHz

## Analiza u frekvencijskom području

• Pretpostavka: sve se veličine u vremenu mijenjaju sinusno

$$\begin{split} &i(t) = \operatorname{Re}\left[\stackrel{\cdot}{i}e^{j\omega t}\right] \;\;; \quad v(t) = \operatorname{Re}\left[\stackrel{\cdot}{v}e^{j\omega t}\right] \; \Longrightarrow \\ &\frac{di(t)}{dt} = j\omega\,\stackrel{\cdot}{i}e^{j\omega t}\;; \quad \frac{d^2i(t)}{dt^2} = -\omega^2\,\stackrel{\cdot}{i}e^{j\omega t} \\ &\frac{dv(t)}{dt} = j\omega\,\stackrel{\cdot}{v}e^{j\omega t}\;; \quad \frac{d^2v(t)}{dt^2} = -\omega^2\,\stackrel{\cdot}{v}e^{j\omega t} \end{split}$$

• Uvrstimo u sustav jednadžbi

 $j\omega L\vec{i} + R\vec{i} + Bl\vec{v} = U$  $-j\omega Bl\vec{i} - \omega^2 m\vec{v} + j\omega b\vec{v} + k\vec{v} = 0$ 

 Time smo sveli diferencijalne na algebarske jednadžbe

## Matrični oblik

$$\begin{bmatrix} j\omega L + R & Bl \\ -j\omega Bl & j\omega b - \omega^2 m + k \end{bmatrix} \begin{bmatrix} \overline{i} \\ \overline{v} \end{bmatrix} = \begin{bmatrix} \overline{U} \\ 0 \end{bmatrix}$$

Kramerovo pravilo

$$\bar{v} = \frac{\det \begin{bmatrix} j\omega L + R & \overline{U} \\ -j\omega Bl & 0 \end{bmatrix}}{\det \begin{bmatrix} j\omega L + R & Bl \\ -j\omega Bl & j\omega b - \omega^2 m + k \end{bmatrix}}$$

• Frekvencijski odziv zvučnika

$$\frac{\overline{v}}{\overline{U}} = \frac{jBl\omega}{kR - (Rm - Lb)\omega^2 + j[(Rb + kL + B^2l^2)\omega - Lm\omega^3]}$$

• Polumjer zavojnice: 0.05m, L=10 mH, R=8 $\Omega$ , m=0.01 kg, b=22.75Ns²/m, broj zavoja 47, B=1 T

